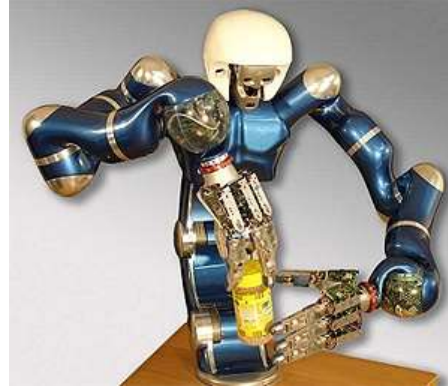
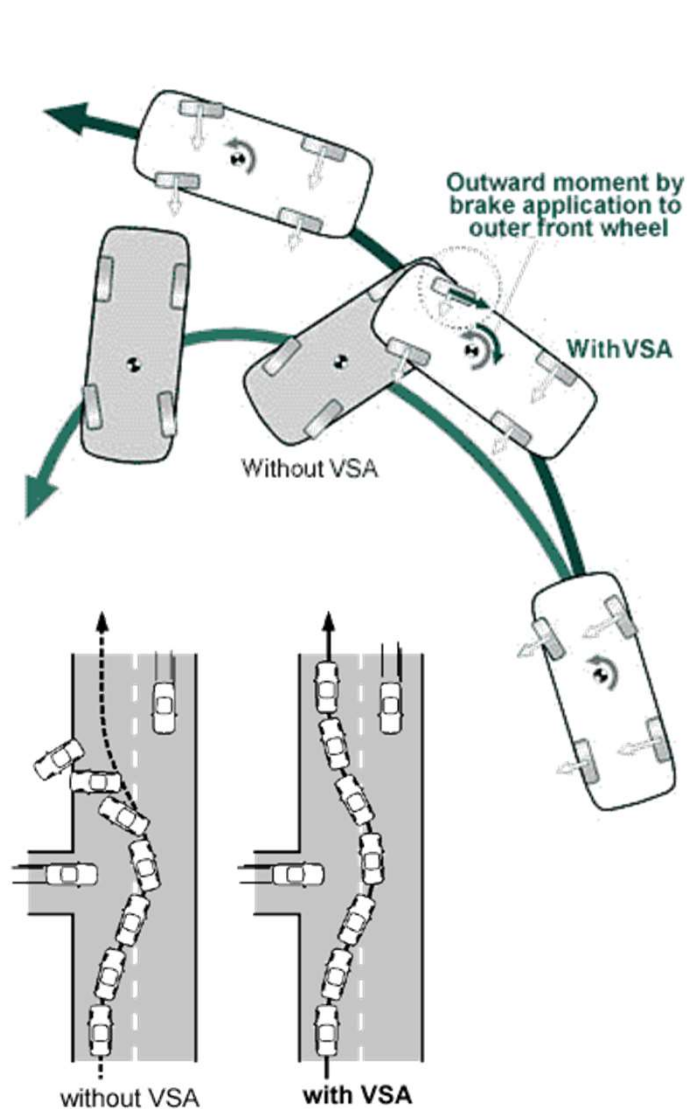


Control System Design for Automated Driving

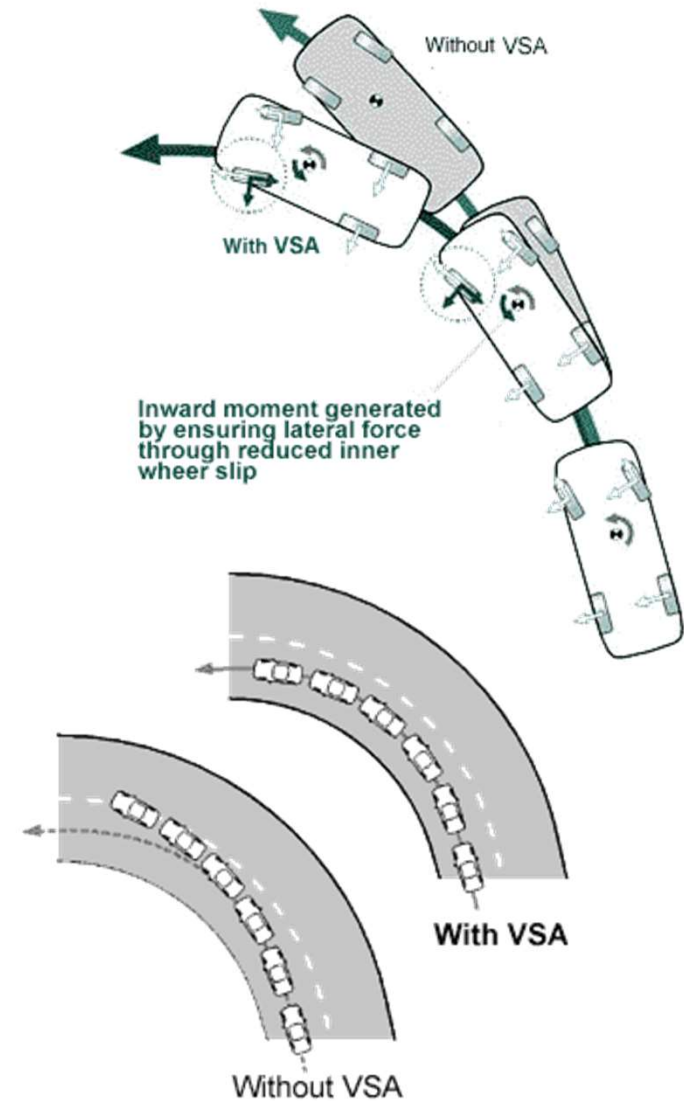
Lecture 08



ESP Control Example



► Oversteer Control



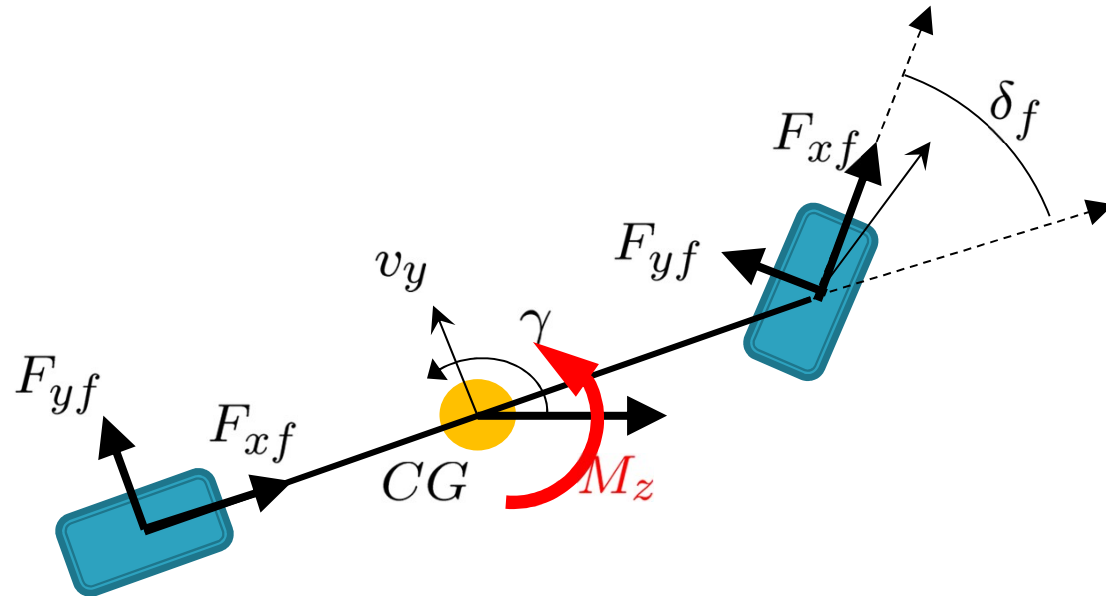
► Understeer Control

<https://www.youtube.com/watch?v=LVz9f5WQhCI>

Bicycle Model with Compensating Yaw Moment

$$\dot{v}_y = \frac{1}{m}(F_{yf} + F_{yr}) - v_x \gamma$$

$$\dot{\gamma} = \frac{1}{I_{zz}}(l_f F_{yf} - l_r F_{yr} + \boxed{M_z})$$



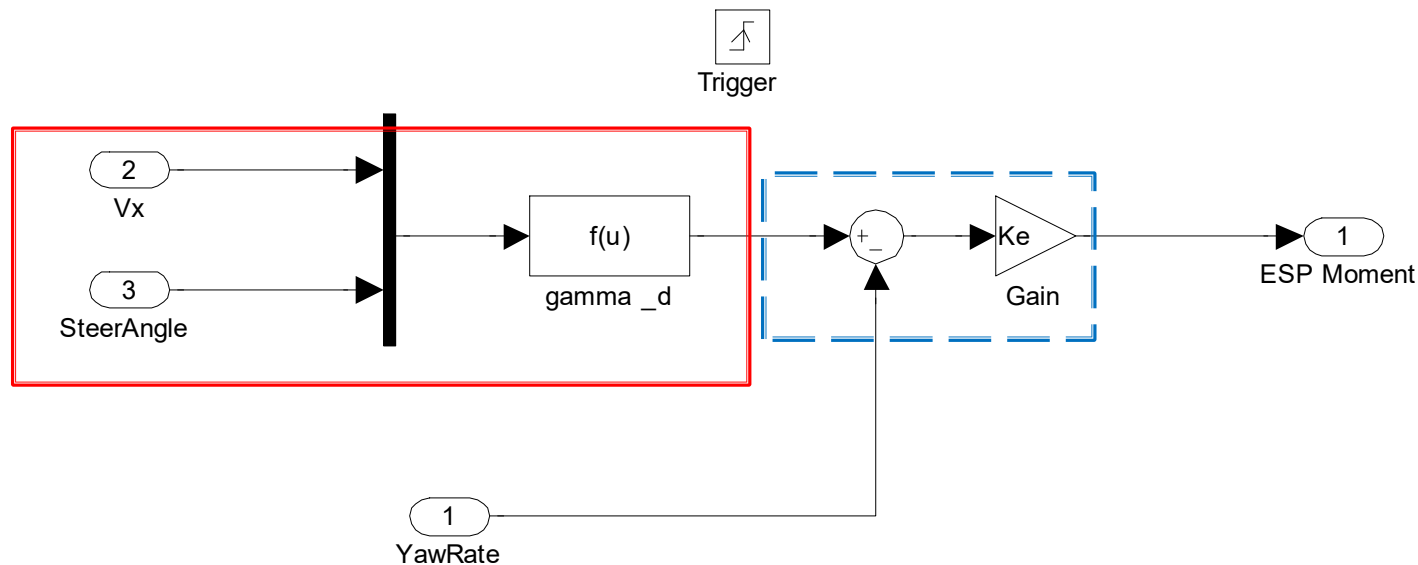
ESP Logic

▶ ESP logic

- Desired Yaw Rate
- proportional control

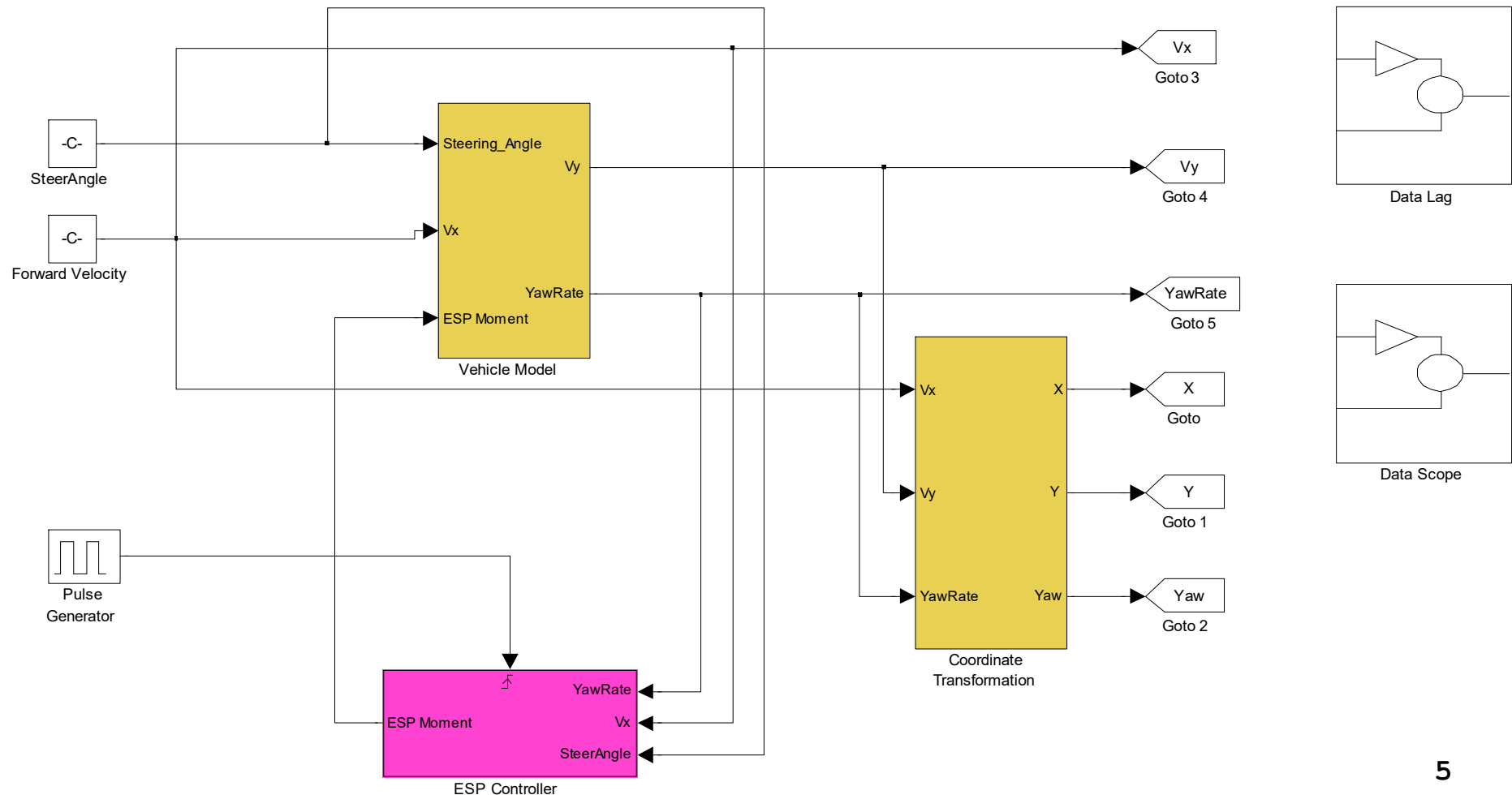
$$\gamma_d = \frac{v_x}{l - \frac{m}{2l} \left(\frac{l_f C_f - l_r C_r}{C_f C_r} \right) v_x^2} \delta_f$$

$$M_z = K_e (\gamma_d - \gamma)$$



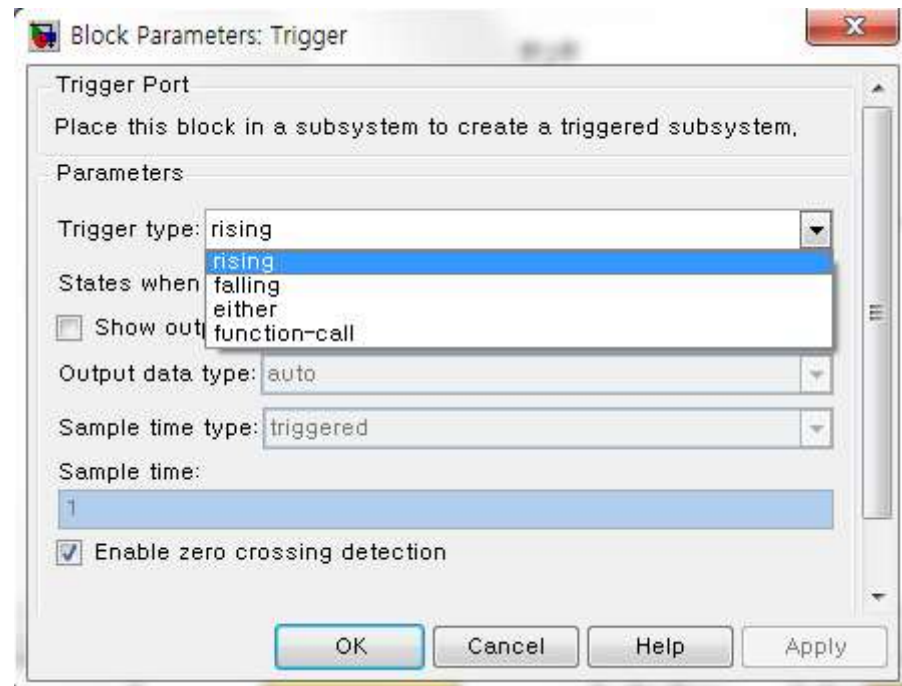
Vehicle Lateral Model with Controller

- ▶ Open vehicle_lateral_model_controller.mdl file.
- ▶ Additional “ESP Controller” block is attached on the vehicle model



Trigger Subsystem

- ▶ “Trigger” block is added in the “ESP controller” subsystem for more “realistic” simulation.
- ▶ Trigger block enables the subsystem only when the trigger condition is satisfied.
- ▶ After the system output is calculated, the same output is held until the next triggering event.

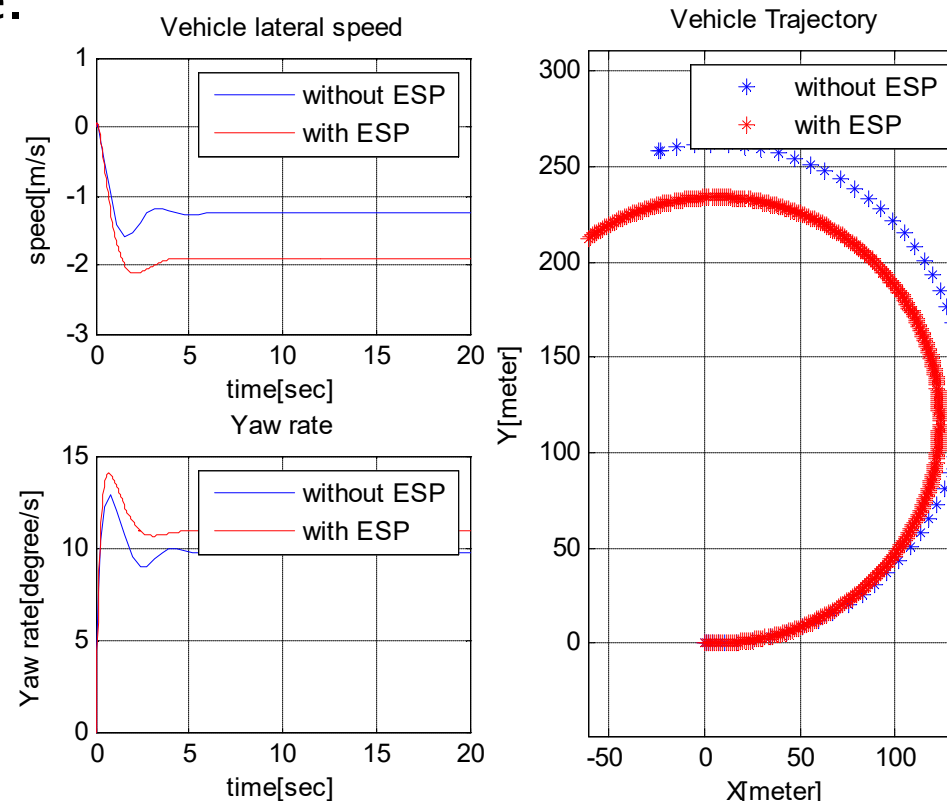


Run two simulations and compare results

- ▶ Comparison of the simulation results with and without ESP control.
- ▶ However, the variable saved in the workspace will be erased after the second simulation starts.
- ▶ Use “sim” command to run simulation by Matlab command.’
- ▶ In “run_two_simulations.m” file
 - `sim('vehicle_lateral_model',Tfinal);`

Run two simulations and compare results

- ▶ Comparison of the simulation results.
- ▶ Data size is different due to addition of “Triggered Subsystem”.
 - Continuous time system + Discrete time system
 - Variable-step solver → Fixed step solver increases number of sampling time.



Trajectory Tracking Problem

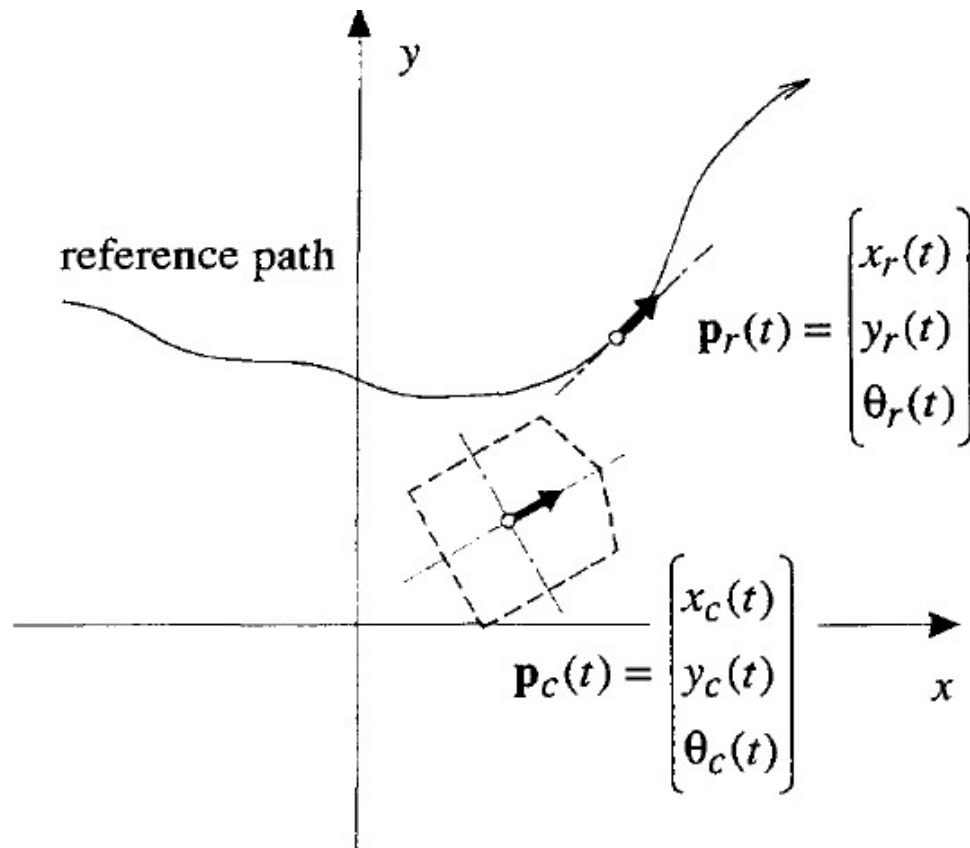


Fig. 1 Reference and Current Postures

제어목표

차량이 원하는 궤적
(경로) $p_r(t)$ 를 추종하
도록 차량속도와 조
향각을 제어

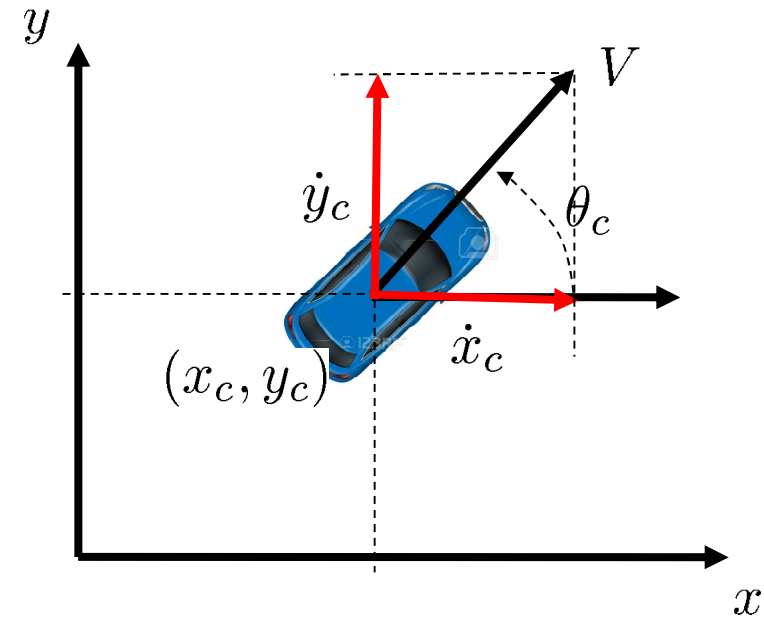
Goal

- Kinematic Equation

$$\begin{aligned}\dot{x}_c &= V \cos(\theta_c) \\ \dot{y}_c &= V \sin(\theta_c) \\ \dot{\theta}_c &= \omega\end{aligned}\quad \begin{bmatrix} \dot{x}_c \\ \dot{y}_c \\ \dot{\theta}_c \end{bmatrix} = \begin{bmatrix} \cos \theta_c & 0 \\ \sin \theta_c & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} v_c \\ w_c \end{bmatrix}$$

- Control Inputs

: Velocity (V), Turn rate (ω)



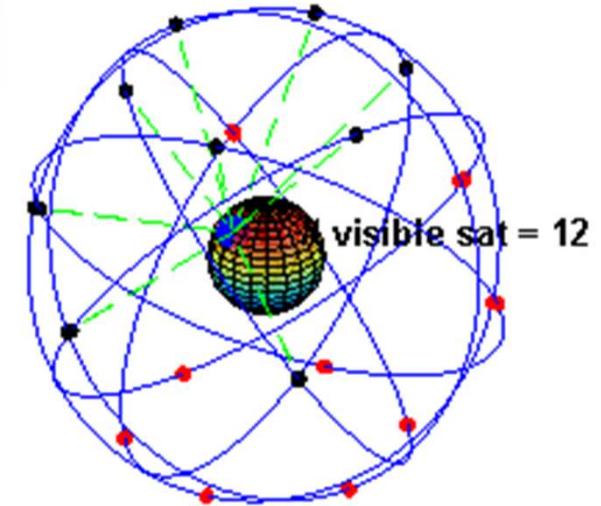
DGPS Sensor



ProPak-V3

Position Accuracy

Single Point L1	1.8 m CEP
Single Point L1/L2	1.5 m CEP
WAAS L1 only	1.2 m CEP
WAAS L1/L2	0.8 m CEP
DGPS	0.45 m CEP
CDGPS	0.7 m CEP
OmniSTAR	
VBS	1.0 m CEP
XP	0.15 m CEP
HP	0.10 m CEP
RT-20 ²	0.2 m CEP
RT-2	1 cm + 1ppm CEP



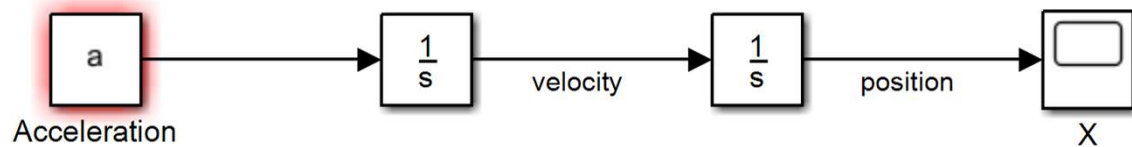
Physical & Electrical

Size	185 x 160 x 71 mm
Weight	1.0 kg
Power	
Input Voltage ⁹	+9 to +18 VDC
Power Consumption	2.2 W (typical) ¹⁰

circular error probable (CEP) (also **circular error probability** or **circle of equal probability**) is a measure of a weapon system's [precision](#). It is defined as the radius of a circle, centered about the mean, whose boundary is expected to include the landing points of 50% of the [rounds](#).

- From Wikipedia.org -

Inertial Navigation Sensor (INS)



Example)

$$a = 0.1 \text{ m/s}^2 \rightarrow D = 0.5 \cdot a \cdot t^2 \rightarrow \text{1분후 오차 180m !!}$$

Output

3D orientation (Quaternions/Matrix/Euler angles)
 3D acceleration
 3D rate-of-turn
 3D earth-magnetic field (normalized)
 Temperature

Orientation performance

Dynamic Range:
 Angular Resolution¹:
 Static Accuracy (Roll/Pitch):
 Static Accuracy² (Heading):
 Dynamic Accuracy³:

all angles in 3D
 0.05 deg
 <0.5 deg
 <1 deg
 2 deg RMS

Sensor performance

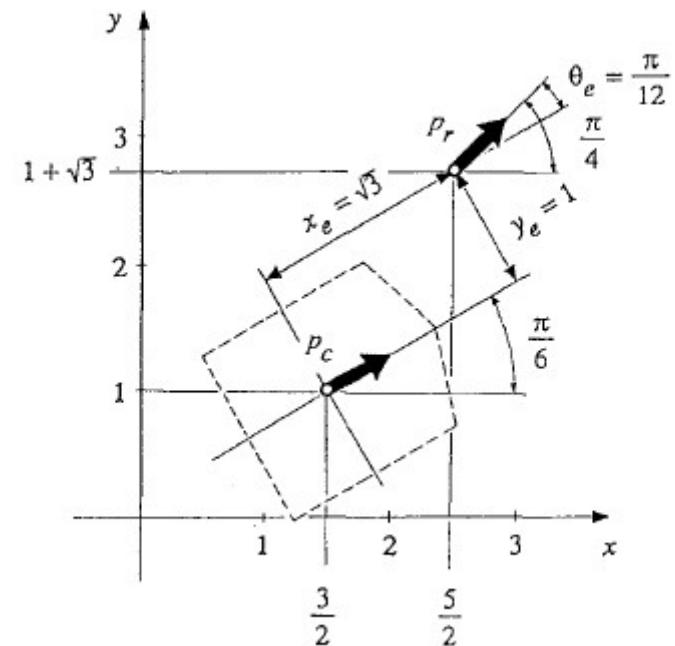
	rate of turn	acceleration	magnetic field	temperature
Dimensions	3 axes	3 axes	3 axes	-
Full Scale (standard)	± 300 deg/s	± 17 m/s ²	± 750 mGauss	-55...+125 °C
Linearity	0.1% of FS	0.2% of FS	0.2% of FS	<1% of FS
Bias stability ⁴ (1σ)	5 deg/s	0.02 m/s ²	0.5 mGauss	0.5 °C accuracy
Scale Factor stability ⁴ (1σ)	-	0.05%	0.5%	-
Noise density	0.1 deg/s/√Hz	0.001 m/s ² /√Hz	0.5 mGauss (1σ)	-
Alignment error	0.1 deg	0.1 deg	0.1 deg	-
Bandwidth (standard)	40 Hz	30 Hz	10 Hz	-

Error Postures

- Error posture Definition

$$\mathbf{p}_e = \begin{bmatrix} x_e \\ y_e \\ \theta_e \end{bmatrix} = \begin{bmatrix} \cos\theta_c & \sin\theta_c & 0 \\ -\sin\theta_c & \cos\theta_c & 0 \\ 0 & 0 & 1 \end{bmatrix} (\mathbf{p}_r - \mathbf{p}_c) \equiv T_e(\mathbf{p}_r - \mathbf{p}_c)$$

- x_e : 종방향 오차
- y_e : 횡방향 오차
- θ_e : 각도 오차



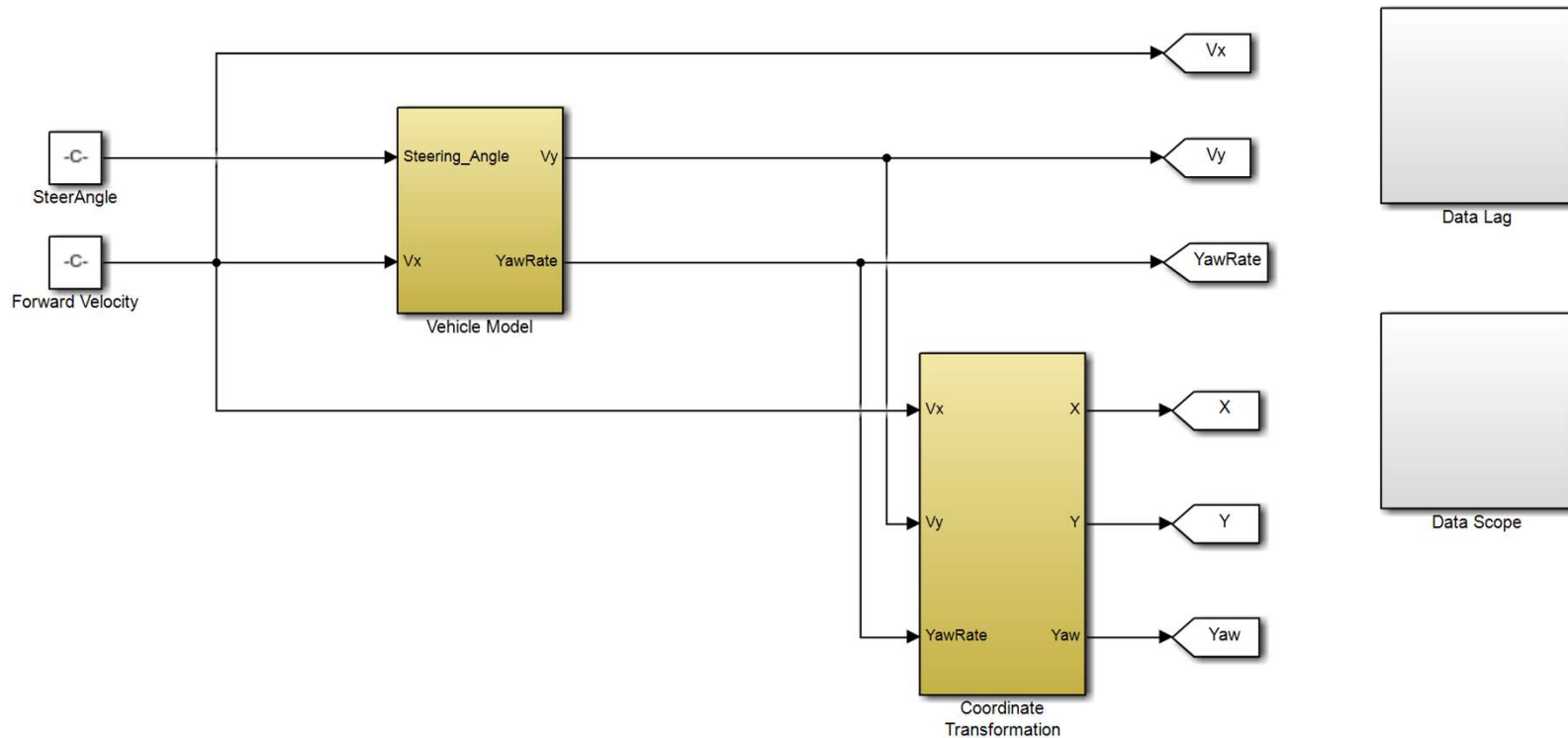
- Control Input Calculation
 - Control Inputs

$$\mathbf{q} = \begin{bmatrix} v \\ \omega \end{bmatrix} = \begin{bmatrix} v(\mathbf{p}_e, \mathbf{q}_r) \\ \omega(\mathbf{p}_e, \mathbf{q}_r) \end{bmatrix} = \begin{bmatrix} v_r \cos\theta_e + K_x x_e \\ \omega_r + v_r (K_y y_e + K_\theta \sin\theta_e) \end{bmatrix}$$

- V_r : reference velocities
- W_r : reference angular velocities
- If you don't have V_r or W_r , let
 $V_r = W_r = 0$
and determine the gain by trial and error.

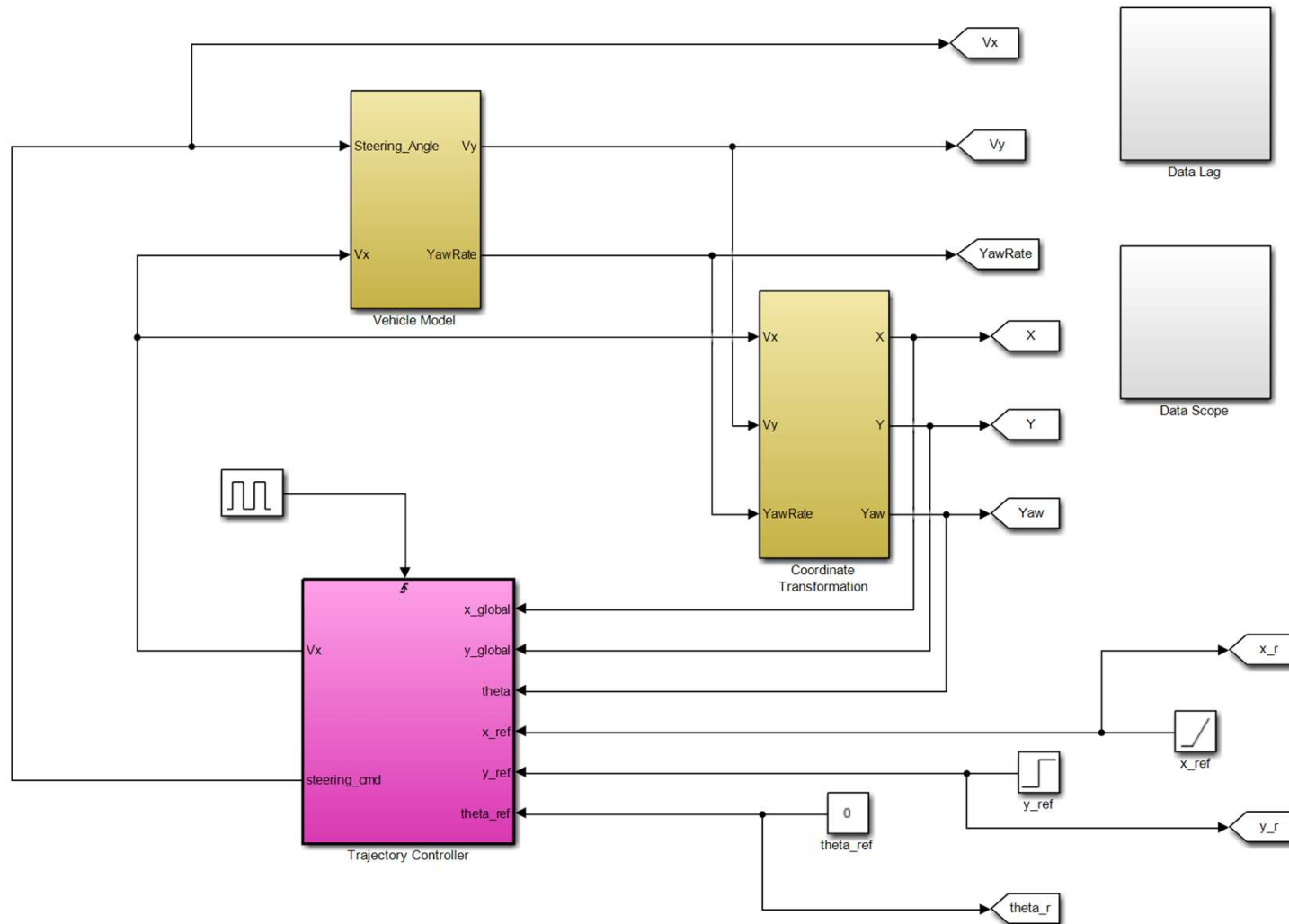
Plant Model

- Simulink Model of Vehicle Kinematics
 - Vehicle Lateral Dynamics



Plant Model

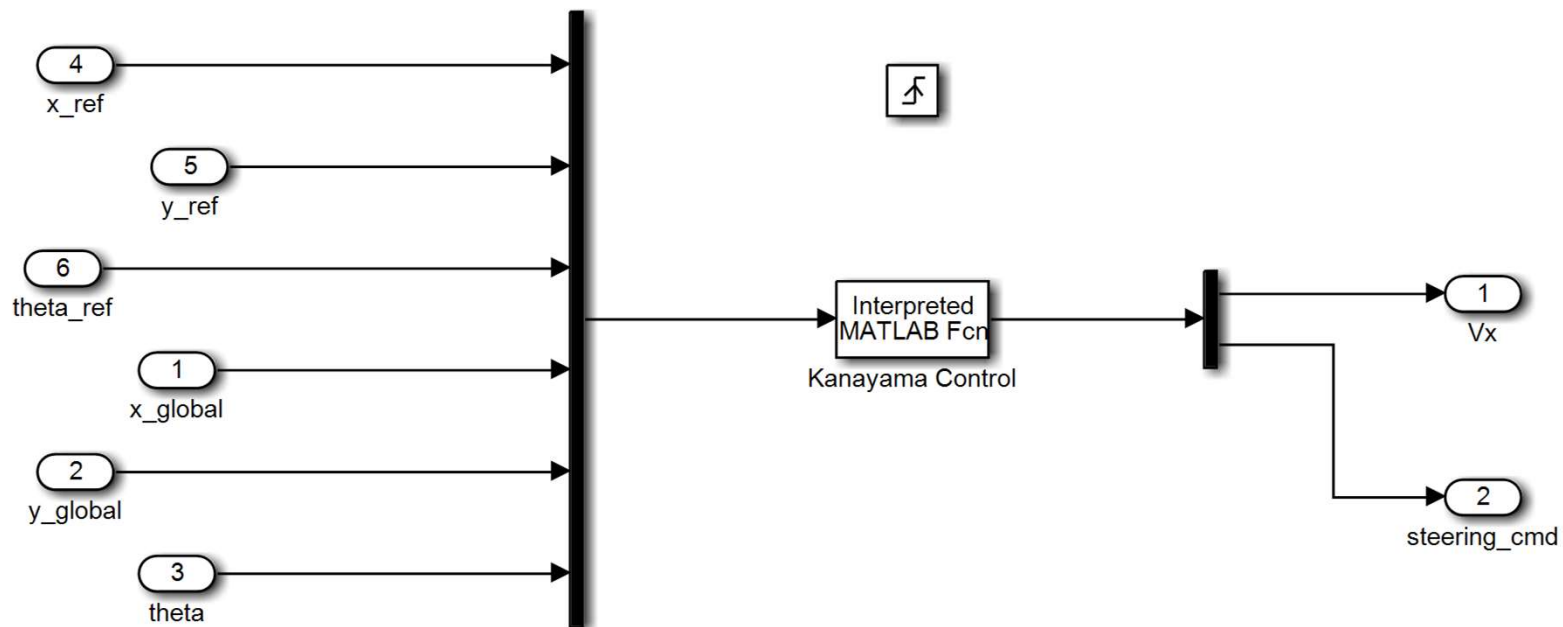
- Vehicle Model with Trajectory Controller




Plant Model with Controller

- Controller (V_r and W_r are ignored for simplicity)

$$\mathbf{q} = \begin{bmatrix} v \\ \omega \end{bmatrix} = \begin{bmatrix} v(\mathbf{p}_e, \mathbf{q}_r) \\ \omega(\mathbf{p}_e, \mathbf{q}_r) \end{bmatrix} = \begin{bmatrix} v_r \cos \theta_e + K_x x_e \\ \omega_r + v_r (K_y y_e + K_\theta \sin \theta_e) \end{bmatrix}$$



Interpreted Matlab Function Block

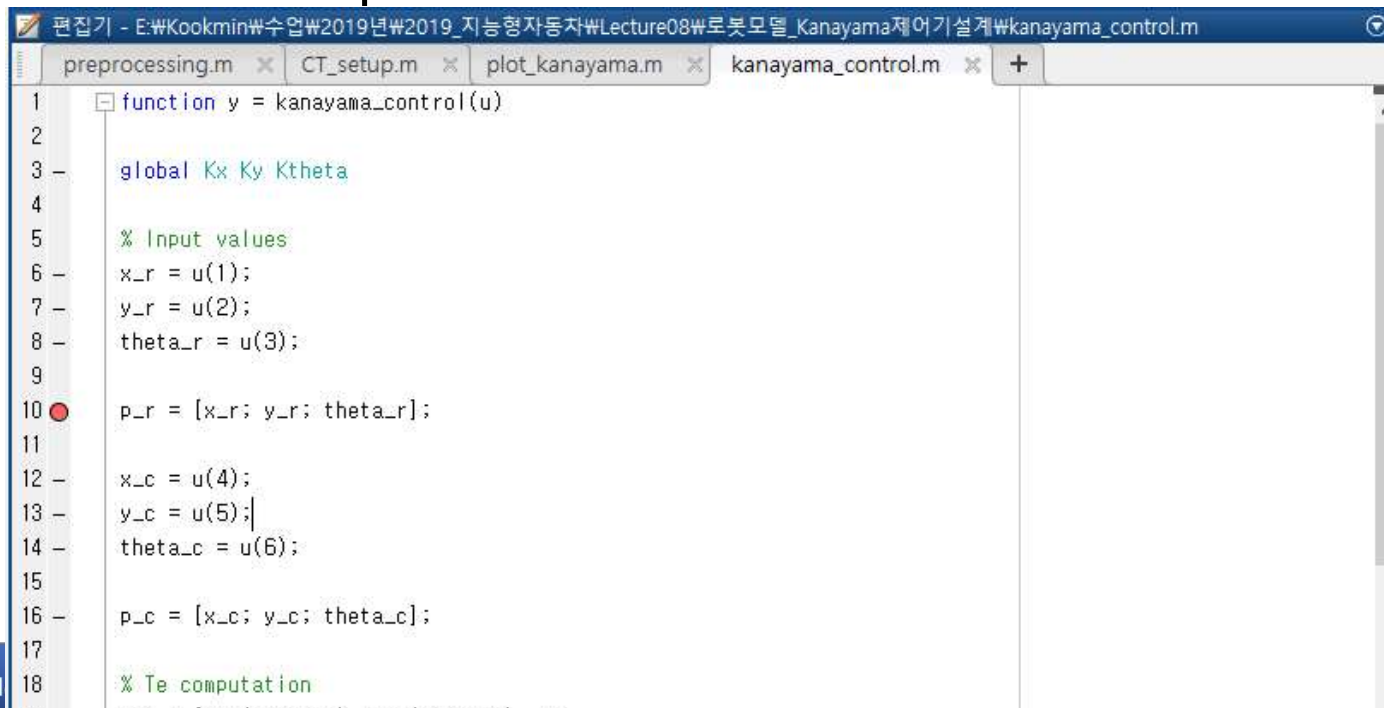
- User-defined Functions Library 
- Applies the specified Matlab function or expression to the input.
- The output of the function must match the output dimensions of the block

Interpreted Matlab Function Block

- In particular, when you want to implement a controller that is too complicated to calculate using atomic Simulink blocks.
- For Automatic C code generation, use Matlab Function block instead. Matlab Function block requires more strict programming rules for code generation in general.
- However, in this example, interpreted Matlab function block is used to employ global variable Kx, Ky, Ktheta.

Interpreted Matlab Function Block

- Debugging Tool
 - break point
 - Click next to the line number, where you would like to stop the program during the simulation.
 - Run the simulation, then the simulation will stop at the break point line



The screenshot shows the MATLAB editor window with the file `kanayama_control.m` open. The code is as follows:

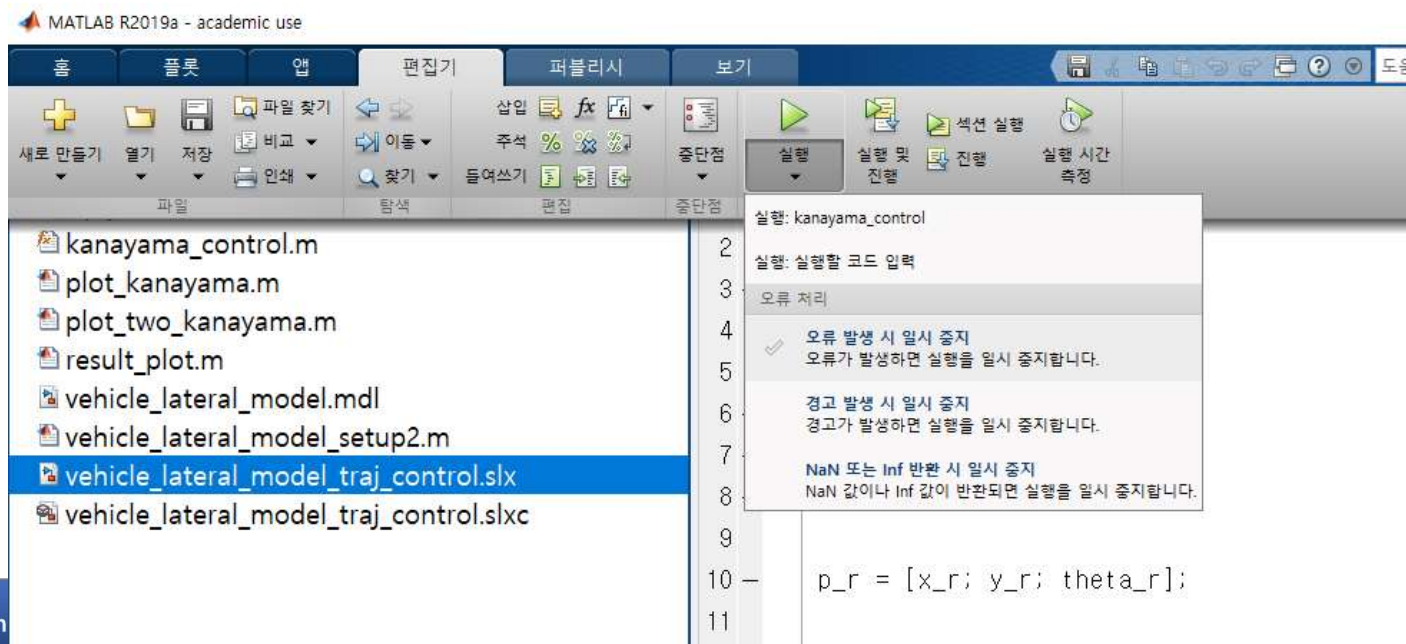
```
1 function y = kanayama_control(u)
2
3 global Kx Ky Ktheta
4
5 % Input values
6 x_r = u(1);
7 y_r = u(2);
8 theta_r = u(3);
9
10 p_r = [x_r; y_r; theta_r];
11
12 x_c = u(4);
13 y_c = u(5);
14 theta_c = u(6);
15
16 p_c = [x_c; y_c; theta_c];
17
18 % Te computation
```

A red circle, indicating a break point, is placed next to line 10. The top of the window shows several tabs: `preprocessing.m`, `CT_setup.m`, `plot_kanayama.m`, and `kanayama_control.m`.

- Debugging Tool
 - break point
 - Press F10 to progress one line
 - Press F11 to step into the function
 - Press F5 to continue
 - Press "디버그중지" to stop the code
 - More break points can be added after the stop.

Interpreted Matlab Function Block

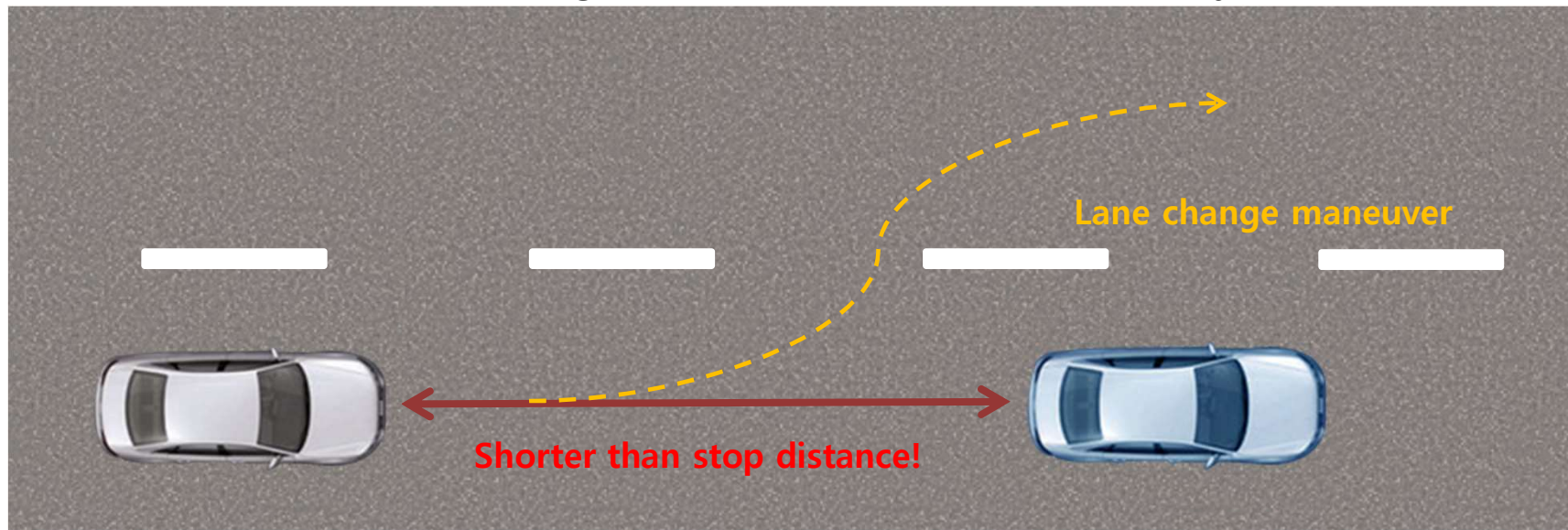
- Debugging Tool
 - “오류발생시 일시중지” Option
 - Stops running the code at the line where the error occurs.
 - “경고 발생시 일시중지” Option
 - “Nan 또는 Inf 반환시 일시중지” Option



Simulation Scenario

<Autonomous Emergency Steering (AES) System>

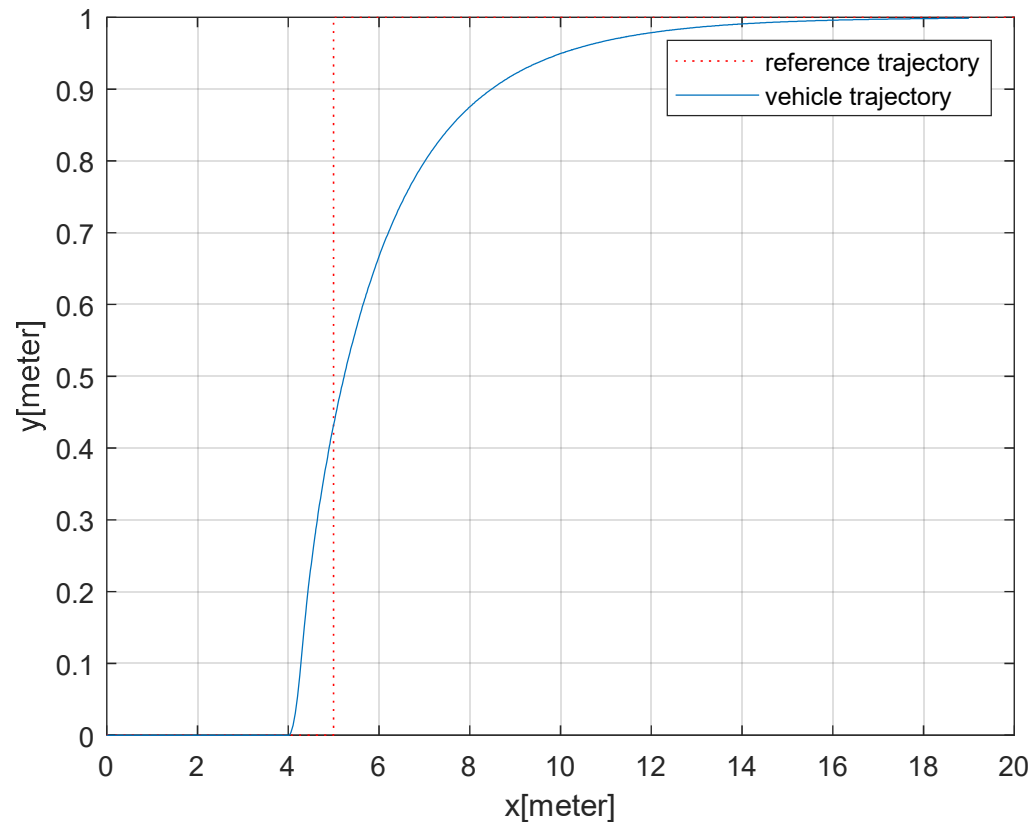
- Avoiding Rear-End collision that AEB cannot avoid.
- During the scenario, the desired lane switches to the next lane when the AES is activated.
- Control **wheel steering angle** & **forward velocity**.
- Assumption : The vehicle can identify the location of the nearby obstacles and make decision that switching to the next lane is the safest way to avoid collision.



<Emergency lane change maneuver>

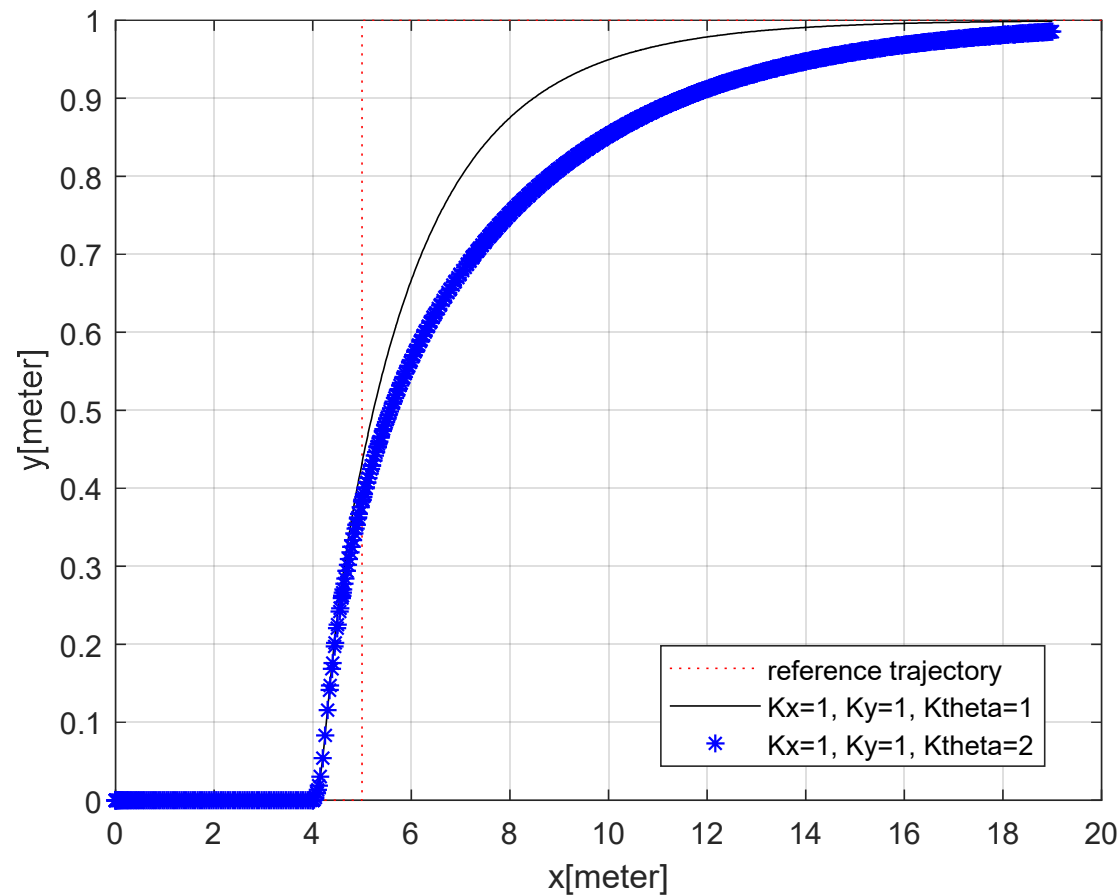
Simulation Result

- Simple Implementation with $K_x = K_y = K_{\theta} = 1$.



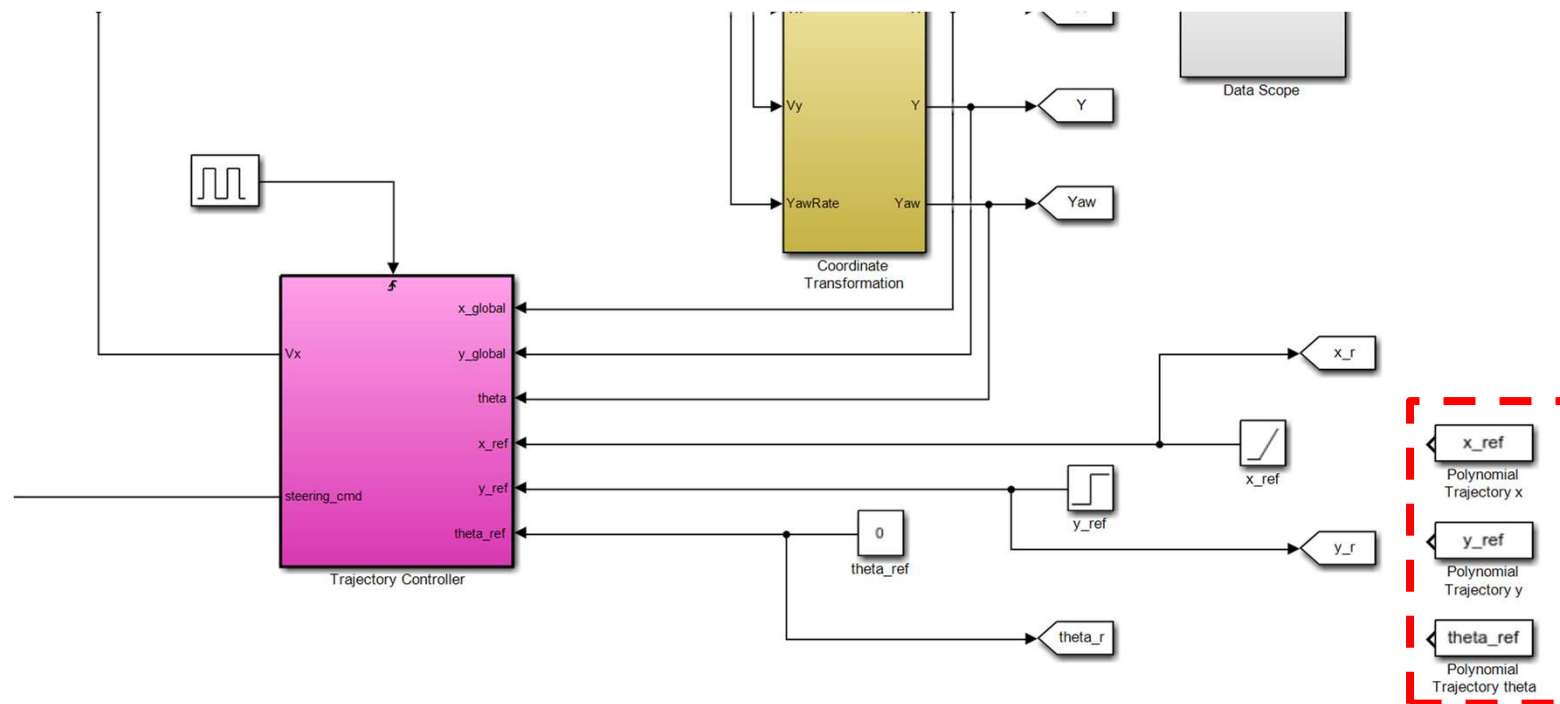
Simulation Results Comparison

- Run with different K gains to compare results



Reference Trajectory Generation

- Use From Workspace blocks to generate a reference x , y , θ trajectory for Kanayama Controller .



- Structure Format Data Generation Example
 - Reference Trajectory Definition

$$Y = 0.01 \times X(X - 5)(X - 10)$$

% Reference Trajectory Generation

```
time = 0:0.1:t_final;
```

```
x_ref.time = time';
```

```
y_ref.time = time';
```

```
theta_ref.time = time';
```

```
x_ref.signals.values = time';
```

```
y_ref.signals.values = [0.01*time.*(time-5).*(time-10)]';
```

```
dx = diff(x_ref.signals.values);
```

```
dy = diff(y_ref.signals.values);
```

```
theta_ref.signals.values = atan2(dy, dx);
```

```
theta_ref.signals.values = [theta_ref.signals.values; theta_ref.signals.values(length(time)-1)];
```

Reference Trajectory Generation

- Simulation Result

