- 1 Contest
- 2 Matma
- 3 Geometria

# Contest (1)

#### sol.cpp

```
#include <bits/stdc++.h>
using namespace std;
using 11 = long long;
#ifdef LOCAL
auto& operator<<(auto&, pair<auto, auto>);
auto operator<<(auto& o, auto x) -> decltype(x.end(), o) {
  for (int i = 0; auto y : x) \circ << ", " + !i++ * 2 << y;
 return o << '}';
auto& operator<<(auto& o, pair<auto, auto> x) {
  return o << '(' << x.first << ", " << x.second << ')';</pre>
void __print(auto... x) { ((cerr << ' ' << x), ...) << endl; }</pre>
#define debug(x...) cerr << "[" #x "]:", __print(x)
#define debug(...) 2137
#endif
int main() {
 ios_base::sync_with_stdio(0);
 cin.tie(0);
```

#### .vimrc

```
set nu et ts=2 sw=2
filetype indent on
syntax on
colorscheme habamax
hi MatchParen ctermfg=66 ctermbg=234 cterm=underline
nnoremap;
nnoremap;
inoremap {<cr> {<cr>} {<cr} {
```

#### Makefile

```
CXXFLAGS=-std=c++20 -Wall -Wextra -Wshadow
sol: sol.cpp
  g++ $(CXXFLAGS) -fsanitize=address,undefined -g -DLOCAL \
     sol.cpp -o sol
fast: sol.cpp
  g++ $(CXXFLAGS) -O2 sol.cpp -o fast
```

#### test.sh

```
#!/bin/bash
for((i=1;i>0;i++)) do
    echo "$i"
    echo "$i" | ./gen > int
    diff -w <(./sol < int) <(./slow < int) || break
done
hash.sh</pre>
```

```
#!/bin/bash
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum |cut -c-6
.bashrc
```

```
alias rm='trash'
alias mv='mv -i'
alias cp='cp -i'
```

# $\underline{\text{Matma}}$ (2)

## 2.1 Arytmetyka modularna

### GCD.h

1

**Opis:** Rozszerzony algorytm Euklidesa. **Czas:**  $\mathcal{O}(\log \min(a, b))$ 

```
11 gcd(l1 a, l1 b, l1 &x, l1 &y) {
   if (!b) return x = 1, y = 0, a;
   l1 d = gcd(b, a % b, y, x);
   return y -= a / b * x, d;
}
```

#### CRT.h

**Opis:** Chińskie twierdzenie o resztach. **Czas:**  $\mathcal{O}(\log \min(m, n))$ 

```
ll crt(ll a, ll m, ll b, ll n) {
   if (n > m) swap(a, b), swap(m, n);
   ll x, y, g = gcd(m, n, x, y);
   assert((a - b) % g == 0); // no solution
   x = (b - a) % n * x % n / g * m + a;
   return x < 0 ? x + m * n / g : x;</pre>
```

#### ModMul.h

**Opis:** Mnożenie i potęgowanie dwóch long longów modulo. Jest to wyraźnie szybsze niż zamiana na \_\_int128.

```
using ull = uint64_t;
ull modmul(ull a, ull b, ull M) {
    ll ret = a * b - M * ull(1.L / M * a * b);
    return ret + M * (ret < 0) - M * (ret >= (ll)M);
}
ull modpow(ull b, ull e, ull mod) {
    ull ans = 1;
    for (; e; b = modmul(b, b, mod), e /= 2)
        if (e & 1) ans = modmul(ans, b, mod);
    return ans;
}
```

## 2.2 Liczby pierwsze

#### MillerRabin.h

Opis: Test pierwszości Millera-Rabina.

```
bool prime(ull n) {
   if (n < 2 || n % 6 % 4 != 1) return (n | 1) == 3;
   ull A[] = {2, 325, 9375, 28178, 450775, 9780504, 1795265022},
        s = __builtin_ctzll(n - 1), d = n >> s;
   for (ull a : A) {
      ull p = modpow(a % n, d, n), i = s;
      while (p != 1 && p != n - 1 && a % n && i--)
```

```
p = modmul(p, p, n);
if (p != n - 1 && i != s) return 0;
}
return 1;
```

#### PollardRho.h

Opis: Algorytm faktoryzacji rho Pollarda.

Czas:  $\mathcal{O}(n^{1/4})$ 

```
ull pollard(ull n) {
  ull x = 0, y = 0, t = 30, prd = 2, i = 1, q;
  auto f = [&](ull x) { return modmul(x, x, n) + i; };
  while (t++ & 40 || __gcd(prd, n) == 1) {
    if (x == y) x = ++i, y = f(x);
    if ((q = modmul(prd, max(x, y) - min(x, y), n))) prd = q;
    x = f(x), y = f(f(y));
}
return __gcd(prd, n);
}
void factor(ull n, map<ull, int>& cnt) {
    if (n == 1) return;
    if (prime(n)) { cnt[n]++; return; }
    ull x = pollard(n);
    factor(x, cnt); factor(n / x, cnt);
}
```

# $\underline{\text{Geometria}}$ (3)

## 3.1 Podstawy

#### Point.h

Opis: Podstawowy szablon do geometrii.

```
template < class T> int sqn(T x) { return (x > 0) - (x < 0); }
template < class T>
struct pt {
  pt operator+(pt o) const { return {x + o.x, y + o.y}; }
  pt operator-(pt o) const { return {x - o.x, y - o.y}; }
  pt operator*(T a) const { return {x * a, y * a}; }
  pt operator/(T a) const { return {x / a, y / a}; }
  friend T cross(pt a, pt b) { return a.x * b.y - a.y * b.x; }
  friend T cross(pt p, pt a, pt b) {
    return cross(a - p, b - p); }
  friend T dot(pt a, pt b) { return a.x * b.x + a.y * b.y; }
  friend T dot(pt p, pt a, pt b) {
    return dot(a - p, b - p); }
  friend T abs2(pt a) { return a.x * a.x + a.y * a.y; }
  friend T abs(pt a) { return sqrt(abs2(a)); }
  auto operator<=>(pt o) const {
    return pair(sqn(x - o.x), sqn(y - o.y)) <=> pair(0, 0); }
 bool operator==(pt o) const {
    return sgn(x - o.x) == 0 && sgn(y - o.y) == 0; }
  friend auto& operator<<(auto& o, pt a) {</pre>
    return o << '(' << a.x << ", " << a.v << ')'; }
};
```

#### AngleCmp.h

 $\mathbf{Opis}\colon$  Sortuje punkty rosnąco po kącie z przedziału  $(-\pi,\pi].$  Punkt(0,0)ma kąt0.

```
template<class P>
bool angle_cmp(P a, P b) {
  auto half = [](P p) { return sgn(p.y) ?: -sgn(p.x); };
```

UW

```
int A = half(a), B = half(b);
return A == B ? sgn(cross(a, b)) > 0 : A < B;
}</pre>
```

### LineDist.h

Opis: Najkrótsza odległość między punktem i prostą/odcinkiem.

```
auto line_dist(auto p, auto a, auto b) {
  return abs(cross(p, a, b)) / abs(b - a);
}
auto seg_dist(auto p, auto a, auto b) {
  if (sgn(dot(a, p, b)) <= 0) return abs(p - a);
  if (sgn(dot(b, p, a)) <= 0) return abs(p - b);
  return line_dist(p, a, b);
}</pre>
```

LineDist 2