

**Problem** (Problem 1): Let  $F$  be a finite field with  $q$  elements.

(a) Find the order of the general linear group

$$\mathrm{GL}_n(F) = \{A \in \mathrm{Mat}_n(F) \mid \det(A) \neq 0\}.$$

(b) Find the order of the special linear group

$$\mathrm{SL}_n(F) = \{A \in \mathrm{Mat}_n(F) \mid \det(A) = 1\}.$$