

# Charge transport in organic microcavities: phonon-assisted zener tunnelling under strong light-matter coupling

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(Dated: July 18, 2017)

Due to the coupling between electronic and vibrational states of organic molecules, strong matter-light coupling in organic microcavities results in a distribution of vibrationally excited states for the ground electronic state of a molecule. These vibrations can assist zener tunnelling (charge transfer) under a moderate applied electric field. The electron-hole pairs created this way add up excitations to the coupled cavity-electronic subsystem when they combine to make excitons, which in turn keeps the probability of excited vibrational states high.

## I. MODEL

Organic molecules are assumed to have two electronic levels with a single harmonic vibrational mode that is coupled to these electronic states (usual electron-phonon coupling). The cavity is assumed to have a single photon mode.

A molecule has four possible (spinless) electronic configurations:

- (i)  $\phi$  (both HOMO and LUMO empty),
- (ii) D (both HOMO and LUMO filled)
- (iii)  $\downarrow$  (HOMO filled, LUMO empty), and
- (iv)  $\uparrow$  (HOMO empty, LUMO filled).

D and  $\phi$  do not couple to the cavity while  $\downarrow$  and  $\uparrow$  do. We treat cavity along with all molecules in  $\downarrow$  or  $\uparrow$  quantum mechanically using the rotating wave approximation for the coupling between them. The rest of the molecules in D or  $\phi$ , and the electron hops between molecules or between contacts and molecules are treated at classical level. An electron hopping induces transitions between the quantum states as do the other dissipative processes like photon leakage and exciton decay. We compute amplitudes for all possible quantum transitions and calculate respective transition probabilities by weighing with a penalty function for their relevant classical hops. Using usual rejection-free Monte Carlo rules, we select a transition at random and change the quantum and classical states accordingly.

### A. What is special?

What is really interesting is that, in the strong coupling regime, the electron hopping from HOMO of a molecule to the LUMO of its neighbour can be assisted by the vibrations that exist due to simultaneous presence of vibronic coupling.

We do not explicitly include the vibrational states in quantum mechanically described subsystem. However, the probability distribution of vibrational states for molecules in  $\downarrow$  state is calculated quantum mechanically (see Fig. 1, for example) and used to calculate the rates for classical hops. This probability distribution can be very different than the thermal one, and if it is suffi-

ciently large for excited vibrational states it plays a vital/paramount role in the charge transport under applied bias. For example,

(i) for two neighbouring molecules in  $\downarrow$ , the vibrations can assist the zener tunnelling by reducing the minimum applied field required for the process.

(ii) these vibrations can enhance the inter-molecule HOMO-HOMO or LUMO-LUMO hop rates just like a higher temperature would [1].

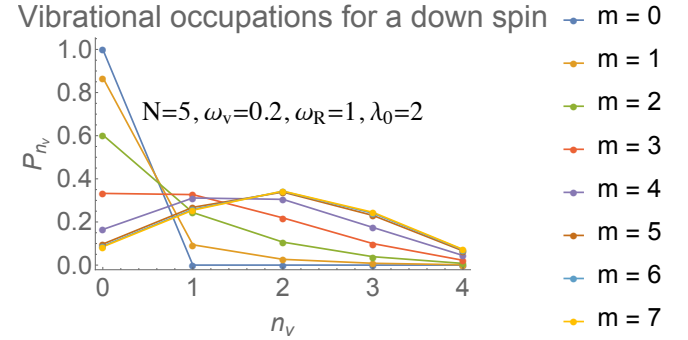


FIG. 1. Probability distribution of vibrational states of a molecule in ground electronic state for different number of excitations  $m$  in the system.

## II. HOPPING PROCESSES

### A. Bulk processes

An electron can jump from a molecule to its neighbour. There are several possible ways this can occur: HOMO-HOMO, LUMO-LUMO, LUMO-HOMO and HUMO-LUMO.

- D hops: when the initial site is doubly occupied and the final site is singly occupied, this will be called a D hop, as the final site would become a D.
- $\phi$  hops: when the initial site is unoccupied and the final site is singly occupied, this will be called a  $\phi$  hop, as the final site would become a  $\phi$ .

- (D, $\phi$ ) creation: when the jump occurs between two singly occupied sites, a pair of D and  $\phi$  is created.
- (D, $\phi$ ) annihilation: when the jump occurs between a D and  $\phi$  pair, two singly occupied sites are created and the pair is annihilated.

### B. Contact processes

An electron can jump from a molecule to a contact or vice versa.

- D/ $\phi$  creation: when the initial site is singly occupied, an electron can jump from the contact to it and make it D or it can jump from the molecule to the contact and make it a  $\phi$ .
- D/ $\phi$  annihilation: It's just the reverse of the D/ $\phi$  creation processes, where an initial D or  $\phi$  becomes singly occupied when an electron jumps to or from it.

## III. CLASSICAL HOPS INDUCE QUANTUM TRANSITIONS

Let's call  $N$  and  $m$  to the number of (singly occupied) sites and number of (conserved) excitations in the quantum sub-system. Whenever any of the processes outlines above happens at any site(s), via any allowed channels (HOMO-HOMO, LUMO-LUMO, etc.), it can accompany a change in  $(N, m)$ . There is a change in the quantum state of the coupled light-matter system and the new state lives in the subspace of the Hilbert space corresponding to the new  $(N, m)$ . Tables I and II show the possible channels and corresponding change in  $(N, m)$  for all hop types described above.

Bulk Process	Change in (N,m)			
$\kappa/\gamma$	0,-1			
	H-H	L-L	H-L	L-H
D/ $\phi$ hops	0,0	0,0	0,1	0,-1
(D, $\phi$ ) creation	-2,-1	-2,-1	-2,0	-2,-1
(D, $\phi$ ) annihilation	2,1	2,1	2,2	2,0

TABLE I. Change in the number of active sites  $N$  and excitations  $m$  in the quantum system for bulk processes.

### A. The state of the system

The overall 'state' of the system at any time is described by the set of D and  $\phi$  sites,  $(N, m)$ , and the quantum state  $|\psi\rangle_{N,m}$ .  $|\psi\rangle_{N,m}$  can be a superposition of eigenstates in a given degenerate sector of the spectrum of the instantaneous quantum subsystem.

Contact Process	Change in (N,m)	
	HOMO	LUMO
D creation	-1,-1	-1,0
D annihilation	1,1	1,0
$\phi$ creation	-1,0	-1,-1
$\phi$ annihilation	1,0	1,1

TABLE II. Change in the number of active sites  $N$  and excitations  $m$  in the quantum system for contact processes.

### B. How the state evolves in time

We find all possible ways a hopping process can occur. For example, every D that has a singly occupied neighbour, can hop to it, every D that has a  $\phi$  as neighbour can combine with it and both get annihilated, every pair of neighbours that are singly occupied can create a (D, $\phi$ ) pair, etc.

Let's label all such possible ways of all hops for all channels by  $\{\alpha\}$ . We calculate their transition matrices  $H_t^\alpha$ , and the set of eigenstates  $\{|\phi_i\rangle\}$  of the Hamiltonian for  $(N_\alpha, m_\alpha)$ , the final number of sites and excitations for hop  $\alpha$ . The amplitudes for the transition from the current quantum state to the final quantum states for hop  $\alpha$  is

$$C_{\alpha,i} = \langle \psi_{N,m} | H_t^\alpha | \phi_{N_\alpha, m_\alpha}^i \rangle. \quad (1)$$

After hop  $\alpha$  we will quickly lose coherence between eigenstates of  $H_{N_\alpha, m_\alpha}$  with different energies, but there are multiple degenerate sectors in the spectrum and the coherence persists between eigenstates lying in the same degenerate sector. So, in Monte Carlo, we consider quantum jumps to all possible degenerate sectors instead of individual states. Suppose  $\{\beta\}$  labels the degenerate sectors of  $H_{N_\alpha, m_\alpha}$ , then the probability that we jump to sector  $\beta$  is

$$P_\beta = f_\alpha(\Delta E) * \sum_{i \in \beta} |C_{\alpha,i}|^2, \quad (2)$$

where  $f_\alpha(\Delta E)$  is a penalty function related to the hop  $\alpha$ . The final state is

$$|\psi_{N_\alpha, m_\alpha}\rangle = \sum_{i \in \beta} C_{\alpha,i} |\phi_{N_\alpha, m_\alpha}^i\rangle. \quad (3)$$

Once we update the overall state, i.e., the set of D and  $\phi$ ,  $(N, m)$  and the quantum state, the cycle starts again.

## IV. EXPLAINING EXPERIMENTS

### A. Experimental findings

Experiments are performed on metal-metal microcavities, with Al mirrors and MEH-PPV as active organic

material (in PMMA matrix?). The fermi level of Al is at  $\sim -4.2\text{eV}$  and HOMO/LUMO of MEH-PPV are at  $\sim -2.7, -5.1\text{eV}$ . Experimentalists think that there exists a moderate energy barrier for electron injection and a large barrier for hole injection such that the charge transport occurs only via electrons in this system because the holes injection at the anode is blocked.

*Observations:* In the experiments, it is found that, at average electric fields  $\sim 10^6\text{V/cm}$ , the current is 2-3 orders of magnitude higher in resonant cavities compared to the non-resonant ones. Further, there is electroluminescence in the resonant case even if the hole injection from the anode is absent due to a hole blocking layer there. No light emission is seen in the non-resonant cavities.

### B. Possible explanations

The observation of electroluminescence in resonant cavities means there is a constant supply of holes so they either enter from the cathode which is less likely, or they are produced in processes that create electron-hole pairs. The average electric field in the experiments ( $\sim 10^6\text{V/cm}$ ) is too small in comparison to the  $\Delta_{\text{HOMO-LUMO}} \sim 2\text{eV}$  and this cannot induce the HOMO-LUMO hops alone. So, either one or both of the following can be at work.

- (i) There are locations in the system/device where the field is much stronger than the average value so that it is able to create  $(D, \phi)$  pairs. In the weak coupling regime/off-resonant cavities, these  $(D, \phi)$  pairs are wasted via creation of excitons close to their birth place and hence do not contribute significantly to the charge transport. However, in the strong coupling regime/resonant cavities, excitons created by them add up excitations in the coupled matter-light quantum subsystem, which allows the creation of  $(D, \phi)$  pairs anywhere. This would effectively evenly distribute the charge carriers ( $D$  and  $\phi$ ) which is much more likely to contribute to the current (and hence enhance the transport via increased carrier concentration as well as via avoiding electron traps, see somewhere below for how to avoid traps).
- (ii) Due to the coupling between electronic and intramolecular vibrational states, there is a sizeable probability of having enough phonons/vibrational quanta on an unexcited molecule ( $\downarrow$ ) that the energy required for the hop from it to the LUMO of a neighbour molecule is available. That is, vibrational/phonon assisted zener tunnelling/charge transfer process becoming possible even at average strengths of bias fields that alone are not sufficient for this process (say,  $\sim 10^6\text{ V/cm}$ ).

**A Test:** Whether this is the reason of higher currents in resonant cavities can be tested by blocking electron

and hole injection from the contacts in a microcavity with no intrinsic holes to establish the strong coupling regime and exciting it with a laser above the exciton energy. Once the system is in strong coupling regime (with enough excitations to have a sizeable probability of phonons in the ground electronic state of molecules), it can start creating  $(D, \phi)$  pairs and add excitations in the quantum system, which should then be sustained even if the laser drive is removed.

### C. Why resonant cavities allow more current? Is it enhanced injection or carrier generation?

Note: If the cavity lowers the molecular levels, would not it be likely to lower the metallic levels too?!

Anyway, some tests:

- *Test 1.* If J-V characteristics of resonant cavities are similar to non-resonant ones at small applied bias (say,  $\lesssim 10^3\text{V/cm}$ ), that means the injection barriers are not drastically different in the two cases.
- *Test 2.* A microcavity with electron and hole blocking layers at cathode and anode would stop any injection. If the J-V characteristics of resonant cavities stay similar, that would mean injection is not playing any role.
- *Test 3.* Take a microcavity with excellent electron and hole injection, e.g., Ca cathode and Au anode with MeH-PPV. At low fields where zener tunnelling is not possible even with vibrational assistance, if the resonant cavities have higher currents, that would mean carrier's mobility is enhanced (due to the vibrations resulting from strong coupling).

### D. What about the traps?

It is well known that the mobility of holes is  $\sim 3$  orders of magnitude higher than electrons in MEH-PPV (and other organic polymers??) due to deep trap states below the LUMO level [2]. This difference in mobility pertains to hole-only and electron-only transport. In the strong coupling regime, when the singly occupied sites can switch between HOMO and LUMO, an electron can avoid traps by going through HOMO and hence this alone is sufficient to increase the current due to increased mobility. But, it is not sustainable on its own as the excitations in the system are constantly dissipated via photon leakage and exciton decay, and an electron is unlikely to be extracted from HOMO at the cathode. **This again means there is some source of excitations in the resonant cavities, as discussed in section IV B. So, the combined effect of increased mobility due to**

avoiding traps and increased carrier concentration is likely to be the reason of orders of magnitude higher current in resonant cavities.

#### E. Photo assisted charge transfer

Does not add excitations! Can't be the reason.

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- [1] E. K. Kudinov and Y. A. Firsov, Soviet Physics JETP **22**, 603 (1996).
  - [2] Y. Zhang, B. de Boer, and P. W. M. Blom, Phys. Rev. B **81**, 085201 (2010).