### Integrating E-commerce Freight Logistics by Optimizing Container Shipping

When I think about efficient logistics in e-commerce, I immediately see how critical precise coordination and optimization are for reducing costs and speeding up delivery times. For me, integrating different facets of e-commerce logistics—like container utilization, shipping schedules, and route optimization—is similar to performing numerical integration in MATLAB. Every container, route, and schedule becomes part of a larger system, and I realize that achieving synchronization and cost-effectiveness requires precise calculations at every step.

## One-Dimensional Integration: Optimizing Container Utilization

I often approach container utilization by thinking about it in terms of numerical integration. When I integrate a function representing the volume of goods being loaded over time, it helps me ensure that containers are fully utilized without any wasted space. By doing this, I can minimize idle capacity and help e-commerce platforms save on shipping costs.

### Two-Dimensional Integration: Balancing Volume and Weight

For me, balancing the volume and weight of goods within a container is like solving a two-dimensional integration problem. I use this approach to ensure that no container is overloaded or poorly balanced. By carefully considering both dimensions, I can achieve efficient loading that adheres to constraints and avoids logistical risks, like imbalances during transit.

#### Three-Dimensional Integration: Synchronizing Multimodal Shipping

I find multimodal logistics—where goods move by cargo ship, rail, and truck—especially complex and fascinating. Synchronizing these modes feels like working with three-dimensional integration. I model how schedules, routes, and capacities interact, allowing me to optimize the entire supply chain. This process enables me to align the flow of goods seamlessly across different transportation methods, ultimately improving efficiency and reducing delays.

```
% Step 1: One-Dimensional Integration (Container Utilization)
f = @(x) exp(-0.1 * x) + 1;
% I defined a function representing the rate of container loading over time,
% where the rate slows down as the container nears full capacity.

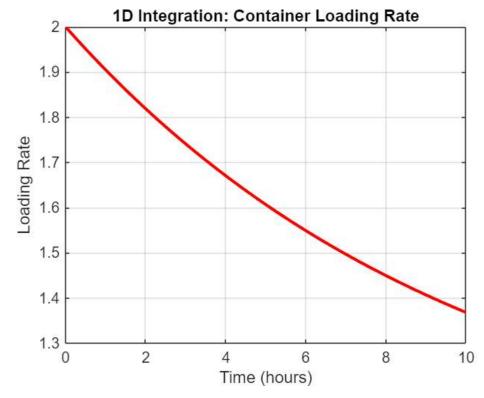
xmin = 0;
xmax = 10;
% The range represents the loading period in hours.

q1 = integral(f, xmin, xmax);
% I used `integral` to calculate the total volume of goods loaded into the container over the given time.
disp(['Total Volume Loaded (1D Integration): ', num2str(q1), ' units']);
```

Total Volume Loaded (1D Integration): 16.3212 units

```
% Plot the 1D function
x_vals = linspace(xmin, xmax, 100);
% I created a range of x values to plot the loading function.
y_vals = f(x_vals);
% I evaluated the function at each x value.

figure;
plot(x_vals, y_vals, 'r', 'LineWidth', 2);
% I plotted the loading rate in red to visualize how it changes over time.
xlabel('Time (hours)');
ylabel('Loading Rate');
title('1D Integration: Container Loading Rate');
grid on;
```



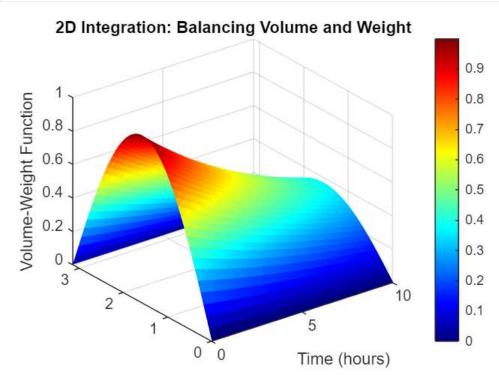
```
% Step 2: Two-Dimensional Integration (Balancing Volume and Weight)
f2 = @(x, y) exp(-0.1 * x) .* sin(y);
% I defined a function where `x` represents the loading time and `y` represents weight distribution.

xmin = 0; xmax = 10;
ymin = 0; ymax = pi;
% The ranges represent the loading time (x) and the angle of inclination caused by weight distribution (y).

q2 = integral2(f2, xmin, xmax, ymin, ymax);
% I used `integral2` to calculate the combined effect of volume and weight over the loading process.
disp(['Balanced Volume-Weight Calculation (2D Integration): ', num2str(q2), ' units']);
```

```
% Plot the 2D function
[x_vals, y_vals] = meshgrid(linspace(xmin, xmax, 50), linspace(ymin, ymax, 50));
% I created a grid of x and y values for visualization.
z_vals = f2(x_vals, y_vals);
% I evaluated the function at each grid point.

figure;
surf(x_vals, y_vals, z_vals, 'EdgeColor', 'none');
% I plotted the 2D function as a surface plot with smooth colors.
colormap('jet');
colorbar;
xlabel('Time (hours)');
ylabel('Weight Distribution Angle (radians)');
zlabel('Volume-Weight Function');
title('2D Integration: Balancing Volume and Weight');
grid on;
```



# Weight Distribution Angle (radians)

```
% Step 3: Three-Dimensional Integration (Multimodal Synchronization)
f3 = @(x, y, z) exp(-0.1 * x) .* sin(y) .* cos(z);
% I defined a function where `x` is the loading time, `y` is weight distribution,
% and `z` represents the route synchronization across transport modes.

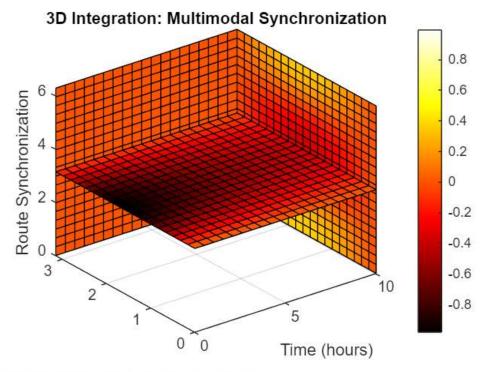
xmin = 0; xmax = 10;
ymin = 0; ymax = pi;
zmin = 0; zmax = 2 * pi;
% The ranges represent loading time, weight distribution angle, and synchronization across transport modes.

q3 = integral3(f3, xmin, xmax, ymin, ymax, zmin, zmax);
% I used `integral3` to model the complete logistics process, synchronizing container loading and transport.
disp(['Multimodal Synchronization (3D Integration): ', num2str(q3), ' units']);
```

Multimodal Synchronization (3D Integration): 6.4832e-13 units

```
% Visualize slices of the 3D function
figure;
[x_vals, y_vals, z_vals] = meshgrid(linspace(xmin, xmax, 20), linspace(ymin, ymax, 20), linspace(zmin, zmax, 20));
% I created a 3D grid of x, y, and z values.
f3_vals = f3(x_vals, y_vals, z_vals);
% I evaluated the function at each point on the 3D grid.
```

```
slice(x_vals, y_vals, z_vals, f3_vals, xmax, ymax, zmax/2);
% I visualized slices of the 3D function to observe the interactions between dimensions.
colormap('hot');
colorbar;
xlabel('Time (hours)');
ylabel('Weight Distribution Angle (radians)');
zlabel('Route Synchronization');
title('3D Integration: Multimodal Synchronization');
grid on;
```



# Weight Distribution Angle (radians)

```
% Step 4: Precision Control for Optimized Logistics
q1_precise = integral(f, xmin, xmax, 'RelTol', 1e-6, 'AbsTol', 1e-4);
% I fine-tuned tolerances for 1D integration to ensure accurate volume calculations.

q2_precise = integral2(f2, xmin, xmax, ymin, ymax, 'RelTol', 1e-6, 'AbsTol', 1e-4);
% I refined tolerances for 2D integration to improve volume-weight balance predictions.

q3_precise = integral3(f3, xmin, xmax, ymin, ymax, zmin, zmax, 'RelTol', 1e-6, 'AbsTol', 1e-4);
% I adjusted tolerances for 3D integration to enhance synchronization accuracy across transport modes.

disp(['Precise Total Volume Loaded: ', num2str(q1_precise), ' units']);
```

Precise Total Volume Loaded: 16.3212 units

```
disp(['Precise Balanced Volume-Weight Calculation: ', num2str(q2_precise), ' units']);
```

Precise Balanced Volume-Weight Calculation: 12.6424 units

```
disp(['Precise Multimodal Synchronization: ', num2str(q3_precise), ' units']);
```

Precise Multimodal Synchronization: 1.038e-07 units