

Problem (Problem 1): Let \mathbb{F} be a finite field with q elements.

- (a) Find the order of the general linear group

$$\mathrm{GL}_n(\mathbb{F}) = \{ A \in \mathrm{Mat}_n(\mathbb{F}) \mid \det(A) \neq 0 \}.$$

- (b) Find the order of the special linear group

$$\mathrm{SL}_n(\mathbb{F}) = \{ A \in \mathrm{Mat}_n(\mathbb{F}) \mid \det(A) = 1 \}.$$