

Attack of the Tails: Yes, You Really Can Backdoor Federated Learning

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Robustness: an Important Challenge

Applied Machine Learning at Facebook: A Datacenter

Infrastructure Perspective [1]

"Adversaries are constantly searching for new ways to bypass our identifiers"



Fig. 5. Facebook global data center locations as of December 2017.

[1] K. Hazelwood et al., "Applied Machine Learning at Facebook: A Datacenter Infrastructure Perspective," 2018 IEEE International Symposium on High Performance Computer Architecture (HPCA), 2018, pp. 620-629, doi: 10.1109/HPCA.2018.00059.



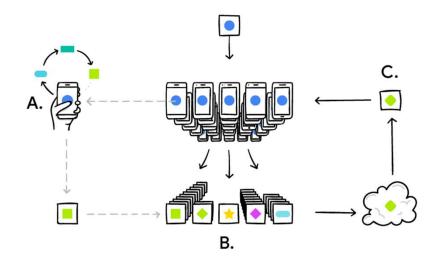


Robustness: an Important Challenge

Advances and Open Problems in Federated Learning [1]

"ML systems can be vulnerable to various kinds of failures."

"federated learning may introduce new attack surfaces at training-time"

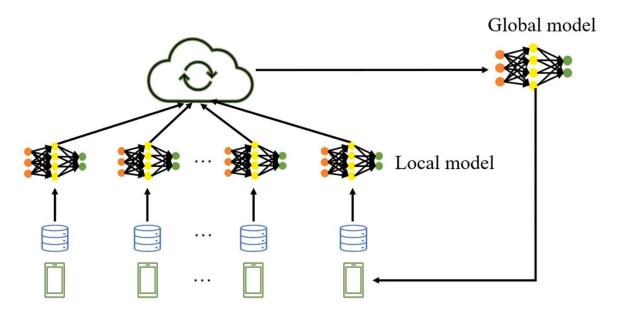


[1] Kairouz P, McMahan H B, Avent B, et al. Advances and open problems in federated learning[J], 2019.





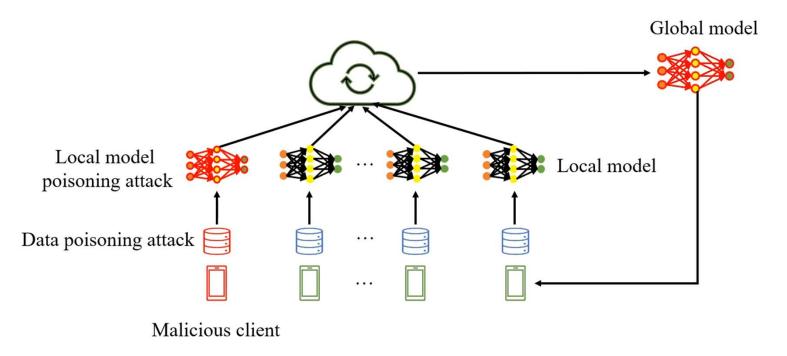
Federated Learning





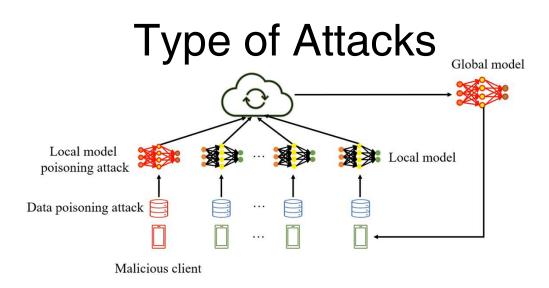


Federated Learning









- Data Poisoning: adversary manipulates data so that local models affect the global model
- Model Poisoning: adversary replaces local model with one that "misbehaves"





How To Backdoor Federated Learning

Eugene Bagdasaryan Andreas Veit Yiqing Hua Deborah Estrin Vitaly Shmatikov Cornell Tech

i) cars with racing stripe



ii) cars painted in green



a) CIFAR backdoor

iii) vertical stripes on background wall







Can You Really Backdoor Federated Learning?

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- Current attacks
 - Do not persist
 - Can be defended by simple norm clipping defenses





Definition

- FL aims to minimize an empirical loss $\sum_{({m x},y)\in\mathcal{D}}\ell({m w};{m x},y)$
- Let $X \sim P_X$. A set of labeled examples $\mathcal{D}_{edge} = \{(\boldsymbol{x}_i, y_i)\}_i$ is called a p-edge-case examples set if

$$P_X(\boldsymbol{x}) \leq p, \ \forall (\boldsymbol{x}, y) \in \mathcal{D}_{edge} \ for \ small \ p > 0$$





- D_{edge} is available to the attackers, their goal:
 - inject a backdoor to the global model so that the global model predicts y_i when the input is x_i , for all $(x_i, y_i) \in D_{edge}$
 - Not recognized as malicious by the server, perform well on the dataset D





Attack Strategies

- Data poisoning attack
 - attackers perform standard local training on a locally crafted dataset D'
 - maximize the accuracy of the global model on $D \cup D_{ed,ge}$
- PGD attack
 - adversaries apply projected gradient descent on the losses for $D \cup D_{ed,ge}$
 - If adversary runs SGD for too long, the resulting model would significantly diverge from its origin
 - the *i*-th adversary chooses an attack budget δ so that their output model w_i respects the constraint $||w w_i|| \leq \delta$.





Attack Strategies

- PGD attack with model replacement
 - combines the PGD attack and the model replacement attack
 - the model parameter is scaled before being sent to the server so as to cancel the contributions from the other benign nodes





PGD attack with model replacement

Assume a adversary client $i \in S$ and denote its updated local model by $oldsymbol{w}_{i'}$

Model replacement transmits back to the server:

$$\frac{n_S}{n_{i'}}(\boldsymbol{w}_{i'}-\boldsymbol{w})+\boldsymbol{w}$$

Assuming that w has almost converged, every benign client i will submit

$$w_i \approx w$$

$$oldsymbol{w}^{ ext{next}} pprox oldsymbol{w} + \sum_{i \in S} rac{n_i}{n_S} (oldsymbol{w}_i - oldsymbol{w}) = oldsymbol{w}_{i'}$$





Definition

- $f_{\mathbf{W}}(\cdot)$ is an L-layer, fully-connected neural network, parameterized by $\mathbf{W}=(\mathbf{W}_1,\dots,\mathbf{W}_L)$
- $\mathbf{X}_{(l)} := [\boldsymbol{x}_1^{(l)}, \boldsymbol{x}_2^{(l)}, \dots, \boldsymbol{x}_{|\mathcal{D} \cup \mathcal{D}_{\text{edge}}|}^{(l)}]^{\top}$ is the activation matrix We say that one can craft ε -adversarial examples for $f_{\mathbf{W}}(\cdot)$ if for all
- We say that one can craft ε -adversarial examples for $f\mathbf{w}(\cdot)$ if for a $(x,y)\in\mathcal{D}_{\mathrm{edge}}$ there exists $\boldsymbol{\varepsilon}(x)$ with $\|\boldsymbol{\varepsilon}(x)\|<\varepsilon$, such that $f_{\mathbf{W}}(x+\boldsymbol{\varepsilon}(x))=y$
- We say that a backdoor for $f_{\mathbf{W}}(\cdot)$ exists, if there exists \mathbf{W}' such that for all $(\mathbf{x},y)\in\mathcal{D}\cup\mathcal{D}_{\mathrm{edge}},\,f_{\mathbf{W}'}(\mathbf{x})=y$





Theory I

If a model is susceptible to adversarial examples, then it is also vulnerable to training-time backdoor attacks.

Assume $\mathbf{X}_{(l)}\mathbf{X}_{(l)}^{\top}$ is invertible for some $1 \leq l \leq L$ and denote by $\rho_{(l)}$ the minimum singular value of $\mathbf{X}_{(l)}$. If ε -adversarial examples exist, then a backdoor exists, where

$$\max_{\boldsymbol{x} \in \mathcal{D}_{edge}, \boldsymbol{x}' \in \mathcal{D}} \frac{\|\mathbf{W}_{l} \cdot (\boldsymbol{x} + \boldsymbol{\varepsilon}(\boldsymbol{x}))^{(l)}\|}{\|\boldsymbol{x}^{(l)} - \boldsymbol{x}'^{(l)}\|} \leq \|\mathbf{W}_{l} - \mathbf{W}_{l}'\| \leq \varepsilon \frac{\sqrt{|\mathcal{D}_{edge}|}}{\rho_{(l)}}$$





Theory I

$$\max_{\boldsymbol{x} \in \mathcal{D}_{edge}, \boldsymbol{x}' \in \mathcal{D}} \frac{\|\mathbf{W}_{l} \cdot (\boldsymbol{x} + \boldsymbol{\varepsilon}(\boldsymbol{x}))^{(l)}\|}{\|\boldsymbol{x}^{(l)} - \boldsymbol{x}'^{(l)}\|} \leq \|\mathbf{W}_{l} - \mathbf{W}_{l}'\| \leq \varepsilon \frac{\sqrt{|\mathcal{D}_{edge}|}}{\rho_{(l)}}$$

- Upper bound:
 - the existence of adversarial examples of small radius implies the existence of backdoors within small perturbations
 - defending against backdoors is at least as hard as defending against adversarial examples
- Lower bound:
 - the model perturbation cannot be small if there exist "good" data points and backdoor data points which are close to each other





- whether or not the defender can detect a backdoor in a given model
 - assume that the defender has access to the labeling function g and the defender is provided a ReLU network f as the model learnt by the FL system
 - checking for backdoors in f using g is equivalent to checking if $f \equiv g$





Theory II

Detecting backdoors in a model is NP-hard, by a reduction from 3-SAT.

The 3-SAT can be reduced to the decision problem of whether f is equal to g





Theory II

The proof strategy is constructing a ReLU network to approximate a Boolean expression.

Given function f, g, define Backdoor as the decision problem of whether there exists some $x \in [0, 1]^n$

$$f(x) \neq g(x)$$





Theory III

Backdoors hidden in regions of small measure (edge-case samples), are unlikely to be detected using gradient-based algorithms.

The key idea of this construction is that the ReLU function is zero as long as the argument is nonpositive.





Goal

highlight the effectiveness of edge-case attack against the state of the art (SOTA) of FL defenses

SOTA defenses:

- norm difference clipping (NDC)
- Krum
- Multi-Krum
- RFA
- weak differential private (DP) defense





Tasks

- Task 1: Image classification on CIFAR-10 with VGG-9 (K = 200,m = 10)
- Task 2: Digit classification on EMNIST with LeNet (K = 3383,m = 30)
- Task 3: Image classification on ImageNet with VGG-11 (K = 1000,m = 10)
- Task 4: Sentiment classification on Sentiment140 with LSTM (K =1948,m = 10)
- Task 5: Next Word prediction on the Reddit dataset with LSTM (K = 80,000, m = 100)

(K means the number of clients and m means the number of clients participates per FL round)





Edge-case VS not-so-edge-case

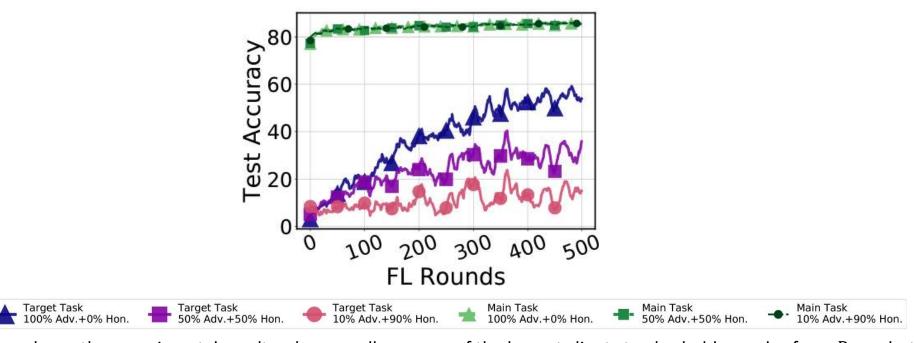
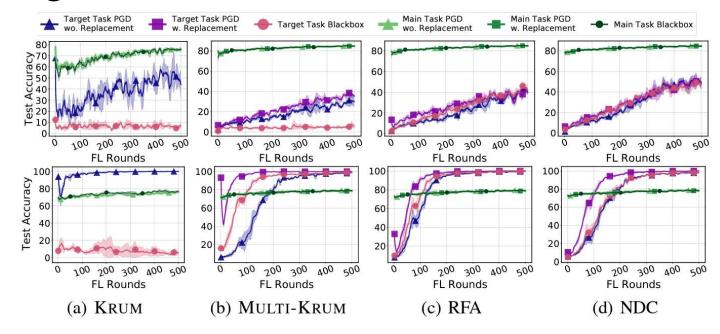


Figure shows the experimental results when we allow some of the honest clients to also hold samples from D_{edge} but with correct labels.





Edge-case Backdoors are hard to filter

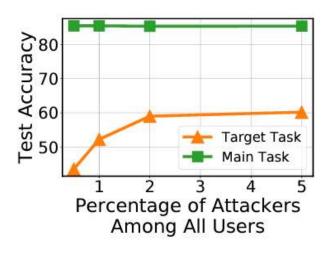


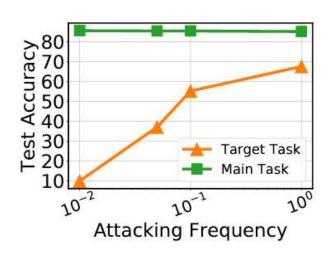
The PGD methods are effective on all of the four defense methods and the data poisoning method may be ineffective against Krum and MultiKrum.





Effectiveness of Edge-case Backdoors

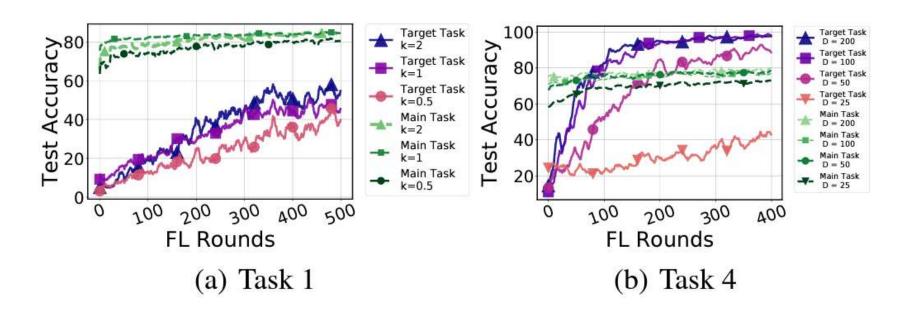








Effectiveness on models of different capacity







Thank You

