

1) a) Algorithm alg1( $L[0 \dots n-1]$ )  
 if ( $n=1$ ) return  $L[0] \rightarrow O(1)$   
 else  
    $tmp = \text{alg1}(L[0 \dots n-2]) \rightarrow T(n-1)$   
   if ( $tmp \leq L[n-1]$ ) return  $tmp \rightarrow O(1)$   
   else return  $L[n-1] \rightarrow O(1)$

$$T(n) = T(n-1) + 1$$

$$T(n) = T(n-1) + 1$$

$$T(n-1) = T(n-2) + 1$$

$$T(n) = T(n-2) + 1 + 1$$

$$T(n-2) = T(n-3) + 1$$

$$T(n) = T(n-3) + 1 + 1 + 1$$

n iter

$$T(n) = O(n)$$

Algorithm 1 and Algorithm 2  
 are the same time complexity  $O(n)$   
 but algorithm 2 has  $O(2n-1)$  time  
 complexity so that it is slower  
 so I choose Algorithm 1.

b) Algorithm  $\text{alg2}(X[1 \dots r])$   
 if  $(l == r)$  return  $X[l] \rightarrow \mathcal{O}(1)$   
 else  
    $\text{flr} = \text{Floor}((l+r)/2) \rightarrow \mathcal{O}(1)$   
    $\text{tmp1} = \text{alg2}(X[1 \dots \text{flr}]) \rightarrow T(n/2)$   
    $\text{tmp2} = \text{alg2}(X[\text{flr}+1 \dots r]) \rightarrow T(n/2)$   
   if  $(\text{tmp1} \leq \text{tmp2})$  return  $\text{tmp1} \rightarrow \mathcal{O}(1)$   
   else return  $\text{tmp2} \rightarrow \mathcal{O}(1)$

$T(n) = 2T(n/2) + 1$   
 using Master Theorem

$$T(n) = aT\left(\frac{n}{b}\right) + f(n)$$

$$T(1) = c$$

$$T(n) = 2T(n/2) + 1 \cdot n^0$$

$$a=2 \quad b=2 \quad d=0$$

$$T(n) = \mathcal{O}(n^{\log_2 2})$$

$$= \mathcal{O}(n) //$$

2)  $p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$  at a given point  $x$ .

The algorithm computes the value of polynomial  $P$  at a given point  $x$

Brute Force Algorithm ( $P[0, n]; x$ )

$a = 0, i = n, j = 1, k = 0$

for  $i$  to 0  $\rightarrow O(n)$

power = 1  $\rightarrow O(1)$

for  $j$  to  $i \rightarrow O(1)$

power = power \*  $x \rightarrow O(1)$

$a = a + P[k] * \text{power} \rightarrow O(1)$

$k++$

return  $a \rightarrow O(1)$

$$T(n) = O(n^2)$$

we can make time complexity better  $n \log n$  or  $n$ , I think we can traverse the polynomial array lowest to highest term in one for loop and we can multiply the power with given  $x$  then we assign to  $a$ ,  $a$  with plus  $P[i]$  multiply with power then we can return  $a$  so time complexity is decreasing from  $O(n^2)$  to  $O(n)$ .

3)

countSubString(str, x, y, n)

totalcount = 0  $\rightarrow O(1)$

countx = 0  $\rightarrow O(1)$

for i to n  $\rightarrow O(n)$

if (str[i] == x)  $\rightarrow O(1)$

countx++  $\rightarrow O(1)$

if (str[i] == y)  $\rightarrow O(1)$

totalcount += countx  $\rightarrow O(1)$

return totalcount  $\rightarrow O(1)$

$T(n) = O(n)$

4) Def `minClosestPoint(P, n)`

`min_val = float('inf')`  $\rightarrow O(1)$

for `i in range(n)`:  $\rightarrow O(n)$

for `j in range(i+1, n)`:  $\rightarrow O(n)$

if `(dist(P[i], P[j], k) < min_val)`:  $\rightarrow O(1)$

`min_val = dist(P[i], P[j], k)`  $\rightarrow O(1)$

return `min_val`

$$T(n) = O(n^2)$$

dist function implementing according to the k dimension  
so I send k only because dist function is given.

---

```

5) a)
Void FindCluster (Arr1[], a1[], a[], Result[]){
    int max_sum = -999; int i = 0; int k = i+2; int result = 0; int l;
    while (i < size) { → O(n^2) → (when k reach the n i increment
        i = 0; → out) one by one so i is increasing
        Arr = List.of(a1[i]); → out every O(n) time later so O(n), O(n)
        max_sum += a[i]; → out increment, size
        Arr[i] = a[i]; i++; → out
        for (int j = i+1; j < k; j++) { → O(n)
            max_sum += a[j];
            Arr[i] = a[j];
            i++;
        }
        if (max_sum > result) { result = max_sum; System.arraycopy(Arr,
            0, Result, i, Arr.length); }
        k++; → out
        if (k == size) { → out
            i++;
            k = i+2;
        }
    }
    print(result); → out
    for (i = 0; i < Result.length; i++) { → out
        print(Result[i]);
    }
}

```

$$T(n) = O(n^2) + O(n) + O(n) + O(1)$$

$$\Rightarrow T(n) = O(n^3)$$