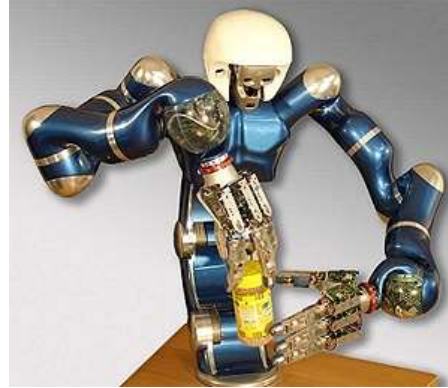


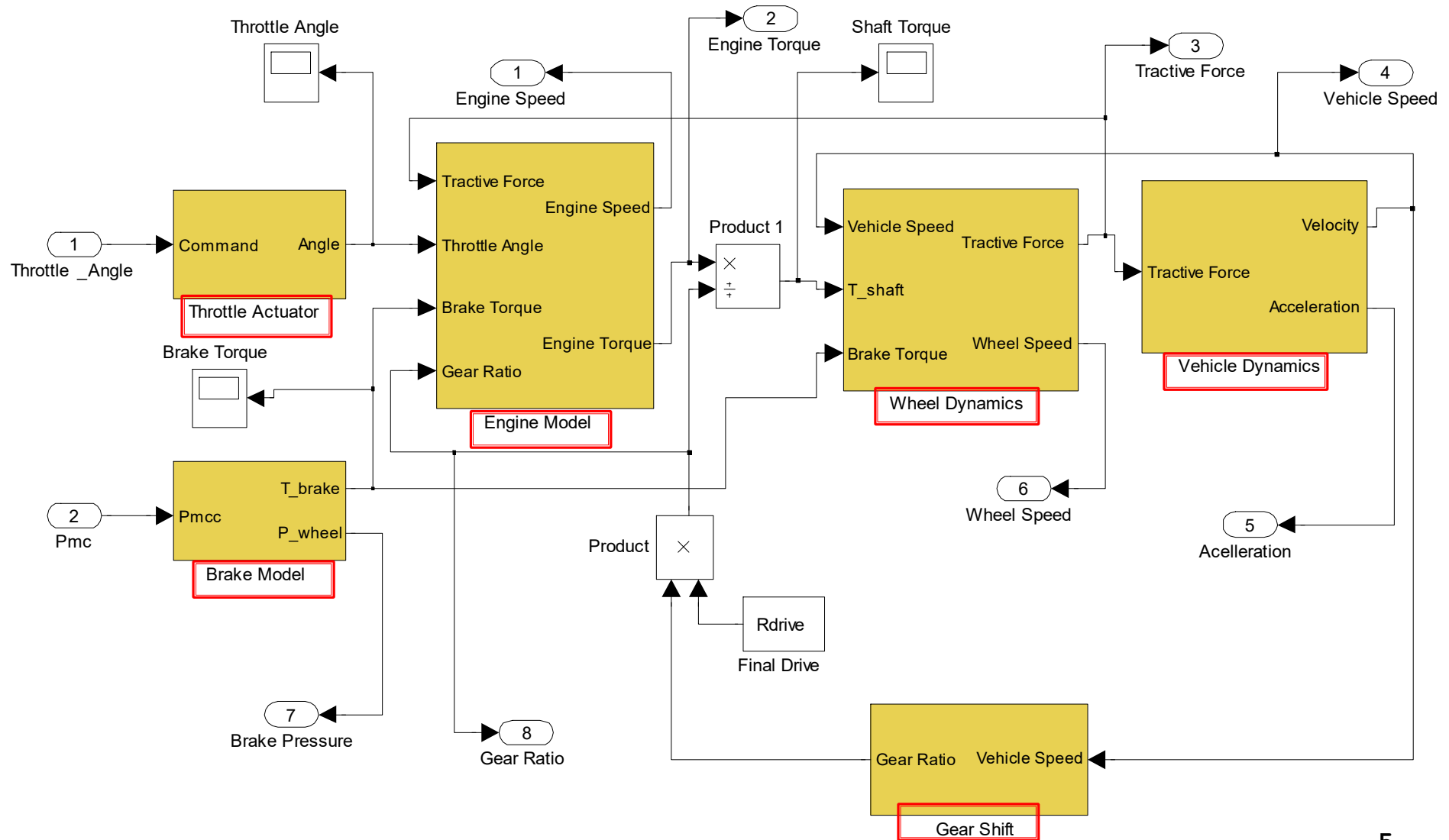
# Control System Design for Automated Driving

## Lecture 05



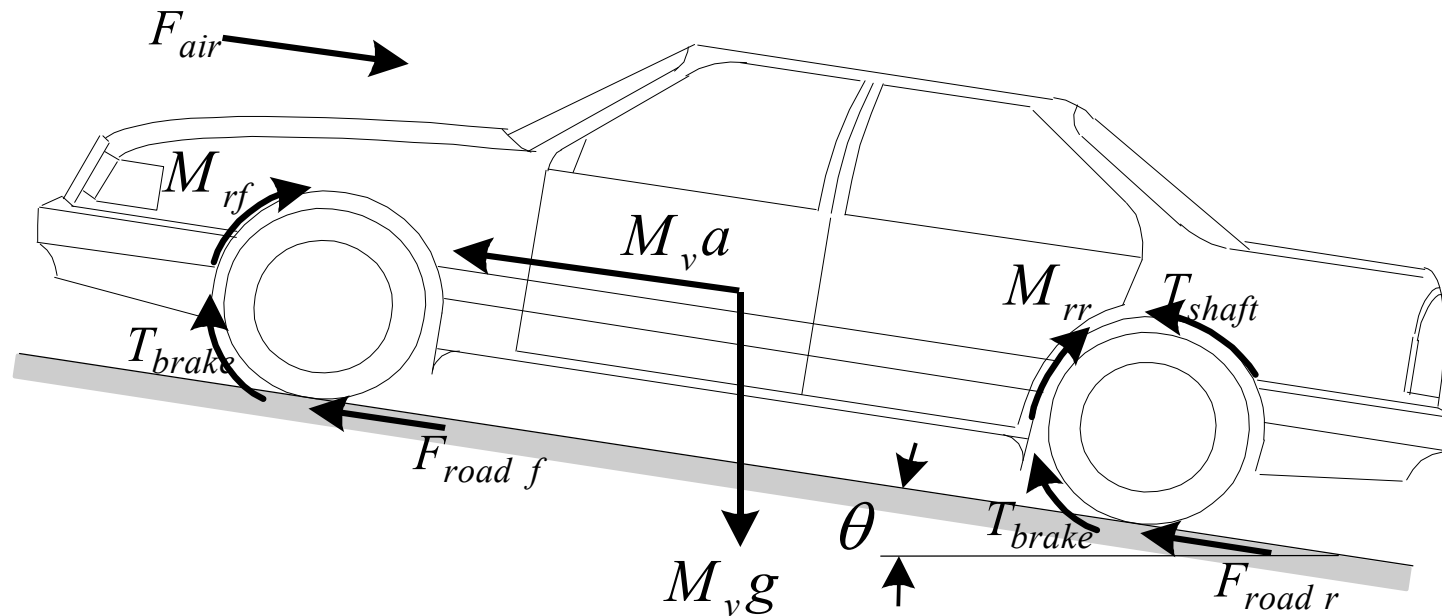
# Simulink Model of Vehicle Longitudinal Dynamics

# Simulink Model of Vehicle Longitudinal Dynamics



# Longitudinal Vehicle & Wheel Dynamics

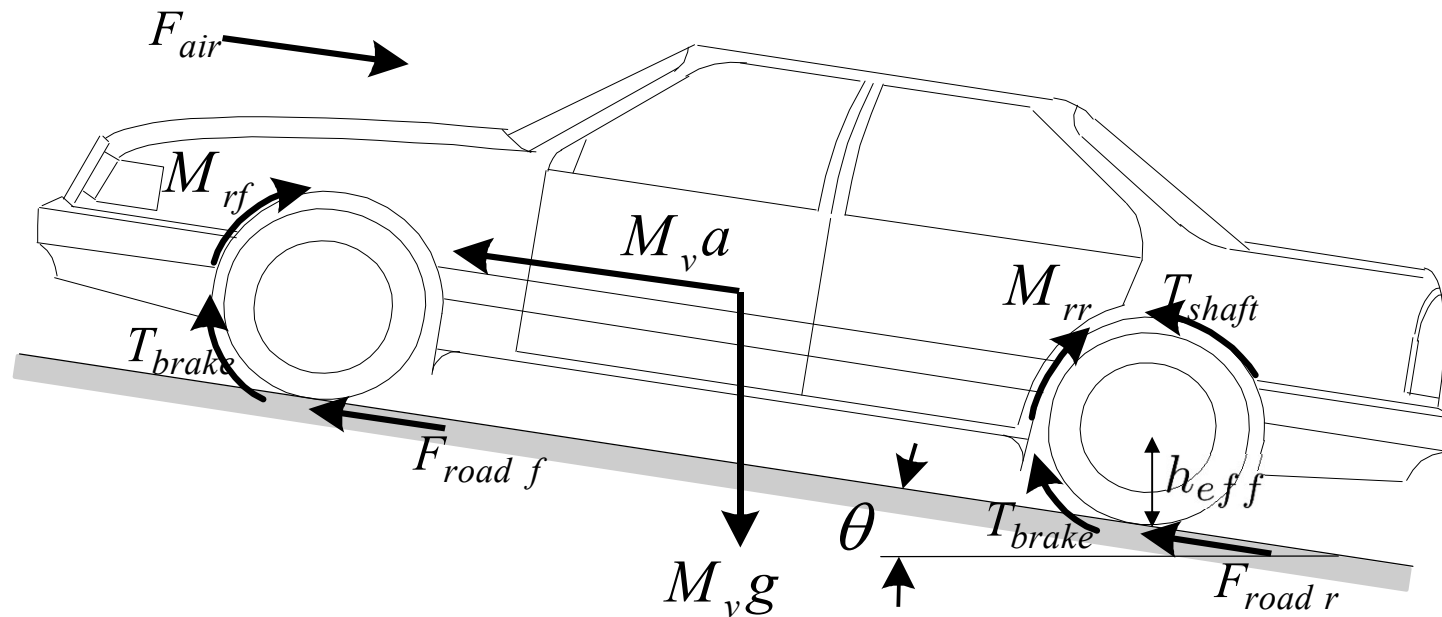
- ▶ Aerodynamic Drag  $F_{air} = \frac{\rho}{2} C_d A_f v^2$
- ▶ Rolling Resistance  $F_{roll} = \text{constant}$
- ▶ Road Traction Force  $F_{road}$  from Tire Model
- ▶ Brake Torque  $T_{brake}$  from Brake Model
- ▶ Shaft Torque  $T_{shaft}$  from Engine & Transmission Model



# Longitudinal Vehicle & Wheel Dynamics

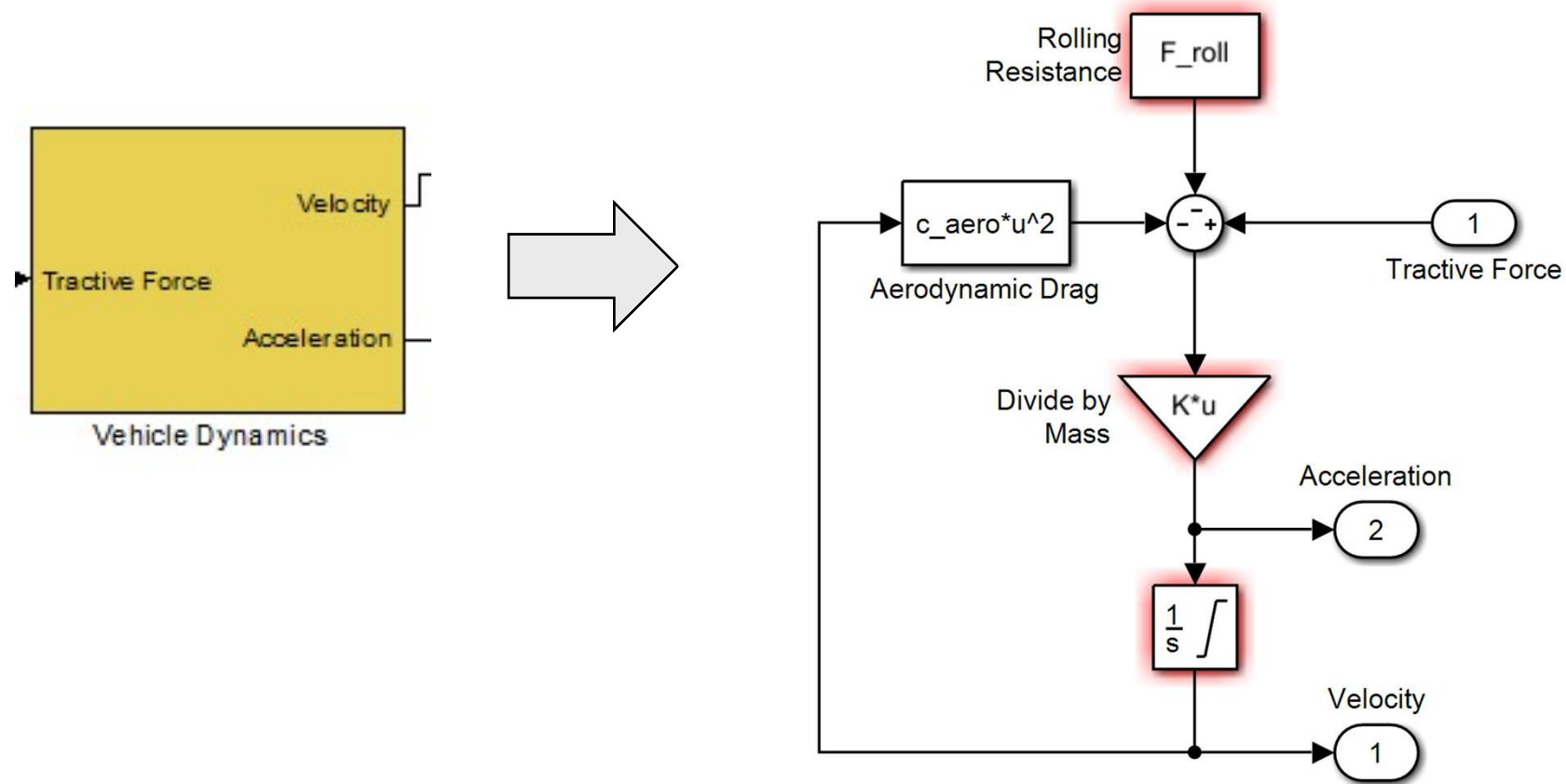
## ► Nonlinear Longitudinal Vehicle Dynamics

- Vehicle Dynamics  $M\dot{v} = F_{road} - F_{roll} - F_{air} - Mg \sin \theta$
- Wheel Dynamics  $J_{\omega}\dot{\omega} = T_{shaft} - T_{brake} - h_{eff}F_{road}$



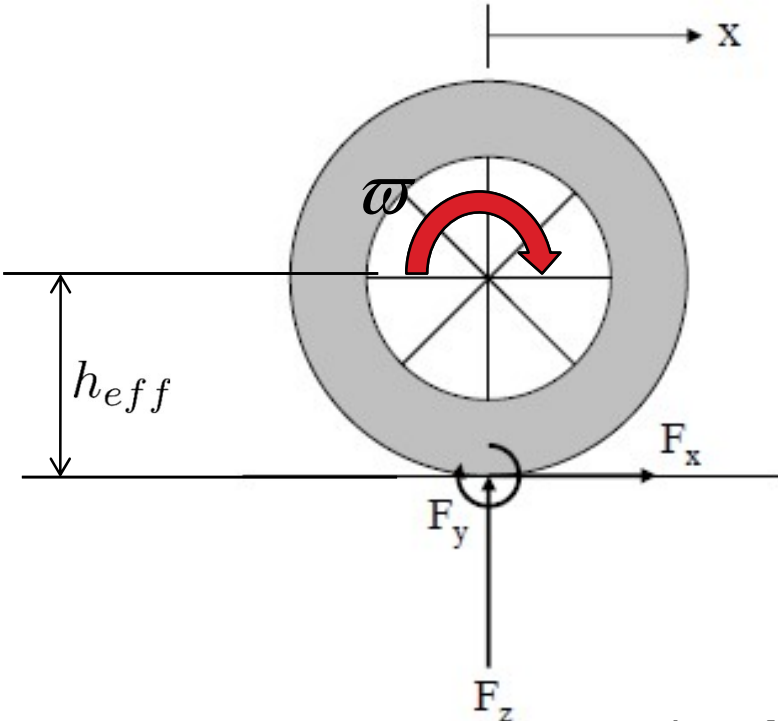
# Longitudinal Vehicle Dynamics

- ▶ Simulink Model of  $M\dot{v} = F_{road} - F_{roll} - F_{air} - Mg \sin \theta$   
(with  $\theta = 0$  )



# Tire Model

- ▶ Tire Road Force  $F_{road}$  is usually modeled by empirical relationship between slip and force.
- ▶ Definition of Longitudinal Tire Slip ratio

$$s = \frac{h_{eff}\omega - v}{\max(h_{eff}\omega, v)}$$


The diagram illustrates a tire model. A gray ring represents the tire, with a red curved arrow inside indicating angular velocity  $\omega$ . A horizontal line represents the road surface, with a vertical double-headed arrow labeled  $h_{eff}$  indicating the effective height. A horizontal arrow labeled  $x$  points to the right. At the contact point, three force vectors are shown:  $F_x$  (horizontal, pointing right),  $F_y$  (vertical, pointing up), and  $F_z$  (vertical, pointing down).

Tire Slip 관련 영상

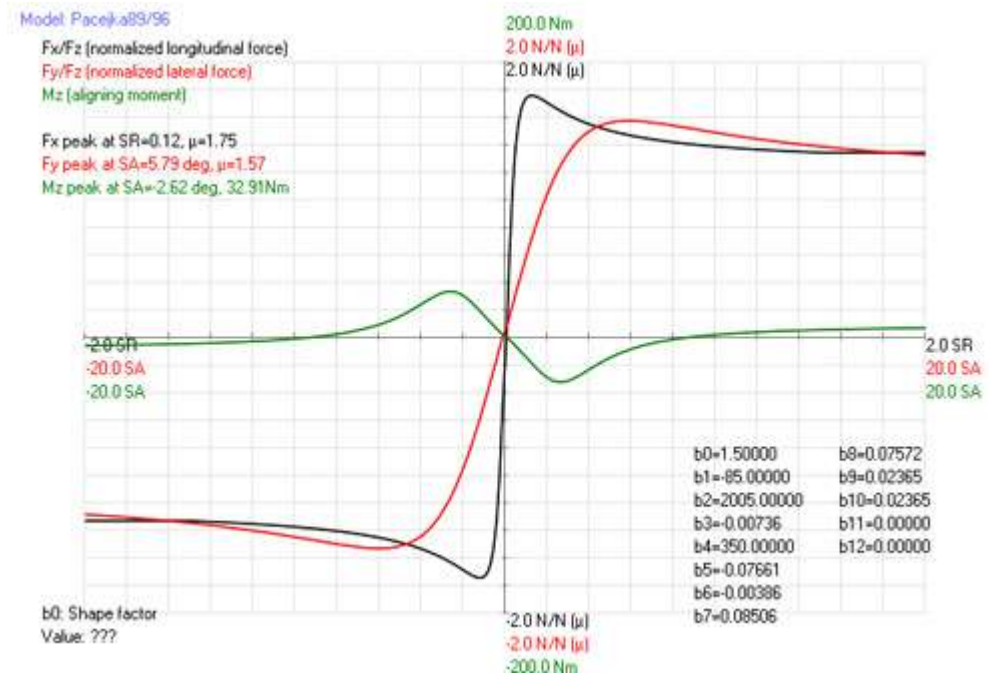
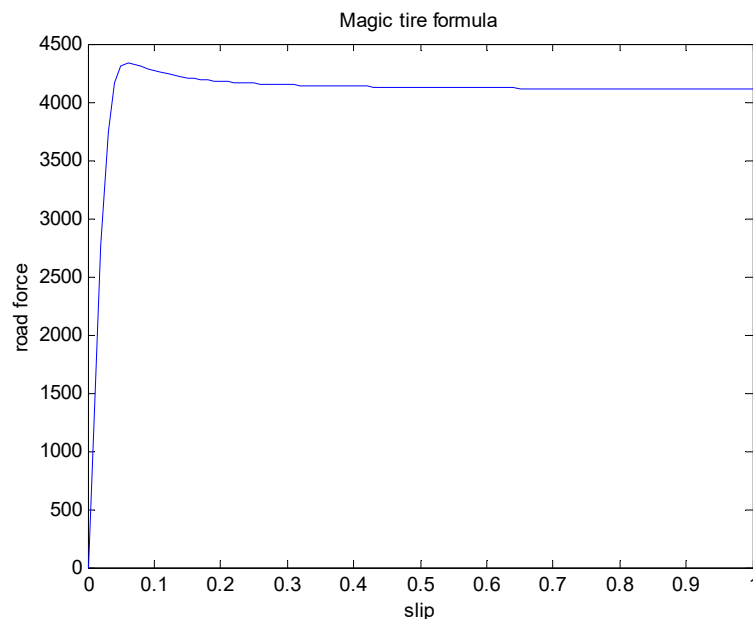
<https://www.youtube.com/watch?v=tsnYqCRWTbE><sup>9</sup>

# Tire Model

## ► Bakker–Pacejka ‘Magic Tire Formula’

$$F_{road} = D \sin[C \arctan\{B(s + S_h) - E(B(s + S_h) - \arctan(B(s + S_h)))\}]$$

- $S_h$  : bias in the slip curve caused by change in effective tire radii, camber angle and etc.





# Road Force & $\mu_{MAX}$

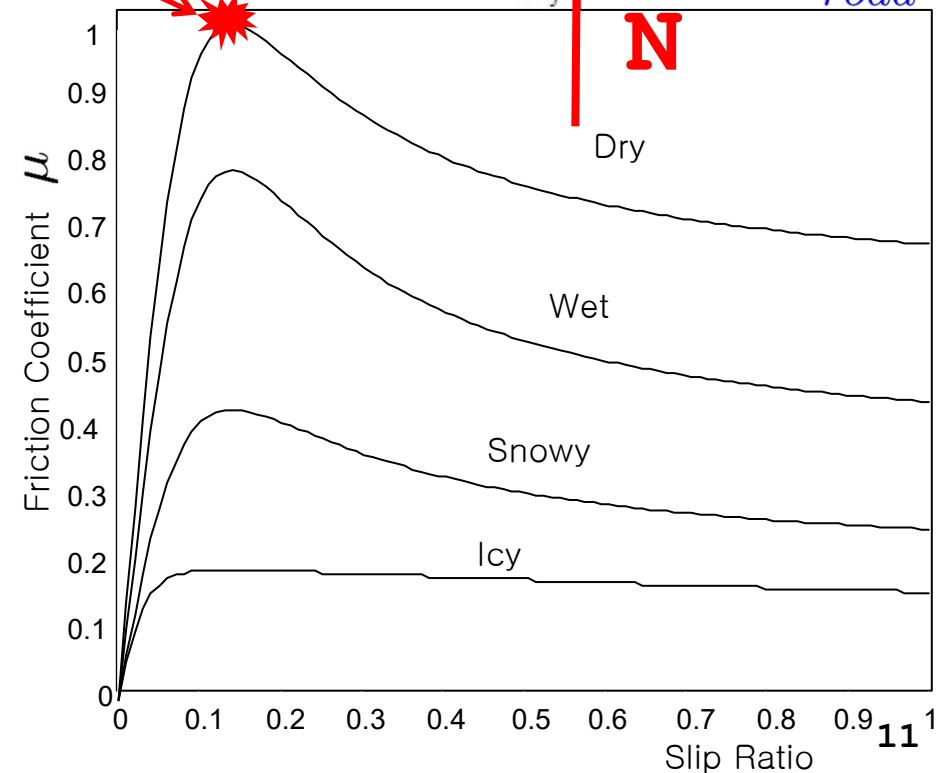
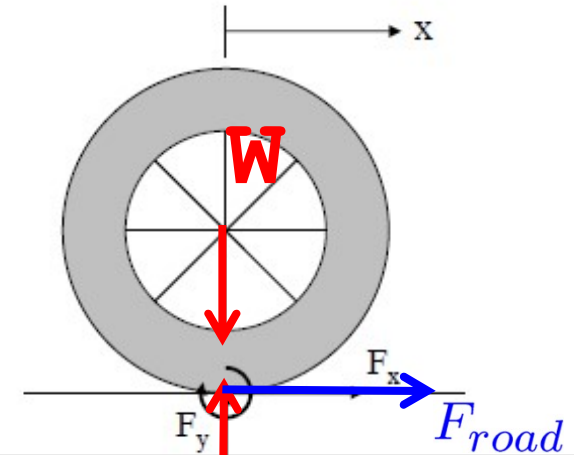
## ▶ Maximum Friction Coefficient

$$F_{road} \leq \mu_{max} N$$

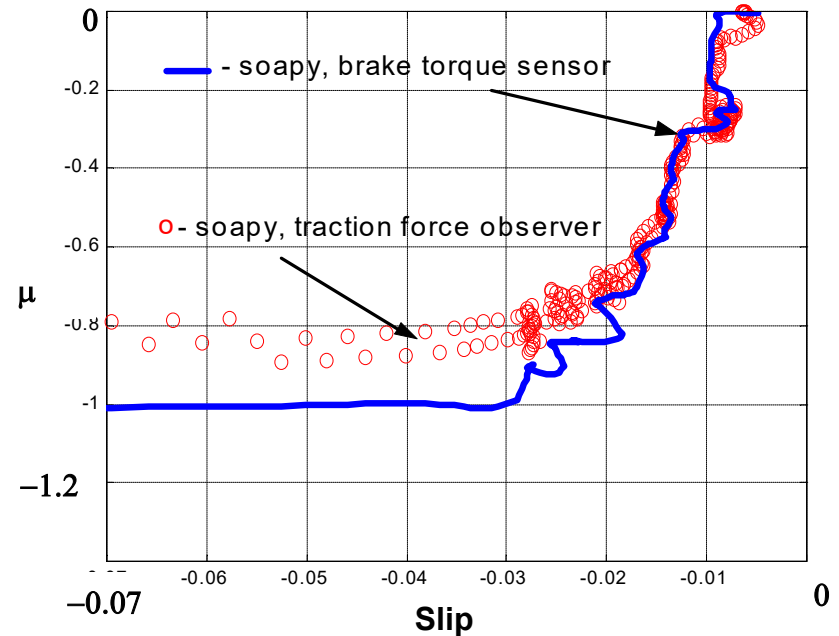
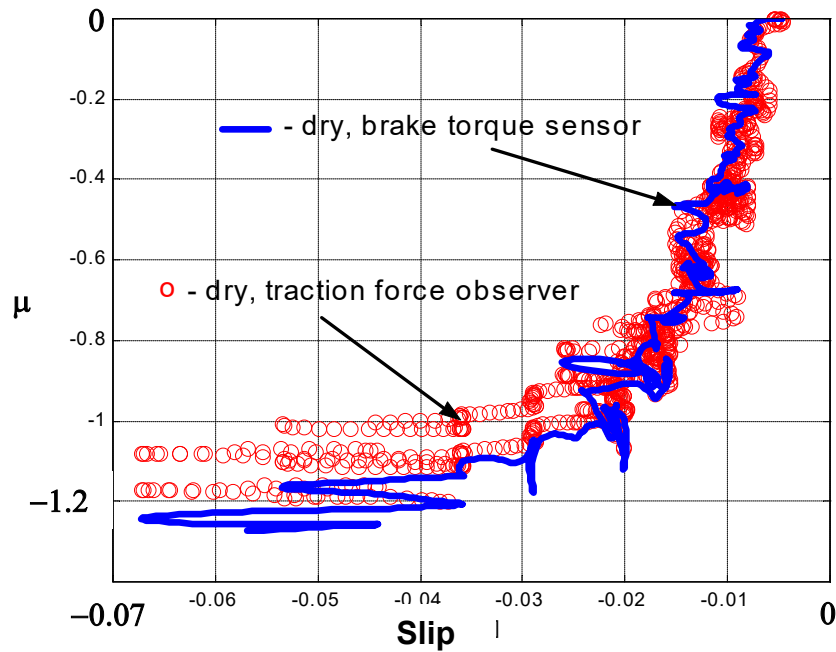
- ▶ Road Condition
- ▶ Tire Type
- ▶ Tread Pattern
- ▶ Tread Depth
- ▶ Velocity

## ▶ Friction Coefficient Definition as Normalized Force

➡  $\mu = F_{road}/N$



# Experimental slip curves



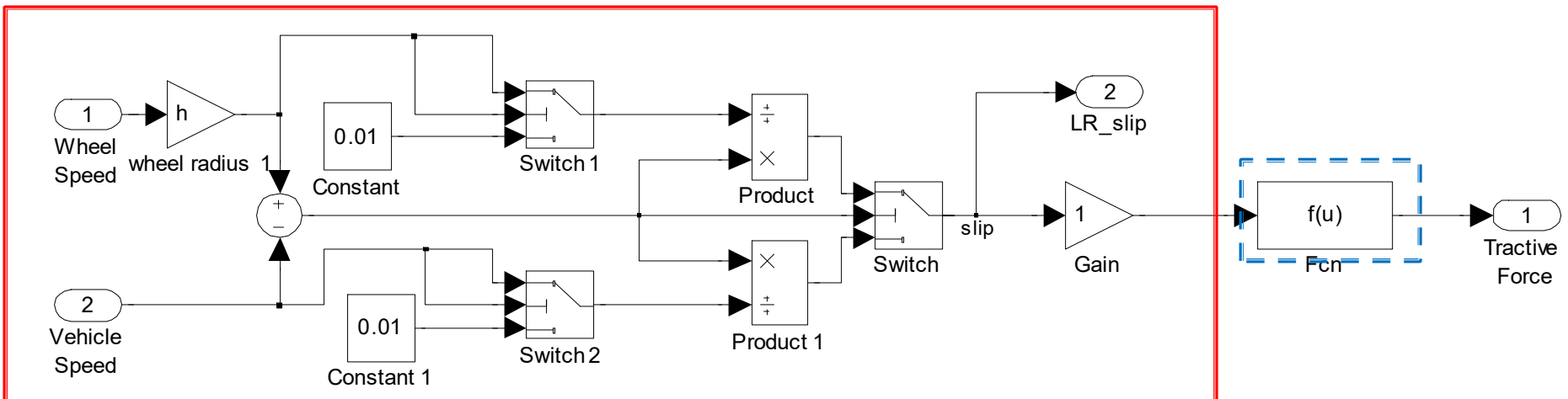
# Tire Model

## ► Simulink Model of Tire

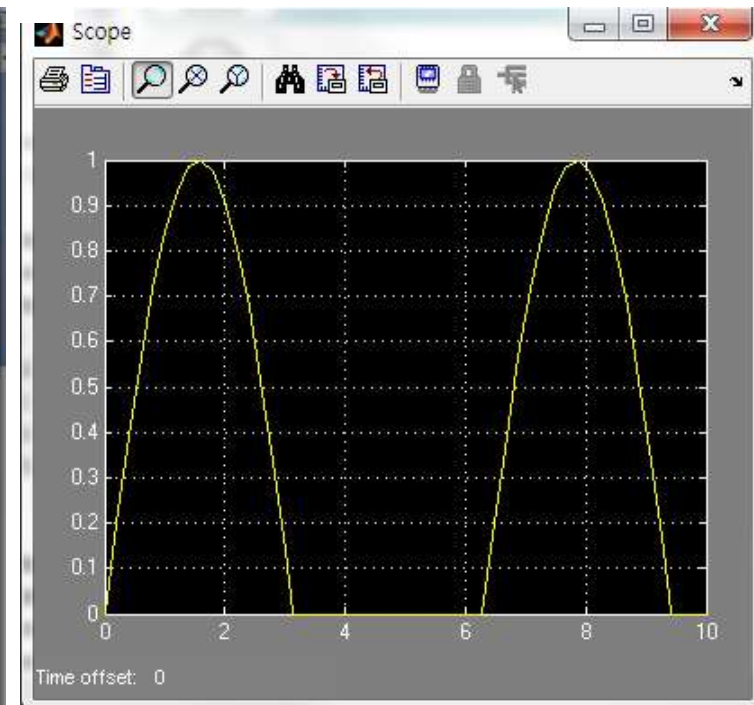
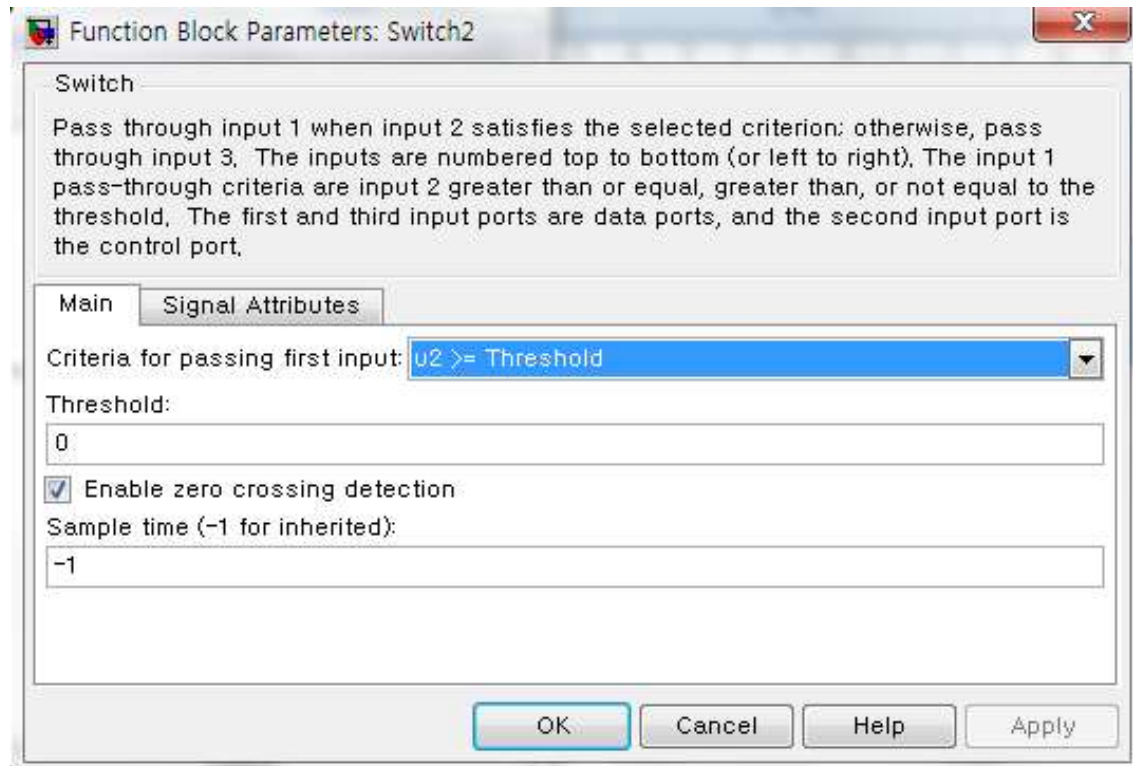
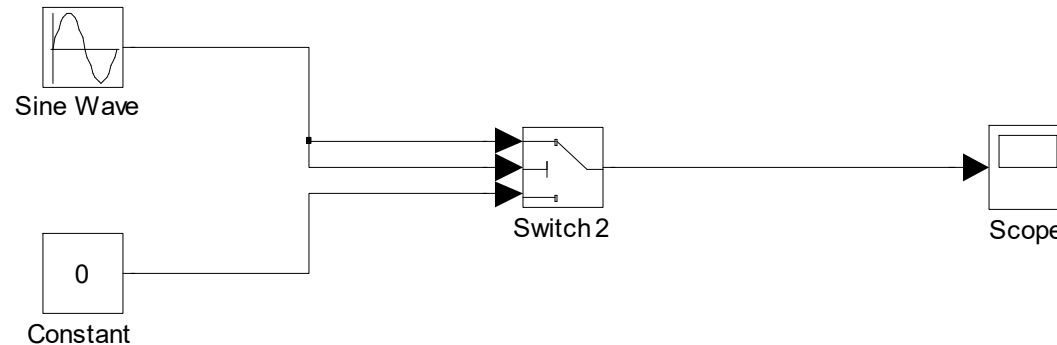
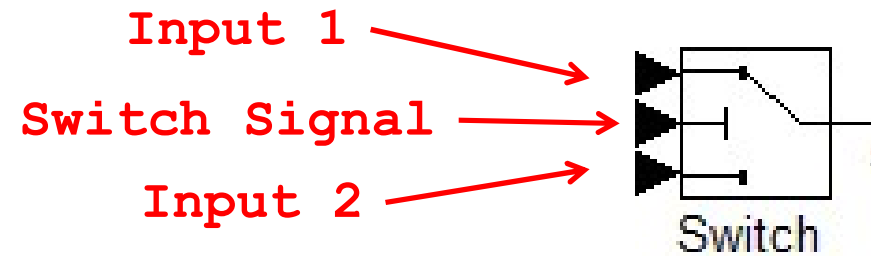
- Constant block is used to avoid the case of “divide by zero”.

$$S = \frac{h_{eff}\omega - v}{\max(h_{eff}\omega, v)}$$

$$F_{road} = D \sin [C \arctan \{B(s + S_h) - E(B(s + S_h) - \arctan(B(s + S_h)))\}]$$



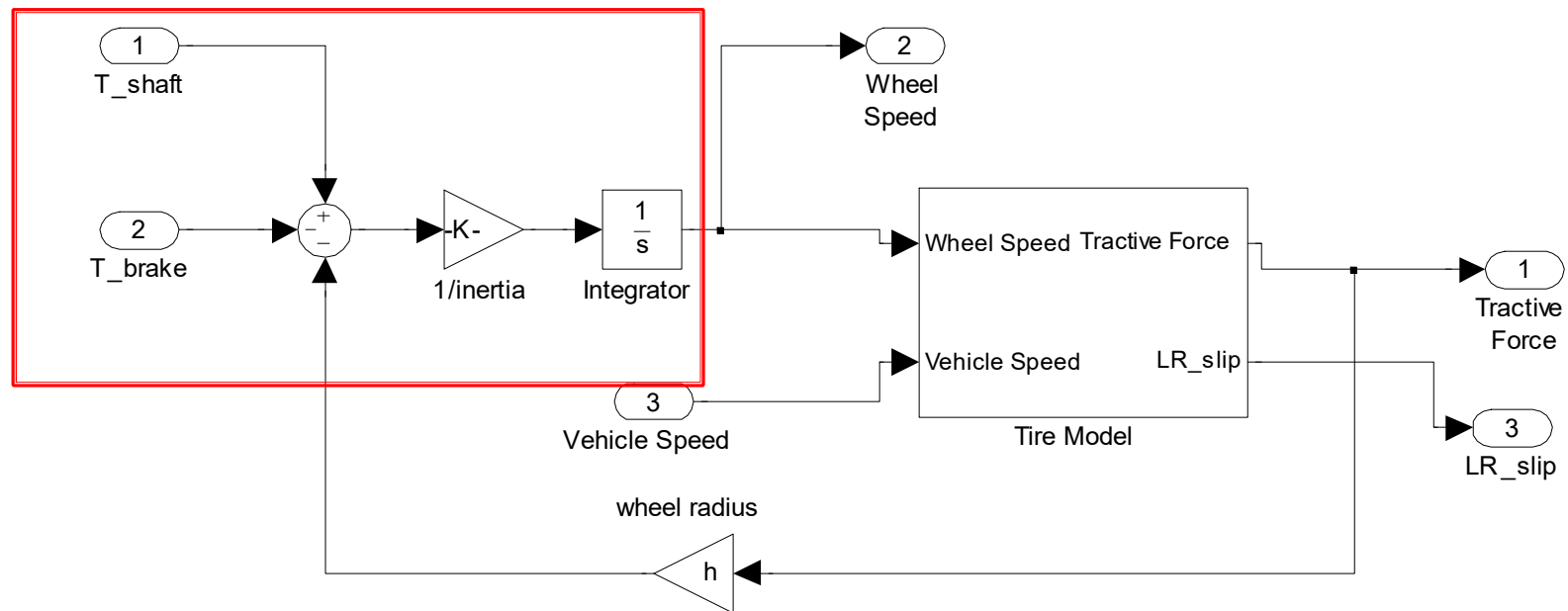
# Tire Model



# Wheel Dynamics

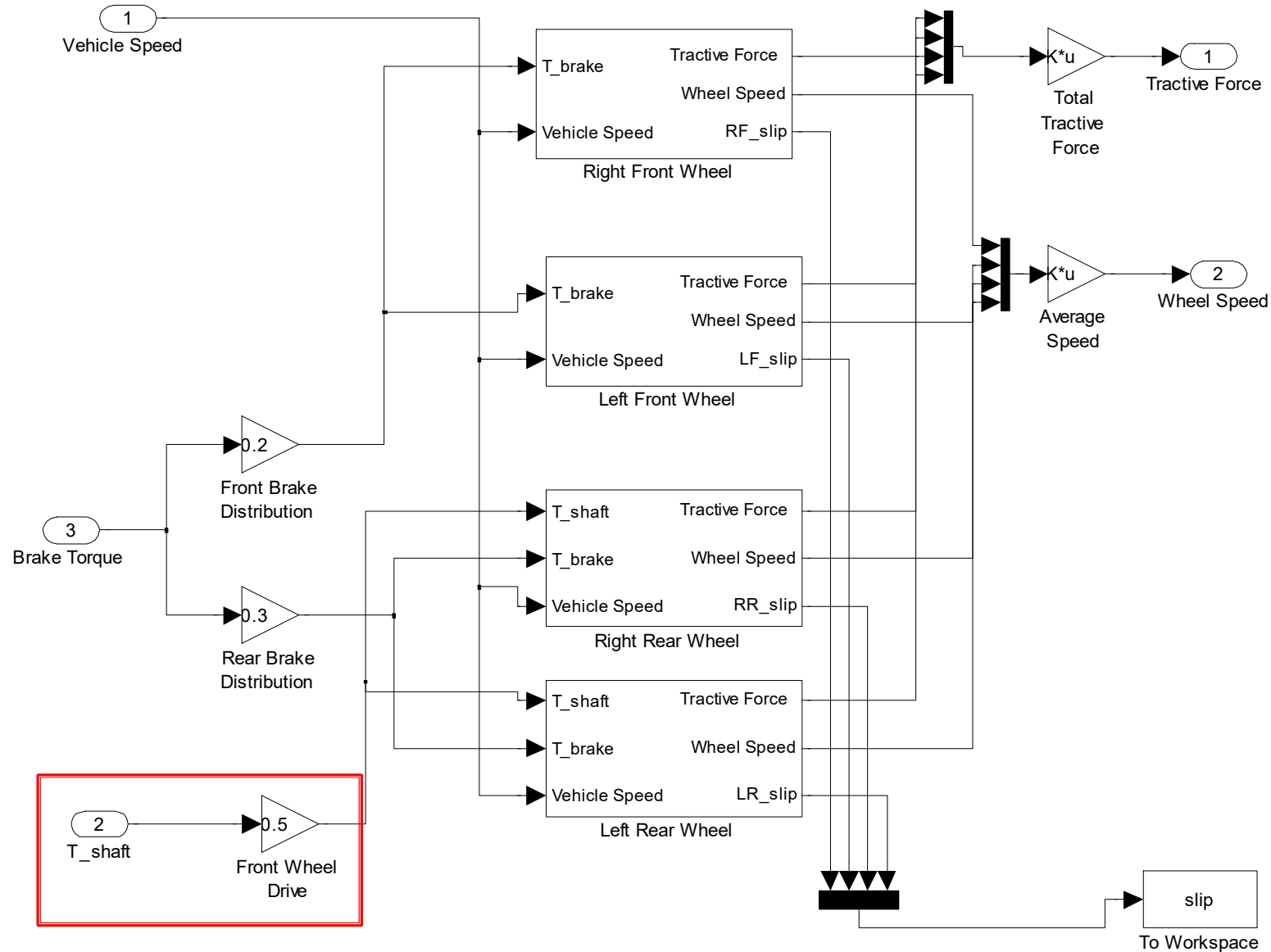
## ► Wheel Dynamics

$$J_{\omega}\dot{\omega} = T_{shaft} - T_{brake} - h_{eff}F_{road}$$



# Wheel Dynamics

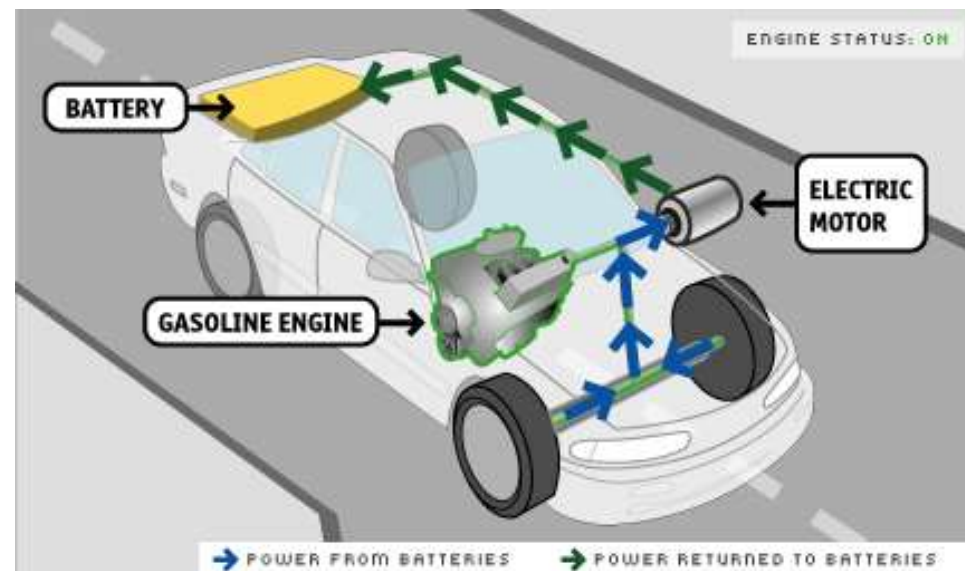
## Front Wheel Drive Model



# 브레이크 제어

## ▶ 브레이크

- 마찰을 이용하여 차량의 운동에너지를 열에너지로 변환시켜 감속
- 최근 Hybrid Electric Vehicle(HEV)는 회생제동시스템을 이용하여 운동에너지를 전기에너지로 변환시켜 버려지는 에너지를 재사용하여 연비 향상

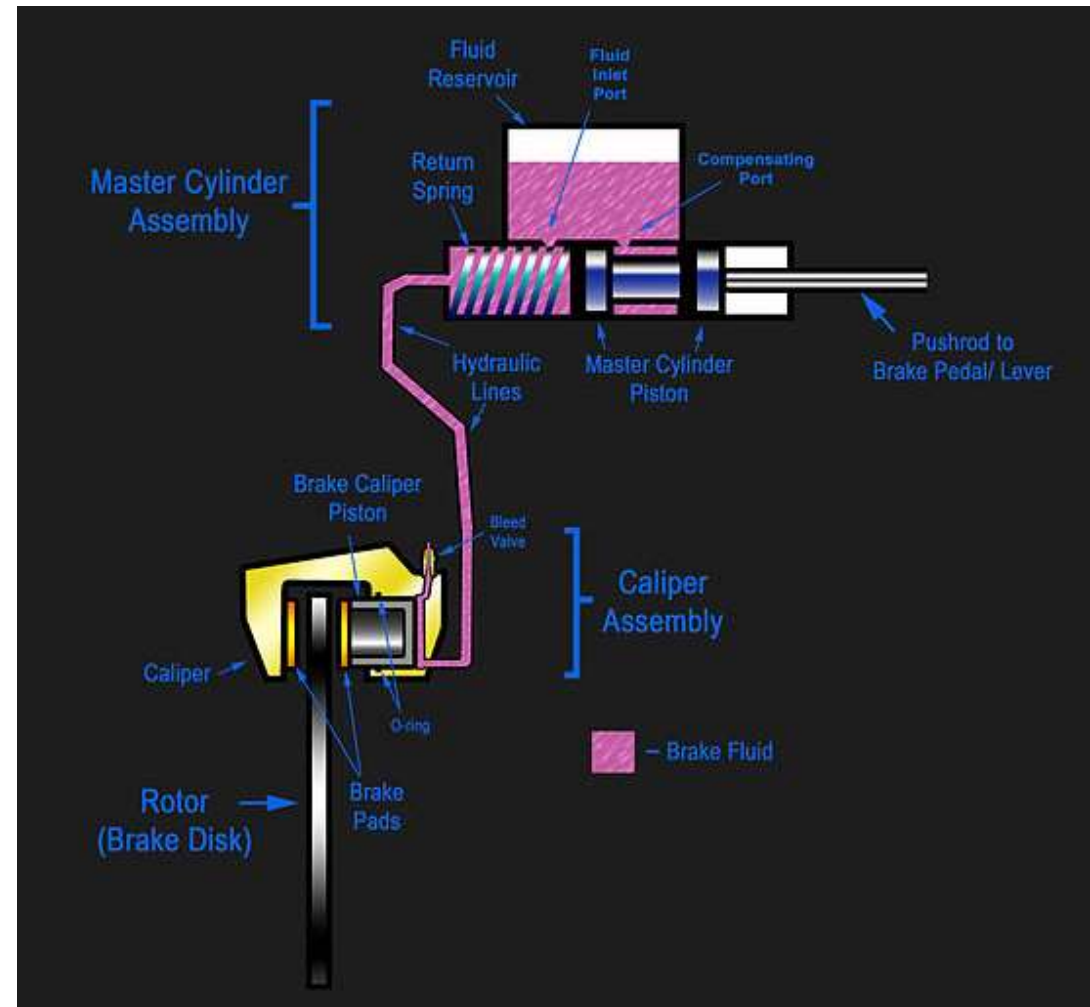


# Brake Model

## ▶ Hydraulic Disc Brake

### ▶ 브레이크 제동력 전달

- 브레이크 페달
  - Push rod
  - 마스터실린더
  - 브레이크 오일
  - 브레이크 피스톤
  - 브레이크패드
  - 브레이크 디스크



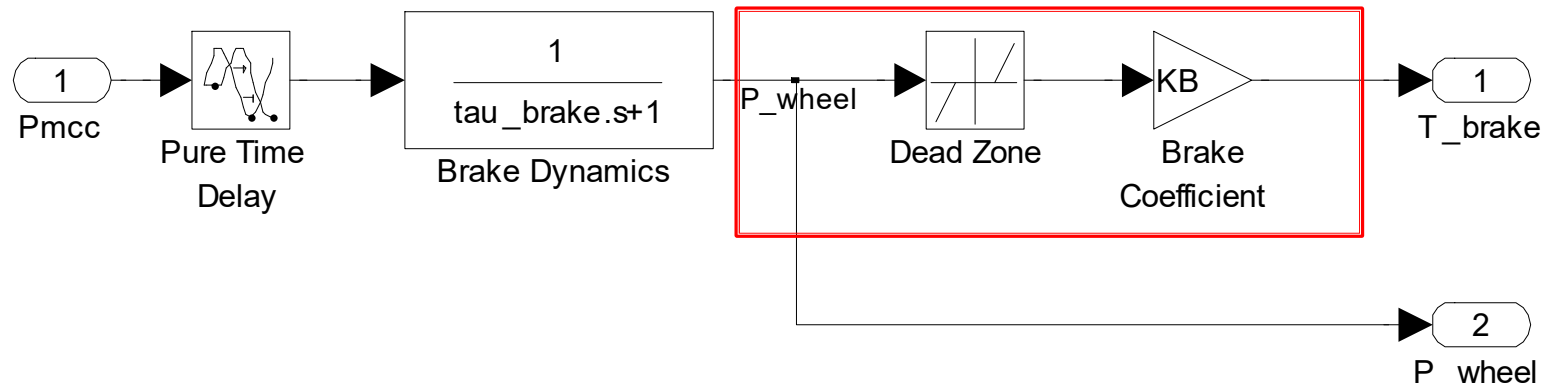
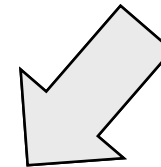
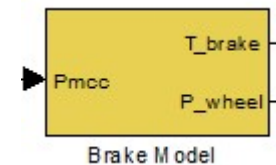


# Brake Model

- ▶ Hydraulic Master Cylinder Pressure Model
- ▶ Constant Weight Distribution Assumption
- ▶ Simple Proportional Model

$$T_b = \begin{cases} K_b(P_w - P_{po}), & P_w \geq P_{po} \\ 0, & \text{otherwise} \end{cases}$$

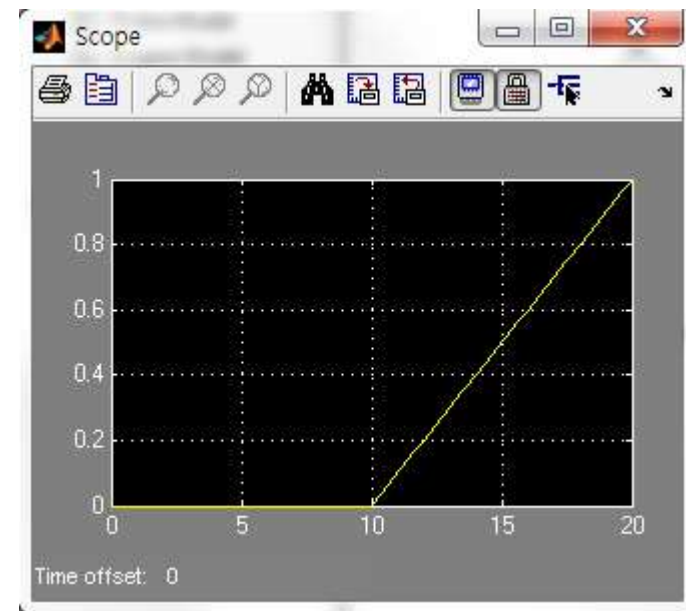
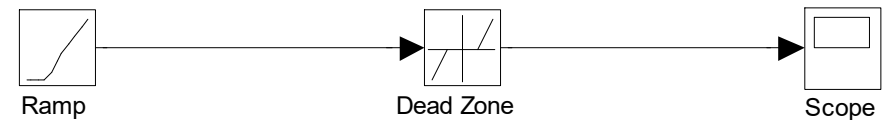
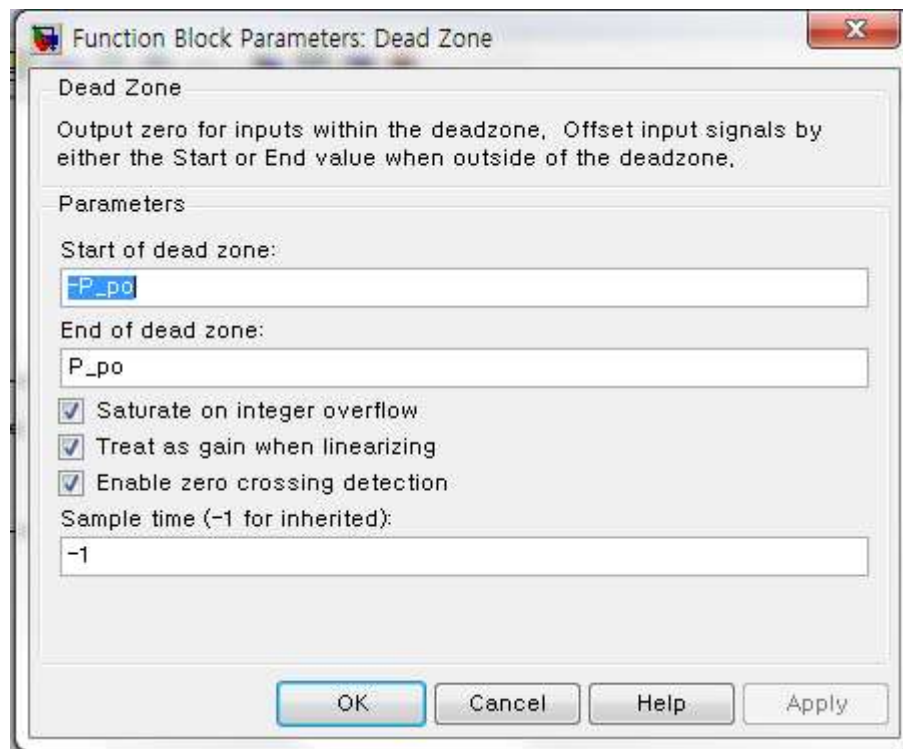
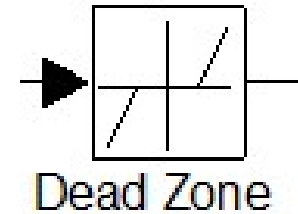
- $K_b$  Brake Coefficient
- $P_{po}$  Pushout Pressure
- $P_{mc}$  Master Cylinder Pressure
- $P_w$  Wheel Pressure



# Brake Model

## ► Dead Zone

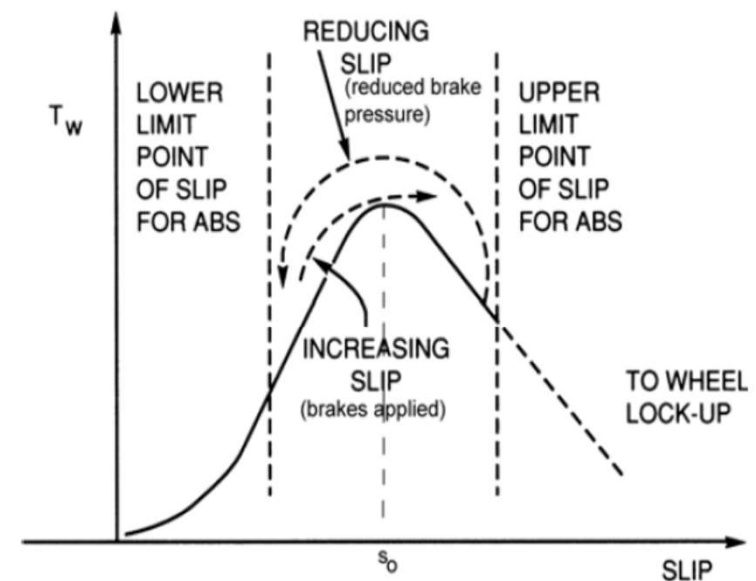
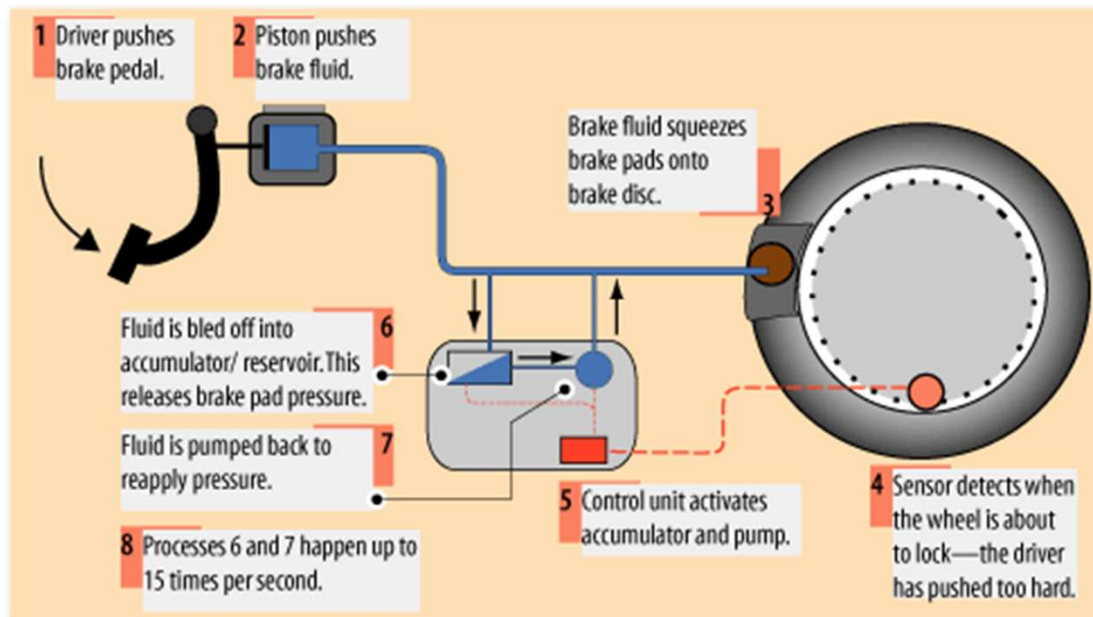
- Typical Nonlinear Dynamics
- Zero the output before the input value is below a certain thresholds



# 전자식 브레이크 제어

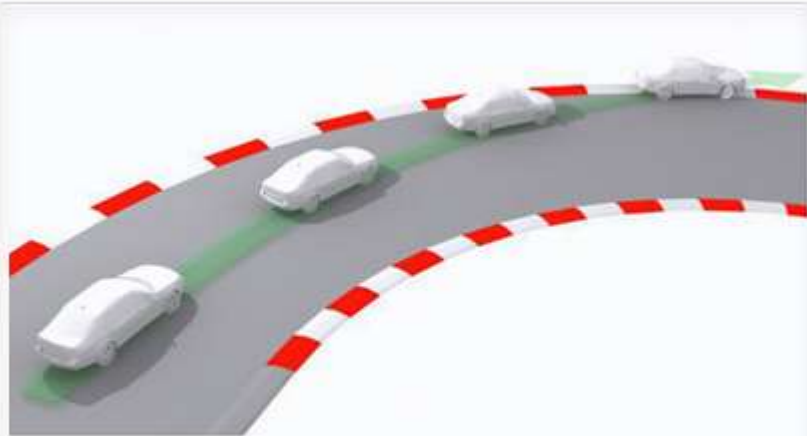
## ▶ Anti-lock Brake System (ABS)

- 브레이크에 과도한 힘이 작용하여 브레이크 패드가 디스크를 꽉 물어 타이어가 잠기는 현상을 방지
- 타이어가 잠기면 자동차는 조향성을 잃고 마찰력이 감소하는 것을 방지

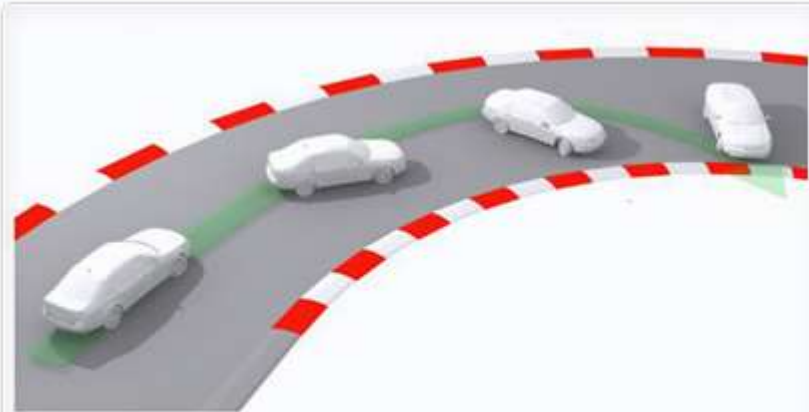


# 전자식 브레이크 제어

- ▶ Electronic Stability Control
  - 브레이크를 통해 횡방향 미끄러짐을 최소화할 수 있도록 제어
  - Understeer, Oversteer를 최소화하기 위하여 좌우 브레이크를 다르게 적용



UNDERSTEER :



OVERSTEER :