

1 Contest

2 Wzory

3 Struktury danych

4 Grafy

5 Matma

6 Teksty

7 Geometria

8 Inne

Contest (1)

| |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| sol.cpp |
| <pre>#include <bits/stdc++.h> using namespace std; using ll = long long; #ifdef LOCAL auto& operator<<(auto&, pair<auto, auto>); auto operator<<(auto& o, auto x) -> decltype(x.end(), o) { o << '{'; for (int i = 0; auto y : x) o << ", " + !i++ * 2 << y; return o << '}''; } auto& operator<<(auto& o, pair<auto, auto> x) { return o << '{' << x.first << ", " << x.second << '}''; } void __print(auto... x) { ((cerr << ' ' << x), ...) << endl; } #define debug(x...) cerr << "[" #x "]:", __print(x) #else #define debug(...) 2137 #endif int main() { ios_base::sync_with_stdio(false); cin.tie(nullptr); }</pre> |
| .vimrc |

```
set nu et ts=2 sw=2
filetype indent on
syntax on
colorscheme habamax
hi MatchParen ctermfg=66 ctermbg=234 cterm=underline
nnoremap ; :
nnoremap : ;
inoremap {<cr> {<cr>}<esc>O <bs>
```

Makefile

```
CXXFLAGS=-std=c++20 -Wall -Wextra -Wshadow
```

```
sol: sol.cpp
```

sol .vimrc Makefile test WaveletTree

| | |
|---|------------------------------------------------------------|
| 1 | g++ \$(CXXFLAGS) -fsanitize=address,undefined -g -DLOCAL \ |
| 1 | sol.cpp -o sol |
| 1 | fast: sol.cpp |
| 1 | g++ \$(CXXFLAGS) -O2 sol.cpp -o fast |
| 1 | test.sh |
| 2 | #!/bin/bash |
| 4 | for((i=1;i>0;i++)) do |
| 4 | echo "\$i" |
| 4 | echo "\$i" ./gen > int |
| 5 | diff -w <(. /sol < int) <(. /slow < int) break |
| 5 | done |
| 5 | |

Wzory (2)

2.1 Kombinatoryka

2.1.1 Lemat Burnside’a

Niech G oznacza grupę symetrii reprezentacji, S zbiór obiektów, a $I(\pi)$ ilość punktów stałych π . Wtedy

$$|S| = \frac{1}{|G|} \sum_{\pi \in G} I(\pi).$$

2.2 Grafy

2.2.1 Twierdzenie Königa

W grafie dwudzielnym zachodzi

- $n_k = p_w$
- $n_k + p_k = n$
- $p_w + n_w = n$

oraz

- p_w to zbiór wierzchołków na brzegu min-cut
- n_w to dopełnienie p_w
- p_k to n_k z dodanymi pojedynczymi krawędziami każdego nieskojarzonego wierzchołka

2.2.2 Twierdzenie Erdősa-Gallaia

Ciąg stopni $d_1 \geq \dots \geq d_n$ opisuje prosty graf wtw gdy $\sum d_i$ jest parzysta oraz dla każdego $1 \leq k \leq n$ zachodzi

$$\sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i, k).$$

2.2.3 Twierdzenie Gale’a-Rysera

Ciągi stopni $a_1 \geq \dots \geq a_n$ oraz b_1, \dots, b_n opisują prosty graf dwudzielny wtw gdy $\sum a_i = \sum b_i$ oraz dla każdego $1 \leq k \leq n$ zachodzi

$$\sum_{i=1}^k a_i \leq \sum_{i=1}^n \min(b_i, k).$$

2.2.4 Przepływy z wymaganiami

Szukamy przepływu $\leq F$ takiego, że $f_i \geq d_i$ dla każdej krawędzi. Tworzymy nowe źródło s' i ujście t' . Następnie dodajemy krawędzie

- $(u_i, t', d_i), (s', v_i, d_i), (u_i, v_i, c_i - d_i)$ zamiast (u_i, v_i, c_i, d_i)
- (t, s, F)

Przepływ spełnia wymagania jeżeli maksymalnie wypełnia wszystkie krawędzie s' .

2.3 Analiza

2.3.1 Mnożniki Lagrange’a

Jeżeli optymalizujemy $f(x_1, \dots, x_n)$ przy ograniczeniach typu $g_k(x_1, \dots, x_n) = 0$ to x_1, \dots, x_n jest ekstremum lokalnym tylko jeżeli gradient $\nabla f(x_1, \dots, x_n)$ jest kombinacją liniową gradientów $\nabla g_k(x_1, \dots, x_n)$.

Struktury danych (3)

WaveletTree.h

Opis: st – początek, ed – koniec, sst – posortowany początek. Niszczy wartości w przedziale [st, ed).

Czas: $\mathcal{O}((n + q) \log n)$

| |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>struct node { int lo, hi; vector<int> s; node *l = 0, *r = 0; node(auto st, auto ed, auto sst) { int n = ed - st; lo = sst[0]; hi = sst[n - 1] + 1; if (lo + 1 < hi) { int mid = sst[n / 2]; if (mid == sst[0]) mid = *upper_bound(sst, sst + n, mid); s.reserve(n + 1); s.push_back(0); for (auto it = st; it != ed; it++) { s.push_back(s.back() + (*it < mid)); } auto k = stable_partition(st, ed, [&](int x) { return x < mid; }); auto sm = lower_bound(sst, sst + n, mid); if (k != st) l = new node(st, k, sst); if (k != ed) r = new node(k, ed, sm); } } };</pre> |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

```
int kth(int a, int b, int k) {
    if (lo + 1 == hi) return lo;
    int x = s[a], y = s[b];
    return k < y - x ? l->kth(x, y, k)
        : r->kth(a - x, b - y, k - (y - x));
}

int count(int a, int b, int k) {
    if (lo >= k) return 0;
    if (hi <= k) return b - a;
    int x = s[a], y = s[b];
    return (l ? l->count(x, y, k) : 0) +
        (r ? r->count(a - x, b - y, k) : 0);
}

int freq(int a, int b, int k) {
    if (k < lo || hi <= k) return 0;
    if (lo + 1 == hi) return b - a;
    int x = s[a], y = s[b];
    return (l ? l->freq(x, y, k) : 0) +
        (r ? r->freq(a - x, b - y, k) : 0);
}
};
```

OrderedSet.h

Opis: s.find_by_order(k) i s.order_of_key(k).
Czas: $\mathcal{O}(\log n)$

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

template <typename T>
using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
```

Treap.h

Czas: $\mathcal{O}(\log n)$

```
mt19937_64 rng(2137);
struct node {
    int val, sz = 1;
    uint64_t pr;
    node *l = 0, *r = 0;
    node(int x) {
        val = x;
        pr = rng();
    }
    void pull() {
        sz = 1 + size(l) + size(r);
    }
    friend int size(node* a) {
        return a ? a->sz : 0;
    }
    friend pair<node*, node*> split(node* a, int k) {
        if (!a) return {0, 0};
        if (k <= size(a->l)) {
            auto [la, lb] = split(a->l, k);
            a->l = lb;
            a->pull();
            return {la, a};
        } else {
            auto [ra, rb] = split(a->r, k - size(a->l) - 1);
            a->r = ra;
            a->pull();
            return {a, rb};
        }
    }
    friend node* merge(node* a, node* b) {
        if (!a || !b) return a ? a : b;
        if (a->pr > b->pr) {
```

```
        a->r = merge(a->r, b);
        a->pull();
        return a;
    } else {
        b->l = merge(a, b->l);
        b->pull();
        return b;
    }
};
```

LineSet.h

Opis: Znajduje maksimum funkcji liniowych online. Dla double div(a,b) = a/b oraz INF = 1/.0.
Czas: $\mathcal{O}(\log n)$

```
struct line {
    mutable ll a, b, p;
    bool operator<(const line& o) const { return a < o.a; }
    bool operator<(ll x) const { return p < x; }
};

struct line_set : multiset<line, less<>> {
    static const ll INF = LLONG_MAX;
    ll div(ll a, ll b) {
        return a / b - ((a ^ b) < 0 && a % b);
    }
    bool inter(iterator x, iterator y) {
        if (y == end()) return x->p = INF, false;
        if (x->a == y->a) x->p = x->b > y->b ? INF : -INF;
        else x->p = div(y->b - x->b, x->a - y->a);
        return x->p >= y->p;
    }
    void add(ll a, ll b) {
        auto z = insert({a, b, 0}), y = z++, x = y;
        while (inter(y, z)) z = erase(z);
        if (x != begin() && inter(--x, y)) inter(x, y = erase(y));
        while ((y = x) != begin() && (--x)->p >= y->p) {
            inter(x, erase(y));
        }
    }
    ll get(ll x) {
        line l = *lower_bound(x);
        return l.a * x + l.b;
    }
};
```

Grafy (4)

4.1 Przepływy

Dinic.h

Opis: Znajduje największy przepływ. Na niektórych grafach może być szybszy bez skalowania.
Czas: $\mathcal{O}(nm \log U)$

```
struct dinic {
    struct edge {
        int to, rev;
        int cap;
    };
    int n;
    vector<vector<edge>> adj;
    vector<int> q, lvl, it;
    dinic(int _n) {
        n = _n;
```

```
        adj.resize(n);
        q.reserve(n);
        lvl.resize(n);
        it.resize(n);
    }
    void add_edge(int u, int v, int cap) {
        int i = ssize(adj[u]), j = ssize(adj[v]) + (u == v);
        adj[u].push_back({v, j, cap});
        adj[v].push_back({u, i, 0});
    }
    bool bfs(int s, int t, int r) {
        q.clear();
        lvl.assign(n, -1);
        lvl[s] = 0;
        q.push_back(s);
        for (int i = 0; i < ssize(q); i++) {
            int u = q[i];
            for (edge& e : adj[u]) {
                if (e.cap >= r && lvl[e.to] == -1) {
                    lvl[e.to] = lvl[u] + 1;
                    q.push_back(e.to);
                    if (e.to == t) return true;
                }
            }
        }
        return false;
    }
    ll dfs(int u, int t, ll cap) {
        if (u == t) return cap;
        ll f = 0;
        for (int& i = it[u]; i < ssize(adj[u]); i++) {
            edge& e = adj[u][i];
            if (e.cap > 0 && lvl[u] + 1 == lvl[e.to]) {
                ll add = dfs(e.to, t, min(cap - f, (ll)e.cap));
                e.cap -= add;
                adj[e.to][e.rev].cap += add;
                f += add;
            }
            if (f == cap) return f;
        }
        lvl[u] = -1;
        return f;
    }
    ll flow(int s, int t, ll cap) {
        ll f = 0;
        for (int i = 29; i >= 0; i--) {
            while (f < cap && bfs(s, t, 1 << i)) {
                it.assign(n, 0);
                f += dfs(s, t, cap - f);
            }
        }
        return f;
    }
};
```

MCMF.h

Opis: Jeżeli są ujemne krawędzie, przed puszczeniem flow w dst trzeba policzyć najkrótsze ścieżki z s i puścić reduce(t).
Czas: $\mathcal{O}(Fm \log n)$

```
#include <ext/pb_ds/priority_queue.hpp>
ll INF64 = 2e18;
struct MCMF {
    struct edge {
        int to, rev;
        int cap;
        ll cost;
    };
    struct cmp {
```

```

    bool operator()(const auto& l, const auto& r) const {
        return l.second > r.second;
    }
};
int n;
vector<vector<edge>> adj;
vector<ll> dst;
ll c = 0;
__gnu_pbds::priority_queue<pair<int, ll>, cmp> q;
vector<decltype(q)::point_iterator> its;
vector<int> id;
MCMF(int _n) {
    n = _n;
    adj.resize(n);
    id.resize(n);
}
void add_edge(int u, int v, int cap, int cost) {
    int i = ssize(adj[u]), j = ssize(adj[v]) + (u == v);
    adj[u].push_back({v, j, cap, cost});
    adj[v].push_back({u, i, 0, -cost});
}
void reduce(int t) {
    for (int i = 0; i < n; i++) {
        for (edge& e : adj[i]) {
            if (dst[i] != INF64 && dst[e.to] != INF64) {
                e.cost += dst[i] - dst[e.to];
            }
        }
    }
    c += dst[t];
}
bool dijkstra(int s, int t) {
    dst.assign(n, INF64);
    its.assign(n, q.end());
    dst[s] = 0;
    q.push({s, 0});
    while (!q.empty()) {
        int u = q.top().first;
        q.pop();
        for (edge& e : adj[u]) {
            if (e.cap > 0) {
                ll d = dst[u] + e.cost;
                if (d < dst[e.to]) {
                    dst[e.to] = d;
                    if (its[e.to] == q.end()) {
                        its[e.to] = q.push({e.to, dst[e.to]});
                    } else {
                        q.modify(its[e.to], {e.to, dst[e.to]});
                    }
                    id[e.to] = e.rev;
                }
            }
        }
    }
    reduce(t);
    return dst[t] != INF64;
}
pair<ll, ll> flow(int s, int t, ll cap) {
    ll ff = 0;
    ll cc = 0;
    while (ff < cap && dijkstra(s, t)) {
        ll f = cap - ff;
        for (int i = t; i != s; i) {
            edge& e = adj[i][id[i]];
            f = min(f, (ll)adj[e.to][e.rev].cap);
            i = e.to;
        }
        for (int i = t; i != s; i) {
            edge& e = adj[i][id[i]];

```

```

            e.cap += f;
            adj[e.to][e.rev].cap -= f;
            i = e.to;
        }
        ff += f;
        cc += f * c;
    }
    return {ff, cc};
}
};

```

4.2 Skojarzenia

Matching.h

Opis: Dinic uproszczony dla grafów dwudzielnych.

Czas: $\mathcal{O}(m\sqrt{n})$

```

struct matching {
    int n, m;
    vector<vector<int>> adj;
    vector<int> pb, pa;
    vector<int> lvl, it;
    matching(int _n, int _m) {
        n = _n;
        m = _m;
        adj.resize(n);
        pb.resize(n, -1);
        pa.resize(m, -1);
        it.resize(n);
    }
    void add_edge(int u, int v) {
        adj[u].push_back(v);
    }
    bool bfs() {
        bool res = false;
        lvl.assign(n, -1);
        queue<int> q;
        for (int i = 0; i < n; i++) {
            if (pb[i] == -1) {
                q.push(i);
                lvl[i] = 0;
            }
        }
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (int j : adj[u]) {
                if (pa[j] == -1) {
                    res = true;
                } else if (lvl[pa[j]] == -1) {
                    lvl[pa[j]] = lvl[u] + 1;
                    q.push(pa[j]);
                }
            }
        }
        return res;
    }
    bool dfs(int u) {
        for (auto& i = it[u]; i < ssize(adj[u]); i++) {
            int v = adj[u][i];
            if (pa[v] == -1 ||
                (lvl[pa[v]] == lvl[u] + 1 && dfs(pa[v]))) {
                pb[u] = v;
                pa[v] = u;
                return true;
            }
        }
    }
}

```

```

        return false;
    }
    int match() {
        int ans = 0;
        while (bfs()) {
            it.assign(n, 0);
            for (int i = 0; i < n; i++) {
                if (pb[i] == -1 && dfs(i)) ans++;
            }
        }
        return ans;
    }
};

```

4.3 Grafy skierowane

SCC.h

Opis: Spójne są posortowane topologicznie.

Czas: $\mathcal{O}(n + m)$

```

struct SCC {
    int n, cnt = 0;
    vector<vector<int>> adj;
    vector<int> p, low, in;
    stack<int> st;
    int tour = 0;
    SCC(int _n) {
        n = _n;
        adj.resize(n);
        p.resize(n, -1);
        low.resize(n);
        in.resize(n, -1);
    }
    void add_edge(int u, int v) {
        adj[u].push_back(v);
    }
    void dfs(int u) {
        low[u] = in[u] = tour++;
        st.push(u);
        for (int v : adj[u]) {
            if (in[v] == -1) {
                dfs(v);
                low[u] = min(low[u], low[v]);
            } else {
                low[u] = min(low[u], in[v]);
            }
        }
        if (low[u] == in[u]) {
            int v = -1;
            do {
                v = st.top();
                st.pop();
                in[v] = n;
                p[v] = cnt;
            } while (v != u);
            cnt++;
        }
    }
    void build() {
        for (int i = 0; i < n; ++i) {
            if (in[i] == -1) dfs(i);
        }
        for (int i = 0; i < n; i++) p[i] = cnt - 1 - p[i];
    }
};

```

Matma (5)

5.1 Arytmetyka modularna

ModInt.h

```
template<int M, int R>
struct mod {
    static const int MOD = M, ROOT = R;
    int x;
    mod(ll y = 0) : x(y % M) { x += (x < 0) * M; }
    mod operator+=(const mod& o) {
        if ((x += o.x) >= M) x -= M;
        return *this;
    }
    mod operator-=(const mod& o) {
        if ((x -= o.x) < 0) x += M;
        return *this;
    }
    mod operator*=(const mod& o) {
        x = 1ll * x * o.x % M;
        return *this;
    }
    mod operator/=(const mod& o) {
        return (*this) *= o.inv();
    }
    friend mod operator+(mod a, const mod& b) { return a += b; }
    friend mod operator-(mod a, const mod& b) { return a -= b; }
    friend mod operator*(mod a, const mod& b) { return a *= b; }
    friend mod operator/(mod a, const mod& b) { return a /= b; }
    auto operator<=>(const mod&) const = default;
    mod pow(ll n) const {
        mod a = x, b = 1;
        while (n > 0) {
            if (n % 2 == 1) b *= a;
            a *= a;
            n /= 2;
        }
        return b;
    }
    mod inv() const {
        return pow(M - 2);
    }
};
using mint = mod<998244353, 3>;
```

GCD.h

Opis: Znajduje x i y takie, że $ax + by = \gcd(a, b)$.
Czas: $\mathcal{O}(\log(\min(a, b)))$

```
ll gcd(ll a, ll b, ll& x, ll& y) {
    if (!b) return x = 1, y = 0, a;
    ll g = gcd(b, a % b, y, x);
    return y -= x * (a / b), g;
}
```

5.2 Wielomiany

NTT.h

Opis: Mnoży dwa wielomiany modulo liczba NTT-pierwsza.
Czas: $\mathcal{O}((n + m) \log(n + m))$

```
template<typename T>
void ntt(vector<T>& a, bool inv) {
    int n = ssize(a);
```

ModInt GCD NTT Conv3 FST KMP Manacher

```
vector<T> b(n);
for (int i = n / 2; i > 0; i /= 2, swap(a, b)) {
    T w = T(T::ROOT).pow((T::MOD - 1) / n * i), m = 1;
    for (int j = 0; j < n; j += 2 * i, m *= w) {
        for (int k = 0; k < i; k++) {
            T u = a[j + k], v = a[j + k + i] * m;
            b[j / 2 + k] = u + v;
            b[j / 2 + k + n / 2] = u - v;
        }
    }
}
if (inv) {
    reverse(a.begin() + 1, a.end());
    T ni = T(n).inv();
    for (int i = 0; i < n; i++) a[i] *= ni;
}
}
template<typename T>
vector<T> conv(vector<T> a, vector<T> b) {
    int s = ssize(a) + ssize(b) - 1;
    int n = 1 << (1lg(2 * s - 1));
    a.resize(n); b.resize(n);
    ntt(a, false); ntt(b, false);
    for (int i = 0; i < n; i++) a[i] *= b[i];
    ntt(a, true);
    a.resize(s);
    return a;
}
```

Conv3.h

Opis: Mnoży dwa wielomiany. Musi zachodzić $n + m \leq 2^{24}$ oraz $c_k \leq 5 \cdot 10^{25}$.
Czas: $\mathcal{O}((n + m) \log(n + m))$

```
template<typename T>
vector<T> mconv(const auto& a, const auto& b) {
    auto cp = [&](const auto& v) {
        vector<T> vv(ssize(v));
        for (int i = 0; i < ssize(v); i++) vv[i] = T(v[i].x);
        return vv;
    };
    return conv(cp(a), cp(b));
}
template<typename T>
vector<T> conv3(const vector<T>& a, const vector<T>& b) {
    using m0 = mod<754974721, 11>; auto c0 = mconv<m0>(a, b);
    using m1 = mod<167772161, 3>; auto c1 = mconv<m1>(a, b);
    using m2 = mod<469762049, 3>; auto c2 = mconv<m2>(a, b);
    m1 r01 = m1(m0::MOD).inv();
    m2 r02 = m2(m0::MOD).inv(), r12 = m2(m1::MOD).inv();
    vector<T> d(ssize(c0));
    for (int i = 0; i < ssize(c0); i++) {
        int x = c0[i].x;
        int y = ((c1[i] - x) * r01).x;
        int z = (((c2[i] - x) * r02 - y) * r12).x;
        d[i] = (T(z) * m1::MOD + y) * m0::MOD + x;
    }
    return d;
}
```

5.3 Sploty

FST.h

Opis: Wykonuje splot bitowy. n musi być potęgą dwójki.
Czas: $\mathcal{O}(n \log n)$

```
void fst(vector<mint>& a, bool inv) {
    int n = ssize(a);
```

```
for (int i = 1; i < n; i *= 2) {
    for (int j = 0; j < n; j += 2 * i) {
        for (int k = 0; k < i; k++) {
            mint u = a[j + k], v = a[j + k + i];
            a[j + k] = u + v, a[j + k + i] = u - v; // XOR
            // a[j + k] = inv ? u - v : u + v; // AND
            // a[j + k + i] = inv ? v - u : u + v; // OR
        }
    }
}
// XOR
if (inv) {
    mint ni = mint(n).inv();
    for (int i = 0; i < n; i++) a[i] = a[i] * ni;
}
}
vector<mint> conv(vector<mint> a, vector<mint> b) {
    int n = ssize(a);
    fst(a, false); fst(b, false);
    for (int i = 0; i < n; i++) a[i] = a[i] * b[i];
    fst(a, true);
    return a;
}
```

Teksty (6)

KMP.h

Opis: p[i] – najdłuższy ścisły sufix s[0:i] który jest prefiksem s.
Czas: $\mathcal{O}(n)$

```
vector<int> kmp(const string& s) {
    int n = ssize(s);
    vector<int> p(n);
    for (int i = 1; i < n; i++) {
        int j = p[i - 1];
        while (j > 0 && s[i] != s[j]) j = p[j - 1];
        p[i] = j + (s[i] == s[j]);
    }
    return p;
}
```

Manacher.h

Opis: Znajduje długość najdłuższego palindromu w każdym środku. p[2 * i] – środek w i , p[2 * i + 1] – środek między i a $i + 1$.
Czas: $\mathcal{O}(n)$

```
vector<int> manacher(const string& s) {
    int n = ssize(s);
    string t(2 * n - 1, '#');
    for (int i = 0; i < n; i++) t[2 * i] = s[i];
    vector<int> p(2 * n - 1);
    for (int i = 0, l = -1, r = -1; i < 2 * n - 1; i++) {
        if (i <= r) p[i] = min(r - i + 1, p[l + r - i]);
        while (p[i] < min(i + 1, 2 * n - 1 - i)) {
            if (t[i - p[i]] != t[i + p[i]]) break;
            p[i]++;
        }
        if (i + p[i] - 1 > r) {
            l = i - p[i] + 1;
            r = i + p[i] - 1;
        }
    }
    for (int i = 0; i < 2 * n - 1; i++) {
        p[i] -= t[i - p[i] + 1] == '#';
    }
    return p;
}
```

```
}

SuffixArray.h
Opis: Jeżeli tekst ma znaki inne niż a-z trzeba zmienić inicjalizację.
Czas:  $\mathcal{O}(n \log n)$ 
```

```
vector<int> suffix_array(const string& s) {
    int n = ssize(s);
    vector<int> p(n), cnt(26);
    for (int i = 0; i < n; i++) cnt[s[i] - 'a']++;
    for (int i = 1; i < 26; i++) cnt[i] += cnt[i - 1];
    for (int i = 0; i < n; i++) p[--cnt[s[i] - 'a']] = i;
    vector<int> rnk(n);
    for (int i = 1; i < n; i++) {
        rnk[p[i]] = s[p[i]] == s[p[i - 1]] ? rnk[p[i - 1]] : i;
    }
    cnt.resize(n);
    vector<int> np(n), nrnk(n);
    for (int len = 1; len < n; len *= 2) {
        iota(cnt.begin(), cnt.end(), 0);
        for (int i = n - len; i < n; i++) np[cnt[rnk[i]]++] = i;
        for (int i = 0; i < n; i++) {
            if (p[i] - len >= 0) {
                np[cnt[rnk[p[i] - len]]++] = p[i] - len;
            }
        }
        nrnk[np[0]] = 0;
        for (int i = 1; i < n; i++) {
            int a = np[i - 1];
            int b = np[i];
            if (max(a, b) + len < n && rnk[a] == rnk[b] &&
                rnk[a + len] == rnk[b + len]) {
                nrnk[b] = nrnk[a];
            } else {
                nrnk[b] = i;
            }
        }
        swap(p, np);
        swap(rnk, nrnk);
    }
    return p;
};

vector<int> build_lcp(const string& s, const vector<int>& sa) {
    int n = ssize(s);
    vector<int> pos(n);
    for (int i = 0; i < n; i++) pos[sa[i]] = i;
    vector<int> lcp(n - 1);
    int k = 0;
    for (int i = 0; i < n; i++) {
        if (pos[i] == 0) continue;
        while (i + k < n && s[i + k] == s[sa[pos[i] - 1] + k]) k++;
        lcp[pos[i] - 1] = k;
        k = max(0, k - 1);
    }
    return lcp;
}
```

Z.h

Opis: $f[i]$ – największe k takie, że $f[i:i+k]$ jest prefiksem s .

Czas: $\mathcal{O}(n)$

```
vector<int> z(const string& s) {
    int n = ssize(s);
    vector<int> f(n);
    f[0] = n;
    for (int i = 1, l = 0, r = 0; i < n; i++) {
        if (i <= r) f[i] = min(r - i + 1, f[i - 1]);
        while (f[i] < n - i && s[i + f[i]] == s[f[i]]) f[i]++;
        if (i + f[i] - 1 > r) {
```

```
            l = i;
            r = i + f[i] - 1;
        }
    }
    return f;
}
```

Geometria (7)

7.1 Podstawy

Point.h

Opis: Podstawowy szablon do geometrii. Do wszystkich porównań należy używać `sgn`.

```
using D = ll;
const D EPS = D(1e-9);
int sgn(D x) { return (x > EPS) - (x < -EPS); }
struct P {
    D x, y;
    P operator+(P o) const { return {x + o.x, y + o.y}; }
    P operator-(P o) const { return {x - o.x, y - o.y}; }
    P operator*(D a) const { return {x * a, y * a}; }
    P operator/(D a) const { return {x / a, y / a}; }
    auto operator<=> (P o) const {
        return pair(sgn(x - o.x), sgn(y - o.y)) <=> pair(0, 0);
    }
    bool operator==(P o) const {
        return sgn(x - o.x) == 0 && sgn(y - o.y) == 0;
    }
};
D cross(P a, P b) { return a.x * b.y - a.y * b.x; }
D dot(P a, P b) { return a.x * b.x + a.y * b.y; }
D norm(P a) { return a.x * a.x + a.y * a.y; }
auto& operator<<(auto& o, P a) {
    return o << '(' << a.x << ", " << a.y << ')';
}
```

AngleCmp.h

Opis: Sortuje punkty w kolejności CCW, zaczynając od $y < 0$. Punkt $(0, 0)$ należy do linii $x \geq 0, y = 0$.

```
int half(P a) {
    if (sgn(a.y) < 0) return -1;
    if (sgn(a.y) == 0 && sgn(a.x) >= 0) return 0;
    return 1;
}
bool angle_cmp(P a, P b) {
    if (half(a) != half(b)) return half(a) < half(b);
    return sgn(cross(a, b)) > 0;
}
```

7.2 Wielokąty

ConvexHull.h

Opis: Znajduje otoczkę wypukłą w kierunku CCW. Usuwa punkty współliniowe.

Czas: $\mathcal{O}(n \log n)$

```
vector<P> convex_hull(vector<P> p) {
    if (ssize(p) <= 1) return p;
    sort(p.begin(), p.end());
    vector<P> h(ssize(p) + 1);
```

```
    int s = 0, t = 0;
    for (int it = 0; it < 2; it++) {
        for (P a : p) {
            while (t >= s + 2) {
                P u = h[t - 2], v = h[t - 1];
                if (sgn(cross(v - u, a - v)) <= 0) t--;
                else break;
            }
            h[t++] = a;
        }
        reverse(p.begin(), p.end());
        s = --t;
    }
    h.resize(t - (t == 2 && h[0] == h[1]));
    return h;
}
```

PolygonTangents.h

Opis: Znajduje najbliższe punkty styczne różne od a . Wielokąt musi być CCW i $n \geq 3$. Punkt a nie może leżeć w ściśłym wnętrzu wielokąta.

Czas: $\mathcal{O}(\log n)$

```
pair<P, P> tangents(const vector<P>& p, P a) {
    int n = ssize(p);
    P t[2];
    for (int it = 0; it < 2; it++) {
        auto dir = [&](int i) {
            P u = p[i] - a;
            P v = p[i < n - 1 ? i + 1 : 0] - a;
            int c = sgn(cross(u, v));
            if (c != 0) return c < 0;
            if (sgn(dot(u, v)) <= 0) return true;
            return sgn(norm(u) - norm(v)) > 0;
        };
        auto dirx = [&](int i) { return dir(i) ^ it; };
        if (dirx(0) == 1 && dirx(n - 1) == 0) {
            t[it] = p[0];
            continue;
        }
        int s[2] = {0, n - 1};
        while (s[1] - s[0] > 2) {
            int mid = (s[0] + s[1]) / 2;
            int x = dirx(mid);
            if (dirx(s[x ^ 1]) == (x ^ 1)) {
                s[x] = mid;
            } else {
                bool b = sgn(cross(p[mid] - a, p[s[1]] - a)) < 0;
                s[b ^ x ^ it ^ 1] = mid;
            }
        }
        t[it] = p[s[0] + 1 + (dirx(s[0] + 1) == 0)];
    }
    return {t[0], t[1]};
}
```

Inne (8)

GCC.h

#pragma GCC optimize("O3,unroll-loops")

#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")