Math 212: Homework 8 Avinash lyer

2:

 $\begin{pmatrix} x(t) \\ y(t) \end{pmatrix} = 2 \begin{pmatrix} \cos(t) \\ \sin(t) \end{pmatrix}$ 

 $0 \le t \le \pi/2$ 

10:

$$\begin{pmatrix} x(t) \\ y(t) \\ z(t) \end{pmatrix} = \begin{pmatrix} 5 \\ 5t - 1 \\ 2t + 1 \end{pmatrix}$$

22:

$$\begin{pmatrix} x(t) \\ y(t) \\ z(t) \end{pmatrix} = \begin{pmatrix} 2\cos(t) \\ 2\sin(t) \\ 1 \end{pmatrix}$$

40:

$$\begin{pmatrix} x(t) \\ y(t) \end{pmatrix} = \begin{pmatrix} t^2 \\ t \end{pmatrix}$$

 $1 \le t \le 8$ 

44:

2:

$$\begin{pmatrix} x(t) \\ y(t) \\ z(t) \end{pmatrix} = \begin{pmatrix} t \\ 5\cos(t) \\ 5\sin(t) \end{pmatrix}$$

64:  $L_1$  and  $L_2$  are the same line.

17.2

$$\vec{v}(t) = \begin{pmatrix} 6t \\ 2t \\ -2t \end{pmatrix}$$

$$\vec{a}(t) = \begin{pmatrix} 6 \\ 2 \\ -2 \end{pmatrix}$$

$$\vec{v}(t) = \begin{pmatrix} -3\sin(3t) \\ 5\cos(5t) \end{pmatrix}$$
$$\|\vec{v}(t)\| = \sqrt{9\sin^2(3t) + 25\cos^2(5t)}$$

Math 212: Homework 8 Avinash lyer

12:

$$\vec{v}(t) = \begin{pmatrix} 3\sin(2t) \\ -\sin(t) \\ 2t \end{pmatrix}$$
$$\|\vec{v}(t)\| = \sqrt{9\sin^2(2t) + \sin^2(t) + 4t^2}$$

14:

$$\int_0^{2\pi} \sqrt{9\sin^2(3t) + 25\cos^2(5t)} dt \approx 24.603$$

20:

$$\vec{v}(t) = \begin{pmatrix} -6t^2 - 3\\ 12t^2 + 6\\ 18t^2 + 9 \end{pmatrix}$$
$$\vec{a}(t) = \begin{pmatrix} -12t\\ 24t\\ 36t \end{pmatrix}$$

24:

$$\vec{v}(t) = \begin{pmatrix} 3t^2 - 12\\ 2t + 10 \end{pmatrix}$$

so when  $t=\pm 2$ , the particle is moving parallel to the x-axis, and when t=-5, the particle is moving parallel to the y-axis. As  $t\to +\infty$ ,  $x,y\to +\infty$ , while as  $t\to -\infty$ ,  $x\to -\infty$  and  $y\to +\infty$ 

28: (a)

$$(1+t) + (5+2t) + (-7+t) = 1$$

$$4t - 1 = 1$$

$$t = \frac{1}{2}$$

$$\begin{pmatrix} x \\ y \\ t \end{pmatrix} = \begin{pmatrix} \frac{3}{2} \\ 6 \\ \frac{13}{2} \end{pmatrix}$$

(b)

$$\|\vec{v}\| = \sqrt{1+4+1}$$
$$= \sqrt{6} \text{ m/s}$$

44: I don't know how to do this problem.

17.3

$$\vec{F}(x,y) = \begin{pmatrix} -y \\ 0 \end{pmatrix}$$

Math 212: Homework 8 Avinash Iyer

4:

$$\vec{F}(x,y) = \begin{pmatrix} -y \\ x \end{pmatrix}$$

6:

$$\vec{F}(x,y) = \begin{pmatrix} x \\ y \end{pmatrix}$$

- 8: The vector field is neither parallel to the x-axis nor the y-axis. As x increases, the length remains constant, while as yincreases, the length also increases.
- 10: The vector field is neither parallel to the x-axis nor the y-axis. As x increases and as y increases, the length also increases.

24:

$$\vec{F}(x,y) = \begin{pmatrix} y \\ y \end{pmatrix}$$

$$\vec{F}(x,y) = \begin{pmatrix} x \\ y \end{pmatrix}$$

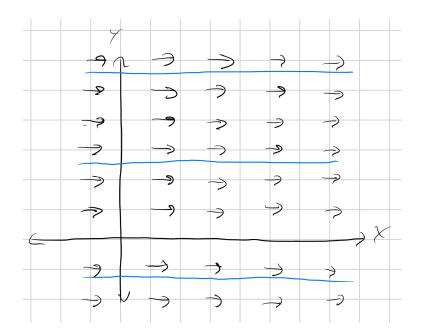
26:

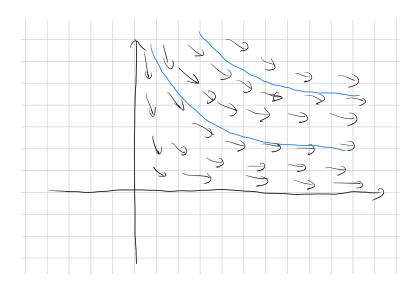
$$\vec{F}(x, y) = \begin{pmatrix} x \\ y \end{pmatrix}$$

- 28: (I) (C)
  - (II) (B)
  - (III)(A)
  - (IV) (D)

$$\vec{F}(x,y) = \begin{pmatrix} x \\ 0 \end{pmatrix}$$

Math 212: Homework 8 Avinash Iyer





$$\begin{pmatrix} x'(t) \\ y'(t) \end{pmatrix} = \begin{pmatrix} x \\ -y \end{pmatrix}$$
$$x'(t) = x(t)$$

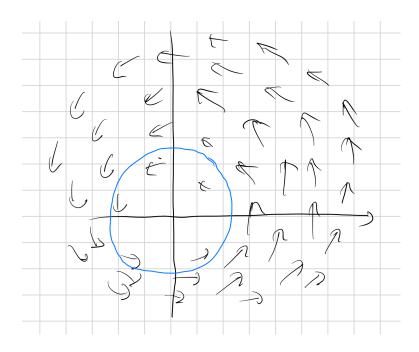
$$\chi'(t) = \chi(t)$$

$$y'(t) = -y(t)$$

$$x'(t) = x_0 e^t$$

$$y'(t) = y_0 e^{-t}$$

Math 212: Homework 8 Avinash Iyer



16:

- (a) (III)
- (b) (l)
- (c) (II)
- (d) (V)
- (e) (VI)
- (f) (IV)

$$\begin{pmatrix} x'(t) \\ y'(t) \end{pmatrix} = \begin{pmatrix} x \\ -y \end{pmatrix}$$
$$\nabla f = \begin{pmatrix} 2x \\ -2y \end{pmatrix}$$
$$\begin{pmatrix} x'(t) \\ y'(t) \end{pmatrix} = \frac{1}{2} \nabla f$$