# Assignment 2: due 8am on Mon, Oct 15, 2018

## **Summary of Instructions**

Note	Read the instructions carefully and follow them exactly			
Assignment Weight	4% of your course grade			
Due Date and time	8am on Monday, Oct 15, 2018			
	As outlined in the syllabus, late submissions will not be accepted			
Important	Any files with syntax errors will automatically be excluded from grading. Be sure			
	to test your code before you submit it			
	For all functions, both in Part 1 and 2, make sure you've written good docstrings			
	that include type contract, function description and the preconditions if any.			

This is an individual assignment. Please review the Plagiarism and Academic Integrity policy presented in the first class, i.e. read in detail pages 15 – 18 of course outline (ITI1120-course-outline-syllabus-Fall2018.pdf). You can find that file on Brightspace under Course Info. While at it, also review Course Policies on pages 13 and 14.

The goal of this assignment is to learn and practice the concepts covered thus far, in particular: strings (including indexing, slicing and string methods), control structures (if statements and for-loops), use of range function, function design and function calls.

The only collection you can use are strings. You may not use any other collection (such as a list/array, tuple, or dictionary) in this assignment. Using any of these in a solution to a question constitues changing that question. Consequently, that question will not be graded.

You can make multiple submissions, but only the last submission before the deadline will be graded. What needs to be submitted is explained next.

The assignment has two parts. Each part explains what needs to be submitted. Put all those required documents into a folder called a2\_xxxxx where you changed xxxxxx to your student number, zip that folder and submit it as explained in Lab 1. In particular, the folder should have the following files:

Part 1: a2\_part1\_xxxxxx.py, a2\_part1\_xxxxxx.txt

Part 2: a2\_part2\_xxxxxx.py and a2\_part2\_xxxxxx.txt

Both of your programs must run without syntax errors. In particular, when grading your assignment, TAs will first open your file a2\_part1\_xxxxxx.py with IDLE and press Run Module. If pressing Run Module causes any syntax error, the grade for Part 1 becomes zero. The same applies to Part 2, when they open and run file a2\_part2\_xxxxxx.py.

Furthermore, for each of the functions (in Part 1 and Part 2), I have provided one or more tests to test your functions with. For example, you should test function <code>split\_tester</code> from Part 1 by making a call in Python shell with <code>split\_tester("12311234","4")</code>. To obtain a partial mark your function may not necessarily give the correct answer on these tests. But if your function gives any kind of python error when run on the tests provided below, that question will be marked with zero points.

Section 3, contains tests for Part 1. Tests for Part 2 are provided after each question in Part 2. To determine your grade, your functions will be tested both with examples provided in Part 2 and Section 3 and with some other examples. Thus you too should test your functions with more example than what I provided in Part 2 and Section 3.

Global variables are not allowed. If you do not know what that means, for now, interpret this to mean that inside of your functions you can only use variables that are created in that function. For example, this is not allowed, since variable x is not a parameter of function a\_times(a) nor is it a variable created in function a\_times(a). It is a global variable created outside of all functions.

```
def a_times(a):
    result=x*a
    return result

x=float(input("Give me a number: "))
print(a_times(10))
```

# 1 Part 1: increasing-splits tester - 40 points

To clarify Part 1 specifications, I have provided sample tests in Section 3 and a video. The behaviour implied by the sample tests and the video should be considered as required specifications in addition to what is explained below.

Here is the link to the video: https://youtu.be/bKROxaTNc1w

**Description:** Some positive integers N can be split into smaller pieces, such that the pieces are comprised of consecutive digits of N and such that each piece contains the same number of digits. Given an integer N and given a number of digits d, one can then ask if N can be split into pieces such that each pieces has d digits and such that the resulting sequence of numbers is strictly increasing.

#### **Examples:**

- For N=154152 and d=2, the answer is yes, since d=2 implies the following sequence 15, 41, 52 which is increasing.
- For N = 154152 and d = 3, the answer is no, since d = 2 implies the following sequence 154, 152 which is not increasing.
- For N = 154152 and d = 5, the answer is no, since 154152 cannot be split into five-digit pieces.
- For N=137 and d=1, the answer is yes, since since d=1 implies the following sequence 1, 3, 7 which is increasing.
- For N = 137 and d = 2, the answer is no, since 137 cannot be split into two-digit pieces.
- For N=113 and d=1, the answer is no, since since d=1 implies the following sequence 1, 1, 3 which is not increasing.
- For N=113 and d=3, the answer is yes, since d=3 implies the following sequence 113 which is increasing.

Design, implement and test a Python program which checks to see if a user-supplied positive integer N and a user-specified split d, are such that N can be split into pieces with d digits such that the resulting sequence is strictly increasing. Here are the steps that your program should have: (Note that since no collection other than strings is allowed you will be working with N and d as strings)

- 0. The program greets the user.
- 1. The program asks the user if they want to test if a number admits an increasing-split of give size.
- 2. The program prompts the user to enter a positive integer. If the user enters an invalid input (anything other than a positive integer), the program will repeat the questions starting with step 1.
- 3. The program prompts the user to enter the number of digits in each piece. The program will verify that the input is valid (a positive integer which is a proper divisor of the number of digits in the first input); If the input is invalid, the program will repeat the questions starting with step 1.
- 4. Once the valid input is obtained, the program splits the number into pieces of specified length and displays/prints those pieces in one line (separated by commas).
- 5. Finally, the program reports whether or not the obtained sequence of numbers is in strictly increasing order. If there is only one piece, it is defined to be in strictly increasing order.

For this part, I provided you with starter code in file called part1\_xxxxxx.py. Begin by replacing xxxxxx in the file name with your student number. Then open the file. Your solution (code) for this part must go into that file in the clearly indicated spaces only. You are not allowed to delete or comment-out or change any parts of the provided code except for the keyword pass.

For this part you need to submit two files: a2\_part1\_xxxxxx.py and a2\_part1\_xxxxxx.txt

a2\_part1\_xxxxxx.py needs to contain your program for Part 1 as explained above and a2\_part1\_xxxxxx.txt needs to contain the proof that you tested your two core function from this part, namely split\_tester.

#### 1.1 The Core Function

Your solution in a2\_part1\_xxxxxx.py must have a function called: split\_tester. You should design and test function split\_tester before moving onto designing and coding the main part of the program. Here are specifications for that function:

split\_tester This function has two parameters, a string N and a string d. These two strings can be assume to be such that each looks like a positive integer and such that the number of digits in N is divisible by the integer represented by d.

Since N and d are assumed to be valid i.e. meet the preconditions, they define a sequence of numbers (as specified in the examples above). The function should print that sequence of numbers in such a way that the consecutive numbers are separated by commas as shown in the test cases. Note that there cannot be a comma after the last number in the sequence.

The function should then return True if the sequences is strictly increasing and False otherwise. (Reporting, i.e. printing, whether or not the obtained sequence of numbers is strictly increasing has to be done in the main and not in the body of the split\_tester function).

Here are two approaches that may help you design this function:

You may find it easier to process the number N, which is given as a string, when you split it into pieces. One approach:

```
start with an empty string to hold the substring, i.e. the split as you loop through the whole number one digit at a time append digits to the substring if the substring reaches the desired length do something with the substring reset the substring to empty to collect the next substring reset the substring length count to zero
```

Another approach:

```
figure out how many substrings you want
loop that number of times
use slices to create the substrings
```

Other suggestions:

- -You can use the isdigit() string method to determine if a string contains only digits. Type help(str.isdigit) in the Python shell for more information.
- You can use the len() function to determine the length of a string i.e. the number of digits in N.
- If you find getting the commas right in the output tricky (because only commas between numbers are allowed), leave that until everything else is working correctly.

# 1.2 The User Interaction i.e. the main part of the program

Now that you have the function that performs the core functionality, you want to code the communication with the user in the main. It is also in the main that you should print the message about whether the sequence is increasing or not.

Advice: Leave error checking of the input for last. Begin by building your function first, and then the main assuming perfect input. Make sure though to leave enough time at the end to get the input checking details right.

The specifications on how your program needs to behave when communicating with the user should be inferred from the test examples and the video. You will notice that the program is required to display greetings surrounded with stars. One of your functions from Assignment 1, may be helpful for that. You can copy paste that function from your Assignment 1 solution (or mine) to your solution in a2\_part1\_xxxxxx.py.

# 2 Part 2: A Library of Functions

For this part of the assignment, you are required to write and test several functions (as you did in Assignment 1). You need to save all functions in part2\_xxxxxx.py where you replace xxxxxx by your student number. You need to test your functions (like you did in Assignment 1) and copy/paste your tests in part2\_xxxxxx.txt. Thus, for this part you need to submit two files: a2\_part2\_xxxxxx.py and a2\_part2\_xxxxxx.txt

## 2.1 min\_enclosing\_rectangle(radius, x, y) - 5 points

Computing a smallest (axis-aligned) rectangle that encloses a set of objects in the plane is a very common computational problem arising in graphics and thus game development too. Write a function, called min\_enclosing\_rectangle, that has 3 input parameters. The first is a number representing a radius of a circle and the next two are two numbers representing the x- and y-coordinates of its center. Consider the smallest axis-aligned rectangle that contains that circle. The function should return the x- and y-coordinates of the bottom-left corner of that rectangle. If side is a negative number, min\_enclosing\_rectangle should return None.

```
>>> min_enclosing_rectangle(1,1,1)
(0, 0)
>>> min_enclosing_rectangle(4.5, 10, 2)
```

```
(5.5, -2.5)
>>> min_enclosing_rectangle(-1, 10, 2)
>>> min_enclosing_rectangle(500, 1000, 2000)
(500, 1500)
```

### 2.2 series\_sum() - 5 points

```
>>> series_sum()
Please enter a non-negative integer: -10
>>> series_sum()
Please enter a non-negative integer: 0
1000
>>> series_sum()
Please enter a non-negative integer: 5
1001.463611111111
```

#### 2.3 pell(n) - 5 points

Pell numbers are a mathematical sequence of numbers that help approximate the value of  $\sqrt{2}$  (check out the Wikipedia page on Pell Numbers:

https://en.wikipedia.org/wiki/Pell number). The sequence is defined recursively as shown in eq. 1.

$$P_n = \begin{cases} 0 & \text{if } n = 0\\ 1 & \text{if } n = 1\\ 2P_{n-1} + P_{n-2} & \text{if } n > 1 \end{cases}$$
 (1)

Write a function called pell that takes one integer parameter n, of type int. If n is negative, pell returns None. Else, pell returns the nth Pell number (i.e.  $P_n$ ).

```
>>> pell(0)
0
>>> pell(1)
1
>>> pell(2)
2
>>> pell(3)
5
>>> pell(-45)
>>> pell(6)
70
```

### 2.4 countMembers(s) - 5 points

In this question you are not allowed to use any of the Python's string methods (i.e. those string functions that you call with dot operator).

Say a character is *extraordinary* if it is one of the following: the lower case letter between e and j (inclusive), the upper case letters between F and X (inclusive), numerals between 2 and 6 (inclusive), and the exclamation point (!), comma (,), and backslash (\)

You are required to count how many times these characters appear in a string.

Write a function called countMembers that takes a single input parameter s, of type str. countMembers then returns the number of characters in s, that are extraordinary. Therefore, if there are two Xs in s, countMembers must count two extraordinary characters (one for each occurrence of X in s).

```
>>> countMembers("\\")
1
>>> countMembers("2\\'")
1
```

```
>>> countMembers("1\'")
0
>>> countMembers("2aAb3?eE'_13")
4
>>> countMembers("one, Two")
2
```

#### 2.5 casual\_number(s) - 5 points

Imagine a customer in a bank is asked to enter a whole number representing their approximate monetary worth. In that case, some people use commas to separate thousands, millions etc, and some don't. In order to perform a some calculations the bank needs that number as na integer. Write a function, called casual\_number(s) that has one parameter, s, as input where s is a string. Function casual\_number(s) should return an integer representing a number in s. If s does not look like a number the function should return None. Note that if a string in s looks like a number but with commas, you may assume that commas are in meaningful places i.e. you may assume that s will not be a string like '1, 1, 345'.

```
>>> casual_number("251")
251
>>> casual_number("1,aba,251")
>>> casual_number("1,251")
1251
>>>casual_number("1251")
1251
>>> casual_number("-97,251")
-97251
>>> casual_number("-97251")
-97251
>>> casual_number("-,,,,")
>>> casual_number("--97,251")
>>> casual_number("-")
>>> casual_number("-1,000,001")
-1000001
>>> casual_number("999,999,999,876")
99999999876
>>> casual_number("-2")
-2
```

#### 2.6 alienNumbers(s) - 5 points

Strange communication has been intercepted between two alien species at war. NASAs top linguists have determined that these aliens use a weird numbering system. They have symbols for various numeric values, and they just add all the values for the symbols in a given numeral to calculate the number. NASA's linguists have given you the following table of symbols and their numeric values. Since they have a lot of these numbers to compute, they want you to write a function that they can use to automate this task.

Symbol	Value	
Т	1024	
У	598	
!	121	
a	42	
N	6	
U	1	

Thus a!ya!U!NaU represents a value of 1095 (see table below for an explanation).

Numeral	Value	Occurrences	Total Value	Running Total
T	1024	0	$0 \times 1024 = 0$	0
У	598	1	$1 \times 598 = 598$	598
!	121	3	$3 \times 121 = 363$	961
a	42	3	$3 \times 42 = 126$	1087
N	6	1	$1 \times 6 = 6$	1093
U	1	2	$2 \times 1 = 2$	1095

Write a function called alienNumbers that takes one string parameter s, and returns the integer value represented by s. Since aliens only know these characters you may assume that no character in s outside of this set: {T,y, !,a, N, U}. Callenge: try to make the whole body of this function only one line long.

```
>>> alienNumbers("a!ya!U!NaU")
1095
>>> alienNumbers("aaaUUU")
129
>>> alienNumbers("")
0
```

#### 2.7 alienNumbersAgain(s) - 5 points

NASA is very pleased with your proof-of-concept solution in the previous question. Now, they've designed a small chip that runs a very restricted version of python - it doesn't have any of the string methods that you are used to. They want you to now rewrite your alienNumbers function to run without using any of those string methods you may have otherwise used. Basically, you can use a loop of some sort and any branching you'd like, but none of the string methods. Use accumulator variable as we have seen in class.'

Write a function called alienNumbersAgain, that takes a single string parameter s, and returns the numeric value of the number that s represents in the alien numbering system.

```
>>> alienNumbersAgain("a!ya!U!NaU")
1095
>>> alienNumbersAgain("aaaUUU")
129
>>> alienNumbersAgain("")
```

The last three questions may be a more challenging to solve especially the last one.

### 2.8 encrypt(s) - 5 points

Hint: Think of how slicing and reversing of strings can help with this problem. (We saw how to do slicing and reversing at the beginning of Lecture 8)

You want to send a note to your friend in class, and because you want to be respectful in class, you don't want to whip out your phone and send a text or an email (or any other digital communication). Instead, you choose to go old school and write it out on a piece of paper and pass it along to your friend. The problem is, you don't want anyone else to read the note as they pass it along. Luckily, your friend and you have come up with an encryption system so that nobody else can understand your message. Here's how it works: you write out your message backwards (so, Hello, world becomes dlrow ,olleH). But you don't stop there, because that's too easy to crack - anyone can figure that out! Now that you've written in backwards, Then you start on either side of the string and bring the characters together. So the first and the last characters become the first and the second character in the encrypted string, and the second and the second last characters become the third and the fourth characters in the string, and so on. Thus, Hello, world ultimately becomes dHlerlolwo, (notice how all punctuation, special characters, spaces, etc are all treated the same) and 0123456789 becomes 9081726354.

Write a function called encrypt, that has one parameter s where s is a string and encrypt returns a string which is the encrypted version of s.

Fun fact in cryptography, s is called "clear text" and the encrypted version you return is called "cipher text"

```
>>> encrypt("Hello, world")
'dHlerlolwo ,'
>>>> encrypt("1234")
'4132'
>>> encrypt("12345")
'51423'
>>> encrypt("1")
'1'
>>> encrypt("123")
'312'
>>> encrypt("12")
'21'
>>> encrypt("Secret Message")
```

```
'eSgeacsrseetM '
>>> encrypt(",'4'r")
"r,''4"
```

### 2.9 oPify(s) - 5 points

Hint: Depending on how you plan to solve this problem, accumulator variable initialized as an empty string may help in this question.

Write a function called oPify, that takes a single string parameter (s) and returns a string. This function considers every pair of consecutive characters in s. It returns a string with the letters o and p inserted between every pair of consecutive characters of s, as follows. If the first character in the pair is uppercase, it inserts an uppercase 0. If however, it is lowercase, it inserts the lowercase p. If the second character is uppercase, it inserts an uppercase P. If however, it is lowercase, it inserts the lowercase p. If at least one of the character is not a letter in the alphabet, it does not insert anything between that pair. Finally, if s has one or less characters, the function returns the same string as s.

Do dir(str) and check out methods isalpha (by typing help(str.isalpha) in Python shell), and isupper

```
>>> oPify("aa")
'aopa'
>>> oPify("aB")
'aoPB'
>>> oPify("ooo")
'oopoopo'
>>> oPify("ax1")
'aopx1'
>>> oPify("abcdef22")
'aophopcopdopeopf22'
>>> oPify("abcdef22x")
'aopbopcopdopeopf22x'
>>> oPify("aBCdef22x")
'aoPBOPCOpdopeopf22x'
>>> oPify("x")
'x'
>>> oPify("123456")
1234561
```

### 2.10 nonrepetitive(s) - 5 points

This may be quite a challenging question to solve. Slicing and remembering that you can ask if two strings (s1==s2) are the same are key to a short solution to this problem.

A nonrepetitive word is a word that does not contain any subword twice in a row. Examples: ana is nonrepetitive.

borborygmus is not nonrepetitive, since it has subword, bor twice in a row.

abracadabra is nonrepetitive.

repetitive is not nonrepetitive since subword ti is repeated twice in a row.

grammar is not nonrepetitive since subword m is repeated twice in a row.

gaga is not s nonrepetitive since subword ga is repeated twice in a row.

rambunctious is nonrepetitive.

abcab is nonrepetitive.

abacaba is nonrepetitive.

zrtzghtghtq is not nonrepetitive since subword ght is repeated twice (in fact three times, but it is enough to find two repetitions to conclude that the word is not nonrepetitive).

aa is not nonrepetitive since subword a is repeated twice.

zatabracabrac is not nonrepetitive since subword abrac is repeated twice in a row.

Write a function, called **nonrepetitive**, that has one parameter, **s**, where **s** is a string. The function returns True if **s** is nonrepetitive and False otherwise.

```
>>> nonrepetitive("")
True
>>> nonrepetitive("a")
True
>>> nonrepetitive("zrtzghtghtghtq")
```

```
False
>>> nonrepetitive("abcab")
True
>>> nonrepetitive("12341341")
False
>>> nonrepetitive("44")
False
```

# 3 Testing your code in Part 1

Here is how you should test your two functions from Part 1 in Python shell.

```
>>> split_tester("12311234","2")
12, 31, 12, 34
>>> split_tester("12311234","4")
1231, 1234
>>> split_tester("0012311234","2")
00, 12, 31, 12, 34
False
>>> split_tester("0012311234","5")
00123, 11234
True
>>> split_tester("1","1")
1
>>> split_tester("1","1")
True
>>> split_tester("734","1")
7, 3, 4
False
>>> split_tester("734","3")
734
True
```

Here is what pressing Run on your program (Part 1) and should give:

```
************
   __Welcome to my increasing-splits tester__
                      Arya Stark
What is your name?
******************
   __Arya Stark, welcome to my increasing-splits tester.__
*********************
Arya Stark, would you like to test if a number admits an increasing-split of give size?
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? sure
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size?
Good choice!
Enter a positive integer: 123156
Input the split. The split has to divide the length of 123156 i.e. 6
4 does not divide 6. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? YES
Good choice!
Enter a positive integer:
                                123156
Input the split. The split has to divide the length of 123156 i.e. 6
123, 156
The sequence is increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
```

```
Good choice!
Enter a positive integer: 3.4
The input can only contain digits. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer:
The input has to be a positive integer. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: 3331
Input the split. The split has to divide the length of 3331 i.e. 4
2
33, 31
The sequence is not increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: twenty
The input can only contain digits. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yeS
Good choice!
Enter a positive integer: 4321
Input the split. The split has to divide the length of 4321 i.e. 4
                     1
4, 3, 2, 1
The sequence is not increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer:
                                     4321
Input the split. The split has to divide the length of 4321 i.e. 4
4
4321
The sequence is increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size?
                                                                                             yes
Good choice!
Enter a positive integer: -2.5
The input can only contain digits. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size?
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? YES
Good choice!
                             0
Enter a positive integer:
The input has to be a positive integer. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: 77
Input the split. The split has to divide the length of 77 i.e. 2
77
The sequence is increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? 345
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: 345
Input the split. The split has to divide the length of 345 i.e. 3
4
4 does not divide 3. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? 345
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: 345
Input the split. The split has to divide the length of 345 i.e. 3
10 does not divide 3. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer:
                                213411800
Input the split. The split has to divide the length of 213411800 i.e. 9
      5
5 does not divide 9. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Good choice!
Enter a positive integer: 213411800
```

```
Input the split. The split has to divide the length of 213411800 i.e. 9
3
213, 411, 800
The sequence is increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? yes
Enter a positive integer: 001230
Input the split. The split has to divide the length of 001230 i.e. 6
001, 230
The sequence is increasing
Arya Stark, would you like to test if a number admits an increasing-split of give size? uf
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size? \dots \text{NO}
Please enter yes or no. Try again.
Arya Stark, would you like to test if a number admits an increasing-split of give size?
  __Good bye Arya Stark!__ *
*********
>>>
```

10