

Vertical AI-driven Scientific Discovery

Anonymous submission

Abstract

Automating scientific discovery has been a grand goal of Artificial Intelligence (AI) and will bring tremendous societal impact if it succeeds. Despite exciting progress, most endeavor in learning scientific equations from experiment data focuses on the *horizontal* discovery paths, i.e., they directly search for the best equation in the full hypothesis space. Horizontal paths are challenging because of the associated exponentially large search space. Our work explores an alternative *vertical* path, which builds scientific equations in an incremental way, starting from one that models data in *control variable experiments* in which most variables are held as constants. It then extends expressions learned in previous generations via adding new independent variables, using new control variable experiments in which these variables are allowed to vary. This vertical path was motivated by human scientific discovery processes. Experimentally, we demonstrate that such vertical discovery paths expedite symbolic regression. It also improves learning physics models describing nano-structure evolution in computational materials science.

Introduction

Automating scientific discovery has been a grand goal of Artificial Intelligence (AI) dating back its founders (Herbert Simon et. al. (Langley et al. 1987; Kulkarni and Simon 1988; Wang et al. 2022)) but remains a holy grail. The underlying societal impact is immense because of its multiplier effect. Indeed, much effort has been made, especially in symbolic equation regression, including search-based methods (Langley 1981; Lenat 1977), genetic programming (Schmidt and Lipson 2009; Virgolin, Alderliesten, and Bosman 2019; Razavi and Gamazon 2022; He et al. 2022), reinforcement learning (Petersen et al. 2021; Scavuzzo et al. 2022; Mundhenk et al. 2021; Petersen et al. 2021), deep function approximation (McConaghy 2011; Chen, Luo, and Jiang 2017; Raissi, Yazdani, and Karniadakis 2020; Raissi, Perdikaris, and Karniadakis 2019; Liu and Tegmark 2021; Xue et al. 2021a; Chen et al. 2018; Jumper et al. 2021; Brunton, Proctor, and Kutz 2016), integrated systems (Valdés-Pérez 1994; King et al. 2004, 2009; Lintott et al. 2008), or simply yet effectively, collecting big datasets (Lintott et al. 2008; Kelling et al. 2012). Most endeavor focuses on *horizontal* discovery paths, i.e., they directly search for the best equation in the full hypothesis space involving all independent variables

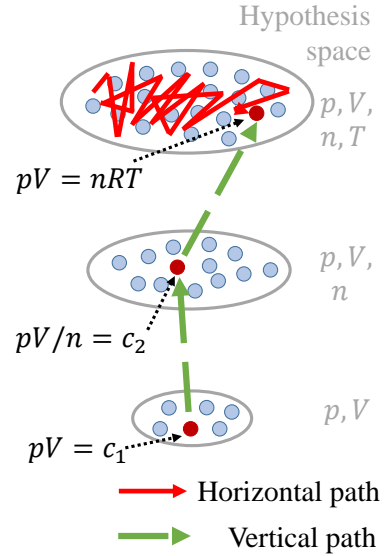


Figure 1: Vertical paths further scale up AI-driven scientific discovery.

(red path in Figure 1). The horizontal search can be challenging because of the exponentially large space. After the conventional wisdom of training with larger models and more data has been stretched to its extremity (e.g., GPT-4), what is the next paradigm-changing idea?

Interestingly, the *vertical* paths have been largely overlooked in AI. To discover the ideal gas law $pV = nRT$, scientists first held n (gas amount) and T (temperature) as constants and find p (pressure) is inversely proportional to V (volume). They then studied the relationship between pV and n, T . This led to a vertical discovery path (green path in Figure 1). The first few steps of a vertical path can be significantly cheaper than the horizontal path, because the searches are in reduced spaces involving a small number of independent variables. As a result, vertical discovery has the potential to supercharge state-of-the-art approaches in modeling complex scientific phenomena with more interlocking contributing factors or processes than what current approaches can handle.

This paper demonstrates the power of vertical scientific

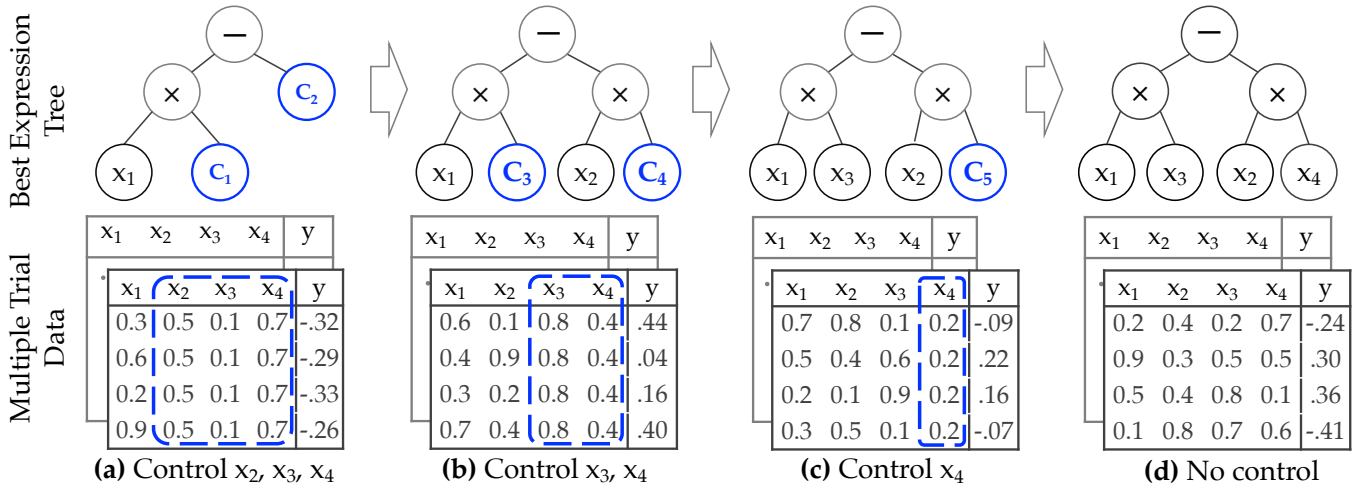


Figure 3: Running example of CVGP. **(a)** Initially, a reduced-form equation $\phi' = C_1x_1 - C_2$ is found via fitting control variable data in which x_2, x_3, x_4 are held as constants and only x_1 is allowed to vary. **(b)** This equation is expanded to $C_3x_1 - C_4x_2$ in the second stage via fitting the data in which only x_3, x_4 are held as constants. **(c,d)** This process continues until the ground-truth equation $\phi = x_1x_3 - x_2x_4$ is found. The data generated for control variable experiment trials in each stage are shown at the bottom.

periment. Figure 2 (a) depicts a symbolic regression task where one needs to find a symbolic expression $y = f(x)$ which best maps the input x to the output y . The author ran this experiment in front of hundreds of undergraduate, graduate students, and a few faculty members. Nobody was able to discover the correct equation given the data in (a). However, when the author controlled the value of x_2 in (b) and (c), a majority of the audience were able to identify the equations in both cases. A little bit of additional thinking combining these two equations yields the ground-truth equation in (d). Clearly, control variable experiments in (b) and (c) helped the audience navigate the regression task. This controlled experiment depicts the essence of vertical scientific discovery.

Symbolic Regression via Control Variable Genetic Programming

Our recently proposed **Control Variable Genetic Programming (CVGP)** (Jiang and Xue 2023) implements the vertical scientific discovery process using Genetic Programming (GP) for symbolic regression over many independent variables. The key insight of CVGP is to learn from *a customized set of control variable experiments*; in other words, the experiment data collection adapts to the learning process. This is in contrast to the current learning paradigm of most symbolic regression approaches, where they learn from a fixed dataset collected a priori.

In CVGP, first, we hold all independent variables except for one as constants and learn an expression that maps the single variable to the dependent variable using GP. GP maintains a pool of candidate expressions and improves the fitness of these equations via mating, mutating, and selection over several generations. Mapping the dependence of one independent variable is easy. Hence GP can usually recover

the ground-truth reduced-form equation. Then, CVGP frees one independent variable at a time. In each iteration, GP is used to modify the equations learned in previous generations to incorporate the new independent variable, via mating, mutating, and selection. Such a procedure repeats until all the independent variables have been incorporated into the symbolic expression. See figure 3 for the high-level idea of algorithm execution. Theoretically, in the original paper we show CVGP as an incremental builder can reduce the exponential-sized search space for candidate expressions into a polynomial one when fitting a class of symbolic expressions. Experimentally, we show CVGP outperforms a number of state-of-the-art approaches on symbolic regression over multiple independent variables (see Table 1).

Vertical Scientific Discovery in Modeling Nano-structure Evolution in Materials Science

We intend to apply the idea of vertical scientific discovery in learning nano-scale defect evolution for material under extreme conditions. Nano-scale crystalline defects can appear in different forms in these materials. Extreme environments of heat and irradiation can cause these defects to evolve in size and position. As shown in the left panel of the figure above, void shaped defects are captured by transmission electron microscope (TEM) cameras during in-situ radiation experiments. These defects appear in round shapes, and drift in position as demonstrated by the change of angles to respectively, as time progresses. They also change size. These changes can affect the physical and mechanical properties of the material. For this reason, characterizing these defects is essential in designing new materials that can resist adverse environments. Collaborating with materials scientists, we have been analyzing terabytes of in-situ TEM videos of this type and have already made scientific discoveries (Sima

Table 1: Median (50%) and 75%-quantile Normalized Mean Squared Error (NMSE) values of the symbolic expressions found by all the algorithms on several *noisy* benchmark datasets (Gaussian noise with zero mean and standard deviation 0.1 is added). Our CVGP finds symbolic expressions with the smallest NMSEs.

| Dataset configs | CVGP (ours) | | GP | | DSR | | PQT | | VPG | | GPMeld | |
|--|--------------|--------------|--------------|--------------|--------|--------|--------|---------|--------|--------|--------|--------|
| | 50% | 75% | 50% | 75% | 50% | 75% | 50% | 75% | 50% | 75% | 50% | 75% |
| (4,4,6) | 0.036 | 0.088 | 0.038 | 0.108 | 1.163 | 3.714 | 1.016 | 1.122 | 1.087 | 1.275 | 1.058 | 1.374 |
| (5,5,5) | 0.076 | 0.126 | 0.075 | 0.102 | 1.028 | 2.270 | 1.983 | 4.637 | 1.075 | 2.811 | 1.479 | 2.855 |
| (5,5,8) | 0.061 | 0.118 | 0.121 | 0.186 | 1.004 | 1.013 | 1.005 | 1.006 | 1.002 | 1.009 | 1.108 | 2.399 |
| (6,6,8) | 0.098 | 0.144 | 0.104 | 0.167 | 1.006 | 1.027 | 1.006 | 1.020 | 1.009 | 1.066 | 1.035 | 2.671 |
| (6,6,10) | 0.055 | 0.097 | 0.074 | 0.132 | 1.003 | 1.009 | 1.005 | 1.008 | 1.004 | 1.015 | 1.021 | 1.126 |
| (a) Datasets containing operators $\{\sin, \cos, \text{inv}, +, -, \times\}$. | | | | | | | | | | | | |
| (3,2,2) | 0.098 | 0.165 | 0.108 | 0.425 | 0.350 | 0.713 | 0.351 | 1.831 | 0.439 | 0.581 | 0.102 | 0.597 |
| (4,4,6) | 0.078 | 0.121 | 0.120 | 0.305 | 7.056 | 16.321 | 5.093 | 19.429 | 2.458 | 13.762 | 2.225 | 3.754 |
| (5,5,5) | 0.067 | 0.230 | 0.091 | 0.313 | 32.45 | 234.31 | 36.797 | 229.529 | 14.435 | 46.191 | 28.440 | 421.63 |
| (5,5,8) | 0.113 | 0.207 | 0.119 | 0.388 | 195.22 | 573.33 | 449.83 | 565.69 | 206.06 | 629.41 | 363.79 | 666.57 |
| (6,6,8) | 0.170 | 0.481 | 0.186 | 0.727 | 1.752 | 3.824 | 4.887 | 15.248 | 2.396 | 7.051 | 1.478 | 6.271 |
| (6,6,10) | 0.161 | 0.251 | 0.312 | 0.342 | 11.678 | 26.941 | 5.667 | 24.042 | 7.398 | 25.156 | 11.513 | 28.439 |
| (b) Datasets containing operators $\{\sin, \cos, +, -, \times\}$. | | | | | | | | | | | | |
| (3,2,2) | 0.049 | 0.113 | 0.023 | 0.166 | 0.663 | 2.773 | 1.002 | 1.992 | 0.969 | 1.310 | 0.413 | 2.510 |
| (4,4,6) | 0.141 | 0.220 | 0.238 | 0.662 | 1.031 | 1.051 | 1.297 | 1.463 | 1.051 | 1.774 | 1.093 | 1.769 |
| (5,5,5) | 0.157 | 0.438 | 0.195 | 0.337 | 1.098 | 3.617 | 1.018 | 5.296 | 1.012 | 1.27 | 1.036 | 3.617 |
| (5,5,8) | 0.122 | 0.153 | 0.166 | 0.186 | 1.009 | 1.103 | 1.017 | 1.429 | 1.007 | 1.132 | 1.07 | 2.904 |
| (6,6,8) | 0.209 | 0.590 | 0.209 | 0.646 | 1.003 | 1.153 | 1.047 | 1.134 | 1.059 | 1.302 | 1.029 | 3.365 |
| (6,6,10) | 0.139 | 0.232 | 0.073 | 0.159 | 1.654 | 3.408 | 1.027 | 1.069 | 1.009 | 1.654 | 1.445 | 2.106 |
| (c) Datasets containing operators $\{\sin, \cos, \text{inv}, +, -, \times\}$. | | | | | | | | | | | | |

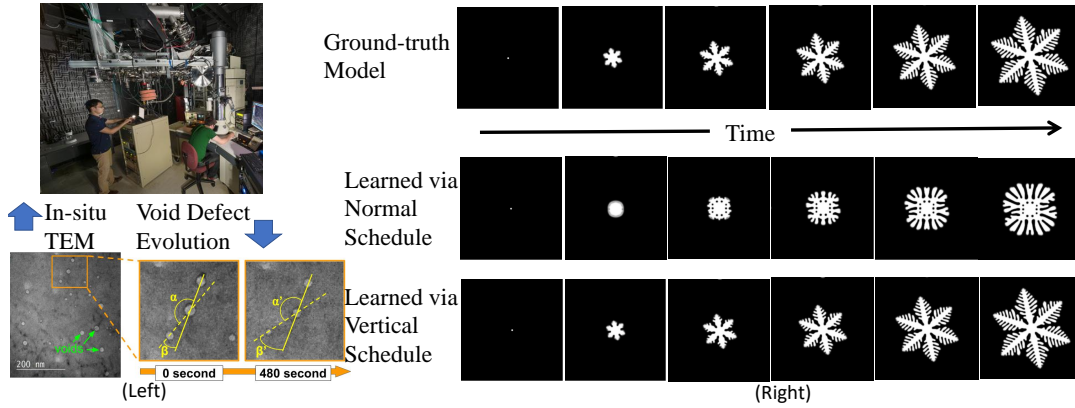


Figure 4: Vertical scientific discovery pipeline can improve learning of physics models behind nano-structure evolution. Left: The Intermediate Voltage Electron Microscopy (IVEM) – Tandem Facility at the Argonne National Laboratory which provides in-situ TEM data. Source: anl.gov. (top) and sample images captured during in-situ radiation experiments (bottom). Right: Learned physics models from vertical scientific discovery pipeline can yield more accurate simulation output close to ground truth compared to baseline approach.

and Xue 2021; Xue et al. 2021b; Nasim et al. 2022, 2023).

As a preliminary study, vertical discovery schedules are used to improve the learning of phase-field models for dendritic solidification. In the vertical schedule, first the learning is concentrated on a subset of model parameters. This is done by feeding the model with designed training data in which the remaining parameters do not affect the dynamics of the PDEs. After this phase, the learning is expanded to all parameters. The right panel of the figure above demonstrate that learning via the vertical schedule is able to identify the correct phase-field model while normal schedules cannot.

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