

13.2

10:

$$\tan^{-1}\left(\frac{18}{15}\right) = 50.2^\circ$$

16:

$$\begin{aligned} F' &= -(F_1 + F_2) \\ &= -11\hat{i} + 4\hat{j} \end{aligned}$$

22:

Find vector sum of first two forces:

$$\begin{aligned} \vec{u} &= (70 \cos(80^\circ) + 100 \cos(30^\circ))\hat{i} + (-70 \cos(80^\circ) + 100 \cos(30^\circ))\hat{j} + 0\hat{k} \\ &= 98.8\hat{i} - 18.9\hat{j} + 0\hat{k} \end{aligned}$$

Magnitude of \vec{u} :

$$\begin{aligned} \|\vec{u}\| &= \sqrt{(70 \cos(80^\circ) + 100 \cos(30^\circ))^2 + (-70 \cos(80^\circ) + 100 \cos(30^\circ))^2} \\ &= 100.55 \end{aligned}$$

Magnitude of \hat{k} component:

$$\begin{aligned} a &= \sqrt{(3000)^2 - ((70 \cos(80^\circ) + 100 \cos(30^\circ))^2 + (-70 \cos(80^\circ) + 100 \cos(30^\circ))^2)} \\ &= 2998.3 \\ \vec{v} &= -98.8\hat{i} + 18.9\hat{j} + 2998.3\hat{k} \end{aligned}$$

24:

$$\begin{aligned} \vec{f} &= \frac{2}{3}\vec{w} + \frac{1}{3}\vec{v} \\ &= (79, 79.3, 89, 68.3, 89.3) \end{aligned}$$

13.3

4:

$$(2\hat{i} + 5\hat{k}) \cdot 10\hat{j} = 0$$

6:

$$\begin{aligned} \vec{u} \cdot \vec{w} &= \|\vec{u}\| \|\vec{w}\| \cos(120^\circ) \\ &= -100 \end{aligned}$$

12:

$$\vec{a} \cdot (\vec{c} + \vec{y}) = -2$$

14:

$$(\vec{a} \cdot \vec{y})(\vec{c} \cdot \vec{z}) = 238$$

22:

$$5x + 4y - z = 3$$

24:

$$5x + y - 2z = 3$$

32:

$$\begin{aligned}\theta &= \cos^{-1} \left(\frac{\vec{u} \cdot \vec{v}}{\|\vec{u}\| \|\vec{v}\|} \right) \\ &= 57.9^\circ\end{aligned}$$

44: (a) $\vec{u} = \hat{i} + 2\hat{j} - \hat{k}$
(b)

$$\begin{aligned}\theta &= \cos^{-1} \left(\frac{\vec{u} \cdot \vec{v}}{\|\vec{u}\| \|\vec{v}\|} \right) \\ &= 136.8^\circ\end{aligned}$$

(c) The angle between \vec{v} and the plane is thus 46.8°

54: There are two vectors such that $\vec{a} \cdot \vec{b} = 4$, with $\cos(\theta) = 0.5 \Rightarrow \Theta = 60^\circ$ and $\theta = 300^\circ$

60:

$$\begin{aligned}W &= \vec{F} \cdot \overrightarrow{PQ} \\ &= -6 \text{ J} \\ &= 4.43 \text{ ft-lb}\end{aligned}$$

13.4

2:

$$\vec{v} \times \vec{w} = -\hat{i}$$

4:

$$\vec{v} \cdot \vec{w} = -2\hat{i} + 2\hat{j}$$

10:

$$\begin{aligned}((\hat{i} + \hat{j}) \times \hat{i}) \times \hat{j} &= (\hat{i} \times \hat{i} + \hat{i} \times \hat{j}) \times \hat{j} \\ &= \hat{k} \times \hat{j} \\ &= -\hat{i}\end{aligned}$$

12:

Finding $\vec{a} \times \vec{b}$

$$\begin{aligned}\vec{a} \times \vec{b} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & -1 \\ 1 & -4 & 2 \end{vmatrix} \\ &= -2\hat{i} - 7\hat{j} - 13\hat{k}\end{aligned}$$

Checking $\vec{a} \cdot (\vec{a} \times \vec{b})$:

$$\begin{aligned}\vec{a} \cdot (\vec{a} \times \vec{b}) &= (-2)(3) + (-7)(1) + (-1)(-13) \\ &= 0\end{aligned}$$

Checking that $\vec{b} \cdot (\vec{a} \times \vec{b})$:

$$\begin{aligned}\vec{b} \cdot (\vec{a} \times \vec{b}) &= (-2)(1) + (-4)(-7) + (2)(-13) \\ &= 0\end{aligned}$$

14:

$$(-\hat{i} + \hat{j}) \times (-\hat{j} + \hat{k}) = \hat{i} + \hat{j} + \hat{k}$$

Therefore, the plane is:

$$x + y + z = 1$$

34 (a):

$$(4\hat{i} - \hat{j} + 4\hat{k}) \times (-2\hat{i} - 3\hat{j} + \hat{k}) = 11\hat{i} - 12\hat{j} - 14\hat{k}$$

Therefore, the plane is:

$$11x - 12y - 14z = -45$$

36: $\vec{v} \times \vec{w}$ is parallel to the z axis, as both of its constituent vectors must lie on the xy -plane, so their cross product must be perpendicular to both.

38:

$$\begin{aligned}\|\vec{v} \times \vec{w}\| &= \sqrt{38} \\ \tan \theta &= \frac{\|\vec{v} \times \vec{w}\|}{\vec{v} \cdot \vec{w}} \\ &= \frac{\sqrt{38}}{3}\end{aligned}$$

40: Since $\vec{v} \times (\hat{i} + \hat{j} + \hat{k}) = 0$, \vec{v} is parallel to $(\hat{i} + \hat{j} + \hat{k})$, so $\vec{v} = 2\hat{i} + 2\hat{j} + 2\hat{k}$.

14.1

2:

$$\begin{aligned}f_x(3, 2) &= \lim_{h \rightarrow 0} \frac{\frac{(3+h)^2}{3} - 3}{h} \\ &= \frac{(3+h)^2 - 9}{3h} \\ &= \frac{h^2 + 6h}{3h} &= 2 \\ f_y(3, 2) &= \lim_{k \rightarrow 0} \frac{\frac{9}{3+h} - 3}{h} &= \frac{3h}{(3+h)h} \\ &= 1\end{aligned}$$

4: (a) Change in price as a function of age.

(b) Negative, due to depreciation of the car.

(c) Change in price as a function of original cost.

(d) Positive, because a more originally expensive car will have a higher price at any given age.

10: (a) $f(A) = 10$

(b) Positive

(c) Zero

14: (a) $f(A) = 40$

(b) Negative

(c) Positive

16: • $f_x > 0$

• $f_y > 0$

20: (a) Positive

(b) Negative

(c) Positive

(d) Negative

22:

$$f_x(3, 5) \approx -\frac{2}{3}$$

36: (a)

$$\frac{\partial T}{\partial x} \Big|_{15,20} \approx -\frac{1}{2} \text{ }^\circ\text{C per meter}$$

$$\frac{\partial T}{\partial x} \Big|_{15,20} \approx \frac{1}{2} \text{ }^\circ\text{C per minute}$$

The wall heats up at $\frac{1}{2}$ a degree Celsius per minute, and cools by $\frac{1}{2}$ degree Celsius per meter away from the heat source.

(b)

$$\frac{\partial T}{\partial x} \Big|_{5,12} \approx 1 \text{ }^\circ\text{C per meter}$$

$$\frac{\partial T}{\partial x} \Big|_{5,12} \approx \frac{1}{6} \text{ }^\circ\text{C per minute}$$

The wall heats up at $\frac{1}{6}$ of a degree Celsius per minute, and cools by 1 degree Celsius per meter away from the heat source.