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Problem 1

Problem. Define

$$\mathfrak{sl}_{n}\left(\mathbb{Q}\right) = \left\{X = \left(x_{i,j}\right) \in \operatorname{Mat}_{n}\left(\mathbb{Q}\right) \middle| \operatorname{Tr}\left(X\right) = \sum_{i=1}^{n} x_{i,i} = 0\right\}.$$

Show that $\mathfrak{sl}_n(\mathbb{Q})$ is a \mathbb{Q} -vector space.