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ENME 351

SP4 – Modal Analysis

In this project you will determine the equations of motion of a two degree of freedom system which consists of two masses and 3 springs as shown in the diagram. In addition, you will solve the equations for 3 cases given below.

- 1. Draw the detailed free body diagrams of the masses of the system. Ignore gravity!
- 2. Using the free body diagrams, determine the equations of motion for the system.
- 3. For each case, what are the natural frequencies and the corresponding mode shapes?
- 4. Obtain the exact mathematical solution to these equations for the 3 cases defined below. In each case, the initial conditions are that m_1 is initially displaced by on centimeter vertically and that its velocity is zero. Also, m_2 has no initial displacement or velocity.

A.
$$m_1 = m_2 = 1 \text{ kg}$$
, $k_1 = k_2 = k = 10 \text{ N/m}$

B.
$$m_1 = 10 m_2$$
, $m_2 = 1 kg$, $k_1 = k_2 = k = 10 N/m$

C.
$$m_1 = m_2 = 1 \text{ kg}$$
, $k_1 = k_2 = 10 \text{ N/m}$, $k = 100 \text{ N/m}$

