```
1 Contest
```

2 Matma

3 Geometria

# Contest (1)

#### sol.cpp

```
#include <bits/stdc++.h>
using namespace std;
using 11 = long long;
#ifdef LOCAL
auto& operator<<(auto&, pair<auto, auto>);
auto operator<<(auto& o, auto x) -> decltype(x.end(), o) {
  for (int i = 0; auto y : x) \circ << ", " + !i++ * 2 << y;
 return o << '}';
auto& operator<<(auto& o, pair<auto, auto> x) {
  return o << '(' << x.first << ", " << x.second << ')';</pre>
void __print(auto... x) { ((cerr << ' ' << x), ...) << endl; }</pre>
#define debug(x...) cerr << "[" #x "]:", __print(x)
#define debug(...) 2137
#endif
int main() {
 ios_base::sync_with_stdio(0);
 cin.tie(0);
```

### .vimrc

```
set nu et ts=2 sw=2
filetype indent on
svntax on
colorscheme habamax
hi MatchParen ctermfg=66 ctermbg=234 cterm=underline
nnoremap ; :
nnoremap : ;
inoremap {<cr> {<cr>}<esc>0 <bs>
```

#### Makefile

```
CXXFLAGS=-std=c++20 -Wall -Wextra -Wshadow
sol: sol.cpp
 q++ $(CXXFLAGS) -fsanitize=address,undefined -q -DLOCAL \
     sol.cpp -o sol
fast: sol.cpp
 q++ $(CXXFLAGS) -02 sol.cpp -o fast
```

#### test.sh

```
#!/bin/bash
for((i=1;i>0;i++)) do
 echo "$i"
 echo "$i" | ./gen > int
 diff -w < (./sol < int) < (./slow < int) || break
done
hash.sh
```

```
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum |cut -c-6
.bashrc
alias rm='trash'
alias mv='mv -i'
alias cp='cp -i'
```

## Matma (2)

### 2.1 Arytmetyka modularna

#### GCD.h

1

Opis: Rozszerzony algorytm Euklidesa. Czas:  $\mathcal{O}(\log \min(a, b))$ 

```
ll gcd(ll a, ll b, ll &x, ll &y) {
 if (!b) return x = 1, y = 0, a;
 11 d = gcd(b, a % b, y, x);
 return y -= a / b * x, d;
```

#### CRT.h

Opis: Chińskie twierdzenie o resztach.

Czas:  $\mathcal{O}(\log \min(m, n))$ 

```
11 crt(ll a, ll m, ll b, ll n) {
 if (n > m) swap(a, b), swap(m, n);
 11 x, y, g = gcd(m, n, x, y);
 assert((a - b) % g == 0); // no solution
 x = (b - a) % n * x % n / g * m + a;
 return x < 0 ? x + m * n / q : x;
```

#### ModMul.h

Opis: Mnożenie i potegowanie dwóch long longów modulo. Jest to wyraźnie szybsze niż zamiana na \_\_int128.

```
using ull = uint64_t;
ull modmul(ull a, ull b, ull M) {
 ll ret = a * b - M * ull(1.L / M * a * b);
 return ret + M * (ret < 0) - M * (ret >= (11)M);
ull modpow(ull b, ull e, ull mod) {
 ull ans = 1;
 for (; e; b = modmul(b, b, mod), e /= 2)
   if (e & 1) ans = modmul(ans, b, mod);
 return ans:
```

## 2.2 Liczby pierwsze

### MillerRabin.h

Opis: Test pierwszości Millera-Rabina.

```
bool prime (ull n) {
 if (n < 2 | | n % 6 % 4 != 1) return (n | 1) == 3;
 ull A[] = \{2, 325, 9375, 28178, 450775, 9780504, 1795265022\}
      s = \underline{\quad} builtin_ctzll(n - 1), d = n >> s;
  for (ull a : A) {
    ull p = modpow(a % n, d, n), i = s;
    while (p != 1 && p != n - 1 && a % n && i--)
```

```
p = modmul(p, p, n);
  if (p != n - 1 && i != s) return 0;
return 1:
```

#### PollardRho.h

Opis: Algorytm faktoryzacji rho Pollarda.

Czas:  $\mathcal{O}(n^{1/4})$ 

```
ull pollard(ull n) {
 ull x = 0, y = 0, t = 30, prd = 2, i = 1, q;
 auto f = [\&] (ull x) \{ return modmul(x, x, n) + i; \};
 while (t++ % 40 || __gcd(prd, n) == 1) {
   if (x == y) x = ++i, y = f(x);
   if ((q = modmul(prd, max(x, y) - min(x, y), n))) prd = q;
   x = f(x), y = f(f(y));
 return __gcd(prd, n);
void factor(ull n, map<ull, int>& cnt) {
 if (n == 1) return;
 if (prime(n)) { cnt[n]++; return; }
 ull x = pollard(n);
 factor(x, cnt); factor(n / x, cnt);
```

## Geometria (3)

## Podstawy

#### Point.h

AngleCmp.h

```
template < class T> int sqn(T x) { return (x > 0) - (x < 0); }
template<class T>
struct pt {
 T x, y;
  pt operator+(pt o) const { return {x + o.x, y + o.y}; }
  pt operator-(pt o) const { return {x - o.x, y - o.y}; }
  pt operator*(T a) const { return {x * a, y * a}; }
  pt operator/(T a) const { return {x / a, y / a}; }
  friend T cross(pt a, pt b) { return a.x * b.y - a.y * b.x; }
  friend T cross(pt p, pt a, pt b) {
   return cross(a - p, b - p); }
  friend T dot(pt a, pt b) { return a.x * b.x + a.y * b.y; }
  friend T dot(pt p, pt a, pt b) {
   return dot(a - p, b - p); }
  friend T abs2(pt a) { return a.x * a.x + a.y * a.y; }
  auto operator<=>(const pt&) const = default;
  friend auto& operator<<(auto& o, pt a) {</pre>
    return o << '(' << a.x << ", " << a.y << ')'; }
using P = pt<11>;
```

**Opis:** Sortuje punkty rosnąco po kącie z przedziału  $(-\pi, \pi]$ . Punkt (0,0)

```
int half(P a) { return sgn(a.y) ?: -sgn(a.x); }
bool angle cmp(P a, P b) {
 int A = half(a), B = half(b);
 return A == B ? cross(a, b) > 0 : A < B;
```