# SA CCR Allocation under consideration of ISDA-SIMM, Master Thesis

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1 INTRODUCTION 1

#### **Abstract**

This will be the abstract.

## 1 Introduction

# 2 Establishing Background

## 2.1 Bilateral initial margin

## 2.1.1 Reducing counterparty credit risk with initial margin

Counterparty credit risk refers to the risk of a default of the counterparty of a derivative. Derivatives are contracts between two institutions which give raise to future cash flows dependent of the performance of its underlying. These future cash flows may be at risk if the counterparty defaults during the lifetime of the derivative.

Over the past decades several measures were established in the derivatives markets to mitigate counterparty credit risk.

The most impactful measure is close-out netting. Close-out netting is a contractual agreement of two counterparties how their bilateral derivative contracts have to be settled if one of the counterparties defaults. With close-out netting, in case one of the two counterparties defaults all derivatives which are yet to mature are immediately closed out based on the current market value. The market values of the individual derivatives are summed up and the netted amount needs to be paid by whichever party is trailing across the portfolio. In case of a default this close-out netting procedure takes priority over all other claims of creditors against the defaulted counterparty. Close-out netting has two major advantages. First, the non-defaulting counterparty only suffers a counterparty credit loss, if it is ahead across the entire portfolio of currently running derivatives with the defaulted party. Just having a positive market value on a few derivatives does not necessarily result in a counterparty credit loss. Secondly, the immediate close-out of the open derivatives of the defaulted counterparty greatly facilitates unwinding its portfolio. A disadvantage of close-out netting is, that it may proof difficult to find an objective market value of the derivatives that have to be closed out especially in a stressed market environment, which is likely to be present if e.g. a large investment bank defaults. The contractual obligation to perform close-out netting is agreed upon in a master agreement, which was introduced to the derivatives market by ISDA in 1985. More details on close-out netting may be found in [3, Chapter 5].

The second most effective measure in mitigating counterparty credit risk is posting variation margin. If the obligation to post variation margin is agreed as part of a master agreement the accrued mark-to-market of the derivative portfolio has to be collateralized by the trailing counterparty. This measure effectively resets counterparty credit risk to zero for both parties every time a variation margin payment is made or the exchanged variation margin is adjusted to the current market value of the portfolio. The exchange of variation margin was common but not a given in the inter-bank market before the financial crisis of 2008. After the crisis it has become commonplace in the interbank market and recently has even been mandated by regulators. Nonfinancial counterparties oftentimes do not collaterialize their derivatives since they are not mandated to do so, shy away from the operational burden and have a harder time funding the significant amount of cash necessary to cover the current mark-to-market value of their entire derivatives portfolio. Collateralizing a derivatives portfolio not only significantly reduces CCR but also significantly alters how the remaining CCR behaves. The CCR of a collateralized portfolio may rather be driven by the terms of the CSA<sup>2</sup> or residual phenomenons such as collateral spikes<sup>3</sup> than by the underlying instruments.

Close-out Netting Variation margin Initial margin

A more comprehensive introduction to counterparty credit risk and its reduction through netting and margining may be found in chapters four through six of [3].

## 2.1.2 Market structure and regulatory background

The derivative market is divided into exchange traded derivatives, cleared OTC derivatives and uncleared OTC derivatives. According to [3, Figure 3.2] based on notional 9% of derivatives are exchange traded, 55% are cleared OTC derivatives and 36% are uncleared OTC derivatives. It has to be noted that these figures are from 2014 and it can be assumed, that the fraction of cleared OTC derivatives has increased since then at the expense of the fraction of uncleared OTC derivatives. The reason for this is, that regulators have incentivised or even mandated the clearing of simpler OTC derivatives over the course of the last years. In connection with this development the large CCPs such as Eurex or the LCH have extended the product range for which they offer OTC clearing in recent years.

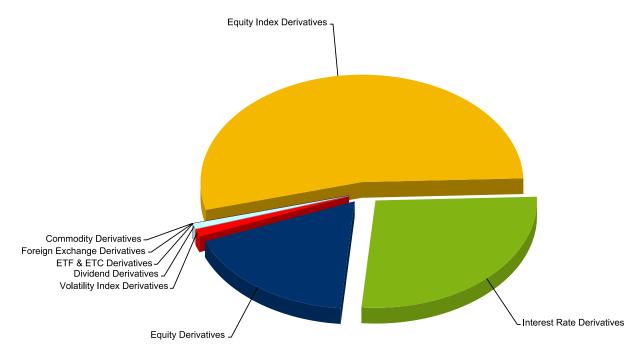
Exchange traded or listed derivatives are usually futures or options on a limited scope

<sup>&</sup>lt;sup>1</sup>In the European Union the exchange of Initial Margin for inter bank bilateral OTC derivatives is compulsory since September of 2016 for large banks or March of 2017 for smaller banks.

<sup>&</sup>lt;sup>2</sup>Explain what a CSA is

<sup>&</sup>lt;sup>3</sup>Quote something regarding collateral Spikes

of underlyings which can be directly traded at a clearing house at a bid and ask quoted by the clearing house. As seen in figure XX usual underlyings are single name equities, equity indices, commodities or baskets of liquid government bonds.



The clearing house acts as a mediator to match market participants which are willing to buy and sell and market participants will not be informed with whom they have been matched. All market participants exchange variation margin with the CCP and have to post a unilateral initial margin to the CCP. This initial margin is calculated by the CCP and is usually calculated using a portfolio based historical simulation VaR model. If a market participants defaults to CCP inherits its positions and needs to auction them to other market participants. The purpose of the initial margin is to cover mark-to-market losses which the portfolio suffers until it can be fully auctioned or otherwise closed by the CCP.

Cleared OTC derivatives are initially bilaterally agreed upon by two market participants. If the parametrization of the derivative is sufficiently common CCPs may offer to clear it and the market participants may choose or even be forced by regulation to clear it using a qualifying CCP. OTC clearing is especially common for simple interest rate derivatives such as interest rate swaps, forward rate agreements or cross currency swaps and for some credit derivatives. Similarly to exchange traded derivatives the CCP will charge both participants an initial margin and will also regularly determine the derivatives present value and execute the exchange of variation margin between the two market participants. If one of the market participants defaults, the CCP inherits the positions of the defaulted party and can again use the initial margin posted by the defaulted party to cover mark-to-market losses until it has auctioned or closed the

inherited positions [1].

Assuming that the CCP cannot default itself, cleared OTC derivatives and listed derivatives bear no counterparty credit risk for the market participants.

As of December 2018 common derivatives that are still uncleared are structured equity derivatives, swaptions and many other interest rate derivatives with optionality, derivatives on securitizations, swaps with unusual cashflow structures or in uncommon currencies and most FX derivatives [5].

What are uncleared OTC derivatives

## 2.1.3 Regulatory requirements for an internal initial margin model

After the 2008 financial crisis the G20 agreed to reduce systematic, counterparty and operational risk and as a result of this commitment has been put into effect by regulators worldwide. In Europe the European Market Infrastructure Regulation (EMIR) came into force in August 2012 and focused on promoting or mandating central clearing as the primary measure to reduce counterparty risk. EMIR also mant

#### 2.1.4 The ISDA-SIMM model

In December of 2013 the International Swap and Derviatives Association (ISDA) published a motivation and basic methodological outline of a common internal initial margin model called Standard Initial Margin Model (SIMM<sup>TM</sup>)[10]. The goal of the model is to meet the model requirements to an internal model of all regulators, while being among others easy to replicate, quick to calculate and relatively cheap to operate, implement and validate.

SIMM is a Delta-Gamma VaR model using Delta and Vega sensitivities calculated by the banks themselves and risk weights and correlations provided and recalibrated annually by ISDA. ISDA provides member with a methodological paper [9] and a paper describing the input format of sensitivities [8].

# 2.2 Capital requirements for counterparty credit risk

Counterparty credit risk is considered to be a part of credit risk by the regulator. Risk weighted assets have to be calculated and need to be backed by own capital. The three main inputs for calculating credit risk are the probability of default (PD) the loss given default (LGD) and the exposure at default (EAD). Assuming the default of a

counterparty over the course of the next year, the EAD is the current estimation of money indebted by the counterparty to the bank at the time of default. Estimating EAD for traditional credit instruments s.a. loans, credit cards, mortgages or bonds is relatively simple. Such instruments do often times have deterministic payment schedules making it easy to predict the exposure in one years time. Credit lines or credit cards behave less deterministic but it is still simple to determine an upper bound to the future exposure by assuming that the entire credit line is exhausted. The counterparty credit risk incurred by derivatives has first been regarded in regulatory capital calculation in Basel II [6]. Due to the stochastic nature of derivatives EAD calculation for counterparty credit risk has always been regulated separately ever since To calculate the counterparty credit risk associated with derivatives a different approach to calculating

#### 2.2.1 The SA-CCR

For analysis we create an SA CCR object that implements SA CCR as specified in [7] When using *SA-CCR* the exposure at default (EAD) has to be calculated as:

$$EAD = \alpha * (RC + PFE)$$

where  $\alpha = 1.4$ 

RC : Replacement Cost

*PFE* : Potential Future Exposure

```
[In]: SA_CCR.calculate_sa_ccr_ead(rc = 10, pfe = 20)
```

[Out]: 42.0

**Relation of RC and PFE** The purpose of the RC is to assess the imidiate loss suffered by the default of a counterparty. It is based on the current MtM of the derivative less the accessible collateral. If a bank has posted collateral to non-segregated accounts of a counterparty this collateral is also assumed to be lost in case of a default which increases the replacement cost.

The potential future exposure (PFE) on the other hand assesses how the RC might develop in the future. The future being defined as during the next year. If the RC

today is 0 but is likely to be larger than 0 in the near future the estimated EAD should take this expected increase in RC into account.

See also Paragraph 130 and 131 of [7]

Paragraph 130 - case without margining:

For unmargined transactions, the *RC* intends to caputre the loss that would occur if a counterparty were to default and were closed out of its transactions immediately. The *PFE* add-on represents a potential conversative increase in expousre over a one-year time horizon from the present date (i.e. the calculation date).

Paragraph 131 - case with margining:

For margined trades, the *RC* intends to capture the loss that would occur if a counterparty were to default at the present or at a future time, assuming that the closeout and replacement of transactions occur instantaneously. However, there may be a period (the margin period of risk) between the last exchange of collateral before default and replacement of the trades in the market. The *PFE* add-on represents the potential change in value of the trades during this time period.

## **Definition of Potential Future Exposure (PFE)**

$$PFE = \text{multiplier} * AddOn^{\text{aggregate}}$$

where  $AddOn^{aggregate}$ : aggregate add-on component multiplier:  $f(V, C, AddOn^{aggregate})$ 

*AddOn* is calculated differently for each asset *a* class. Since no netting is allowed between asset classes the aggregate is calculated as:

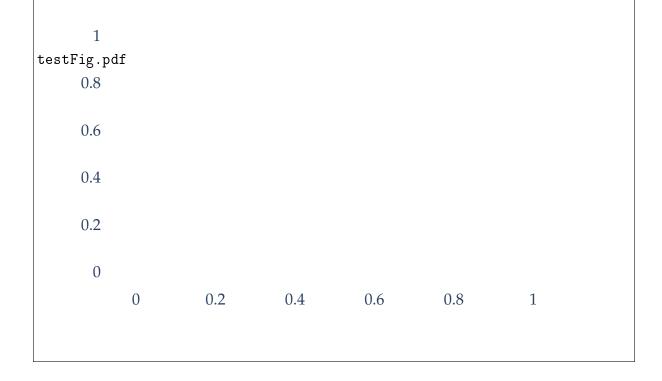
$$AddOn^{aggregate} = \sum_{a} AddOn^{a}$$

Collateralization is taken into account of the PFE calculation through the multiplier that uses the collateral held as an input. As overcollateralization e.g. through IM increases, the multiplier decreases. However, the multiplier is floored at 5%.

$$multiplier = min \left\{ 1; Floor + (1 - Floor) \exp \left( \frac{V - C}{2(1 - Floor)AddOn^{aggregate}} \right) \right\}$$
 where 
$$Floor = 5\%$$

It is important to note that the multiplier can only be below 1 if C > V, i.e. if the portfolio is overcollateralized. If the portfolio is overcollateralized, the AddOn comes into play. The idea behind the AddOn is related to the idea of value at risk. The higher the AddOn the faster the SA-CCR model expects the positions to lose in value. Therefore, the higher the value, the higher the multiplier.

In the example below the current NPV of the portfolio is 30 and the received collateral (IM + VM) is 37. The portfolio is overcollateralized as it should be when initial margin is used. On the other hand, as collateralization decreases e.g. V=C since only VM is exchanged or C=0 in the case of an uncollateralized portfolio the multiplier increases.



# 3 AddOn calculation

Most of the SA-CCR logic is hidden inside the AddOn calculation. At first it is important to define the following four data parameters:

 $M_i$ 

Maturity of the derivative contract. If the underlying of a derivative is another derivative - e.g. in the case of a swaption the maturity date of the underlying needs to be chosen.

 $S_i$ 

For interest rate and credit derivatives the start date of the time periodreferenced by an interst rate or credit contract. If the derivtives underlying is another interest rate or credit intsrument (eg swaption or bond option)  $S_i$ is the start date of the underlying instead.

 $E_i$ 

Defined as  $S_i$  but referencing the end date instead of the start date.

 $T_i$ 

For options across all asset classes this is the latest contractual exercise date.

# 3.1 Trade level adjusted notional

Each trade i has a trade level adjusted notional  $d_i^a$  assigned to it. This is calculated differently for the different asset classes.

**Interest rate and credit derivatives** The notional of the trade is usually a well defined value in domestic currency for interest rate and credit derivatives. It is multiplied by a supervisory duration factor. The basic idea is, that the value of the derivative can change more the longer the remaining

$$d_i = \text{Notional}_i * SD_i$$

where 
$$SD_i = \frac{\exp(-0.05 * S_i) - \exp(-0.05 * E_i)}{0.05}$$

**FX derivatives** While the wording in the BCBS paper is a bit more specific we will just assume that every FX traded derivative has a USD leg and set the notional equal the to USD notional.

**Equity and commodity derivatives** The notional is defined as the price of the underlying. Therefore, it fluctuates over time.

**Notional of exotic derivatives** For more exotic derivatives which do have adjustable notionals, resetting notionals etc. detailed handling of the notional is defined in paragraph 158.

Within this thesis we investigate only equity and interest rate derivatives. For these we can make a few exemplary calculations of the trade level adjusted notional.

For equity trades determining the trade level adjusted notional is trivial as it always is the spot price of the underlying. As an example consider the two trades defined below:

Let the spot price of Adidas stock be 42. Then, the adjusted notional of eqOption1, an at the money call on Adidas, is 42 and the adjusted notional of eqOption2, a short in the money put on Adidas, is also 42.

For interest rate derivatives such as interest rate swaps or swaptions on the other hand, the notional is adjusted by the supervisory duration factor. As the supervisory duration depends on *S* and *E* it is important to understand how these are determined for the different interest rate derivatives.

Trade Type	S	E	
Interest Rate Swap	Current date	Maturity date	
Forward starting	Start date of the	Maturity date of the	
IRS	underlying swap	underlying swap	
Swaption	Start date of the	Maturity data of the	
	underlying swap	underlying swap	

## 3.2 Supervisory delta adjustments: $\delta_i$

For linear derivatives  $\delta$  is 1 for long derivatives and -1 for short derivatives.

For options  $\delta$  is defined as under Black-Scholes:

$$\delta_{\text{long Call}} = +\Phi\left(\frac{\ln\left(P_i/K_i\right) + 0.5 * \sigma_i^2 * T_i}{\sigma_i * \sqrt{T_i}}\right)$$

where  $\Phi$ : standard normal cdf

 $\sigma_i$ : supervisory volatility as defined in Table 2 in paragraph 183

This delta is multiplied by -1 in case of a long Put option or a short Call option. This formula is used for both, equity options and swaptions.

No detail is given at this point on the delta calculation of CDO tranches as these are not in the scope of this thesis.

In the case of an european equity option the parametrization is quite straight forward.

 $\sigma_i$ : 1.2 is the supervisory volatility for a single stock option

 $K_i$ : The strike of the option

*P<sub>i</sub>*: The spot price of the underlying stock

 $T_i$ : The maturity of the option

A swaption on the other hand is parametrized as follows for calculation of its supervisory delta:

 $\sigma_i$ : 0.5 is the supervisory volatility for any interst rate option.

 $K_i$ : The strike of the option is the fixed rate of the underlying swap

 $P_i$ : Is the current par rate of the underlying (forward starting) swap

 $T_i$ : The maturity of the option. Please note the difference to  $E_i$  used for calculation of the adjusted notional, which is the maturity of the underlying swap.

SA-CCR uses the same Black-Scholes based formula for Swaps as it uses for Equities. It differentiates options in two dimensions. Whether they are *bought* or *sold* and whether they are *Call* or *Put* options (Compare paragraph 159).

SA-CCR defines an option as a call option if it rises in value as the underlying rises in value. A fixed payer swap rises in value as the underlying interest rate rises in value. Therefore, an option to buy a fixed payer swap at a predetermined strike also rises in value as the underlying interest rate rises in value. Therefore, a swaption on a payer swap is considered a *Call* under SA-CCR, while a swaption on a receiver swap is considered a *Put*.

For the at the money option eqOption1 that was set up above we yield a supervisory delta adjustment of 0.7257.

For an examplary short european swaption that has a par swap as underlying (i.e. the NPV of the swap is 0) that is set up as follows:

#### [Out]: -0.5987063256828626

we yield a regulatory delta of -0.5987.

## 3.2.1 Risk Horizon

For unmargined transaction the margining factor is

$$MF_i^{\text{unmargined}} = \sqrt{\frac{\min(M_i; 1 \text{ year})}{1 \text{ year}}}$$

This factor can be used to scale down a risk weight calibrated for a 1 year horizon to a shorter period.

With margining the margin period of risk (MPOR) is:

- 10 business days for small, uncleared OTC portfolios
- 5 business days for cleared derivatives
- 20 business days for netting sets with more than 5000 transactions that are not with a central counterparty
- and doubling this period for portfolios with outstanding disputes

The margining factor is then

$$MF_i^{\text{margined}} = \frac{3}{2} \sqrt{\frac{MPOR_i}{1 \text{ year}}}$$

At this point we need to introduce a collateral agreement object. For simplicities sake we will not differentiate between collateral and netting sets in this thesis. All trades that are covered by the same collateral agreement are also admissible for netting with each other. (Also refer to the introduction of close out netting above). To take into account the different parameters determining the risk horizon a couple of parameters are required to create a collateral agreement. As an example, below we are setting up a collateral agreement for uncleared derivatives without exchange of variation margin or initial margin.

The SA\_CCR paper provides a small exemplary portfolio in Annex 4a Example 1. It consists of the following trades:

Trac	le	Residual	Base	Notional		Receive	Market
#	Nature	Maturity	Ccy	(tsd)	Pay Leg	Leg	value (tsd)
1	Interest rate swap	10 years	USD	10000	Fixed	Floating	30
2	Interest rate	4 years	USD	10000	Floating	Fixed	-20
3	swap European Swaption		EUR	5000	Floating	Fixed	50

To set up this examplary portfolio we need to find fixed rates for the swaps and underlying swaps to match the desired market values.

Through optimization and using the market data of the 10th of May 2019 the fixed rates to match the market values in Example 1 were identified.

For trade 1 the matching fixed rate is 2.3754%, for trade 1 it is 2.2108% and for the underlying swap of trade 3 it is 0.1610%

# 3.3 Approaches to allocation

With increasing sophistication of risk, own capital and margining models the need for equally sophisticated tools for attributing these measures rises aswell. Allocating the variation margin or the current exposure method (CEM) to individual trades is trivial as these measures may just be calculated for an individual trade and then added up across all trades to obtain the correct aggregate value. For measures which take portfolio effects into account such as a state of the art VaR model, ISDA-SIMM or SA-CCR however, this approach is not possible. The advent of portfolio based models for internal risk measurement in the late 1990s and for regulatory risk measurement in the late 2000s sparked research into how such measures should be reallocated. Gregory [3, Chapter 10.7] states that three approaches are used in practice:

- Incremental allocation
- Marginal allocation
- Pro rata allocation

Additionally [4] Eigenschaften von Allokationen

- Nativ additiv
- Risk sensitivity
- Unabhaengig von Portfoliozusammensetzung
- Stable through time

## 3.3.1 Incremental allocation

Incremental allocation can only be applied when observing the development of a portfolio through time. Given a pre-existing portfolio P consisting of n trades  $t_1$  through  $t_n$  and a portfolio-based measure M the incremental contribution of the first and second additional trade may be calculated as:

$$M_{\text{inc},t_{n+1}} = M(t_1 \dots t_{n+1}) - M(t_1 \dots t_n)$$
  
 $M_{\text{inc},t_{n+2}} = M(t_1 \dots t_{n+2}) - M(t_1 \dots t_{n+1})$ 

It can be easily seen that this approach yields a natively additive allocation since it forms a telescoping sum<sup>4</sup>:

$$M_{\text{inc},t_1} = M(t_1)$$

$$M_{\text{inc},t_i} = M(t_i) - M(t_{i-1})$$

$$M_{\text{inc},t_n} = M(t_n) - M(t_{n-1})$$

$$\sum_{i=1}^{n} M_{\text{inc},i} = M(t_1) - M(t_1) + \dots + M(t_{n-1}) - M(t_{n-1}) + M(t_n) = M(t_n)$$

The incremental allocation can be calculated as or before a new trade is added to the portfolio. It is a risk sensitive value when it is calculated as it accurately reflect how the additional trade changes the risk measure. If the trade is mitigating risk at the time of its inception according to M its incremental allocation  $M_{inc}$  is negative. If it increases the risk its  $M_{inc}$  is positive. However,  $M_{inc}$  does not adapt over time and is likely to loose its accurate risk depiction as additional trade are added to the portfolio. As a portfolio develops it may well be possible, that a trade for which a negative  $M_{inc}$  was calculated at its inception may loose its risk mitigation. Due to this property  $M_{inc}$  of a given trade should ideally only be used at or before trade inception. One such use case is the PnL calculation of a new trade to determine the performance of the trading desk or trader which initiated the trade. Another would be to use it prior to an investment decision [11]. It can however not be used to analyse an existing portfolio to e.g.

<sup>&</sup>lt;sup>4</sup>For brevity in Notation let  $M(t_i)$  be equivalent to  $M(t_1 ... t_i)$ 

identify trades which drive risk or determine how increases or decreases in a given position would impact the portfolio measure. It also cant be calculated deterministically a posteriori for a portfolio without knowing its composition through time.

In the past, some academic work focussed on approximating the incremental VaR as it requires a recalculation of the VaR for the entire portfolio. An overview of these works and their potential pitfalls may be found in [11]. Since this work will rather focus on marginal than incremental allocation further details may be found in the referred paper. In the empirical analysis the incremental allocation will be calculated exactly.

## 3.3.2 Marginal allocation

Next, we are setting up a function to calculate the *AddOn* for derivatives from the FX asset class. The approach is a little simpler than that for the IR asset class as no differentiaten between time buckets is necessary. All derivatives on a common currency pair can be set off against each other.

$$AddOn^{FX} = \sum_{j} AddOn^{FX}_{HS_{j}}$$
 
$$AddOn^{FX}_{HS_{j}} = SF_{j}^{FX} * | \text{EffectiveNotional}_{j}^{FX} |$$
 
$$\text{EffectiveNotional}_{j}^{FX} = \sum_{i \in HS_{j}} \delta_{i} * d_{i}^{FX} * MF_{i}^{type}$$

With the hedging sets  $i \in HS$  referencing all derivatives on a common currency pair. In the following example we will create a swap and display its price.

```
irs = IRS(notional = 100,
    timeToSwapStart=ql.Period(2, ql.Days),
    timeToSwapEnd=ql.Period(10, ql.Years),
    swapDirection=SwapDirection.PAYER,
    index=InterestRateIndex.EURIBOR6M,
    fixed_rate=0.02
    )

irs.get_price()
```

## [2]: -15.11727999472697

#### [3]: -165.77717223100274

Now we shall have a final example of this glorious integration of Jupyter and LaTeX. For this I will create an equity swap and print its price.

Well, I do think that I do need to change a tiny bit here to be honest.

#### [5]: 1024.5398107359952

This is a markdown cell that I want to see.

```
[7]: 0 1 2
0 1 2 3
1 2 3 4
```

4 OUTLOOK 17

- 3.3.3 Euler allocation
- 3.3.4 Shapley allocation
- 3.4 Allocation of SA-CCR
- 3.4.1 Allocation without margining
- 3.4.2 Allocation under VM collateralization
- 3.4.3 Allocation under VM and IM collateralization
- 3.5 Comparison of allocation approaches
- 3.6 Calculating the Euler allocation
- 4 Outlook

REFERENCES 18

# References

[1] Eurex. Eurex Default Management Process. http://www.eurexclearing.com/clearing-en/risk-management/default-management-process. Accessed: 2019-01-24.

- [2] Eurex. Eurex Monthly Statistics December 2018. http://www.eurexchange.com/blob/3571518/1aa0157c4b96709caa97b254a4075aaf/data/monthlystat\_201812.pdf. Accessed: 2019-01-22.
- [3] J. Gregory. *The XVA Challenge: Counterparty Credit Risk, Funding, Collateral and Capital*. John Wiley & Sons, 2015.
- [4] U. Koyluoglu and J. Stoker. Risk decomposition honour your contribution. *RISK-LONDON-RISK MAGAZINE LIMITED-*, 15(4):90–94, 2002.
- [5] B. of International Settlements (BIS). OTC derivatives outstanding. https://www.bis.org/statistics/derstats.htm. Accessed: 2019-01-24.
- [6] B. C. on Banking Supervision (BCBS). International convergence of capital measurement and capital standards, a revised framework comprehensive version. https://www.bis.org/publ/bcbs128.htm, 2009. Accessed: 2019-04-29.
- [7] B. C. on Banking Supervision (BCBS). The standardised approach for measuring counterparty credit risk exposures. https://www.bis.org/publ/bcbs279.htm, 2014. Accessed: 2020-04-25.
- [8] I. Swaps and D. A. (ISDA). ISDA SIMM<sup>TM</sup> Methodology: Risk Data Standards, version 1.36. https://www.isda.org/a/owEDE/risk-data-standards-v1-36-public.pdf. Accessed: 2019-04-29.
- [9] I. Swaps and D. A. (ISDA). ISDA SIMM<sup>TM</sup> Methodology, version 2.1. https://www.isda.org/a/zSpEE/ISDA-SIMM-v2.1-PUBLIC.pdf. Accessed: 2019-04-29.
- [10] I. Swaps and D. A. (ISDA). ISDA Standard Initial Margin Model (SIMM<sup>TM</sup>) for Non-Cleared Derivatives. https://www.isda.org/a/gwEDE/march-26-simm-for-non-cleared-paper.pdf. Accessed: 2019-04-29.
- [11] L. Tibiletti. Incremental value-at-risk: traps and misinter-pretations. In *Mathematical Finance*, pages 355–364. Springer, 2001.