

- 1 Contest
- 2 Struktury danych
- 3 Grafy
- 4 Matma
- 5 Geometria

Contest (1)

sol.cpp

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;

#ifdef LOCAL
auto& operator<<(auto&, pair<auto, auto>);
auto& operator<<(auto& o, auto x) {
    o << '{';
    for (int i = 0; auto y : x) o << ", " + !i++ * 2 << y;
    return o << '}' ;
}
auto& operator<<(auto& o, pair<auto, auto> x) {
    return o << '(' << x.first << ", " << x.second << ')';
}
void __print(auto... x) { ((cerr << ' ' << x), ...) << endl; }
#define debug(x...) cerr << "[" #x "]:", __print(x)
#else
#define debug(...) 2137
#endif

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);
}
```

.vimrc

```
set nu expandtab tabstop=2 shiftwidth=2 autoindent
syntax on
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hi MatchParen ctermfg=66 ctermbg=234 cterm=underline
nnoremap ; :
nnoremap ; :
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```

Makefile

```
CXXFLAGS=-std=c++20 -Wall -Wextra -Wshadow
```

```
sol: sol.cpp
    g++ $(CXXFLAGS) -fsanitize=address,undefined -g -DLOCAL \
        sol.cpp -o sol
```

```
fast: sol.cpp
    g++ $(CXXFLAGS) -O2 sol.cpp -o fast
```

test.sh

```
#!/bin/bash

for ((i=1;i>0;i++)) do
    echo "$i"
    echo "$i" | ./gen > int
    diff -w <(. /sol < int) <(. /slow < int) || break
done
```

3

Struktury danych (2)

wavelet.cpp

Stosowanie: st – początek, ed – koniec, sst – posortowany początek.
Czas: $\mathcal{O}((n + q) \log n)$

```
struct node {
    int lo, hi;
    vector<int> s;
    node *l = 0, *r = 0;
    node(auto st, auto ed, auto sst) {
        int n = ed - st;
        lo = sst[0];
        hi = sst[n - 1] + 1;
        if (lo + 1 < hi) {
            int mid = sst[n / 2];
            if (mid == sst[0]) mid = *upper_bound(sst, sst + n, mid);
            s.reserve(n + 1);
            s.push_back(0);
            for (auto it = st; it != ed; it++) {
                s.push_back(s.back() + (*it < mid));
            }
            auto k = stable_partition(st, ed, [&](int x) {
                return x < mid;
            });
            auto sm = lower_bound(sst, sst + n, mid);
            if (k != st) l = new node(st, k, sst);
            if (k != ed) r = new node(k, ed, sm);
        }
    }
    int kth(int a, int b, int k) {
        if (lo + 1 == hi) return lo;
        int x = s[a], y = s[b];
        return k < y - x ? l->kth(x, y, k)
            : r->kth(a - x, b - y, k - (y - x));
    }
    int count(int a, int b, int k) {
        if (lo >= k) return 0;
        if (hi <= k) return b - a;
        int x = s[a], y = s[b];
        return (l ? l->count(x, y, k) : 0) +
            (r ? r->count(a - x, b - y, k) : 0);
    }
    int freq(int a, int b, int k) {
        if (k < lo || hi <= k) return 0;
        if (lo + 1 == hi) return b - a;
        int x = s[a], y = s[b];
        return (l ? l->freq(x, y, k) : 0) +
            (r ? r->freq(a - x, b - y, k) : 0);
    }
};
```

pbds.cpp

Stosowanie: s.find_by_order(k) i s.order_of_key(k).
Czas: $\mathcal{O}(\log n)$

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
```

```
using namespace __gnu_pbds;
```

```
template <typename T>
using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
```

treap.cpp

Czas: $\mathcal{O}(\log n)$

```
mt19937_64 rng(2137);
struct node {
    int val, sz = 1;
    uint64_t pr;
    node *l = 0, *r = 0;
    node(int x) {
        val = x;
        pr = rng();
    }
    void pull() {
        sz = 1 + size(l) + size(r);
    }
    friend int size(node* a) {
        return a ? a->sz : 0;
    }
    friend pair<node*, node*> split(node* a, int k) {
        if (!a) return {0, 0};
        if (k <= size(a->l)) {
            auto [la, lb] = split(a->l, k);
            a->l = lb;
            a->pull();
            return {la, a};
        } else {
            auto [ra, rb] = split(a->r, k - size(a->l) - 1);
            a->r = ra;
            a->pull();
            return {a, rb};
        }
    }
    friend node* merge(node* a, node* b) {
        if (!a || !b) return a ? a : b;
        if (a->pr > b->pr) {
            a->r = merge(a->r, b);
            a->pull();
            return a;
        } else {
            b->l = merge(a, b->l);
            b->pull();
            return b;
        }
    }
};
```

Grafy (3)

3.1 Przepływy

dinic.cpp

Czas: $\mathcal{O}(nm \log U)$

```
struct dinic {
    struct edge {
        int to, rev;
        int cap;
    };
    int n;
```

```

vector<vector<edge>> adj;
vector<int> q, lvl, it;
dinic(int _n) {
    n = _n;
    adj.resize(n);
    q.reserve(n);
    lvl.resize(n);
    it.resize(n);
}
void add_edge(int u, int v, int cap) {
    int i = ssize(adj[u]), j = ssize(adj[v]) + (u == v);
    adj[u].push_back({v, j, cap});
    adj[v].push_back({u, i, 0});
}
bool bfs(int s, int t, int r) {
    q.clear();
    lvl.assign(n, -1);
    lvl[s] = 0;
    q.push_back(s);
    for (int i = 0; i < ssize(q); i++) {
        int u = q[i];
        for (edge& e : adj[u]) {
            if (e.cap >= r && lvl[e.to] == -1) {
                lvl[e.to] = lvl[u] + 1;
                q.push_back(e.to);
                if (e.to == t) return true;
            }
        }
    }
    return false;
}
ll dfs(int u, int t, ll cap) {
    if (u == t) return cap;
    ll f = 0;
    for (int& i = it[u]; i < ssize(adj[u]); i++) {
        edge& e = adj[u][i];
        if (e.cap > 0 && lvl[u] + 1 == lvl[e.to]) {
            ll add = dfs(e.to, t, min(cap - f, (ll)e.cap));
            e.cap -= add;
            adj[e.to][e.rev].cap += add;
            f += add;
        }
        if (f == cap) return f;
    }
    lvl[u] = -1;
    return f;
}
ll flow(int s, int t, ll cap) {
    ll f = 0;
    for (int i = 29; i >= 0; i--) {
        while (f < cap && bfs(s, t, 1 << i)) {
            it.assign(n, 0);
            f += dfs(s, t, cap - f);
        }
    }
    return f;
}
};

```

mcmf.cpp

Stosowanie: Jeżeli są ujemne krawędzie, przed pusczeniem flow w dst trzeba policzyć najkrótsze ścieżki z s i puścić reduce(t).

Czas: $\mathcal{O}(Fm \log n)$

```

#include <ext/pb_ds/priority_queue.hpp>
ll INF64 = 2e18;
struct MCMF {
    struct edge {
        int to, rev;

```

```

        int cap;
        ll cost;
    };
    struct cmp {
        bool operator() (const auto& l, const auto& r) const {
            return l.second > r.second;
        }
    };
    int n;
    vector<vector<edge>> adj;
    vector<ll> dst;
    ll c = 0;
    __gnu_pbds::priority_queue<pair<int, ll>, cmp> q;
    vector<decltype(q)::point_iterator> its;
    vector<int> id;
    MCMF(int _n) {
        n = _n;
        adj.resize(n);
        id.resize(n);
    }
    void add_edge(int u, int v, int cap, int cost) {
        int i = ssize(adj[u]), j = ssize(adj[v]) + (u == v);
        adj[u].push_back({v, j, cap, cost});
        adj[v].push_back({u, i, 0, -cost});
    }
    void reduce(int t) {
        for (int i = 0; i < n; i++) {
            for (edge& e : adj[i]) {
                if (dst[i] != INF64 && dst[e.to] != INF64) {
                    e.cost += dst[i] - dst[e.to];
                }
            }
        }
        c += dst[t];
    }
    bool dijkstra(int s, int t) {
        dst.assign(n, INF64);
        its.assign(n, q.end());
        dst[s] = 0;
        q.push({s, 0});
        while (!q.empty()) {
            int u = q.top().first;
            q.pop();
            for (edge& e : adj[u]) {
                if (e.cap > 0) {
                    ll d = dst[u] + e.cost;
                    if (d < dst[e.to]) {
                        dst[e.to] = d;
                        if (its[e.to] == q.end()) {
                            its[e.to] = q.push({e.to, dst[e.to]});
                        } else {
                            q.modify(its[e.to], {e.to, dst[e.to]});
                        }
                        id[e.to] = e.rev;
                    }
                }
            }
        }
        reduce(t);
        return dst[t] != INF64;
    }
}
pair<ll, ll> flow(int s, int t, ll cap) {
    ll ff = 0;
    ll cc = 0;
    while (ff < cap && dijkstra(s, t)) {
        ll f = cap - ff;
        for (int i = t; i != s;) {
            edge& e = adj[i][id[i]];
            f = min(f, (ll)adj[e.to][e.rev].cap);

```

```

            i = e.to;
        }
        for (int i = t; i != s;) {
            edge& e = adj[i][id[i]];
            e.cap += f;
            adj[e.to][e.rev].cap -= f;
            i = e.to;
        }
        ff += f;
        cc += f * c;
    }
    return {ff, cc};
}
};

```

3.1.1 Przepływy z wymaganiami

Szukamy przepływu $\leq F$ takiego, że $f_i \geq d_i$ dla każdej krawędzi. Tworzymy nowe źródło s' i ujście t' . Następnie dodajemy krawędzie

- (u_i, t', d_i) , (s', v_i, d_i) , $(u_i, v_i, c_i - d_i)$ zamiast (u_i, v_i, c_i, d_i)
- (t, s, F)

Przepływ spełnia wymagania jeżeli maksymalnie wypełnia wszystkie krawędzie s' .

3.2 Grafy dwudzielne

matching.cpp

Czas: $\mathcal{O}(m\sqrt{n})$

```

struct matching {
    int n, m;
    vector<vector<int>> adj;
    vector<int> pb, pa;
    vector<int> lvl, it;
    matching(int _n, int _m) {
        n = _n;
        m = _m;
        adj.resize(n);
        pb.resize(n, -1);
        pa.resize(m, -1);
        it.resize(n);
    }
    void add_edge(int u, int v) {
        adj[u].push_back(v);
    }
    bool bfs() {
        bool res = false;
        lvl.assign(n, -1);
        queue<int> q;
        for (int i = 0; i < n; i++) {
            if (pb[i] == -1) {
                q.push(i);
                lvl[i] = 0;
            }
        }
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (int j : adj[u]) {
                if (pa[j] == -1) {
                    res = true;
                } else if (lvl[pa[j]] == -1) {
                    lvl[pa[j]] = lvl[u] + 1;

```

```

        q.push(pa[j]);
    }
}
return res;
}
bool dfs(int u) {
    for (auto& i = it[u]; i < ssize(adj[u]); i++) {
        int v = adj[u][i];
        if (pa[v] == -1 ||
            (lvl[pa[v]] == lvl[u] + 1 && dfs(pa[v]))) {
            pb[u] = v;
            pa[v] = u;
            return true;
        }
    }
    return false;
}
int match() {
    int ans = 0;
    while (bfs()) {
        it.assign(n, 0);
        for (int i = 0; i < n; i++) {
            if (pb[i] == -1 && dfs(i)) ans++;
        }
    }
    return ans;
}
};

```

3.2.1 Rozszerzone twierdzenie Königa

W grafie dwudzielnym zachodzi

- $nk = pw$
- $nk + pk = n$
- $pw + nw = n$

oraz

- pw to zbiór wierzchołków na brzegu min-cut
- nw to dopełnienie pw
- pk to nk z dodanymi pojedynczymi krawędziami każdego nieskojarzonego wierzchołka

3.3 Grafy skierowane

scc.cpp

Czas: $\mathcal{O}(n + m)$

```

struct SCC {
    int n, cnt = 0;
    vector<vector<int>> adj;
    vector<int> p, low, in;
    stack<int> st;
    int tour = 0;
    SCC(int _n) {
        n = _n;
        adj.resize(n);
        p.resize(n, -1);
        low.resize(n);
        in.resize(n, -1);
    }
    void add_edge(int u, int v) {
        adj[u].push_back(v);
    }
}

```

```

void dfs(int u) {
    low[u] = in[u] = tour++;
    st.push(u);
    for (int v : adj[u]) {
        if (in[v] == -1) {
            dfs(v);
            low[u] = min(low[u], low[v]);
        } else {
            low[u] = min(low[u], in[v]);
        }
    }
    if (low[u] == in[u]) {
        int v = -1;
        do {
            v = st.top();
            st.pop();
            in[v] = n;
            p[v] = cnt;
        } while (v != u);
        cnt++;
    }
}
void build() {
    for (int i = 0; i < n; ++i) {
        if (in[i] == -1) dfs(i);
    }
    for (int i = 0; i < n; i++) p[i] = cnt - 1 - p[i];
}
};

```

Matma (4)

ntt.cpp

Stosowanie: Liczby NTT-pierwsze: $(998244353, 3) - 2^{23}$, $(754974721, 11) - 2^{24}$, $(167772161, 3) - 2^{25}$, $(469762049, 3) - 2^{26}$.

Czas: $\mathcal{O}((n + m) \log(n + m))$

```

const int ROOT = 3;
void ntt(vector<mint>& a) {
    int n = ssize(a), d = __lg(n);
    vector<mint> w(n);
    mint ww = 1, r = mint(ROOT).pow((MOD - 1) / n);
    for (int i = 0; i < n / 2; i++) {
        w[i + n / 2] = ww;
        ww *= r;
    }
    for (int i = n / 2 - 1; i > 0; i--) w[i] = w[2 * i];
    vector<int> rev(n);
    for (int i = 0; i < n; i++) {
        rev[i] = (rev[i >> 1] | ((i & 1) << d)) >> 1;
        if (i < rev[i]) swap(a[i], a[rev[i]]);
    }
    for (int i = 1; i < n; i *= 2) {
        for (int j = 0; j < n; j += 2 * i) {
            for (int k = 0; k < i; k++) {
                mint z = w[i + k] * a[j + k + i];
                a[j + k + i] = a[j + k] - z;
                a[j + k] += z;
            }
        }
    }
}
vector<mint> conv(vector<mint> a, vector<mint> b) {
    int n = 1, s = ssize(a) + ssize(b) - 1;
    while (n < s) n *= 2;
    a.resize(n);
}

```

```

b.resize(n);
ntt(a);
ntt(b);
for (int i = 0; i < n; i++) a[i] *= b[i];
ntt(a);
reverse(a.begin() + 1, a.end());
a.resize(s);
mint inv = mint(n).inv();
for (int i = 0; i < s; i++) a[i] *= inv;
return a;
}

```

Geometria (5)

tangents.cpp

Stosowanie: Wielokąt musi być CCW i $n \geq 3$. Zwraca najbliższe punkty styczne różne od a .

Czas: $\mathcal{O}(\log n)$

```

pair<pt, pt> tangents(const vector<pt>& p, pt a) {
    int n = ssize(p);
    pt t[2];
    for (int it = 0; it < 2; it++) {
        auto dir = [&](int i) {
            pt u = p[i] - a;
            pt v = p[i < n - 1 ? i + 1 : 0] - a;
            ll c = cross(u, v);
            if (c != 0) return c < 0;
            if (dot(u, v) > 0) return norm(u) > norm(v);
            return true;
        };
        auto dirx = [&](int i) { return dir(i) ^ it; };
        if (dirx(0) == 1 && dirx(n - 1) == 0) {
            t[it] = p[0];
            continue;
        }
        int s[2] = {0, n - 1};
        while (s[1] - s[0] > 2) {
            int mid = (s[0] + s[1]) / 2;
            int x = dirx(mid);
            if (dirx(s[x ^ 1]) == (x ^ 1)) {
                s[x] = mid;
            } else {
                ((cross(p[mid] - a, p[s[1]] - a) < 0) ^ it
                 ? s[x]
                 : s[x ^ 1]) = mid;
            }
        }
        t[it] = dirx(s[0] + 1) == 0 ? p[s[0] + 2] : p[s[0] + 1];
    }
    return {t[0], t[1]};
}

```