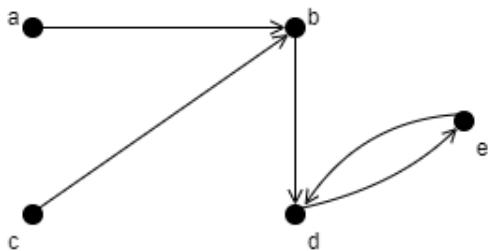


# CENG213 Assignment 1

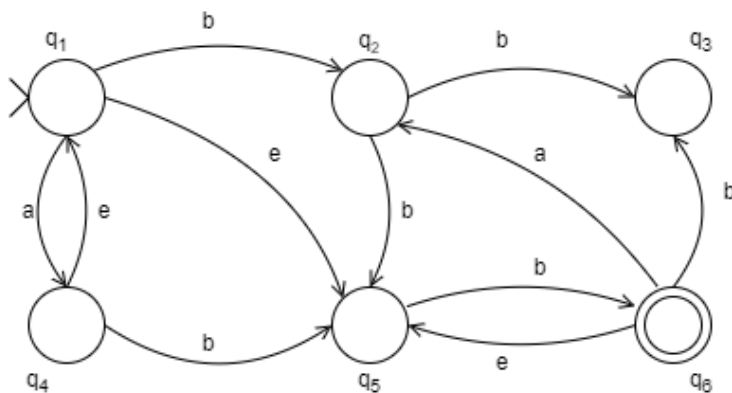
07.11.2023

Due Date: 21.11.2023

- 1) (15 pts) Construct a DFA to accept the following language:  
 $L = \{ w \in \{0,1\}^* : w \text{ has even number of substrings } 101 \}$
- 2) (15 pts) Describe the equivalence classes ( $\approx_L$ ) for the following language:  
 $L = \{ w \in \{0,1\}^* : \text{no three adjacent characters are the same} \}$
- 3) (15 pts) Give a context-free grammar generating the complement of the following language:  
 $L = \{ 0^n 1^m \mid n \geq 0, m \geq 1 \}$
- 4) (15 pts) Design a DFA that recognizes the language  $L$  over the alphabet  $\Sigma = \{0, 1\}$  where  $L$  consists of all strings that, when interpreted as binary numbers, are divisible by 3 (i.e., the binary representation of the number is a multiple of 3).
- 5) (10 pts) Find the transitive closure of the directed graph shown below using the Warshall algorithm.



- 6) (15 pts) Use the state minimization algorithm on the NFA shown below. Show your steps clearly.



- 7) (15 pts) Draw the state diagram for the nondeterministic finite automaton that accepts this language:  $((aba)^* \cup b)^* \cup (aa \cup b^*)^*$