Using Venn diagrams to calculate probability of joint events

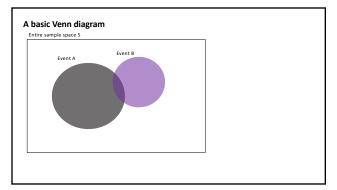
Corinne Riddell September 23, 2022

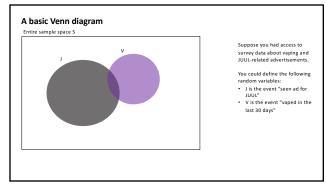
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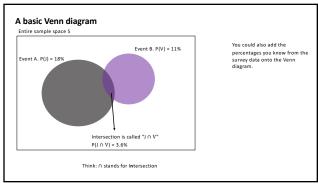
Learning objectives for today

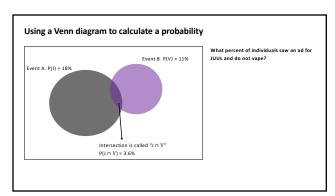
- How to make a Venn diagram
- How to use a Venn diagram to compute probabilities
- Determine whether two events are independent or dependent
- Conditional probability
- \bullet General addition rule for probability
- General multiplication rule for probability

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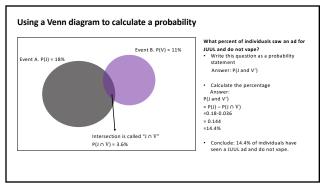


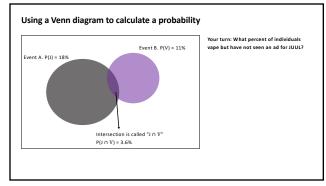


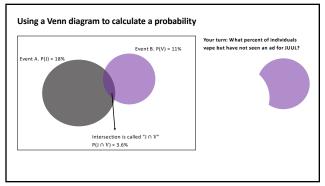


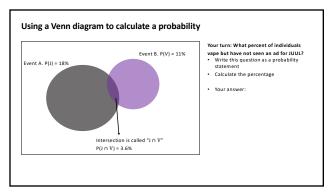


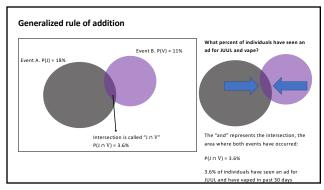
Using a Venn diagram to calculate a probability Event A. P(J) = 18% Event A. P(J) = 18% Using a Venn diagram to calculate a probability Event A. P(J) = 18% Intersection is called "J \(\text{V}" \) P(J \(\text{V} \text{V}) = 3.6%

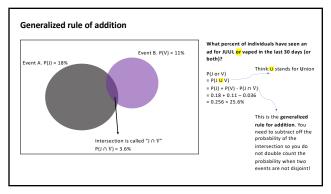


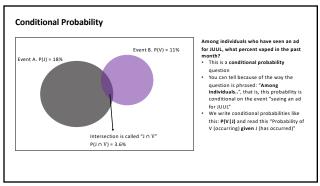


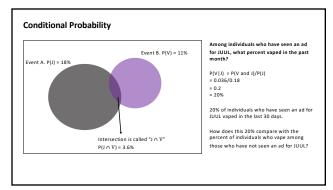


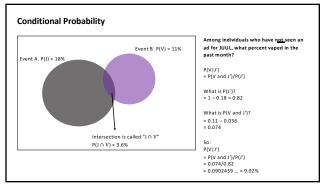


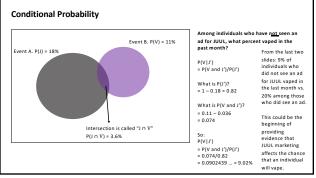


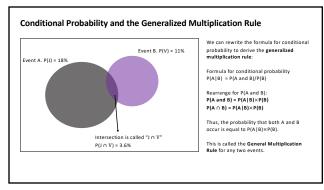


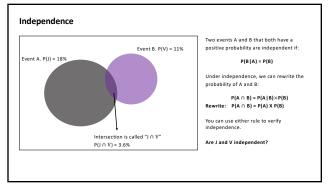


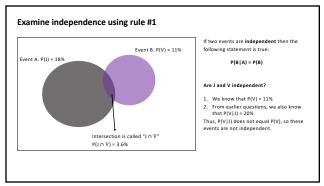












	Event B. P(V) = 11%	If two events are independent then the following statement is true:
Event A. P(J) = 18%		$P(A \cap B) = P(A) \times P(B)$
		Are J and V independent?
		1. P(J ∩ V) = 3.6%
		2. P(J) X P(V) = 0.18×0.11 = 0.0198 = 1.98
		Since these quantities are not equal, thes
	Intersection is called "J ∩ V"	two events are not independent.
	P(J ∩ V) = 3.6%	

Additional slides on independence

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Independence

 What sorts of events are independent? Two events are independent if knowing that one event occurred does not change the probability that the other occurred

Exam	pl	e	1a

- \bullet Down syndrome is a genetic disorder caused when abnormal cell division results in an extra full or partial copy of chromosome 21. 1
- \bullet The largest risk factor for having a child with Down syndrome is advanced maternal age. 1
- Suppose that Martha is 40 and her baby has been diagnosed with Down syndrome. Martha's best friend Jane, also 40, is hoping to conceive. Is her baby's risk of Down syndrome independent of Martha's baby's risk?

Reference: https://www.mayoclinic.org/diseases-conditions/down-syndrome/symptoms-causes/syc-20355977

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Example 1b

 The risk of having a baby with Down syndrome is 1/100 among 40 year olds. Suppose that Jenny and Samantha are two 40-year old women. What is the probability that they both have babies with Down syndrome?

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Example 2a

- \bullet Breast Cancer is the most common cancer diagnosed in women in the US.
- If a woman's mother, sister, or daughter was diagnosed with breast cancer, her estimated risk of breast cancer is doubled (compared to a woman whose mother/sister/daughter has not been diagnosed).¹
- Jacqueline was diagnosed with breast cancer. Is her daughter's chance of developing breast cancer independent or dependent on Jacqueline's diagnosis?

Reference. https://www.mayoclinic.org/diseases-conditions/breast-cancer/symptoms-causes/syc-20352470

Example 2b

- A white woman aged 40 who had her first period at age 12 and first child at age 27. Her mother had Breast Cancer. Given this information, she has an estimated 5-year risk of breast cancer of 1.1% and lifetime risk of breast cancer of 18.8%.
- Had the woman's mother not had breast cancer, here 1-year risk would have been 0.6% and lifetime risk 11.1%. Based on these risk estimates, are the events "mother has breast cancer" and "daughter has breast cancer" independent? Why?
- (See <u>here</u> to calculate breast cancer risk under a variety of settings. For the above risk estimates I set the variables as specified and selected "Unknown" for having the BRCA1/2 gene, and ever having a breast biopsy. I selected "No" for every having a medical history of any breast cancer.)