

CENG213 Assignment 2

14.12.2023

Due Date: 28.12.2023

- 1) (20 points) Construct a Turing machine that copies the first four nonblank symbols over the next four nonblank symbols, in reverse order.

Example: $\sqcup a b \sqcup c \sqcup d \sqcup e f \sqcup g h k \sqcup \rightarrow \sqcup a b \sqcup c \sqcup d \sqcup d c \sqcup b a k \sqcup$

- 2) (20 points) Construct a standard Turing machine to decide the language $(aa)^*c(bb)^*$
- 3) (20 points) Let G be the grammar (W, Σ, R, S) , where

$$W = \{S, A, N, V, P\} \cup \Sigma,$$

$$\Sigma = \{\text{elephant, big, mouse, small, chased}\},$$

$$R = \{P \rightarrow N,$$

$$P \rightarrow AP,$$

$$S \rightarrow PVP,$$

$$A \rightarrow \text{small},$$

$$A \rightarrow \text{big},$$

$$N \rightarrow \text{elephant},$$

$$N \rightarrow \text{mouse},$$

$$V \rightarrow \text{chased}\}.$$

Draw a parse tree for the following example string: "big mouse chased small elephant".
Is this grammar ambiguous? Explain your reasoning.

- 4) (20 points) Construct a pushdown automaton for the following language:
 $\{a^i b^j c^k \mid i, j, k \geq 0, i + k = j\}$
- 5) (20 points) Construct a pushdown automaton for the following language:
 $\{a^i b^j c^k d^m \mid i, j, k, m \geq 0, i = k \text{ or } j = m\}$