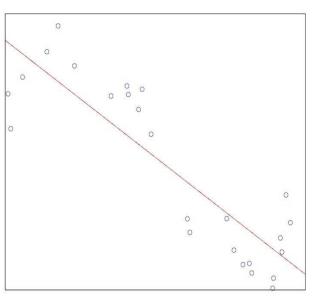
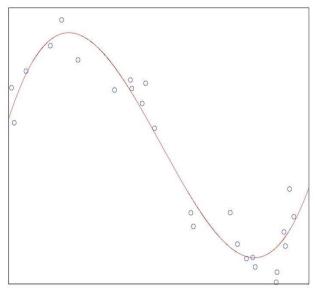
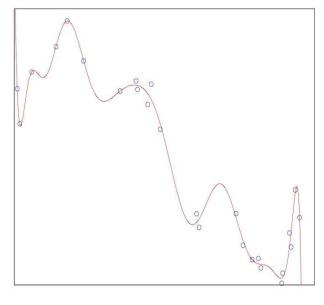
• Bias Variance trade-off

• Bias Variance trade-off





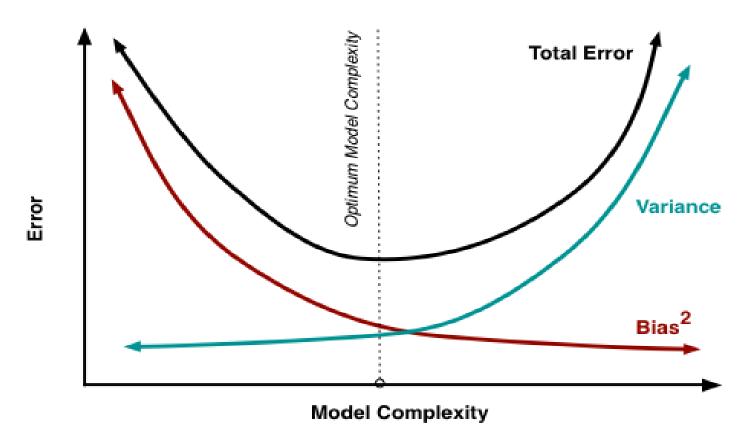


underfit (degree = 1)

ideal fit (degree = 3)

overfit (degree = 20)

• Bias Variance trade-off



Score function for model selection

Score function for model selection

score(model) = error(model) + penalty-function(model)

## **Akaike Information Criterion**

## **Akaike Information Criterion**

#### Maximum likelihood case

$$AIC = -2 \log \mathcal{L}(\hat{\theta}|y) + 2k$$
 bias variance

- $\mathbf{\nabla} \mathcal{L}$ : likelihood function.
- $\nabla \hat{\theta}$ : maximum likelihood estimate of  $\theta$ .
- $\nabla$  k: number of estimated parameters (including the variance).
- $\nabla$  y is the random sample from the density function f(x).

# **Bayesian Information Criterion**

# **Bayesian Information Criterion**

$$\mathrm{BIC} = -2 \cdot \ln L + k \ln(n)$$

- ▼ L: likelihood function
- ▼ k: number of parameters
- n: number of observations