

Machine Intelligence:: Deep Learning

Week 1

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Institut für Datenanalyse und Prozessdesign
Zürcher Hochschule für Angewandte Wissenschaften

Beate's Background

Heidelberg

Study of physics
& mathematics

Lausanne: UNIL, DAFL

Head of bioinformatics
Focus: Gene expression

Zürich: ETH

PhD and Postdoc
Contract lecturer

Winterthur: ZHAW, SoE

Researcher and
Professor for applied
statistics

Basel: OncoScore

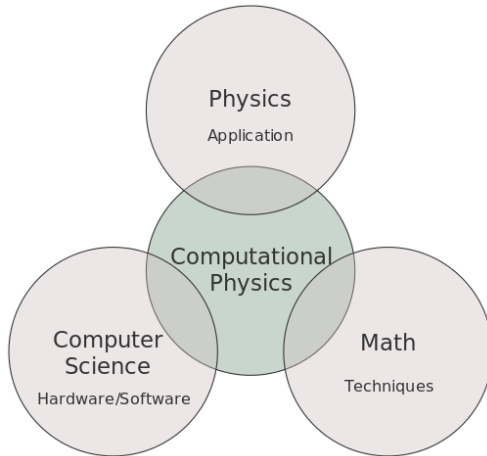
Biomarker detection

UZH: EBPI, Biostatistics

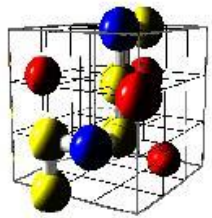
Researcher and lecturer
Focus: Biostatistics, DL

Oliver's Background

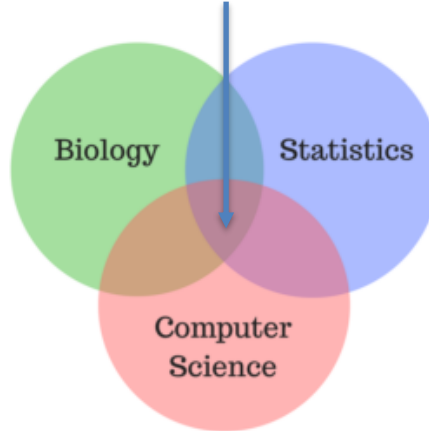
Computational Physics



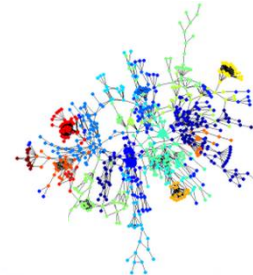
1990's
Uni-Konstanz



Bioinformatics

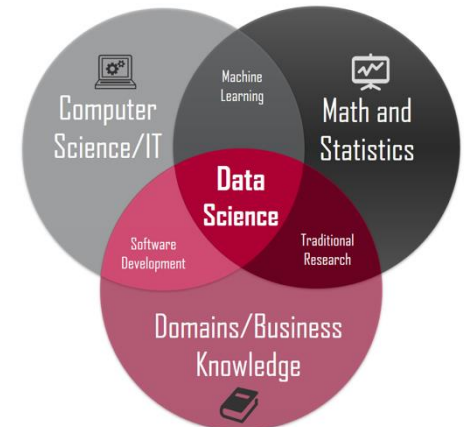


2000's
Genedata Basel

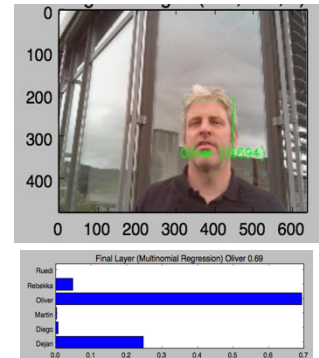


eclipse

Data Science



2010's
ZHAW Winterthur HTWG Konstanz



Tell us something about you

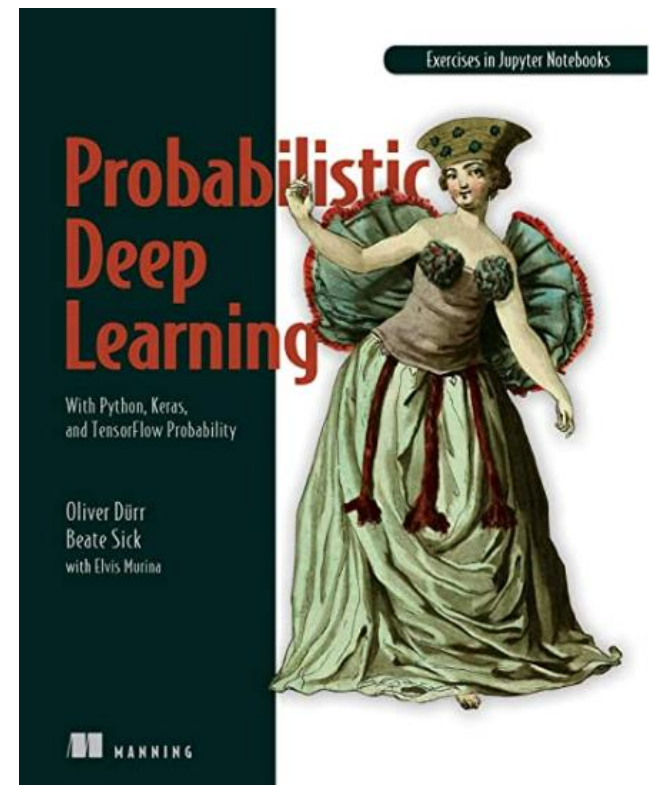
- Computer Science Background
 - Fluent in python?
- Statistics / Math
 - Who visited CAS StMo (statistisches Modellieren)?
 - What is a distribution?
 - Vector times Matrix?
 - Please make sure to check https://tensorchiefs.github.io/dl_course_2024/prerequisites.html
- Any contacts with deep learning yet?

Technical details for this course

- Running the code:
 - Colab Notebooks
 - needs no installation, only internet and google account
 - Anaconda
 - Installation by your own (no support)

Material for the course

- Website and Github repository
 - The CAS Deep Learning Course
 - https://tensorchiefs.github.io/dl_course_2024/
- [Our Book “Probabilistic Deep Learning”](#)
 - Can be used in addition to the course
 - https://github.com/tensorchiefs/dl_book



Organizational Issues: ~~Test~~ Projects

- Projects (2-3 People)
- Presented on the last day
 - Spotlight talk (5 Minutes)
 - Poster
- Topics
 - You can / should choose a topic of your own (please discuss your topic with us by week4 latest)
 - Possible Topics (see website)
 - Take part in a Kaggle Competition (e.g. Leaf Classification / Dogs vs. Cats)
 - Music classification
 - Polar bear detection
 - ...
- Computing: colab, laptop (or cloud computing)

Organizational Issues: Times

- Dates and times: see our webpage [CAS machine intelligence](#)
- Afternoon sessions
 - 13:30-17:00
- Theory and exercises will be mixed
 - Could be 50 minutes theory 30 minutes exercises
 - Could be vice versa
- **Please interrupt us if something is unclear! The less we talk the better!**

Outline of the DL Module (tentative)

- Day 1: Jumpstart to DL
 - What is DL
 - Basic Building Blocks
 - Keras
- Day 2: CNN I
 - ImageData
- Day 3: CNN II and RNN
 - Tips and Tricks
 - Modern Architectures
 - 1-D Sequential Data
- Day 4: Looking at details
 - Linear Regression
 - Backpropagation
 - Resnet
 - Likelihood principle
- Day 5: Probabilistic Aspects
 - TensorFlow Probability (TFP)
 - Negative Loss Likelihood NLL
 - Count Data
- Day 6: Probabilistic models in the wild
 - Complex Distributions
 - Generative modes with normalizing flows
- Day 7: Uncertainty in DL
 - Bayesian Modeling
- Day 8: Uncertainty cont'd
 - Bayesian Neural Networks
 - Projects

Day 1-4 should get you ready for your project.

Learning Objectives for today

- Get a rough idea what the DL is about
- Framework
 - Introduction to Keras

Introduction to Deep Learning

--what's the hype about?

Machine Perception

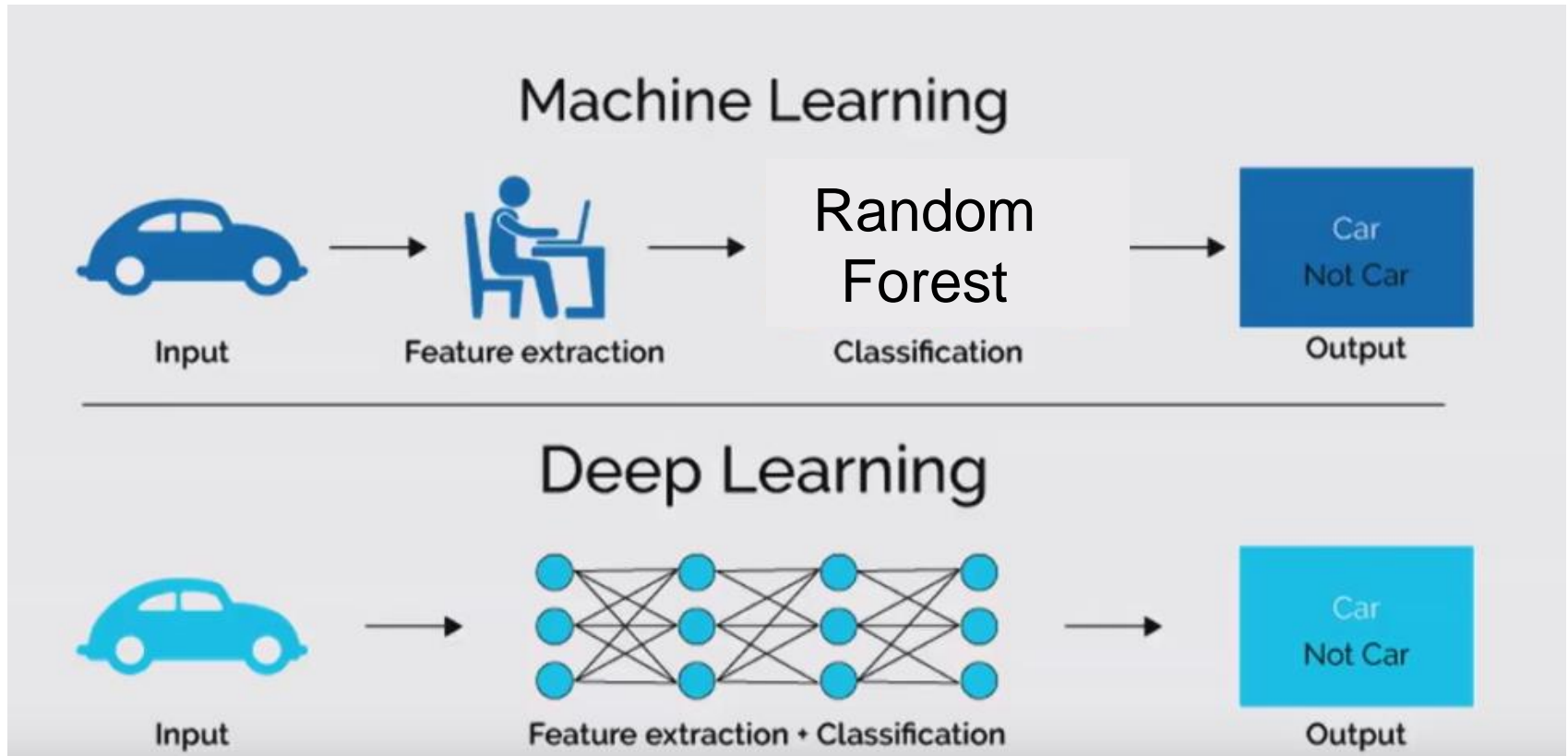
- Computers have been quite bad in things which are easy for humans (images, text, sound)
- A Kaggle contest 2012
- In the following we explain why

[Kaggle dog vs cat competition](#)



Deep Blue beat Kasparov at chess in 1997.
Watson beat the brightest trivia minds at Jeopardy in 2011.
Can you tell Fido from Mittens in 2013?

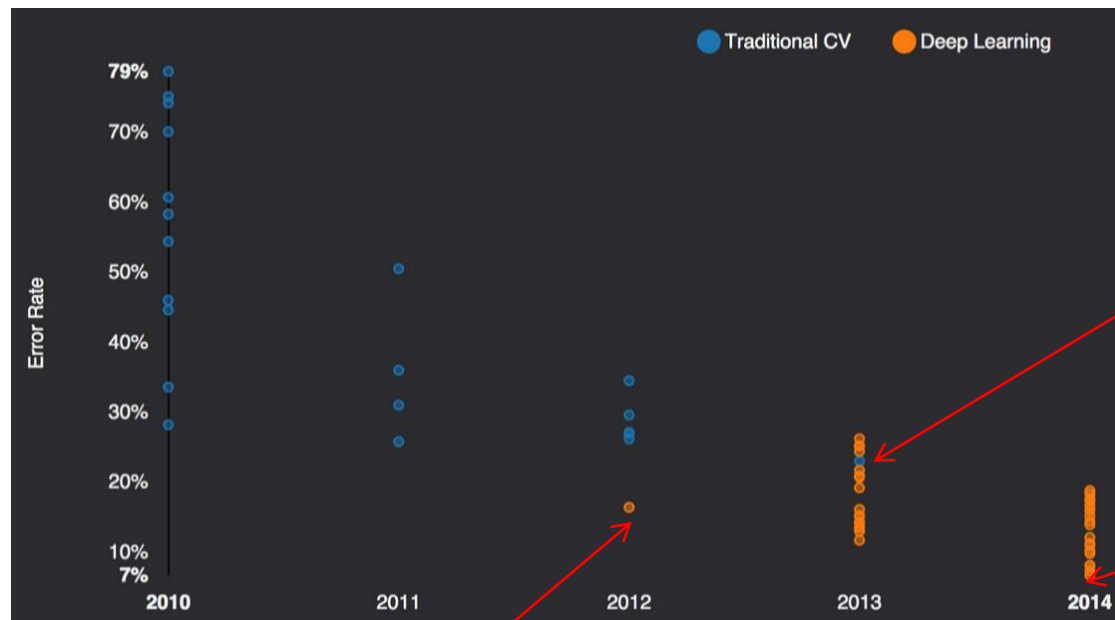
Deep Learning vs. Machine Learning



The most convincing case for
DL (subjective view)

Why DL: Imagenet 2012, 2013, 2014, 2015

1000 classes
1 Mio samples



Human: 5% misclassification

Only one non-CNN approach in 2013

GoogLeNet 6.7%

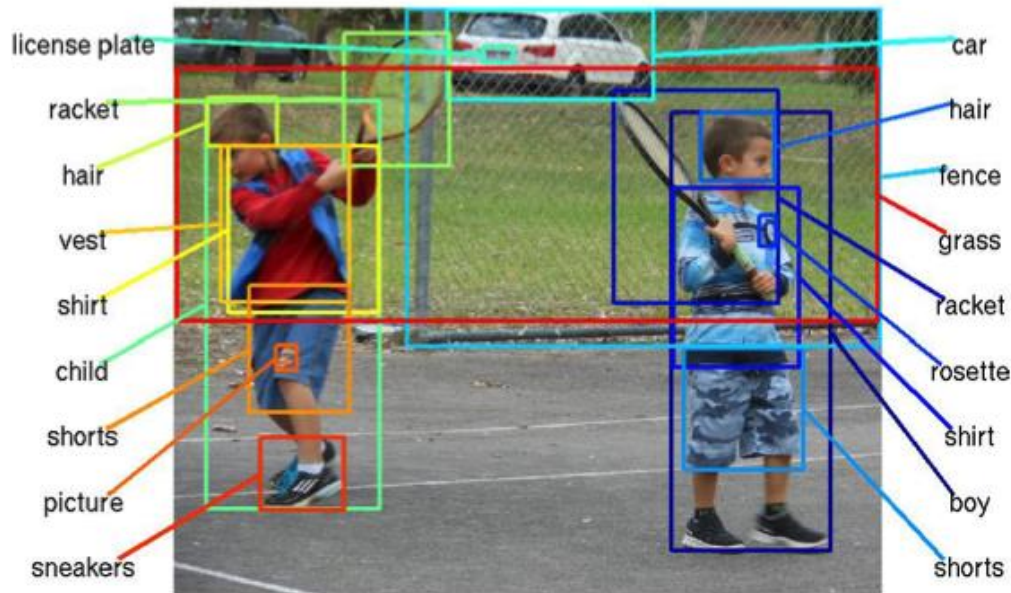
A. Krizhevsky
first CNN in 2012
Und es hat zoom gemacht

2015: It gets tougher

4.95% Microsoft ([Feb 6](#) surpassing human performance 5.1%)
4.8% Google ([Feb 11](#)) -> further improved to 3.6 (Dec)?
4.58% Baidu (May 11 [banned due too many submissions](#))
3.57% Microsoft (Resnet winner 2015) -> **task solved!**

The computer vision success story

- With DL it took approx. 3 years to solve object detection and other computer vision task

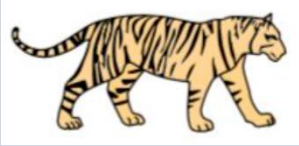




Deep Blue beat Kasparov at chess in 1997.
Watson beat the brightest trivia minds at Jeopardy in 2011.
Can you tell Fido from Mittens in 2013?



"man in black shirt is playing
guitar."

Use cases of deep learning

Input x to DL model		Output y of DL model	Application
Images		Label "Tiger"	Image classification
Audio		Sequence / Text "see you tomorrow"	Voice Recognition
Sequence (prompt) An astronaut riding a horse in a photorealistic style			Image Generation
Sequences (prompt) "Hallo, wie?"		Next word "geht"	Language Models
Simple number (age) age=52		Simple number (SPB) sbp = 152	Simple Regression Educational

Deep Learning öffnet Tür zu hören, sehen und Texten.
Status Quo: kein Verstehen aber Erfassung statistische Zusammenhänge.

This is the new shit: LLM/ChatGPT



Die gefühlte Revolution

4. Dezember 2022, 18:51 Uhr | Lesezeit: 3 min



Das kommt heraus, wenn man der künstlichen Intelligenz Dall-E die Anweisung gibt: "Ein Roboter lässt beim Turing-Test einen Menschen glauben, dass sie ein Mensch ist, im Stil von Kehinde Wiley." (Foto: Dall-E-Bild: SZ)



GPT (short for "Generative Pre-training Transformer")

is a type of language processing AI model developed by OpenAI. It is a large, deep learning model that has been trained on a diverse range of texts and can generate human-like text when given a prompt.

First Neural Network

The Single Neuron: Biological Motivation

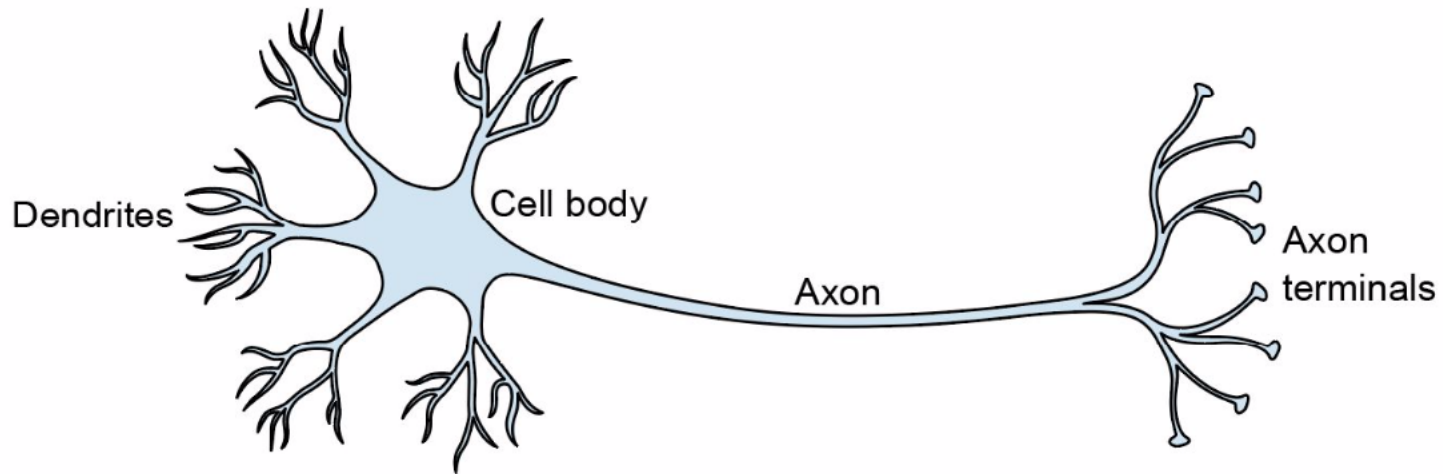
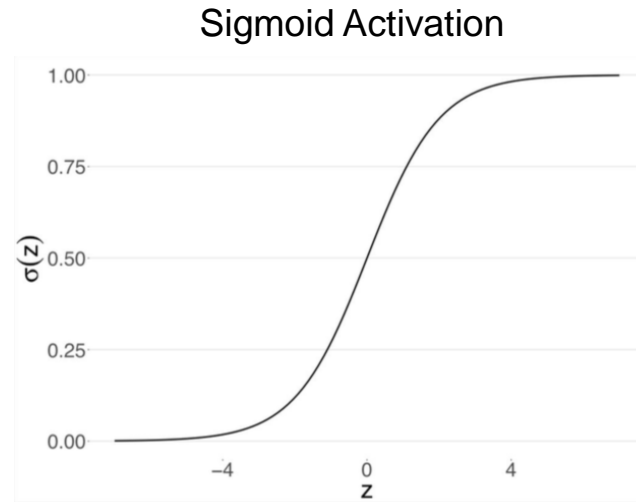
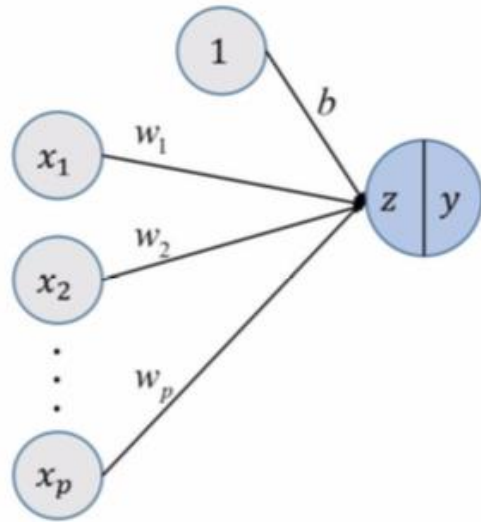


Figure 2.2 A single biological brain cell. The neuron receives the signal from other neurons via its dendrites shown on the left. If the cumulated signal exceeds a certain value, an impulse is sent via the axon to the axon terminals, which, in turn, couples to other neurons.

Neural networks are **loosely** inspired by how the brain works

The Single Neuron: Mathematical Abstraction

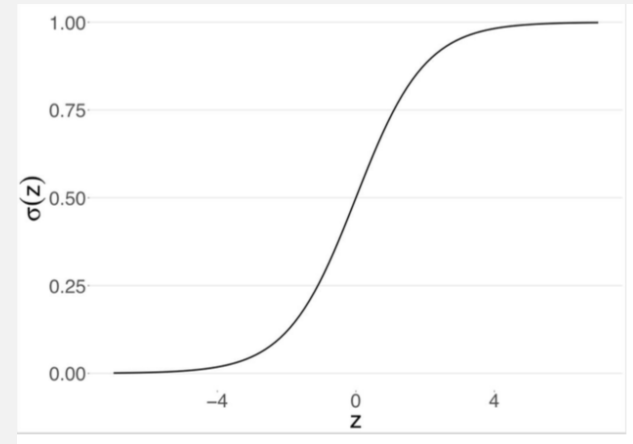
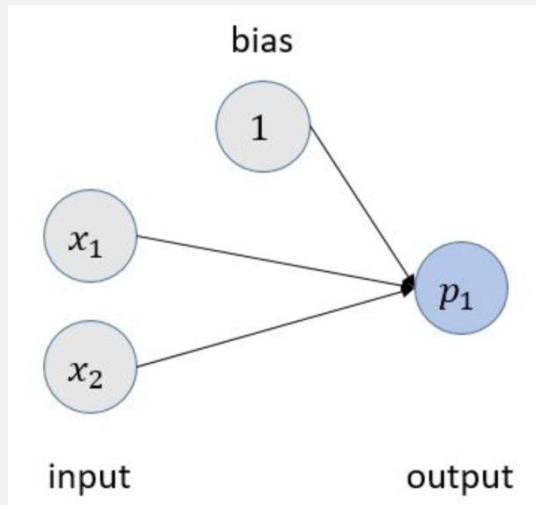


$$z = b + x_1 \cdot w_1 + x_2 \cdot w_2 + \cdots x_p \cdot w_p$$

$$y = \sigma(z) = \sigma(\beta_0 + \beta_1 x_{i1} + \cdots + \beta_{ip} x_{ip}) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_{i1} + \cdots + \beta_{ip} x_{ip})}}$$

The output after the sigmoid activation can be interpreted as probability for $y=1$

Exercise: Part 1



Model: The above network models the **probability** p_1 that a given banknote is false.

TASK (with pen and paper)

The weights (determined by a training procedure later) are given by

$$w_1 = 0.3, w_2 = 0.1, \text{ and } b = 1.0$$

What is the probability that a banknote, that is characterized by $x_1=1$ and $x_2 = 2.2$, is a faked banknote?




GPUs love Vectors



$F^{\mu\nu}$

In Math:

$$p_1 = \text{sigmoid} \left((x_1 \quad x_2) \cdot \begin{pmatrix} w_1 \\ w_2 \end{pmatrix} + b \right)$$


In code:

```
## function to return the probability output after the matrix multiplication
def predict_no_hidden(X):
    return sigmoid(np.matmul(X,W)+b)
```

Toy Task

- Task tell fake from real banknotes
- Banknotes described by two features

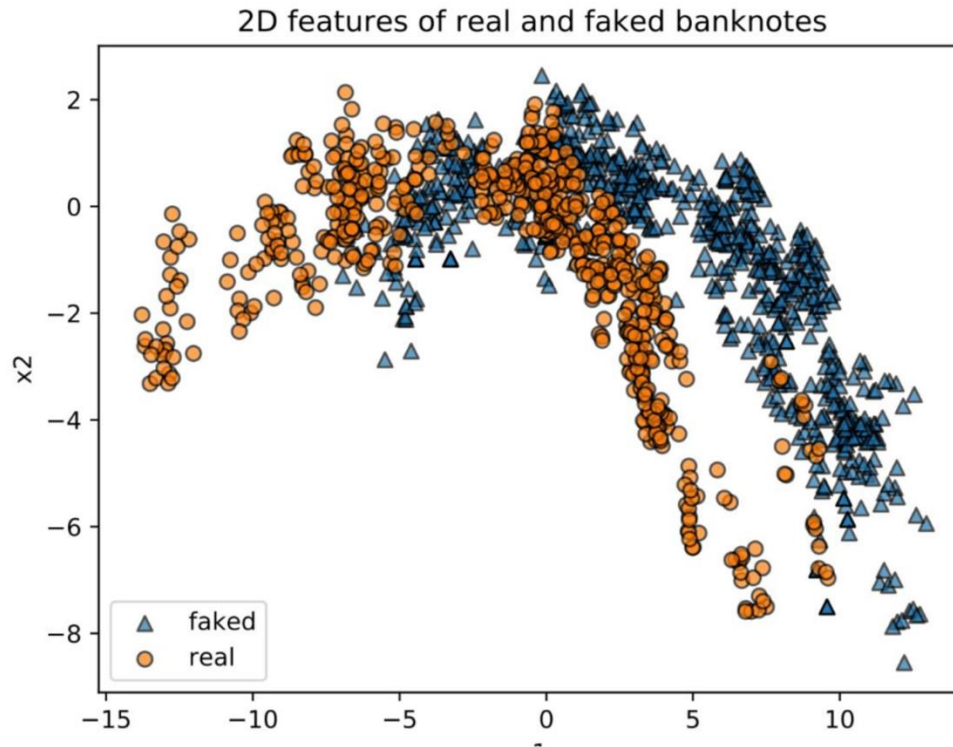
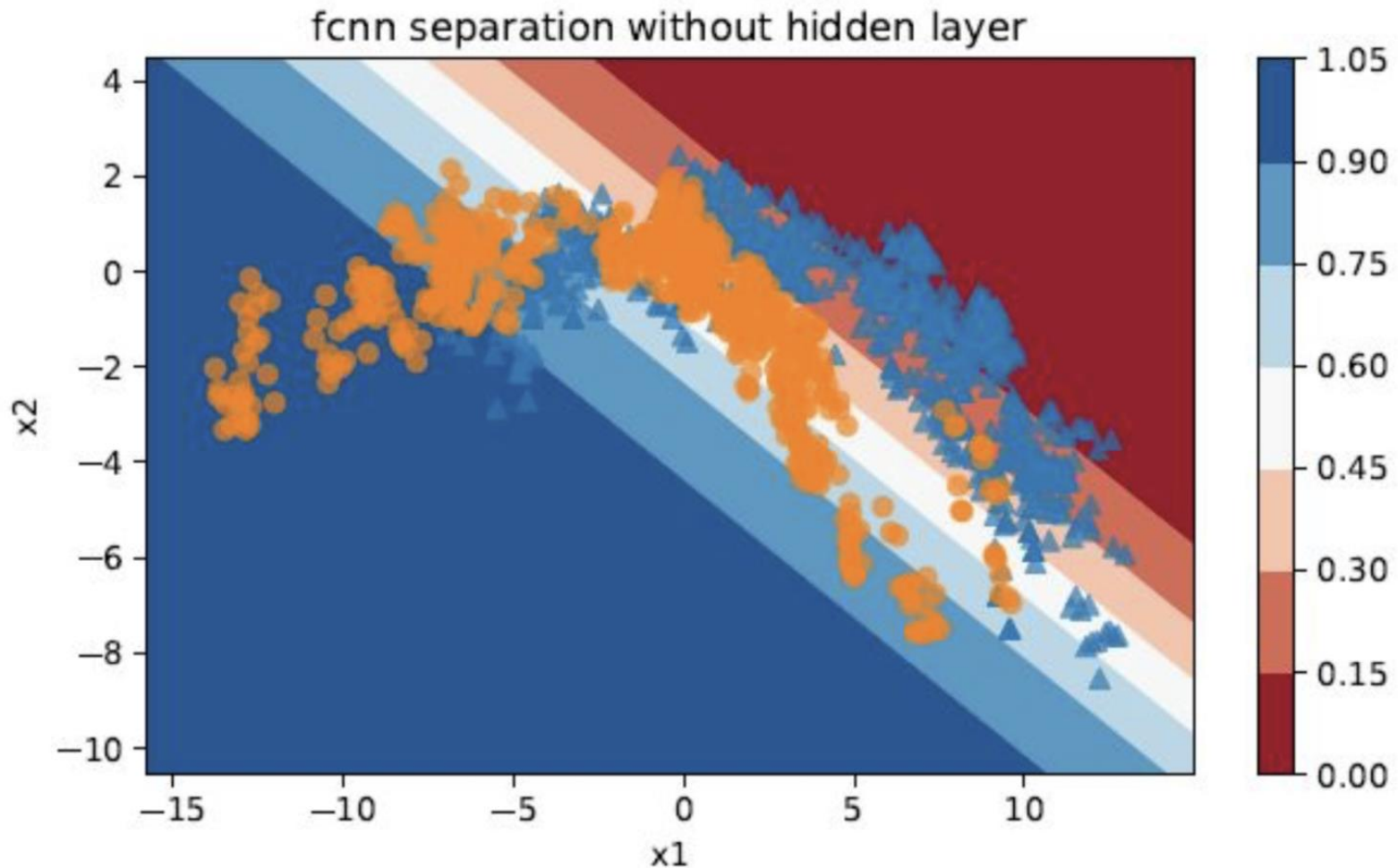


Figure 2.5 The (training) data points for the real and faked banknotes

Result (see later in the notebook)



General rule: Networks without hidden layer have linear decision boundary.

Our take on Deep Learning: Probabilistic Viewpoint

Tasks in supervised DL

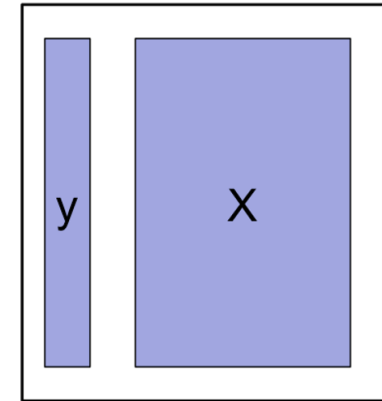
- 2 Main tasks in DL predict y given x

- **Classification**

- Point prediction: Predict a class label
- Probabilistic prediction:
predict a discrete probability distribution over all possible class labels

- **Regression**

- Point prediction: Predict a number
- Probabilistic prediction:
predict a continuous probability distributions over the possible Y value range



Supervised Learning

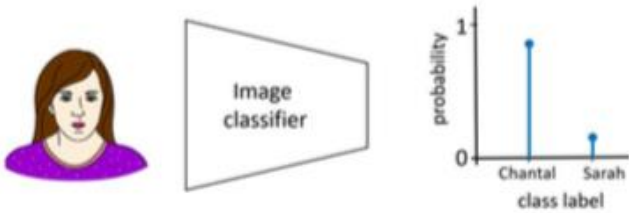
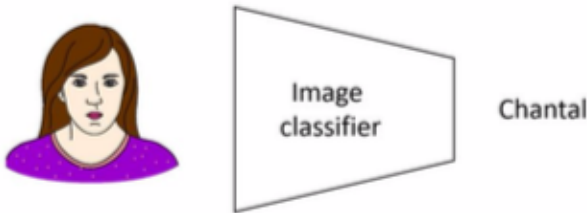
- The loss function depends on the task

Probabilistic vs deterministic models

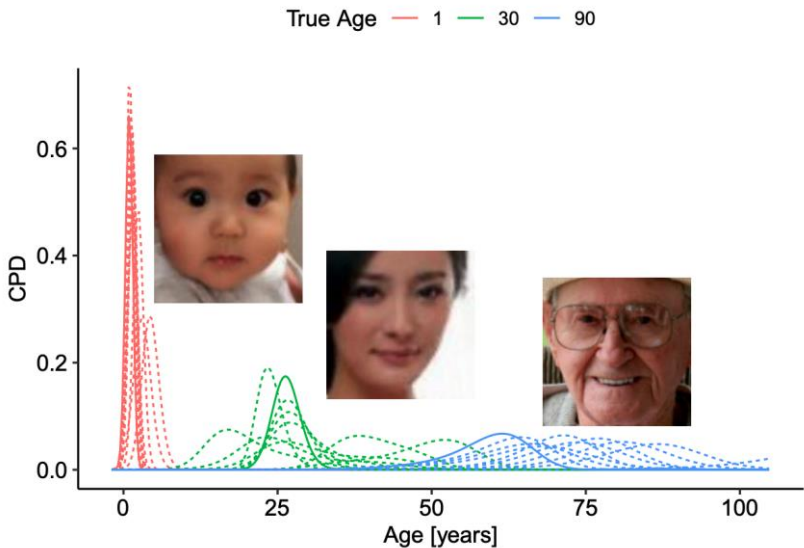
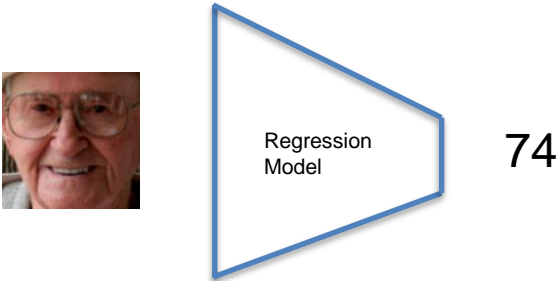
Deterministic

Probabilistic

“Classification”



“Regression”



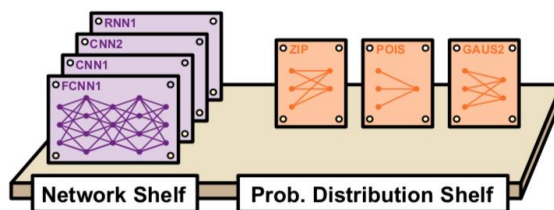
Conditional probability distribution (CPD)
 $p(y|x)$

Guiding Theme of the course

- We treat DL as *probabilistic models*, as statistical model (logistic regression, ...) to predict the conditional probability distribution $P(Y|x)$ for the outcome
- The models are fitted to training data with maximum likelihood (or Bayes)

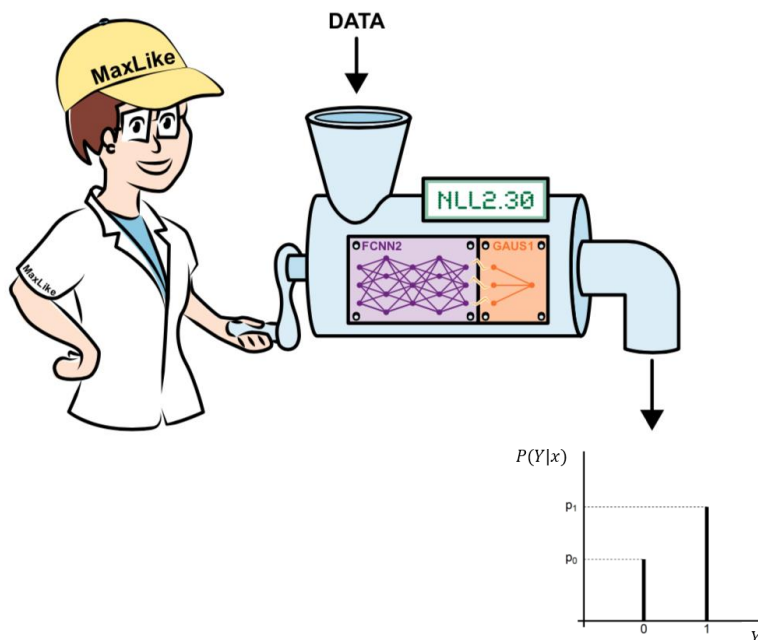
Special networks for x

- Vector FCNN
- Image CNN
- Text CNN/RNN



NN heads tailored for Y

- Probabilistic classification
- Probabilistic regression



Recall linear regression from statistics

$$(Y|X = x_i) \sim N(\mu(x_i), \sigma^2)$$

$$Y \in \mathbb{R},$$

$$\mu_x \in \mathbb{R}$$

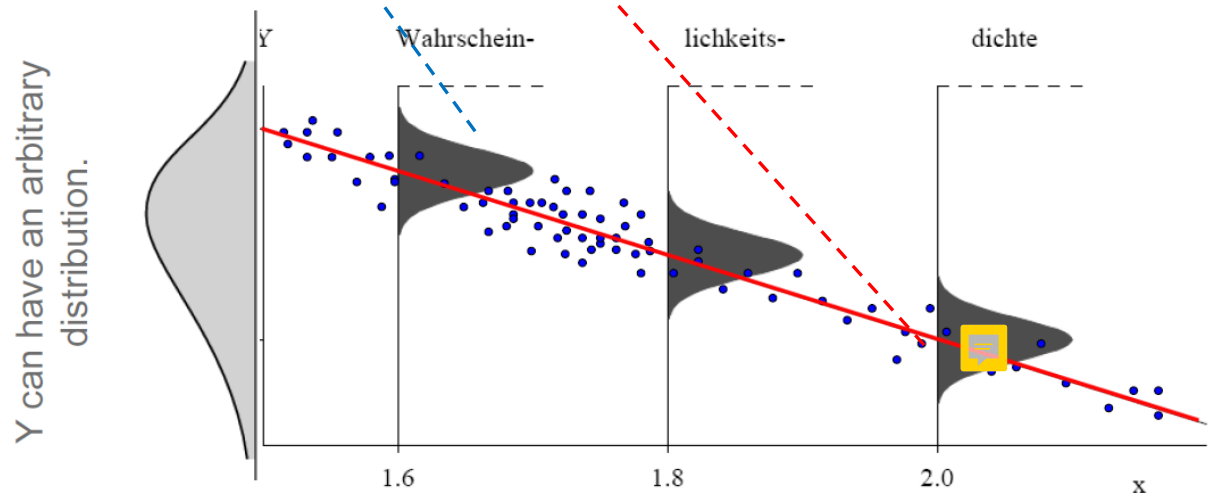
Probabilistic linear regression predicts for each input x_i a Gaussian conditional probability distribution for the output $P(Y|x_i)$ that assigns each possible value of Y a likelihood.

$$y_i = \beta_0 + \beta_1 \cdot x_{i1} + \varepsilon_i$$

$$E(Y_{X_i}) = \mu_{x_i} = \hat{y}_{x_i} = \beta_0 + \beta_1 \cdot x_{i1}$$

$$\text{Var}(Y_{X_i}) = \text{Var}(\varepsilon_i) = \sigma^2$$

$$\varepsilon_i \sim N(0, \sigma^2)$$



Recall logistic regression from statistics

$(Y|X_i) \sim \text{Ber}(p_{x_i})$

$Y \in \{0,1\}$

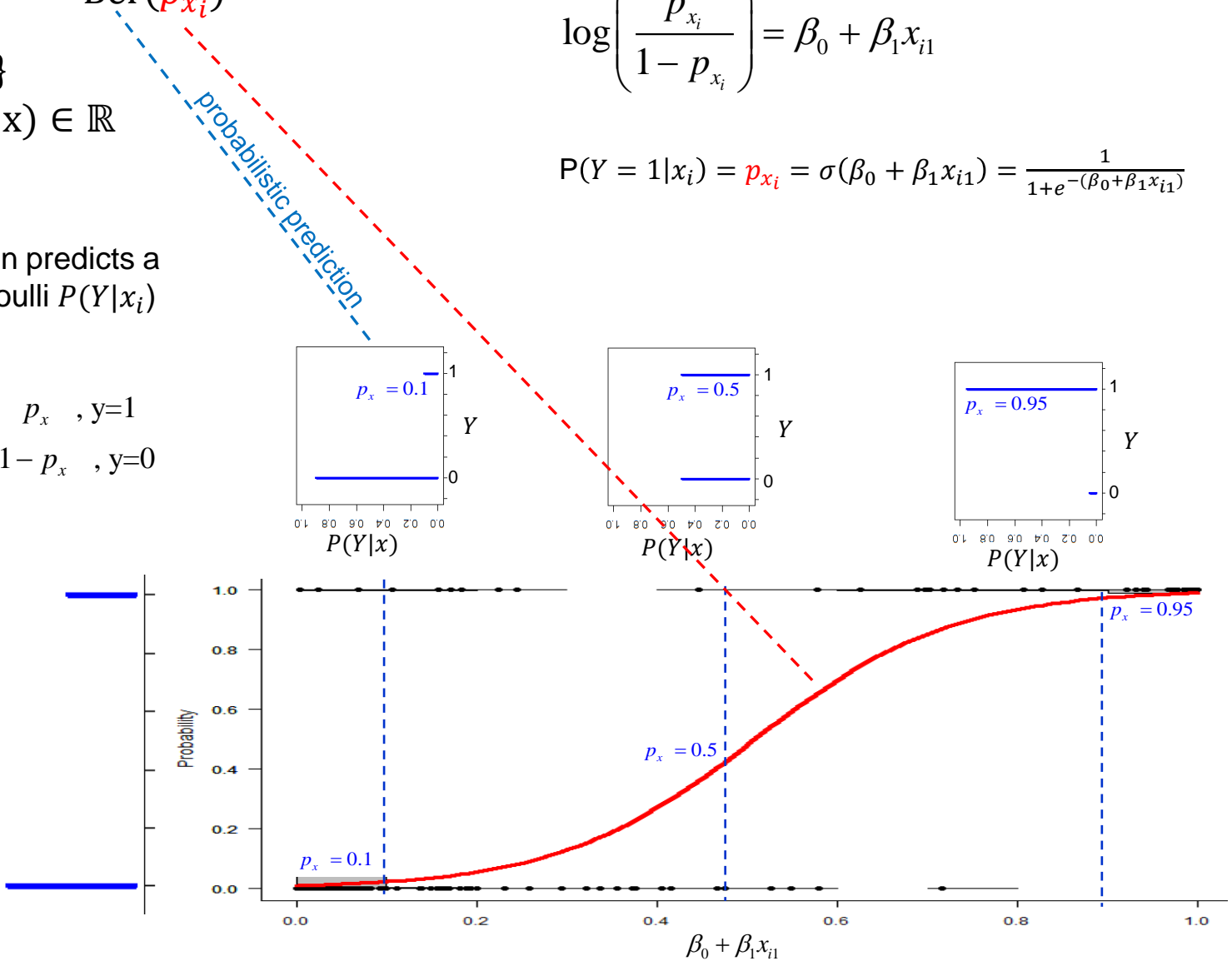
$p_x = P(Y = 1|x) \in \mathbb{R}$

Logistic regression predicts a conditional Bernoulli $P(Y|x_i)$

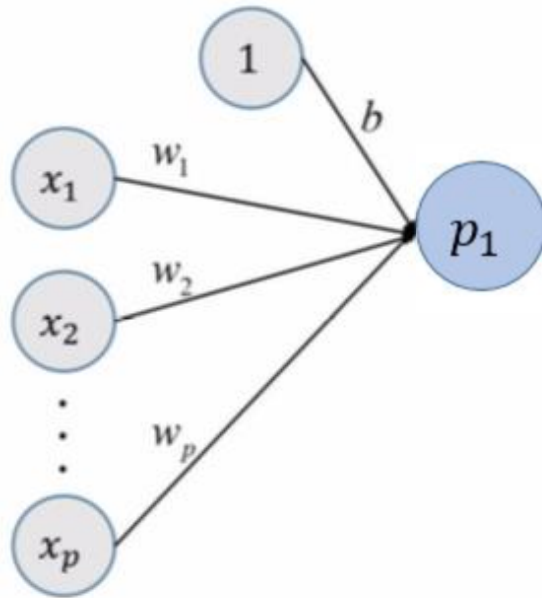
$\log\left(\frac{p_{x_i}}{1 - p_{x_i}}\right) = \beta_0 + \beta_1 x_{i1}$

$P(Y = 1|x_i) = p_{x_i} = \sigma(\beta_0 + \beta_1 x_{i1}) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_{i1})}}$

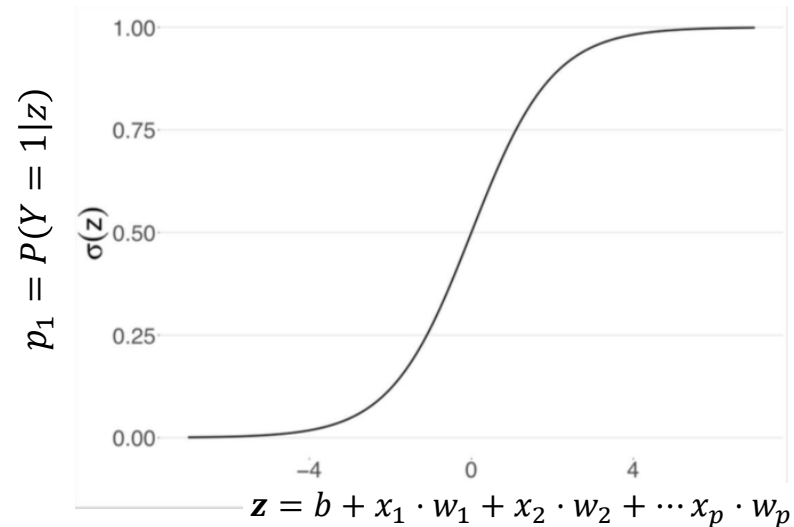
$$P(Y | X = x) = \begin{cases} p_x & , y=1 \\ 1 - p_x & , y=0 \end{cases}$$



Logistic regression in DL view



Sigmoid Activation



$$p_1 = P(Y = 1|z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$

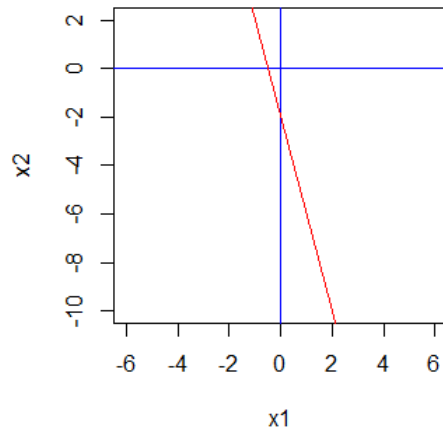
A NN for a binary outcome with only 1 neuron with sigmoid-activation (and no hidden layer) is nothing else than logistic regression!

Logistic regression yield linear/planar decision curves

Logistic regression model: $\ln\left(\frac{p}{1-p}\right) = 1 + 2x_1 + 0.5x_2$

Determine the **separation curve between $Y=1$ and $Y=0$** in the feature room which is spanned by x_1 and x_2 and draw it in the following plot x_2 and x_1 .

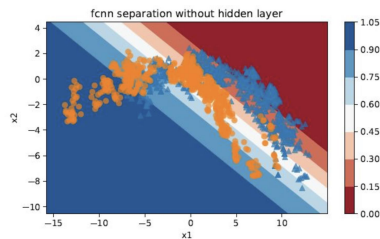
Hint: on the separation curve should hold: $P(Y = 1|x) = 0.5$
-> plug in 0.5 for p and solve for x_2 .



$$\ln\left(\frac{0.5}{1-0.5}\right) = 0 = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

$$x_2 = -\frac{\beta_0}{\beta_2} - \frac{\beta_1}{\beta_2} \cdot x_1$$

$$x_2 = -2 - 4 \cdot x_1$$



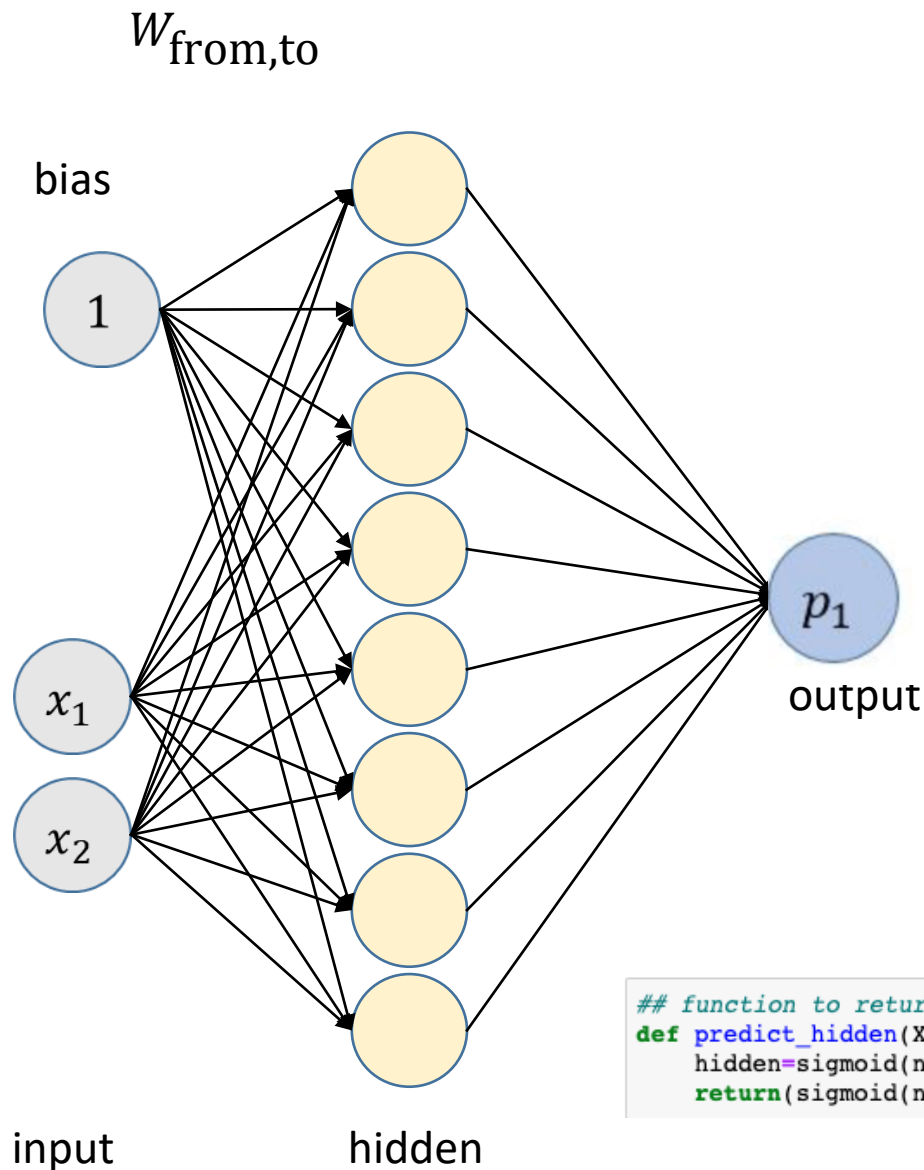
Hence a NN with 1 output neuron with sigmoid-activation w/o hidden layer have linear decision boundary

A close-up shot of Leonardo DiCaprio in a dark suit and tie, looking slightly to his right with a serious expression. Another man's profile is visible on the right side of the frame. The background is dark and out of focus.

WE NEED TO GO

DEEPER

A first deep network



In math ($f = \text{sigmoid}$)
$$p = f(f(X \cdot W_1 + b_1) \cdot W_2 + b_2)$$

In code:

```
## function to return the probability output after the hidden layer
def predict_hidden(X):
    hidden=sigmoid(np.matmul(X,W1)+b1)
    return(sigmoid(np.matmul(hidden,W2)+b2))
```

To go deep non-linear activation functions are needed

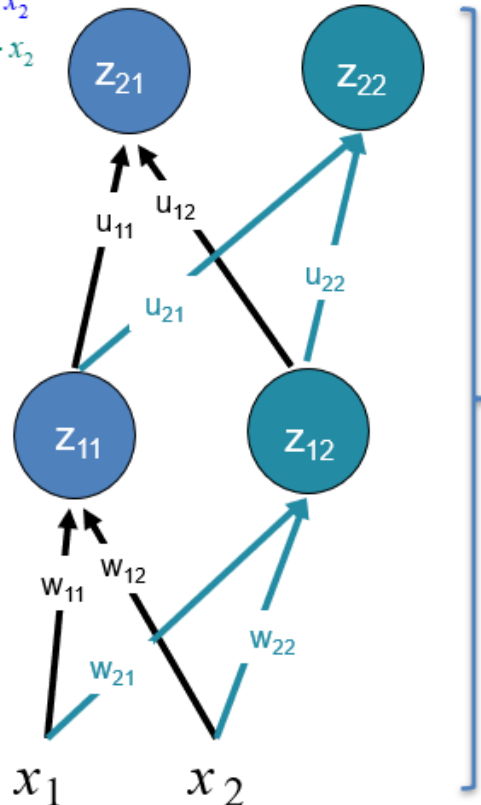
2 linear layers can be replaced by 1 linear layer -> can't go deep with linear layers!

$$z = (x \cdot W) \cdot U = x \cdot (W \cdot U) = x \cdot V$$

$$\begin{aligned} z_{21} &= z_{11} \cdot u_{11} + z_{12} \cdot u_{12} = (w_{11} \cdot x_1 + w_{12} \cdot x_2) \cdot u_{11} + (w_{21} \cdot x_1 + w_{22} \cdot x_2) \cdot u_{12} \\ &= x_1 \cdot (w_{11} \cdot u_{11} + w_{21} \cdot u_{12}) + x_2 \cdot (w_{12} \cdot u_{11} + w_{22} \cdot u_{12}) \end{aligned}$$

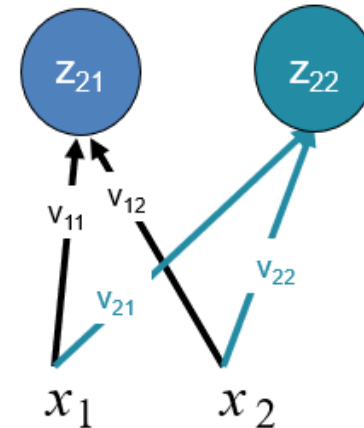
$$z_{11} = w_{11} \cdot x_1 + w_{12} \cdot x_2$$

$$z_{12} = w_{21} \cdot x_1 + w_{22} \cdot x_2$$



=

$$z_{21} = v_{11} \cdot x_1 + v_{12} \cdot x_2$$



$$v_{11} = w_{11} \cdot u_{11} + w_{21} \cdot u_{12}$$

$$v_{12} = w_{12} \cdot u_{11} + w_{22} \cdot u_{12}$$

$$v_{21} = w_{11} \cdot u_{21} + w_{21} \cdot u_{22}$$

$$v_{22} = w_{12} \cdot u_{21} + w_{22} \cdot u_{22}$$

Remark: biases are ignored here, but do not change fact

Recap: Matrix Multiplication aka dot-product of matrices

We can only multiply matrices if their dimensions are compatible.

$$\mathbf{A} \times \mathbf{B} = \mathbf{C}$$
$$(m \times n) \times (n \times p) = (m \times p)$$

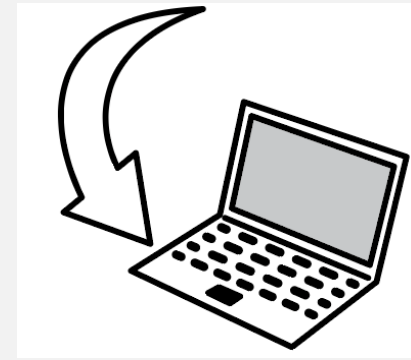
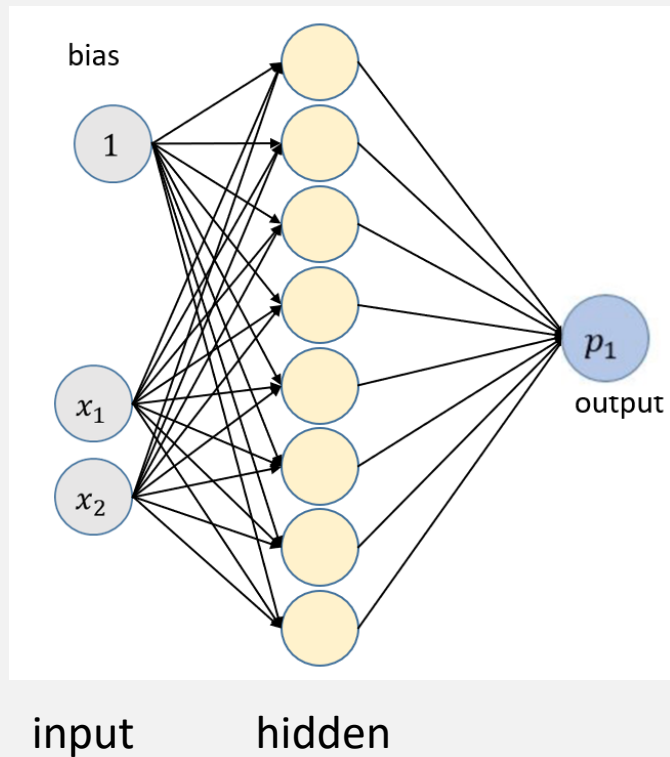
$$\begin{matrix} \mathbf{A}_{3 \times 3} & \times & \mathbf{B}_{3 \times 2} & = & \mathbf{C}_{3 \times 2} \\ \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} & \times & \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{bmatrix} & = & \begin{bmatrix} c_{11} & c_{12} \\ c_{21} & c_{22} \\ c_{31} & c_{32} \end{bmatrix} \end{matrix}$$

$$\begin{aligned} c_{11} &= a_{11}b_{11} + a_{12}b_{21} + a_{13}b_{31} \\ c_{12} &= a_{11}b_{12} + a_{12}b_{22} + a_{13}b_{32} \\ c_{21} &= a_{21}b_{11} + a_{22}b_{21} + a_{23}b_{31} \\ c_{22} &= a_{21}b_{12} + a_{22}b_{22} + a_{23}b_{32} \\ c_{31} &= a_{31}b_{11} + a_{32}b_{21} + a_{33}b_{31} \\ c_{32} &= a_{31}b_{12} + a_{32}b_{22} + a_{33}b_{32} \end{aligned}$$

Example:

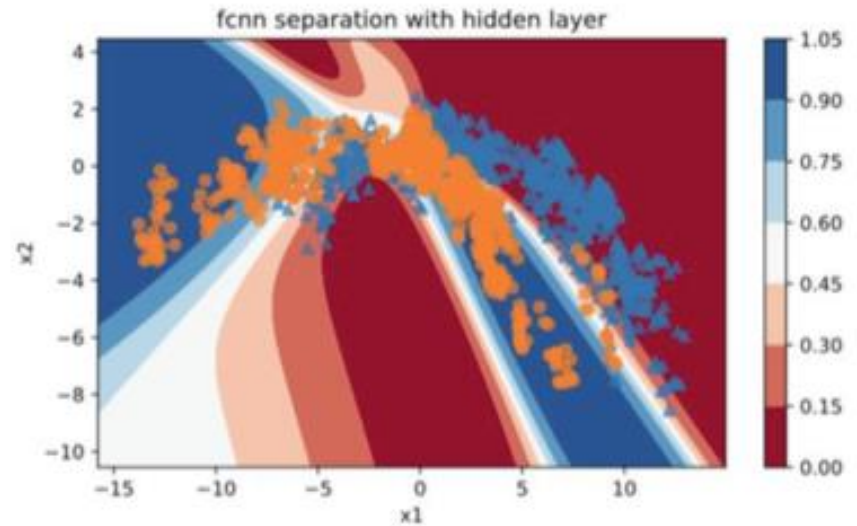
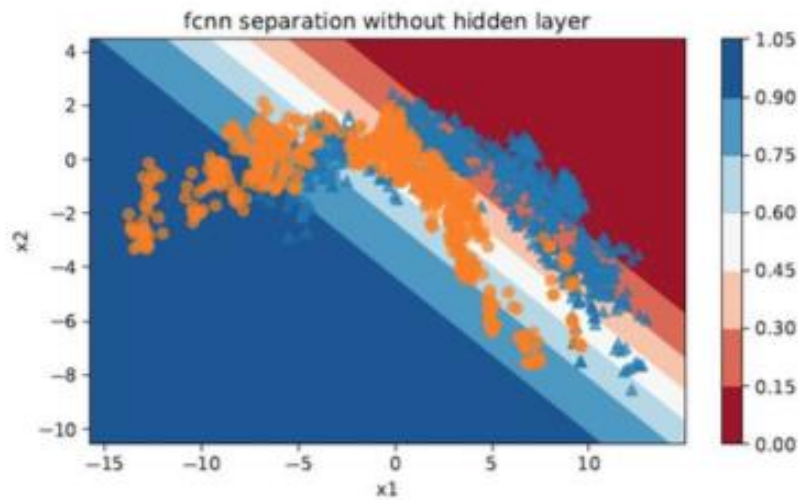
$$\mathbf{A}_{2 \times 2} = \begin{pmatrix} 2 & 1 \\ 0 & 3 \end{pmatrix} \quad \mathbf{B}_{2 \times 3} = \begin{pmatrix} 3 & 1 & 7 \\ 8 & 2 & 4 \end{pmatrix} \quad \mathbf{C}_{2 \times 3} = \mathbf{A}_{2 \times 2} \cdot \mathbf{B}_{2 \times 3} = \begin{pmatrix} 11 & 4 & 18 \\ 24 & 6 & 12 \end{pmatrix}$$

Exercise:

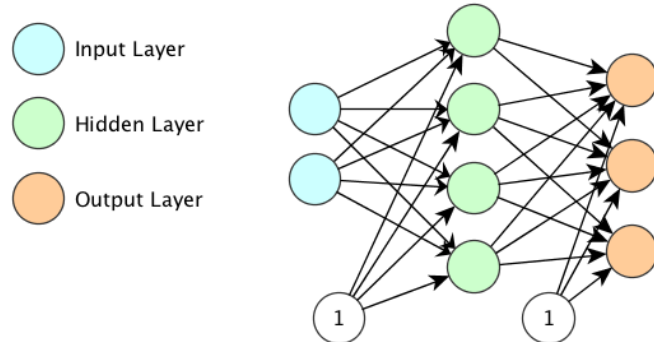


Open NB [01_simple_forward_pass.ipynb](#) and do exercise stop before Keras

Observations from NB: The benefit of hidden layers

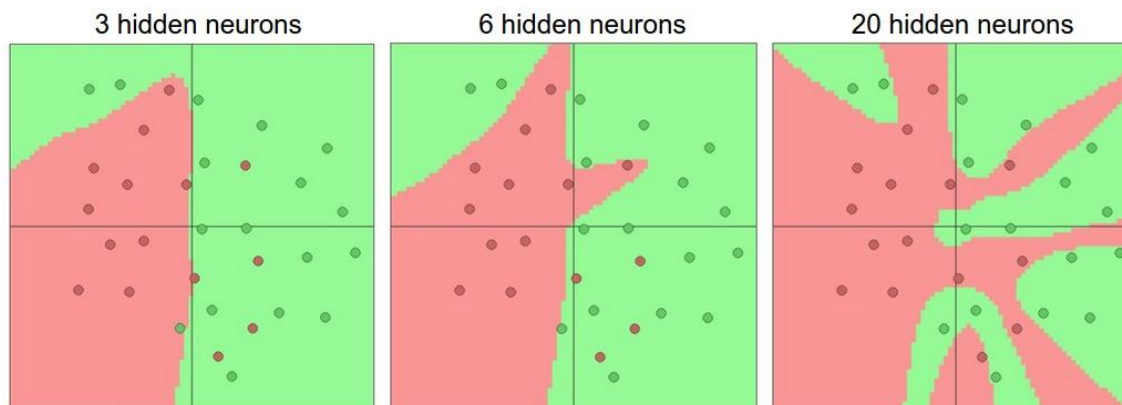


One hidden Layer is “in theory” enough



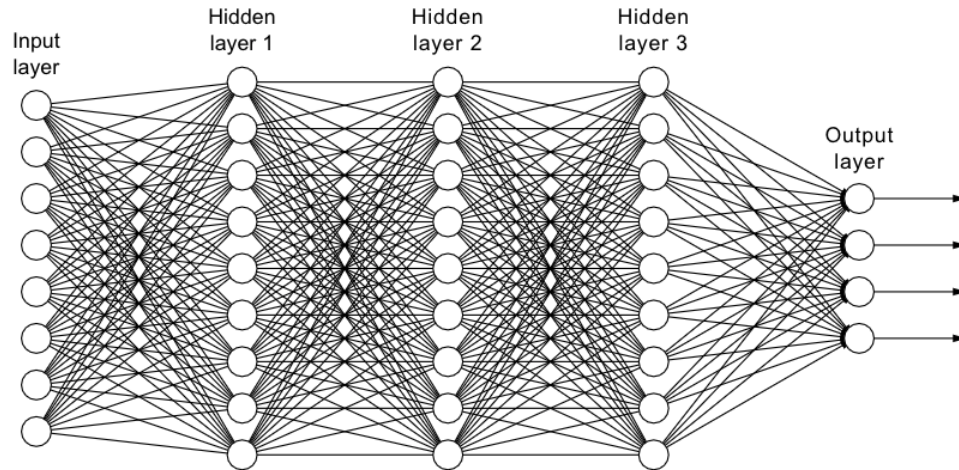
A network with one hidden layer is a universal function approximator!

→ Each decision curve can be fitted with a NN with large enough hidden layer



**Training NN:
Minimize the loss function**

How to determine the weights



Given the input, the output of a NN is defined by the weights

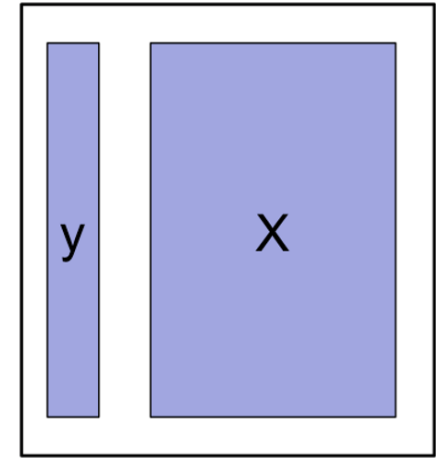


Typical >1 Mio. weights

During training the weights (including biases) are tuned so that the NN bests fulfils its specific tasks by minimizing a loss function.

Tasks in DL

- The loss function depends on the task
- 2 Main tasks in DL predict y given x



Supervised Learning

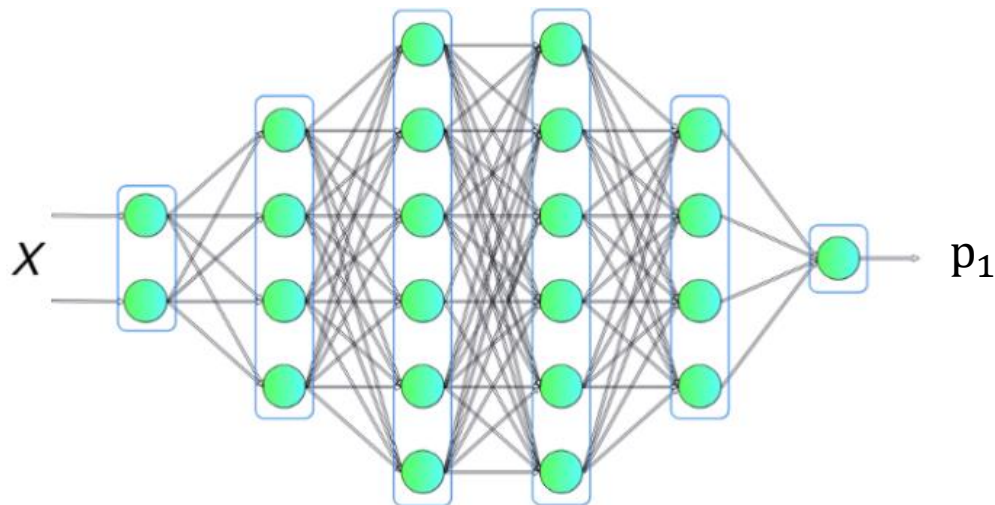
– Classification

- Point prediction: Predict a class label
- Probabilistic prediction: predict a discrete probability distribution over the class labels
- **First we focus on probabilistic binary classification where $Y \in \{0, 1\}$**

– Regression

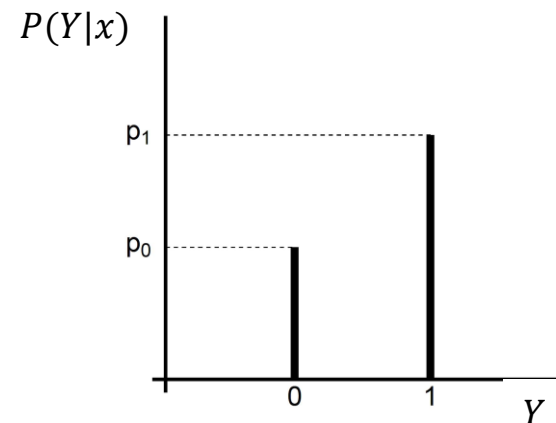
- Point prediction: Predict a number
- Probabilistic prediction: predict a continuous distributions

Example of a NN for binary classification



For binary classification we can use one neuron in the last layer with sigmoid activation yielding a conditional probability p_1 for $Y = 1$

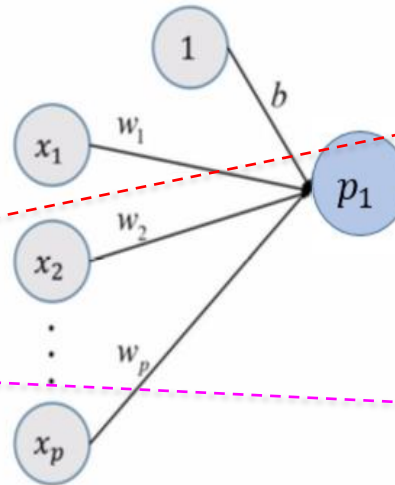
Given (=conditioned on) the input features x of an observation, the NN predicts as output the probability that this observation corresponds to class $Y = 1$ by $p_1 = P(Y = 1|x)$, and hence the probability for the $Y = 0$ is $p_0 = P(Y = 0|x) = 1 - p_1$.



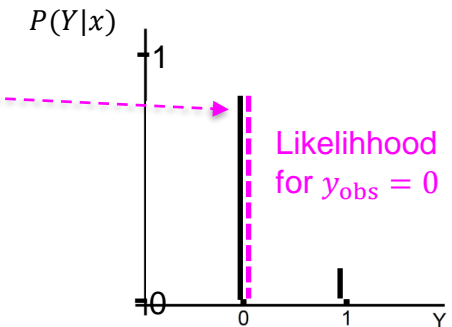
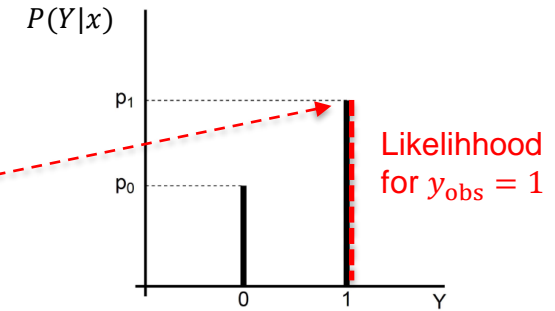
Probabilistic binary classification aka logistic regression

Training data set

x1	...	x_p	y
0.4	...	-1.3	0
1.1	...	0.2	1
⋮	⋮	⋮	⋮
0.6	...	-0.9	0



probabilistic prediction



Given (=conditioned on) the input features x of an observation i , a well trained NN

- should predict large $p_1 = P(Y = 1|x)$ if the observed class is $y_i = 1$
- should predict small p_1 hence large $p_0 = P(Y = 0|x)$ if observed is $y_i = 0$

→ The likelihood (for the observed outcome) or LogLikelihood should be large



$$\text{LogLikelihood} = \sum_{i=1}^n [y_i \log(p_{1i}) + (1 - y_i) \log(1 - p_{1i})] \quad \text{Notation trick in statistics – it selects correct log-probability since } y_i \in \{0,1\}$$

Fitting a probabilistic binary classification

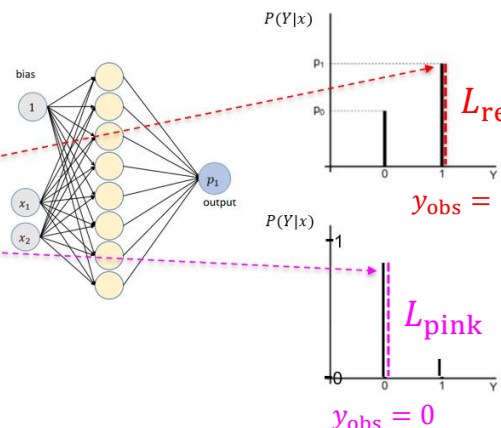
The Likelihood of an observation i is the likelihood (probability), that the predicted probability distribution $P(Y|x_i)$ assigns to the observed outcome y_i .

Note: the predicted $P(Y|x_i)$ and the corresponding likelihood for the observed y_i depends on the data-point (x_i, y_i) and the model parameter values

→ The higher the likelihood, the better is the model prediction $P(Y|x)$

Training data set

x_1	...	x_p	y
0.4	...	-1.3	0
1.1	...	0.2	1
⋮	⋮	⋮	⋮
0.6	...	-0.9	0



L_{red} is likelihood of red observation with $y_{\text{obs}} = 1$

L_{pink} is likelihood of pink observation with $y_{\text{obs}} = 0$

Maximum likelihood principle:

Statistical models are fit to maximize the average LogLikelihood

$$L = \frac{1}{N} \sum L_i = \frac{1}{N} \sum [y_i \log(p_{1i}) + (1 - y_i) \log(1 - p_{1i})]$$

we often use the simplified notation average logLik : $L = \frac{1}{N} \sum \log(p_i)$

Predicted probability for the observed outcome y_{obs}

NLL Loss for probabilistic binary classification

In DL we aim to minimize a loss function $L(\text{data}, w)$ which depends on the weights

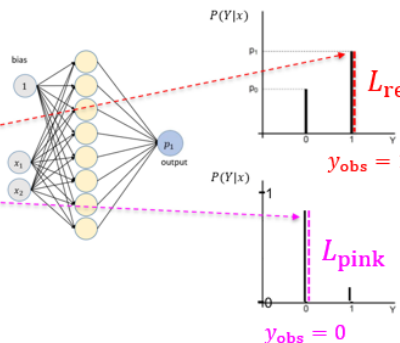
→ Instead of maximizing the average LogLikelihood

we minimize the averaged Negative LogLikelihood (NLL):

$$\text{loss} = \text{NLL} = -\frac{1}{N} \sum \log(L_i)$$

Training data set

x1	...	xp	y
0.4	...	-1.3	0
1.1	...	0.2	1
⋮	⋮	⋮	⋮
0.6	...	-0.9	0



L_{red} is likelihood of red observation with $y_{\text{obs}} = 1$

L_{pink} is likelihood of pink observation with $y_{\text{obs}} = 0$

The best possible value of the NLL contribution of an observation i is $\log(L_i) = -\log(1) = 0$

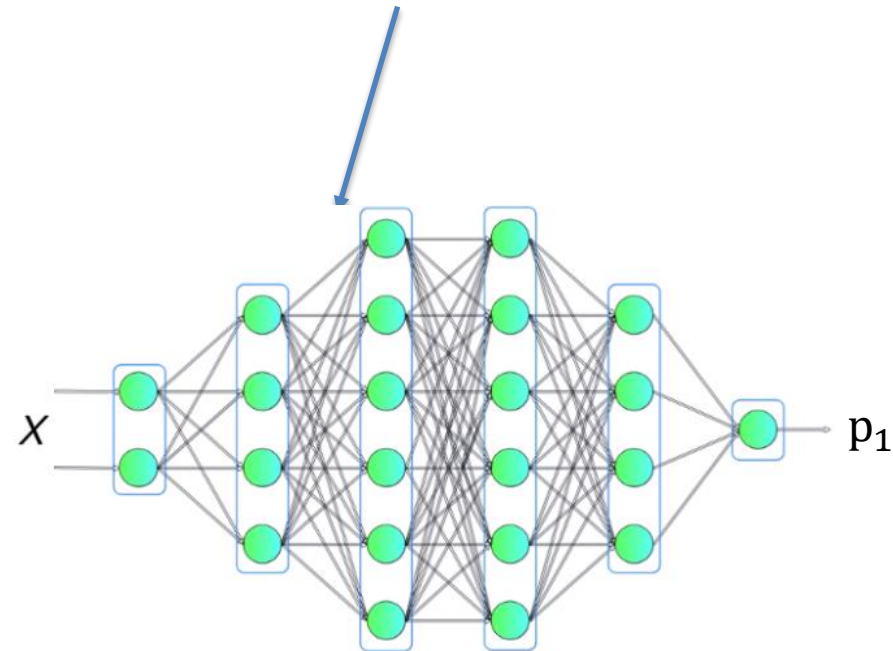
The worst possible value of the NLL contribution of an observation i is $\log(L_i) = -\log(0) = \infty$

Note: In Keras we use the loss 'binary_crossentropy', if we do probabilistic binary classification with one output node with sigmoid activation.

Optimization in DL

- DL many parameters
 - Optimization by gradient descent
- Algorithm
 - Take a batch of training examples
 - Calculate the loss of that batch
 - Tune the parameters so that loss gets minimized

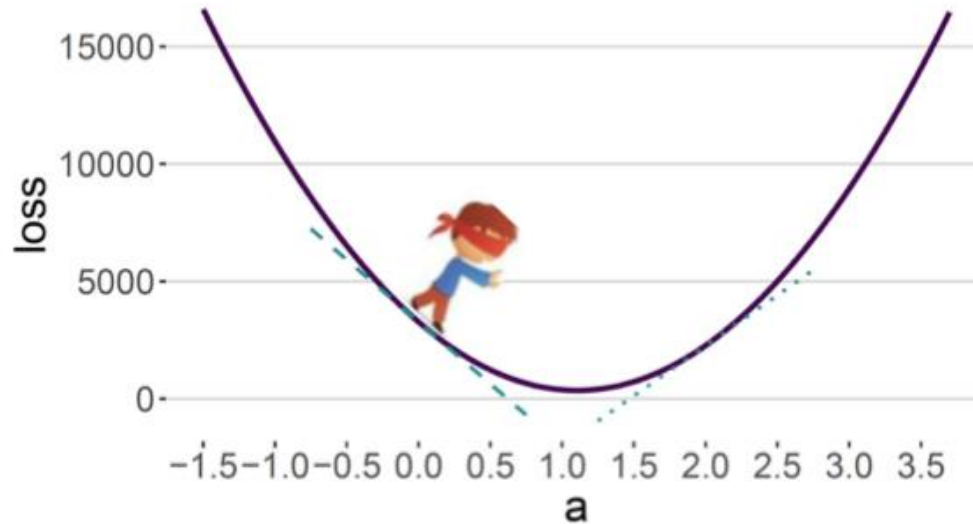
Parameters of the NN are the weights.



Modern Networks have Billions (10^9) of weights. Record 2020 1.5E9
<https://openai.com/blog/better-language-models/>

Idea of gradient descent

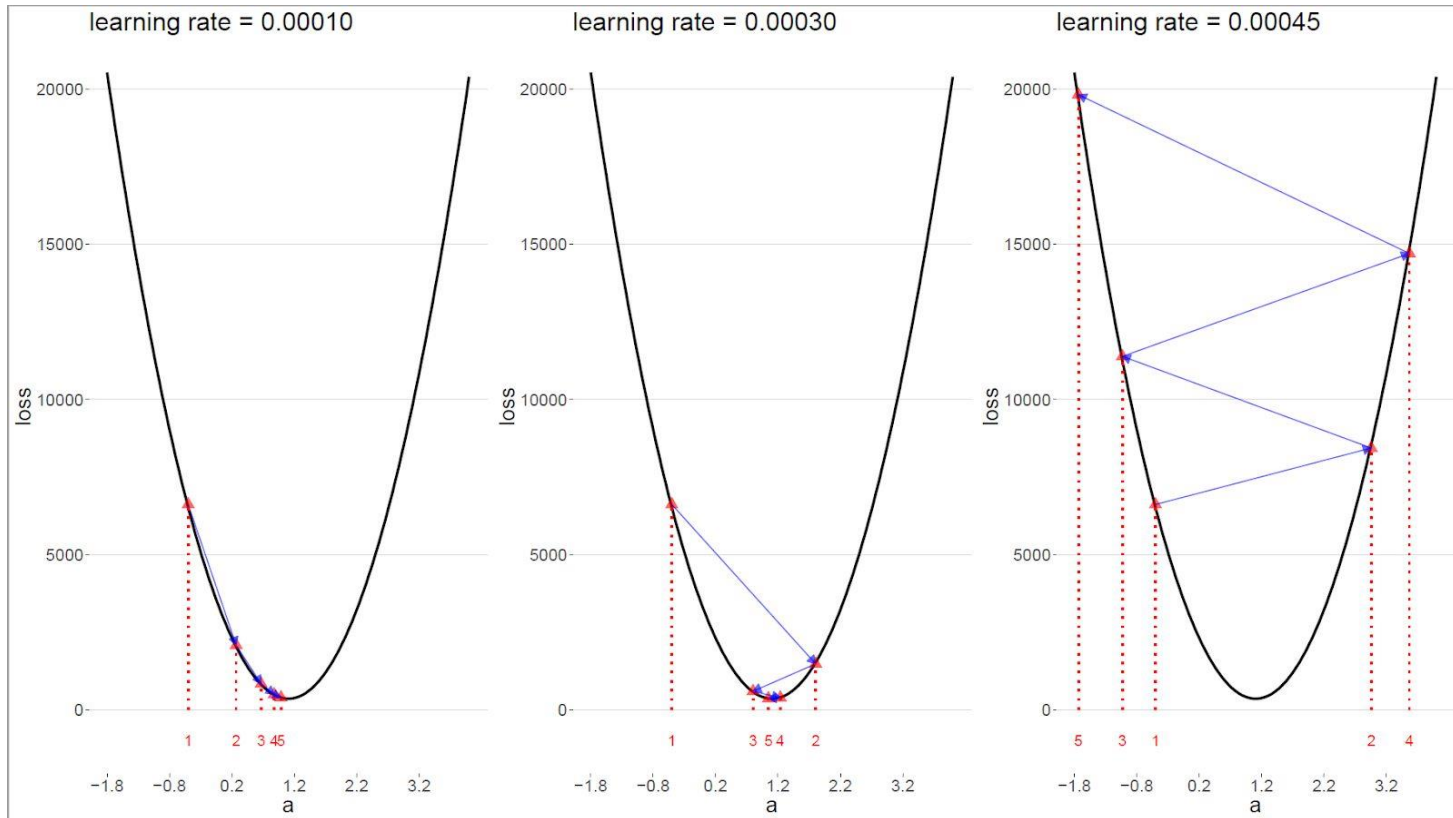
- Shown loss function for a single parameter a



- Take a large step if slope is steep (you are away from minimum)
- Slope of loss function is given by gradient of the loss w.r.t. a
- Iterative update of the parameter a

$$a^{(t)} = a^{(t-1)} - \underset{\substack{\uparrow \\ \text{learning rate}}}{\varepsilon^{(t)}} \left. \frac{\partial L(a)}{\partial a} \right|_{a=a^{(t-1)}}$$

The learning rate is a very important parameter for DL



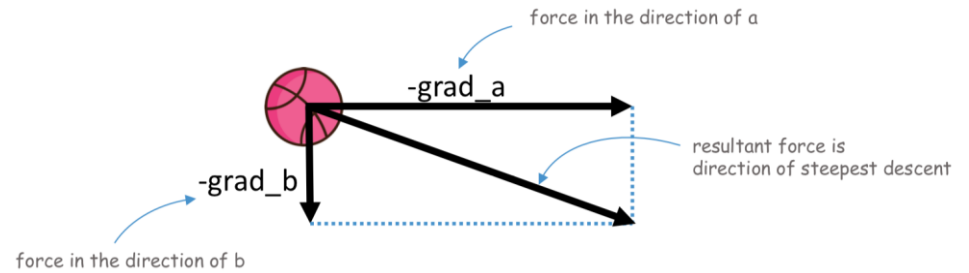
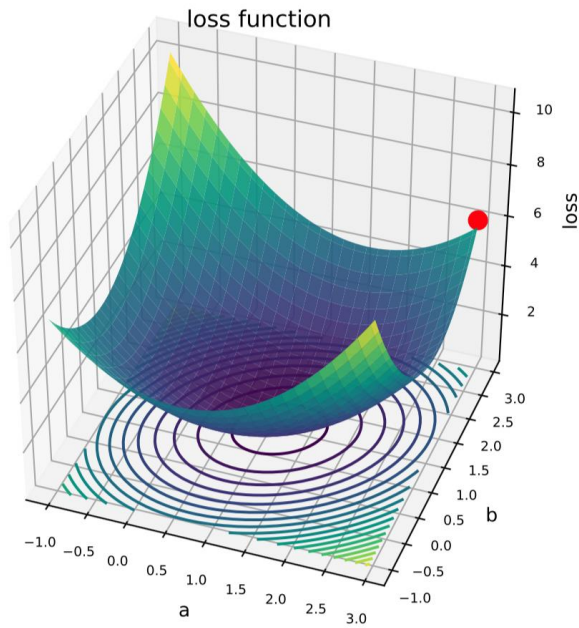
good – little slow

good

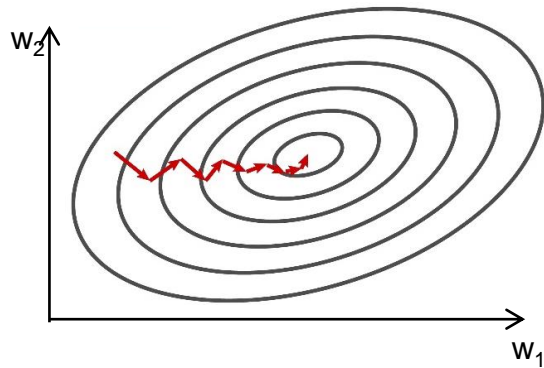
learning rate too high

If the loss diverges to infinity: Don't panic, lower the learning rate!

In two dimensions



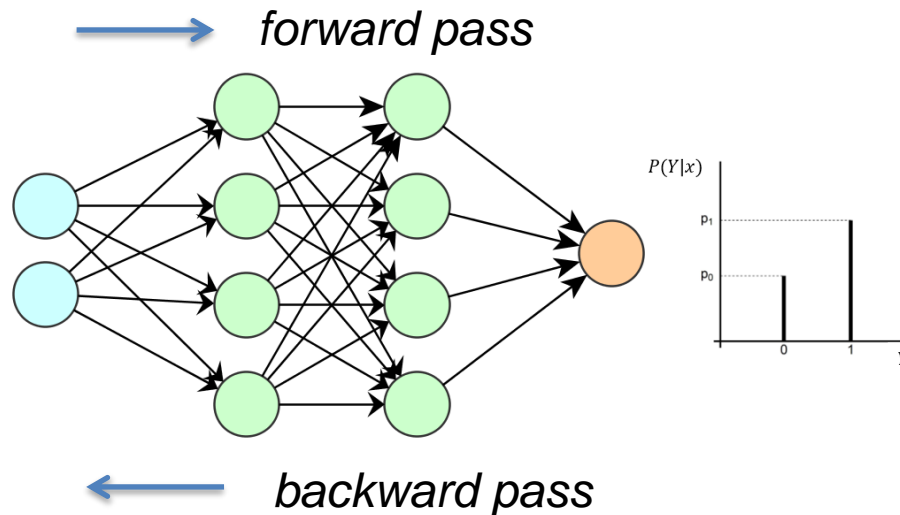
Gradient is perpendicular to contour lines



$$w_i^{(t)} = w_i^{(t-1)} - \varepsilon^{(t)} \left. \frac{\partial L(\mathbf{w})}{\partial w_i} \right|_{w_i = w_i^{(t-1)}}$$

Backpropagation

- We efficiently train the weights in a NN via forward and backward pass
 - Forward Pass propagate training example through network
 - Predicts as output $P(Y|x_i)$ for each input x_i in the batch given the NN weights w
→ With $P(Y|x_i)$ and the observed y_i we compute the loss $L = \left(\text{NLL} = -\frac{1}{N} \sum \log(L_i) \right)$
 - Backward pass propagate gradients through network
 - Via chain rule all gradients $\frac{\partial L(w)}{\partial w_k}$ are determined
→ update the weights $w_i^{(t)} = w_i^{(t-1)} - \varepsilon^{(t)} \frac{\partial L(w)}{\partial w_i} \Big|_{w_i=w_i^{(t-1)}}$



The miracle of gradient descent in DL



Loss surface in DL (is not convex) but SGD magically also works for non-convex problems.

Typical Training Curve / ReLU

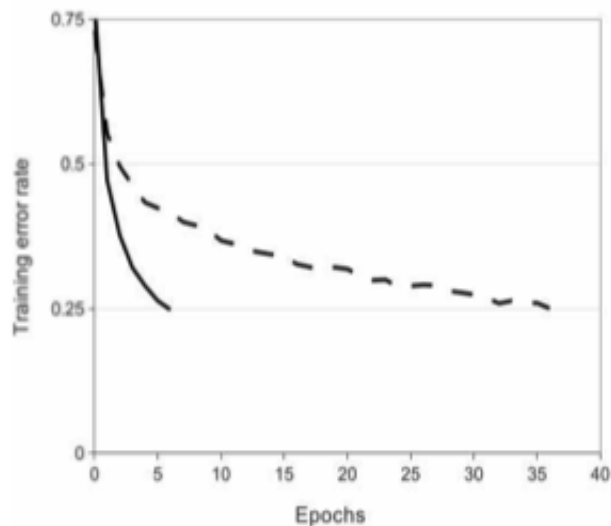
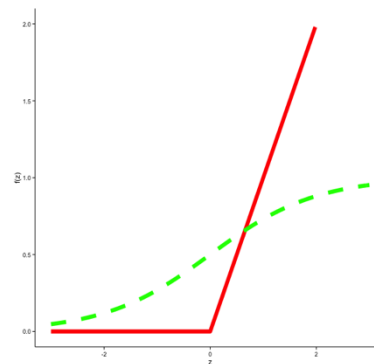
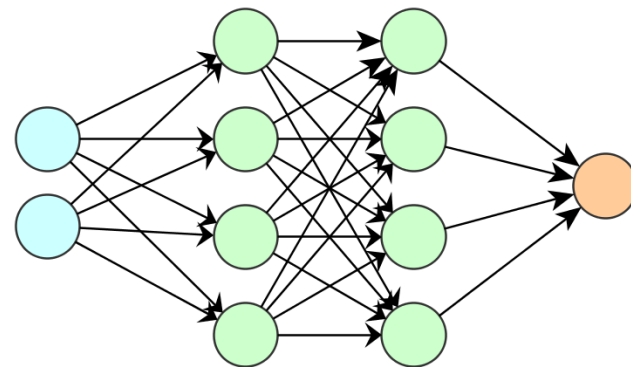
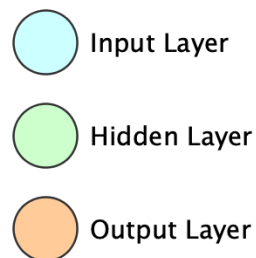


Figure 1: A four-layer convolutional neural network with ReLUs (**solid line**) reaches a 25% training error rate on CIFAR-10 six times faster than an equivalent network with tanh neurons

Source:
Alexnet
Krizhevsky et al 2012



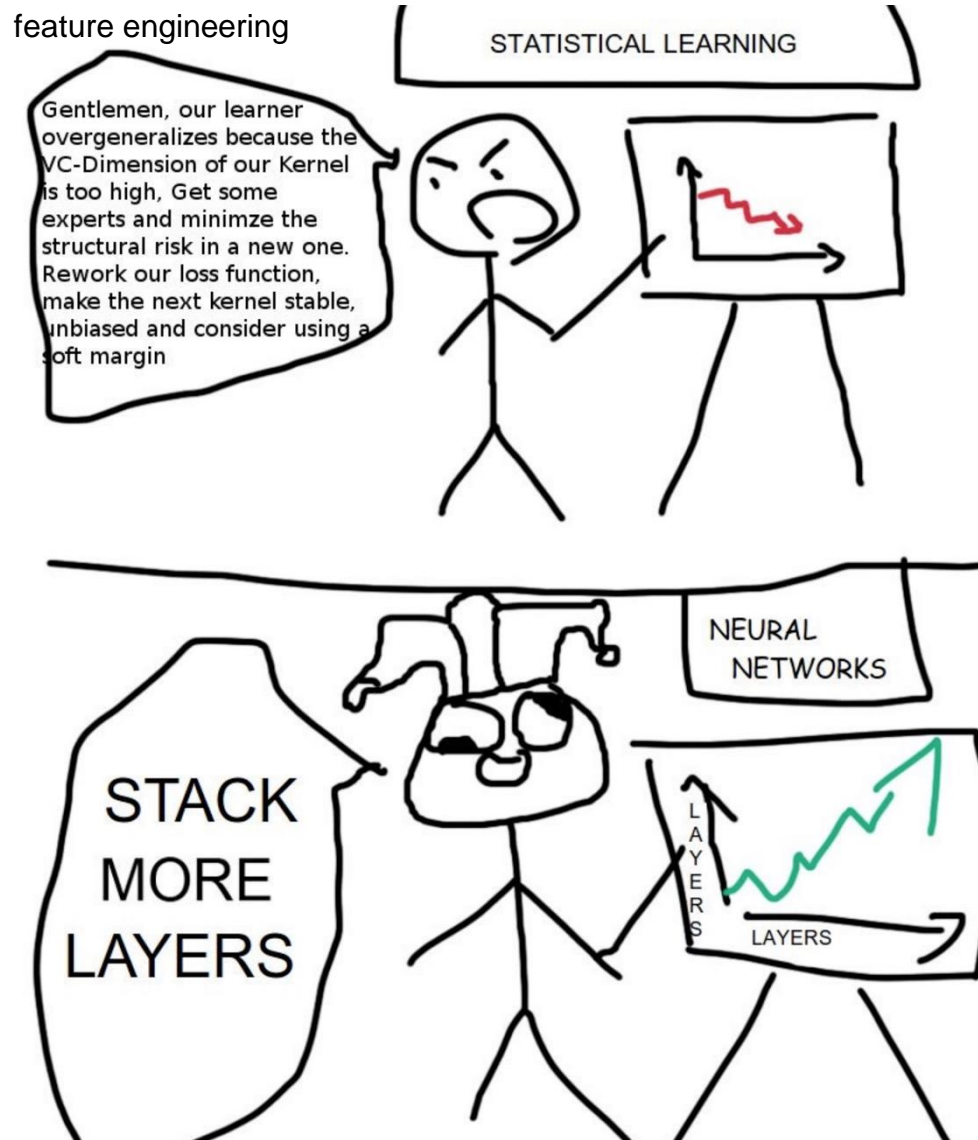
Motivation:

Green:
sigmoid.

Red:
ReLU faster
convergence

Epochs: "each training examples is used once"

Game time - Recall learning DL vs Statistical Learning



Experiment yourself (homework)

FEATURES

Which properties do you want to feed in?



+ - 2 HIDDEN LAYERS

+ -

3 neurons

+ -

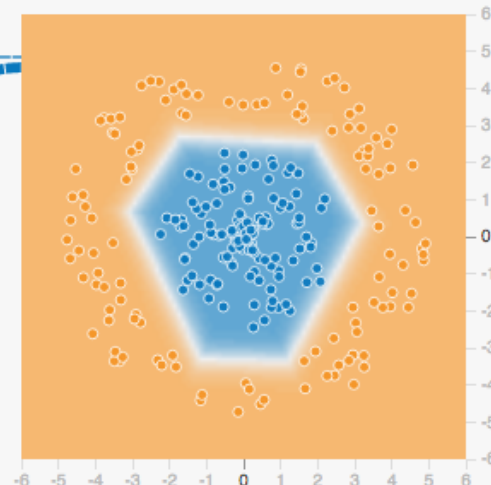
2 neurons

This is the output from one **neuron**. Hover to see it larger.

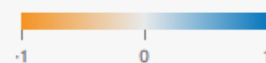
The outputs are mixed with varying **weights**, shown by the thickness of the lines.

OUTPUT

Test loss 0.016
Training loss 0.003



Colors shows data, neuron and weight values.



☐ Show test data

☐ Discretize output

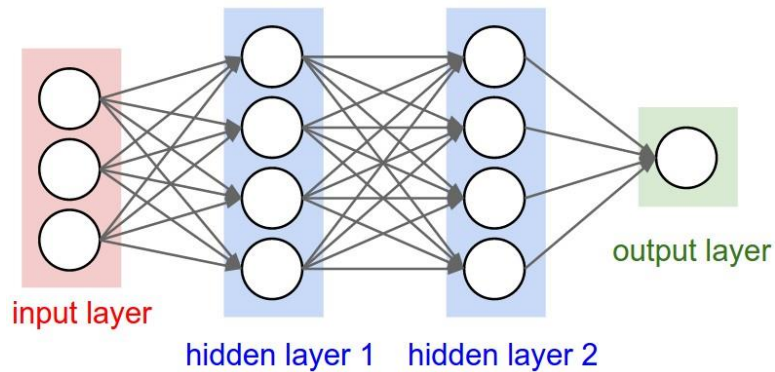
<http://playground.tensorflow.org>

Let's you explore the effect of hidden layers

Introduction to Keras

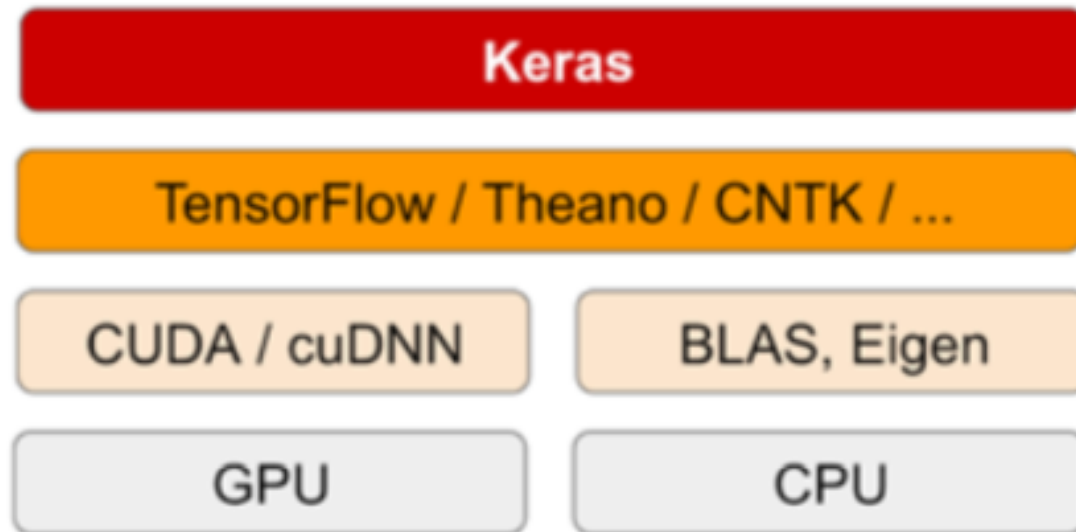
Keras as High-Level library to TensorFlow

- We use Keras as high-level library
- Libraries make use of the Lego like block structure of networks

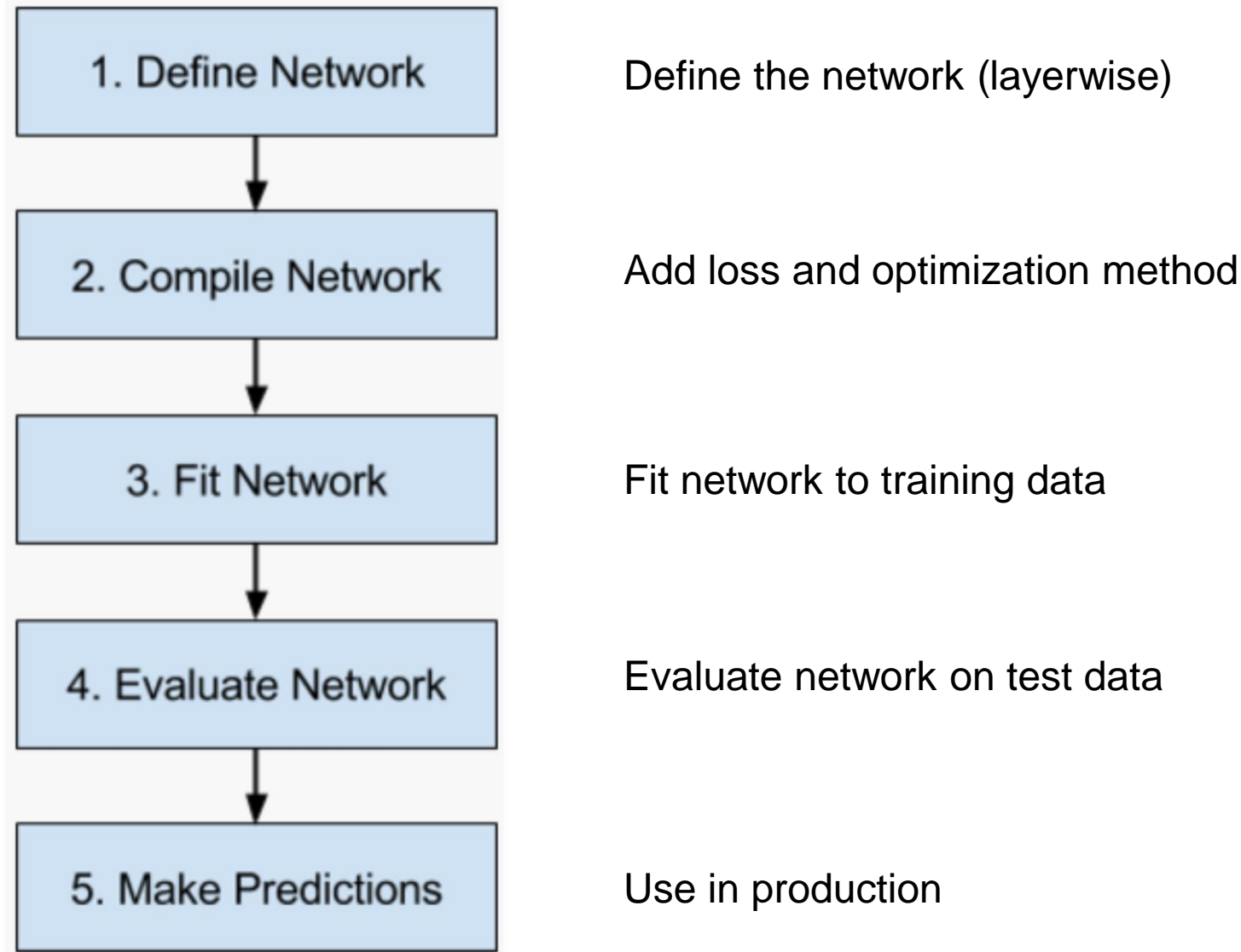


High Level Libraries

- Keras
 - Keras is now part of TF core
 - <https://keras.io/>



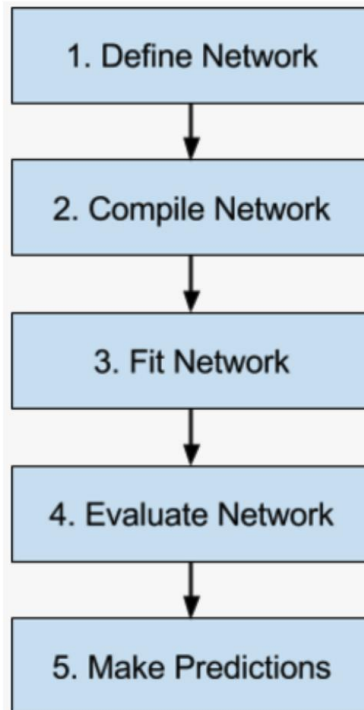
Keras Workflow



A first run through

Define the network

Sequential API, layers output are the input for the next layer, Alternative Functional API



```
# Define fcNN
model = Sequential()
model.add(Dense(8,
                 batch_input_shape=(None, 2),
                 activation='sigmoid'))
model.add(Dense(1,
                 activation='sigmoid'))
```

Hidden layer with 8 Neurons,
Activation function: sigmoid

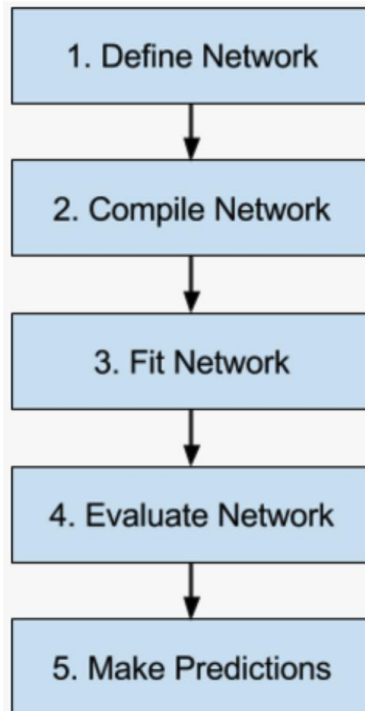
Last layer with one output neuron for
binary classification

Input shape needs to be defined only at the beginning.

Alternative: input_dim=2, Functional API or Sequential API

Compile the network

Which optimizer should be used?
Here Stochastic Gradient Descent

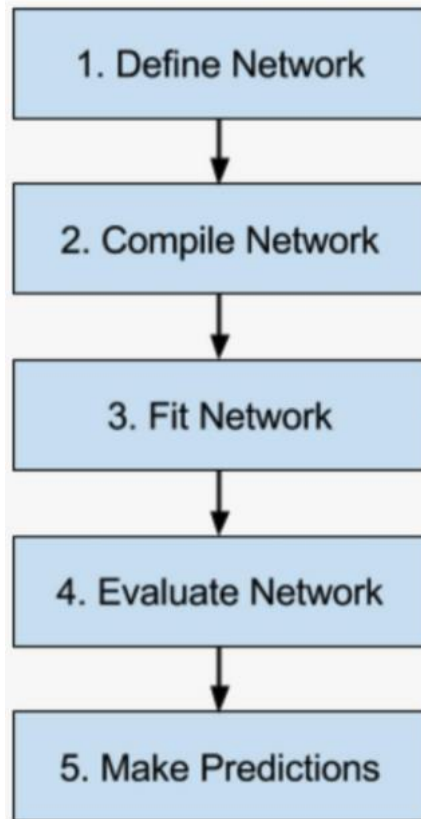


```
model.compile(optimizer=SGD(learning_rate=0.01),  
              loss='binary_crossentropy',  
              metrics=['accuracy'])
```

Loss Function to optimize
Here: Binary CE

Which metrics do we want to track,
Here: Accuracy

Fit the network



Data Tensor X for training

Label Tensor Y

Validation at
End of each epoch

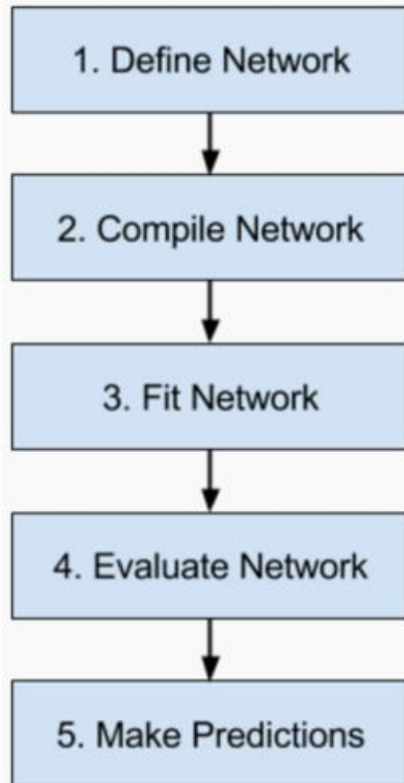
```
history = model.fit(X_train,  
                    y_train,  
                    validation_data=(X_val, y_val),  
                    epochs=1000,  
                    batch_size=10,  
                    verbose=1)
```

How many time do
we feed the whole
dataset to the
model

How many samples per
batch, 1 batch = 1 iteration
of weight updates

Should we see the whole
output? If no verbose = 0

Evaluate the network



Unseen (to the model) Test Data X with labels Y

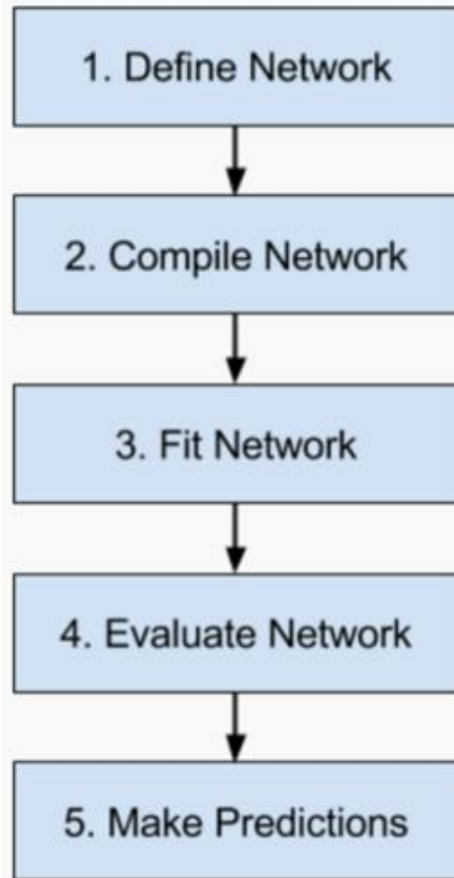
`model.evaluate(X_test, y_test, verbose=0)`

Test Loss: 0.33591118454933167, Test Accuracy: 0.8581818342208862

Remember from the
.compile

```
loss='binary_crossentropy',  
metrics=['accuracy'])
```

Make Predictions



predict with the model,
Weights are fixed now

First 10 rows
(observations) from
Testdata

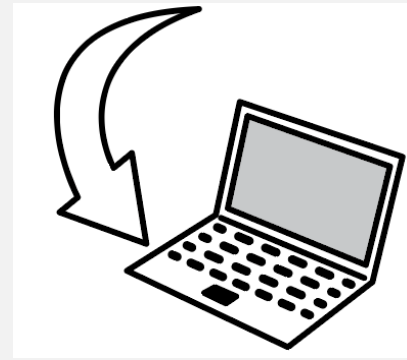
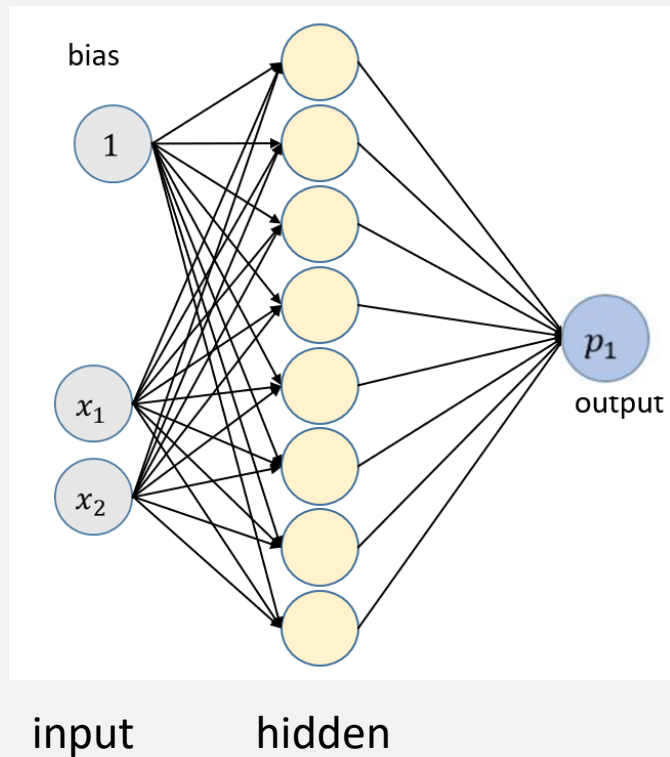
All features, here: 2

```
model.predict(X_test[0:10,:])
```

```
1/1 [=====] - 0s 148ms/step
array([[5.9251189e-01],
       [8.8978779e-01],
       [7.8563684e-01],
       [9.1934395e-01],
       [6.1078304e-01],
       [8.2838058e-01],
       [2.5862646e-01],
       [3.1314052e-05],
       [2.6938611e-01],
       [3.7005499e-02]], dtype=float32)
```

Each of the observations
Gets a probability to
Belong to class 1

Exercise:



Open NB [01_simple_forward_pass.ipynb](#) and do the Keras part

Summary

- A neuron in a NN is loosely inspired by a neuron in the brain.
- The value of a neuron is computed by the weighted sum of the values in connected neurons of the previous layer, which is then passed through an activation function such as sigmoid or relu
- For a binary classification task we can use the sigmoid activation function for a single neuron in the last layer.
As loss we use in Keras 'binary_crossentropy' which is the NLL
- To achieve a non-linear (non-planar) decision boundary between the classes in binary classification, we need NNs with hidden layers.
- The weights of a NN are learned during the training via backpropagation minimizing the loss using SGD (Stochastic Gradient Descent)
- For efficient training use the relu activation function for hidden layers.
- If the loss diverges to infinity: Don't panic, lower the learning rate!