```
1 Contest
```

2 Grafy

3 Matma

4 Teksty

5 Geometria

# $\underline{\text{Contest}}$ (1)

#include <bits/stdc++.h>

#### sol.cpp

```
using namespace std;
#define rep(i, a, b) for (int i = (a); i < (b); i++)
#define all(x) begin(x), end(x)
#define sz(x) int((x).size())
using 11 = long long;
using pii = pair<int, int>;
using vi = vector<int>;
#ifdef LOCAL
auto& operator<<(auto&, pair<auto, auto>);
auto operator<<(auto& o, auto x) -> decltype(x.end(), o) {
  for (int i = 0; auto y : x) o << ", " + !i++ * 2 << y;</pre>
  return o << '}';
auto& operator<<(auto& o, pair<auto, auto> x) {
  return o << '(' << x.first << ", " << x.second << ')';
void __print(auto... x) { ((cerr << ' ' << x), ...) << endl; }</pre>
\label{eq:define} \texttt{#define} \ \texttt{debug}(\texttt{x...}) \ \texttt{cerr} << \texttt{"[" $\#$x "]:", $$\_print(\texttt{x})$}
#define debug(...) 2137
#endif
int main() {
  cin.tie(0)->sync_with_stdio(0);
```

#### .vimrc

```
set nu et ts=2 sw=2
filetype indent on
syntax on
colorscheme habamax
hi MatchParen ctermfg=66 ctermbg=234 cterm=underline
nnoremap;:
nnoremap;;
inoremap {<cr> {<cr>} <cr>} <cr>} <cr>} <cr>} <cr>} <cr>} <cr>> <cr>< <cr
```

#### Makefile

```
CXXFLAGS=-std=c++20 -Wall -Wextra -Wshadow
sol: sol.cpp
g++ $(CXXFLAGS) -fsanitize=address,undefined -g -DLOCAL \
sol.cpp -o sol
fast: sol.cpp
g++ $(CXXFLAGS) -O2 sol.cpp -o fast
```

#### test.sh

1

3

3

```
#!/bin/bash
for((i=1;i>0;i++)) do
   echo "$i"
   echo "$i" | ./gen > int
   diff -w <(./sol < int) <(./slow < int) || break
done</pre>
```

#### hash.sh

#### .bashrc

```
alias rm='trash'
alias mv='mv -i'
alias cp='cp -i'
```

# Grafy (2)

## 2.1 Przepływy

#### Dinic.h

Opis: Dinic ze skalowaniem. Należy ustawić zakres it w flow zgodnie z U. Czas:  $\mathcal{O}(nm\log U)$ 

```
struct dinic {
 struct edge {
    int to, rev:
   11 cap;
 };
 vi lvl, ptr, q;
 vector<vector<edge>> adj;
 dinic(int n) : lvl(n), ptr(n), q(n), adj(n) {}
 void add_edge(int u, int v, ll cap, ll rcap = 0) {
    int i = sz(adj[u]), j = sz(adj[v]);
    adj[u].push_back(\{v, j + (u == v), cap\});
    adj[v].push_back({u, i, rcap});
 11 dfs(int v, int t, 11 f) {
   if (v == t || !f) return f;
    for (int& i = ptr[v]; i < sz(adj[v]); i++) {</pre>
     edge& e = adj[v][i];
     if (lvl[e.to] == lvl[v] + 1)
       if (ll p = dfs(e.to, t, min(f, e.cap))) {
          e.cap -= p, adj[e.to][e.rev].cap += p;
         return p;
    return 0;
 11 flow(int s, int t) {
   11 f = 0; q[0] = s;
    for (int it = 29; it >= 0; it--) do {
     lvl = ptr = vi(sz(q));
     int qi = 0, qe = lvl[s] = 1;
      while (qi < qe && !lvl[t]) {
       int v = q[qi++];
       for (edge e : adj[v])
         if (!lvl[e.to] && e.cap >> it)
            q[qe++] = e.to, lvl[e.to] = lvl[v] + 1;
      while (ll p = dfs(s, t, LLONG_MAX)) f += p;
```

```
} while (lvl[t]);
return f;
}
```

#### GomoryHu.h

Opis: Tworzy drzewo gdzie min cut to minimum na ścieżce.

Czas:  $\mathcal{O}(n)$  przepływów

```
struct edge { int u, v; ll w; };
vector<edge> gomory_hu(int n, const vector<edge>& ed) {
  vector<edge> t; vi p(n);
  rep(i, 1, n) {
    dinic d(n);
    for (edge e : ed) d.add_edge(e.u, e.v, e.w, e.w);
    t.push_back({i, p[i], d.flow(i, p[i])});
    rep(j, i + 1, n) if (p[j] == p[i] && d.lvl[j]) p[j] = i;
  }
  return t;
}
```

#### MCMF.h

**Opis:** MCMF z Dijkstrą. Jeżeli są ujemne krawędzie to przed puszczeniem flow w pi trzeba policzyć najkrótsze ścieżki z s. **Czas:**  $\mathcal{O}(Fm\log n)$ 

```
#include <ext/pb_ds/priority_queue.hpp>
const 11 INF = 2e18;
struct MCMF {
  struct edge {
    int from, to, rev;
    11 cap, cost;
  };
  int n;
  vector<vector<edge>> adj;
  vector<ll> dst, pi;
  __gnu_pbds::priority_queue<pair<11, int>> q;
  vector<decltype(q)::point_iterator> it;
  vector<edge*> p;
  MCMF(int _n) : n(_n), adj(n), pi(n), p(n) {}
  void add_edge(int u, int v, ll cap, ll cost) {
    int i = sz(adj[u]), j = sz(adj[v]);
    adj[u].push\_back({u, v, j + (u == v), cap, cost});
    adj[v].push_back({v, u, i, 0, -cost});
 bool path(int s, int t) {
    dst.assign(n, INF); it.assign(n, q.end());
    q.push(\{dst[s] = 0, s\});
    while (!q.empty()) {
      int u = q.top().second; q.pop();
      for (edge& e : adj[u]) {
        ll d = dst[u] + pi[u] + e.cost - pi[e.to];
        if (e.cap && d < dst[e.to]) {</pre>
          dst[e.to] = d, p[e.to] = &e;
          if (it[e.to] == q.end())
            it[e.to] = q.push({-dst[e.to], e.to});
          else
            q.modify(it[e.to], {-dst[e.to], e.to});
    rep(i, 0, n) pi[i] = min(pi[i] + dst[i], INF);
    return pi[t] != INF;
 pair<11, 11> flow(int s, int t, 11 cap) {
    11 f = 0, c = 0;
    while (f < cap && path(s, t)) {
     11 d = cap - f;
      for (edge* e = p[t]; e; e = p[e->from])
```

```
d = min(d, e->cap);
for (edge* e = p[t]; e; e = p[e->from])
    e->cap -= d, adj[e->to][e->rev].cap += d;
    f += d, c += d * pi[t];
}
return {f, c};
}
};
```

### 2.2 DFS

#### SCC.h

**Opis:** Znajduje SCC w kolejności topologicznej. **Czas:**  $\mathcal{O}(n+m)$ 

```
struct SCC {
  int n, t = 0, cnt = 0;
  vector<vi> adi;
  vi val, p, st;
  SCC(int _n) : n(_n), adj(n), val(n), p(n, -1) {}
  void add edge(int u, int v) { adj[u].push back(v); }
  int dfs(int u) {
    int low = val[u] = ++t; st.push_back(u);
    for (int v : adj[u]) if (p[v] == -1)
     low = min(low, val[v] ?: dfs(v));
    if (low == val[u]) {
     for (int x = -1; x != u;)
       p[x = st.back()] = cnt, st.pop_back();
     cnt++;
   return low;
  void build() {
   rep(i, 0, n) if (!val[i]) dfs(i);
   rep(i, 0, n) p[i] = cnt - 1 - p[i];
};
```

# TwoSat.h Opis: 2-SAT. Czas: O(n+m)

```
struct two_sat {
 int n:
  vector<pii> ed;
  vector<bool> b;
 two_sat(int _n) : n(_n) {}
  int add_var() { return n++; }
  void either(int x, int y) {
   x = max(2 * x, -1 - 2 * x), y = max(2 * y, -1 - 2 * y);
   ed.push_back({x, y}); }
  void implies(int x, int y) { either(~x, y); }
  void must(int x) { either(x, x); }
  void at_most_one(const vi& v) {
   if (sz(v) <= 1) return;
   int cur = ~v[0];
   rep(i, 2, sz(v)) {
     int nxt = add_var();
     either(cur, ~v[i]); either(cur, nxt);
     either(~v[i], nxt); cur = ~nxt;
   either(cur, ~v[1]);
  bool solve() {
   SCC scc(2 * n);
   for (auto [u, v] : ed)
     scc.add_edge(u ^ 1, v), scc.add_edge(v ^ 1, u);
```

```
scc.build(); b.resize(n, 1);
rep(i, 0, n) {
    if (scc.p[2 * i] == scc.p[2 * i + 1]) return 0;
    if (scc.p[2 * i] < scc.p[2 * i + 1]) b[i] = 0;
}
return 1;
}
};</pre>
```

# $\underline{\text{Matma}}$ (3)

### 3.1 Arytmetyka modularna

#### GCD.h

**Opis:** Rozszerzony algorytm Euklidesa. **Czas:**  $\mathcal{O}(\log \min(a, b))$ 

```
ll gcd(ll a, ll b, ll &x, ll &y) {
   if (!b) return x = 1, y = 0, a;
   ll d = gcd(b, a % b, y, x);
   return y -= a / b * x, d;
}
```

#### CRT.h

**Opis:** Chińskie twierdzenie o resztach. **Czas:**  $O(\log \min(m, n))$ 

```
11 crt(ll a, ll m, ll b, ll n) {
   if (n > m) swap(a, b), swap(m, n);
   ll x, y, g = gcd(m, n, x, y);
   assert((a - b) % g == 0); // no solution
   x = (b - a) % n * x % n / g * m + a;
   return x < 0 ? x + m * n / g : x;
}</pre>
```

#### ModMul.h

**Opis:** Mnożenie i potęgowanie dwóch long longów modulo. Jest to wyraźnie szybsze niż zamiana na \_\_int128.

```
using ull = uint64_t;
ull modmul(ull a, ull b, ull M) {
    ll ret = a * b - M * ull(1.L / M * a * b);
    return ret + M * (ret < 0) - M * (ret >= (ll)M);
}
ull modpow(ull b, ull e, ull mod) {
    ull ans = 1;
    for (; e; b = modmul(b, b, mod), e /= 2)
        if (e & 1) ans = modmul(ans, b, mod);
    return ans;
}
```

#### ModInt.h

```
template<int M, int R>
struct mod {
    static const int MOD = M, ROOT = R;
    int x;
    mod(ll y = 0) : x(y % M) { x += (x < 0) * M; }
    mod operator+=(mod o) {
        if ((x += 0.x) >= M) x -= M;
        return *this; }
    mod operator-=(mod o) {
        if ((x -= 0.x) < 0) x += M;
        return *this; }
    mod operator*=(mod o) {</pre>
```

```
x = 111 * x * o.x % M;
return *this; }
mod operator/=(mod o) { return (*this) *= o.inv(); }
friend mod operator+(mod a, mod b) { return a += b; }
friend mod operator-(mod a, mod b) { return a -= b; }
friend mod operator*(mod a, mod b) { return a *= b; }
friend mod operator/(mod a, mod b) { return a *= b; }
friend mod operator/(mod a, mod b) { return a /= b; }
auto operator<=>(const mod&) const = default;
mod pow(11 n) const {
  mod a = x, b = 1;
  for (; n; n /= 2, a *= a) if (n & 1) b *= a;
  return b;
}
mod inv() const { return pow(M - 2); }
};
using mint = mod<998244353, 3>;
```

### 3.2 Liczby pierwsze

#### MillerRabin.h

Opis: Test pierwszości Millera-Rabina.

```
bool prime(ull n) {
   if (n < 2 || n % 6 % 4 != 1) return (n | 1) == 3;
   ull A[] = {2, 325, 9375, 28178, 450775, 9780504, 1795265022},
        s = __builtin_ctzll(n - 1), d = n >> s;
   for (ull a : A) {
        ull p = modpow(a % n, d, n), i = s;
        while (p != 1 && p != n - 1 && a % n && i--)
            p = modmul(p, p, n);
        if (p != n - 1 && i != s) return 0;
    }
   return 1;
}
```

#### PollardRho.h

Opis: Algorytm faktoryzacji rho Pollarda.

Czas:  $\mathcal{O}(n^{1/4})$ 

```
ull pollard(ull n) {
  ull x = 0, y = 0, t = 30, prd = 2, i = 1, q;
  auto f = [&](ull x) { return modmul(x, x, n) + i; };
  while (t++ % 40 || __gcd(prd, n) == 1) {
    if (x == y) x = ++i, y = f(x);
    if ((q = modmul(prd, max(x, y) - min(x, y), n))) prd = q;
    x = f(x), y = f(f(y));
  }
  return __gcd(prd, n);
}
void factor(ull n, map<ull, int>& cnt) {
  if (n == 1) return;
  if (prime(n)) { cnt[n]++; return; }
  ull x = pollard(n);
  factor(x, cnt); factor(n / x, cnt);
}
```

# 3.3 Wielomiany

### NTT.h

Czas:  $\mathcal{O}((n+m)\log(n+m))$ 

```
template<class T>
void ntt(vector<T>& a, bool inv) {
  int n = sz(a); vector<T> b(n);
  for (int i = n / 2; i; i /= 2, swap(a, b)) {
   T w = T(T::ROOT).pow((T::MOD - 1) / n * i), m = 1;
   for (int j = 0; j < n; j += 2 * i, m *= w) rep(k, 0, i) {
     T u = a[j + k], v = a[j + k + i] * m;
     b[j / 2 + k] = u + v, b[j / 2 + k + n / 2] = u - v;
  if (inv) {
   reverse(1 + all(a));
   T z = T(n).inv(); rep(i, 0, n) a[i] *= z;
template<class T>
vector<T> conv(vector<T> a, vector<T> b) {
 int s = sz(a) + sz(b) - 1, n = 1 << __1q(2 * s - 1);
  a.resize(n); ntt(a, 0); b.resize(n); ntt(b, 0);
  rep(i, 0, n) a[i] *= b[i];
  ntt(a, 1); a.resize(s);
 return a;
Conv3.h
Opis: NTT z Garnerem. Działa dla n + m < 2^{24} i c_k < 5 \cdot 10^{25}.
Czas: \mathcal{O}((n+m)\log(n+m))
template < class T>
vector<T> mconv(const auto& x, const auto& y) {
  auto con = [&](const auto& v) {
   vector<T> w(sz(v)); rep(i, 0, sz(v)) w[i] = v[i].x;
    return w: };
  return conv(con(x), con(y));
template < class T>
vector<T> conv3(const vector<T>& a, const vector<T>& b) {
  using m0 = mod<754974721, 11>; auto c0 = mconv< m0>(a, b);
  using m1 = mod<167772161, 3>; auto c1 = mconv<m1>(a, b);
  using m2 = mod<469762049, 3>; auto c2 = mconv<m2>(a, b);
  int n = sz(c0); vector<T> d(n); m1 r01 = m1(m0::MOD).inv();
  m2 r02 = m2 (m0::MOD).inv(), r12 = m2 (m1::MOD).inv();
  rep(i, 0, n) {
   int x = c0[i].x, y = ((c1[i] - x) * r01).x,
       z = (((c2[i] - x) * r02 - y) * r12).x;
   d[i] = (T(z) * m1::MOD + y) * m0::MOD + x;
```

# Teksty (4)

return d;

### 4.1 Podstawy

```
KMP.h
Czas: \mathcal{O}(n)
```

```
vi kmp(const string& s) {
 vi p(sz(s));
  rep(i, 1, sz(s)) {
   int g = p[i - 1];
   while (g \&\& s[i] != s[g]) g = p[g - 1];
   p[i] = g + (s[i] == s[g]);
  return p;
```

```
Czas: \mathcal{O}(n)
vi z(const string& s) {
 int n = sz(s), 1 = -1, r = -1;
 vi f(n); f[0] = n;
 rep(i, 1, sz(s)) {
    if (i < r) f[i] = min(r - i, f[i - 1]);
    while (i + f[i] < n \&\& s[i + f[i]] == s[f[i]]) f[i]++;
    if (i + f[i] > r) l = i, r = i + f[i];
 return f;
Manacher.h
Opis: p[1][i] - \text{środek w } i, p[0][i] - \text{środek między } i - 1 \text{ a } i.
Czas: \mathcal{O}(n)
array<vi, 2> manacher(const string& s) {
 int n = sz(s);
 array < vi, 2 > p = {vi(n + 1), vi(n)};
 rep(z, 0, 2) for (int i = 0, l = 0, r = 0; i < n; i++) {
    int t = r - i + !z;
    if (i < r) p[z][i] = min(t, p[z][1 + t]);
    int L = i - p[z][i], R = i + p[z][i] - !z;
    while (L >= 1 \&\& R + 1 < n \&\& s[L - 1] == s[R + 1])
      p[z][i]++, L--, R++;
    if (R > r) l = L, r = R;
 return p;
```

Opis: Rozkłada słowo na nierosnący ciąg podsłów mniejszych od swoich wszystkich nietrywialnych sufiksów.

Czas:  $\mathcal{O}(n)$ 

```
vi duval(const string& s) {
 int n = sz(s); vi f;
 for (int i = 0; i < n;) {</pre>
    int j = i + 1, k = i;
    for (; j < n \&\& s[k] \le s[j]; ++j) {
     if (s[k] < s[j]) k = i;
    for (; i <= k; i += j - k) f.push_back(i);</pre>
 return f.push_back(n), f;
```

# Geometria (5)

# 5.1 Podstawy

Point.h

Opis: Podstawowy szablon do geometrii.

```
template < class T> int sqn(T x) { return (x > 0) - (x < 0); }
template<class T>
struct pt {
 T x, y;
 pt operator+(pt o) const { return {x + o.x, y + o.y}; }
  pt operator-(pt o) const { return {x - o.x, y - o.y}; }
  pt operator*(T a) const { return {x * a, y * a}; }
  pt operator/(T a) const { return {x / a, y / a}; }
```

```
friend T cross(pt a, pt b) { return a.x * b.y - a.y * b.x; }
  friend T cross(pt p, pt a, pt b) {
    return cross(a - p, b - p); }
  friend T dot(pt a, pt b) { return a.x * b.x + a.y * b.y; }
  friend T dot(pt p, pt a, pt b) {
    return dot(a - p, b - p); }
  friend T abs2(pt a) { return a.x * a.x + a.y * a.y; }
  friend T abs(pt a) { return sqrt(abs2(a)); }
  auto operator <=> (pt o) const {
    return pair(sgn(x - o.x), sgn(y - o.y)) <=> pair(0, 0); }
 bool operator==(pt o) const {
    return sgn(x - o.x) == 0 && sgn(y - o.y) == 0; }
 friend auto& operator<<(auto& o, pt a) {</pre>
    return o << '(' << a.x << ", " << a.y << ')'; }
using P = pt<11>;
```

AngleCmp.h

**Opis:** Sortuje punkty rosnaco po kacie z przedziału  $(-\pi, \pi]$ . Punkt (0,0)

```
bool angle_cmp(P a, P b) {
 auto half = [](P p) { return sgn(p.y) ?: -sgn(p.x); };
 int A = half(a), B = half(b);
 return A == B ? sgn(cross(a, b)) > 0 : A < B;
```

#### LineDist.h

Opis: Najkrótsza odległość między punktem i prostą/odcinkiem.

```
auto line_dist(P p, P a, P b) {
  return abs(cross(p, a, b)) / abs(b - a);
auto seg_dist(P p, P a, P b) {
  if (sgn(dot(a, p, b)) <= 0) return abs(p - a);</pre>
  if (sgn(dot(b, p, a)) <= 0) return abs(p - b);</pre>
  return line_dist(p, a, b);
```

#### Wielokaty 5.2

ConvexHull.h

Opis: Otoczka wypukła w kierunku CCW.

Czas:  $\mathcal{O}(n \log n)$ 

```
vector<P> convex_hull(vector<P> pts) {
 if (sz(pts) <= 1) return pts;</pre>
 sort(all(pts));
 vector<P> h(sz(pts) + 1);
 int s = 0, t = 0;
 for (int it = 2; it--; s = --t, reverse(all(pts)))
   for (P p : pts) {
      while (t >= s + 2 \& \&
             sgn(cross(h[t - 2], h[t - 1], p)) \le 0) t--;
     h[t++] = p;
 return {h.begin(), h.begin() + t - (t == 2 && h[0] == h[1])};
```