

# Loss Functions for Deep Metric Learning Using Binary Supervision and Beyond

Suha Kwak

[suha.kwak@postech.ac.kr](mailto:suha.kwak@postech.ac.kr)

Graduate School of Artificial Intelligence  
Dept. of Computer Science and Engineering

**POSTECH**

# Metric Learning

How much **similar/dissimilar** semantically?

$$D \left( \begin{array}{c} \text{[Image of Tony Stark]} \\ , \\ \text{[Image of Tony Stark in Iron Man suit]} \end{array} \right) < D \left( \begin{array}{c} \text{[Image of Tony Stark]} \\ , \\ \text{[Image of Thor]} \end{array} \right)$$

**Metric:** Function that quantifies a **distance**

**Metric Learning:** Learning a metric from a set of data

# Applications



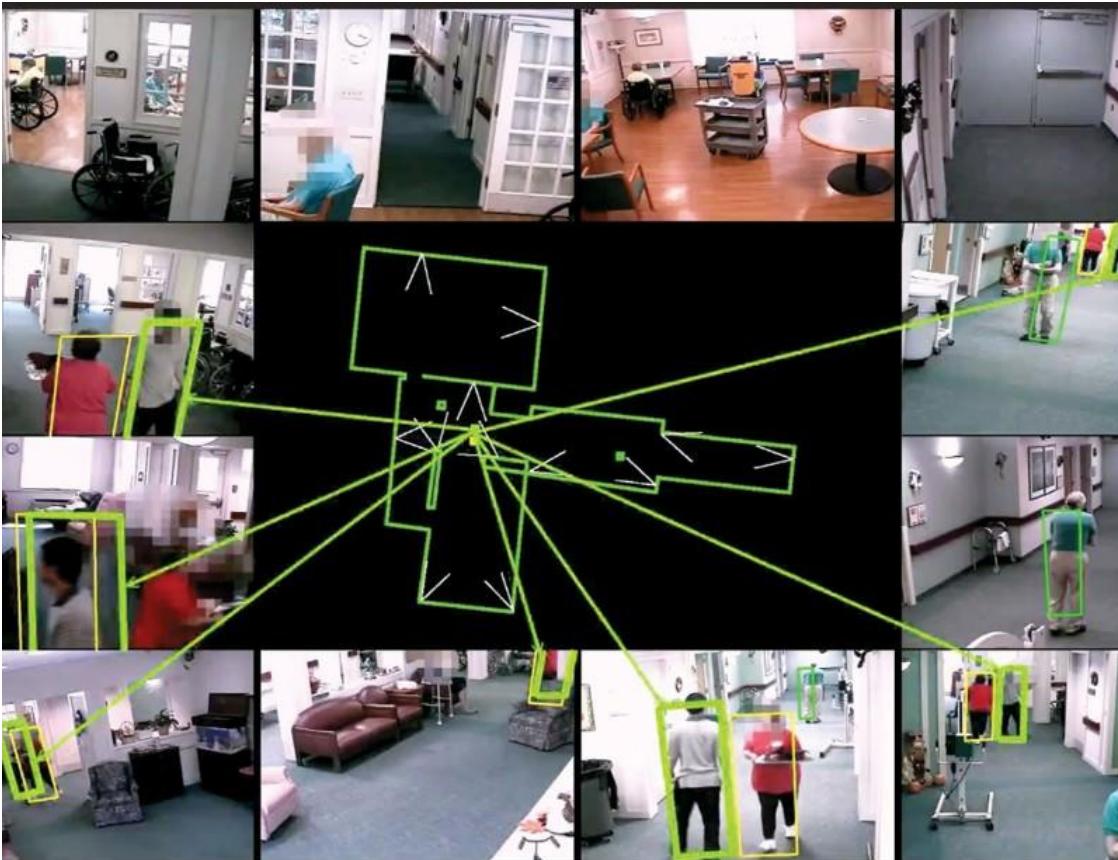
Content-based image retrieval



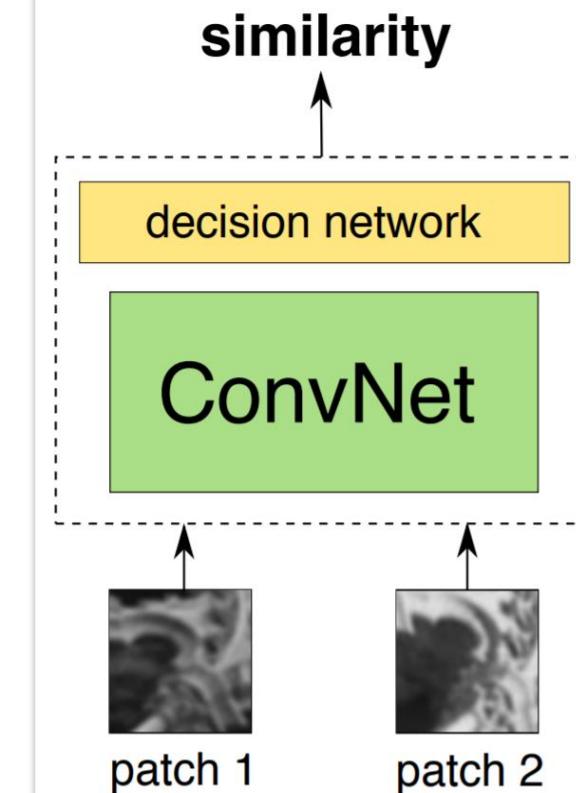
Face verification/identification<sup>[1]</sup>

[1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015

# Applications



Person re-identification<sup>[2]</sup>



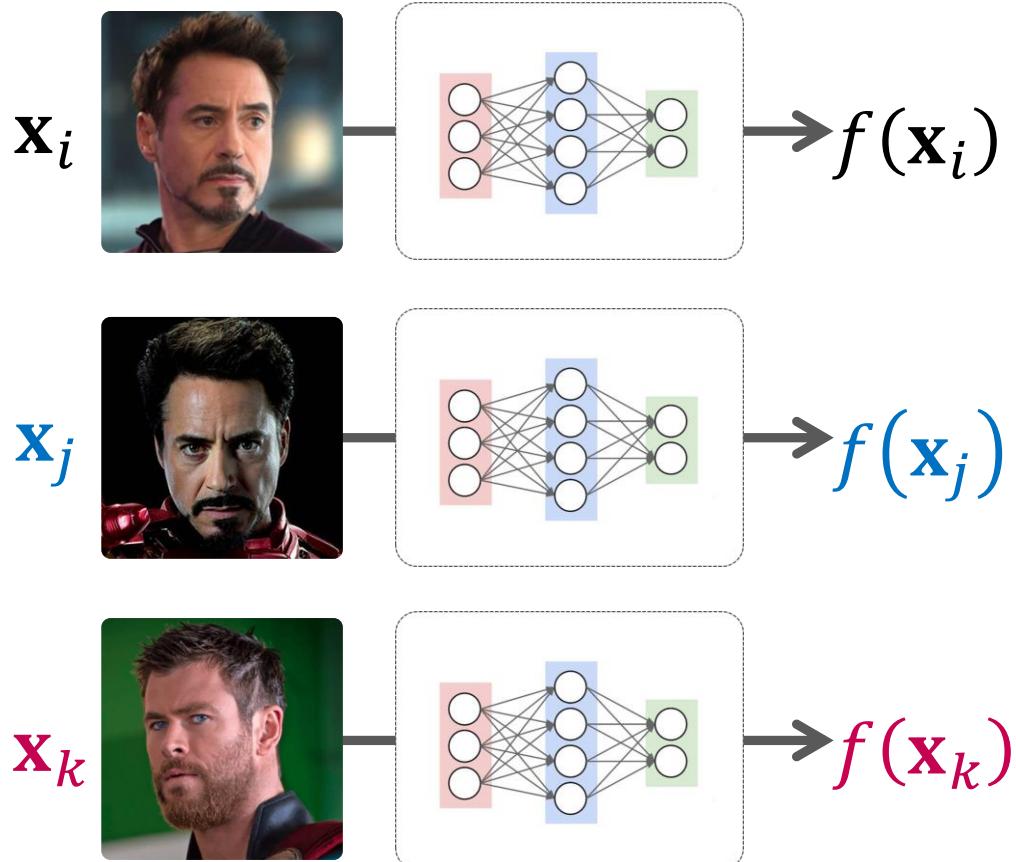
Patch matching/stereo imaging<sup>[3]</sup>

[2] Beyond triplet loss: a deep quadruplet network for person re-identification, CVPR 2017

[3] Learning to compare image patches via convolutional neural networks, CVPR 2015

# Deep Metric Learning

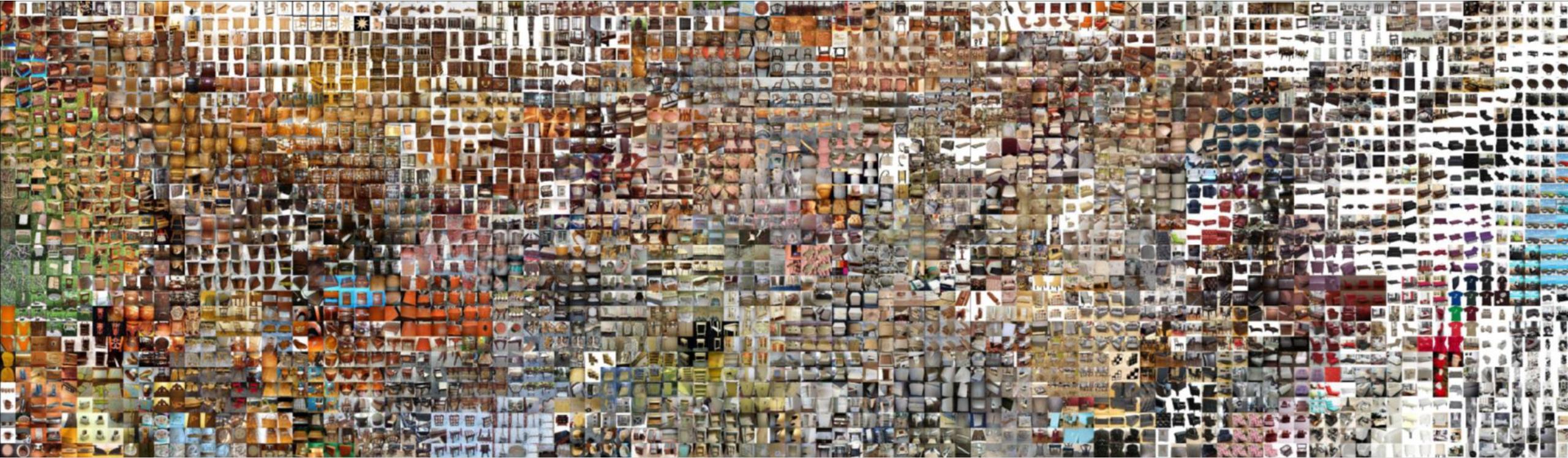
Learning a deep embedding network  $f$  so that semantically similar images are closely grouped together



Distance = Semantic dissimilarity

*This quality of the embedding space is mainly determined by **loss functions** used for training the network.*

$\mathbb{R}^d$



# Proxy Anchor Loss for Deep Metric Learning

Sungyeon Kim

Dongwon Kim

Minsu Cho

Suha Kwak

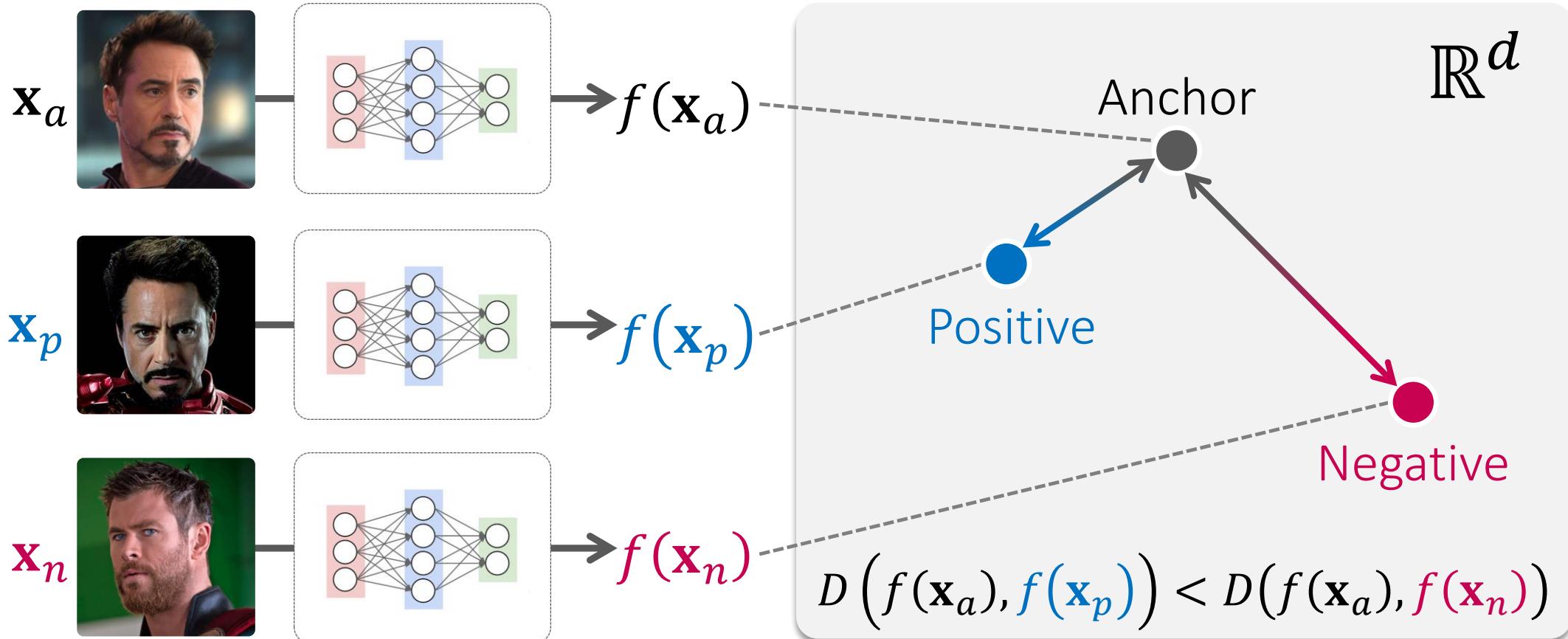
{tjddus9597, kdwon, mscho, suha.kwak}@postech.ac.kr

**POSTECH**

# Well-known Examples of Metric Learning Losses

- Triplet rank loss<sup>[1]</sup>

$$\ell_{\text{tri}}(a, p, n) = [D(f_a, f_p) - D(f_a, f_n) + \delta]_+$$

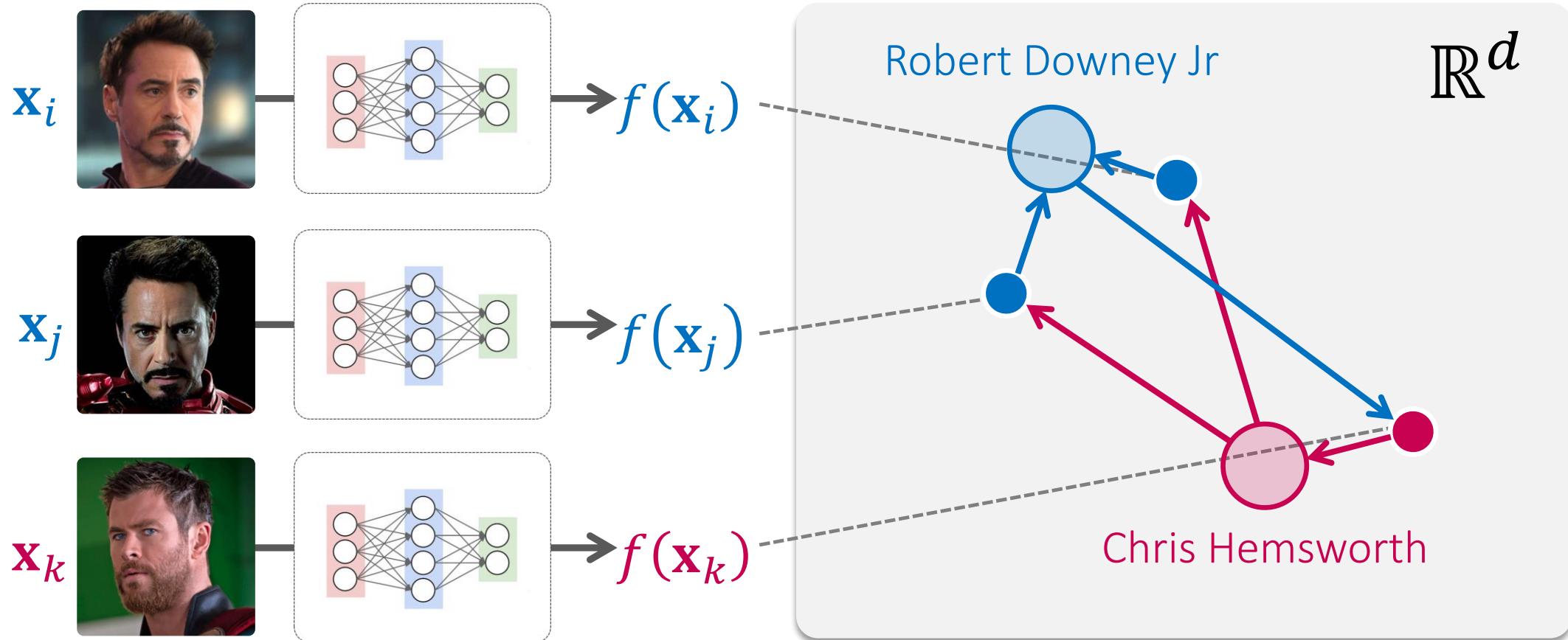


[1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015

# Well-known Examples of Metric Learning Losses

- Proxy NCA loss<sup>[6]</sup>

$$\ell_{\text{proxyNCA}}(B) = \sum_{i \in B} \left\{ D(f_i, p^+) - \log \sum_{p^- \in P^-} \exp(-D(f_i, p^-)) \right\}$$



# Two Categories of Existing Metric Learning Losses

- Pair-based losses
  - (+) Exploiting *data-to-data relations*, fine-grained relations between data
  - (–) Prohibitively high training complexity
- Examples
  - Contrastive loss<sup>[4]</sup>
$$\ell_{\text{ctr}}(i, j) = y_{ij} D(f_i, f_j)^2 + (1 - y_{ij}) [\delta - D(f_i, f_j)]_+^2$$
  - Triplet rank loss<sup>[1]</sup>
$$\ell_{\text{tri}}(a, p, n) = [D(f_a, f_p) - D(f_a, f_n) + \delta]_+$$
  - N-pair loss<sup>[5]</sup>
$$\ell_{\text{NP}}(a, p, n_1, \dots, n_{N-1}) = \log \left( 1 + \sum_{i=1}^{N-1} \exp(D(f_a, f_p) - D(f_a, f_{n_i})) \right)$$

[1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015

[4] Learning a similarity metric discriminatively with application to face verification, CVPR 2005

[5] Improved deep metric learning with multi-class N-pair loss objective, NeurIPS 2016

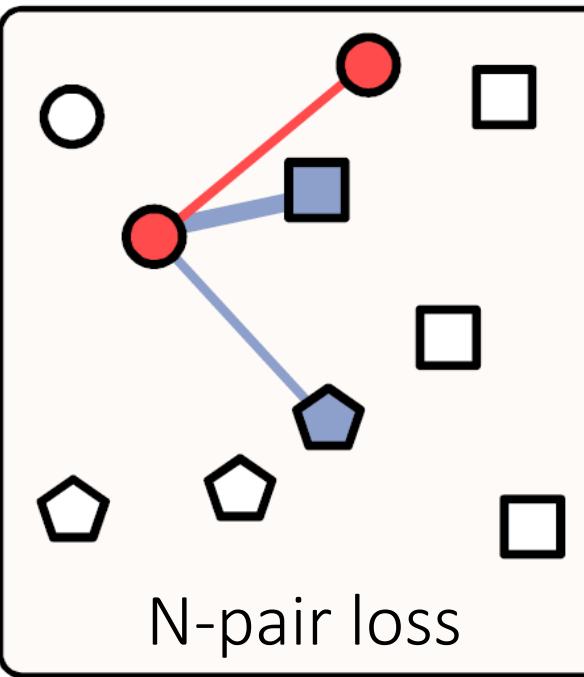
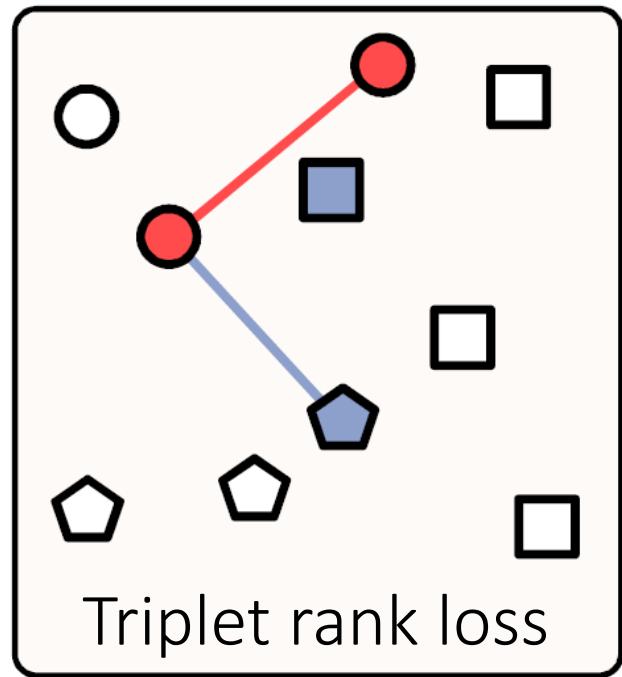
# Two Categories of Existing Metric Learning Losses

- Proxy-based losses
  - Proxy
    - Representative of a subset of training data
    - Learned as a part of the network parameters
  - Taking each data point as an anchor and associating it with proxies
    - (+) Lower training complexity, faster convergence in general
    - (+) More robust against label noises and outliers
    - (–) Leveraging impoverished data-to-proxy relations only
  - Example: Proxy-NCA loss<sup>[6]</sup>

$$\ell_{\text{proxyNCA}}(B) = - \sum_{i \in B} \log \frac{\exp(-D(f_i, p^+))}{\sum_{p^- \in P^-} \exp(-D(f_i, p^-))}$$

# Two Categories of Existing Metric Learning Losses

## Pair-based losses

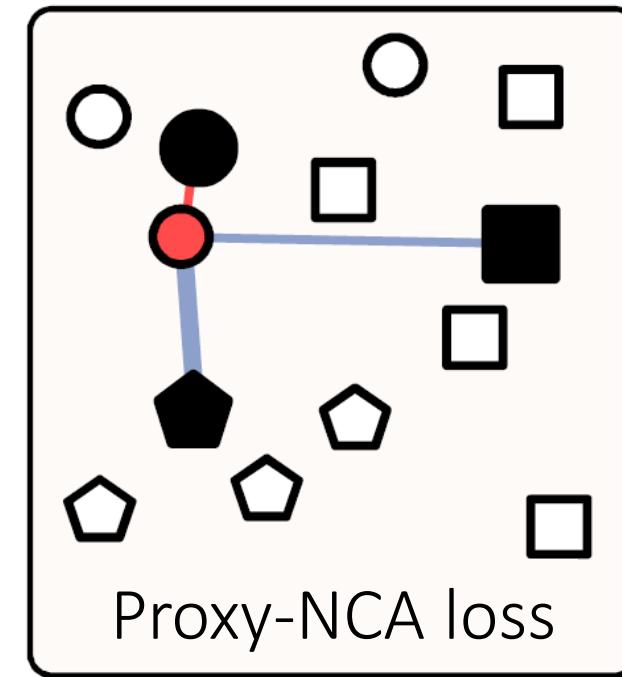


“Data-to-data relations”

*Rich and fine-grained*

*Demanding high training complexity*

## Proxy-based losses



“Data-to-proxy relations”

*Reducing training complexity*

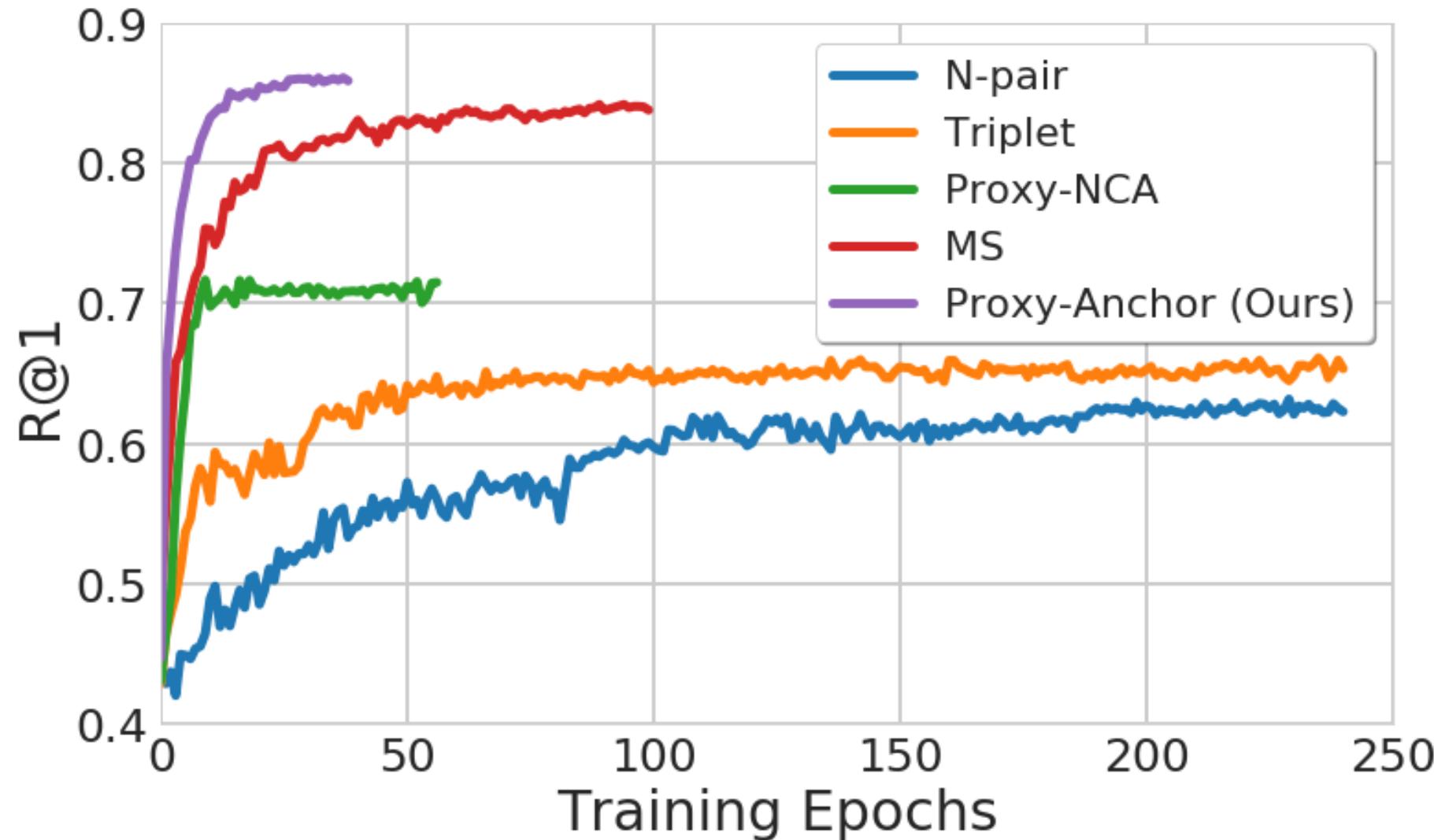
*Impoverished information*

# Our Method

- A new proxy-based loss called *proxy anchor loss*
  - Taking only advantages of both categories
  - Overcoming their limitations
- How it works
  - Using a proxy as an anchor, and associating it with all data in a batch
  - Fast convergence thanks to the use of proxies
  - Taking data-to-data relations into account by allowing data points to interact with each other during training
- Results
  - State-of-the-art performance
  - Fastest convergence (on the Cars-196 dataset)

# Our Method

Recall@1 vs. training epochs on the Cars-196 dataset



# Details of Proxy Anchor Loss

- Mathematical form and its interpretation

$$\begin{aligned}\ell(B) &= \frac{1}{|P^+|} \sum_{p \in P^+} \log \left( 1 + \sum_{i \in B_p^+} \exp[-\alpha(S(f_i, p) - \delta)] \right) \\ &\quad + \frac{1}{|P|} \sum_{p \in P} \log \left( 1 + \sum_{j \in B_p^-} \exp[\alpha(S(f_j, p) + \delta)] \right) \\ &= \frac{1}{|P^+|} \sum_{p \in P^+} [\text{SoftPlus} \left( \text{LSE}_{i \in B_p^+} - \alpha(S(f_i, p) - \delta) \right)] \\ &\quad + \frac{1}{|P|} \sum_{p \in P} [\text{SoftPlus} \left( \text{LSE}_{j \in B_p^-} \alpha(S(f_j, p) + \delta) \right)]\end{aligned}$$

$S(\cdot, \cdot)$

Cosine similarity

**SoftPlus**

A smooth approx.  
of ReLU

**LSE**

A smooth approx.  
of MAX

# Details of Proxy Anchor Loss

- Mathematical form and its interpretation

$$\ell(B) = \frac{1}{|P^+|} \sum_{p \in P^+} [\text{SoftPlus}_{i \in B_p^+} (\text{LSE} - \alpha(S(f_i, p) - \delta))] \\ + \frac{1}{|P^-|} \sum_{p \in P^-} [\text{SoftPlus}_{i \in B_p^-} (\text{LSE} \alpha(S(f_j, p) + \delta))]$$

Regarding LSE as MAX: pull  $p$  and its hardest positive example together, push  $p$  and its hardest negative example apart.

In practice pull/push all embedding vectors in the batch, but with different degrees of strength determined by their relative hardness.

# Details of Proxy Anchor Loss

- Analysis on its gradients

$$\frac{\partial \ell(B)}{\partial S(f_i, p)} = \begin{cases} \frac{1}{|P^+|} \frac{-\alpha h_p^+(f_i)}{1 + \sum_{j \in B_p^+} h_p^+(f_j)}, & \forall i \in B_p^+, \\ \frac{1}{|P^-|} \frac{\alpha h_p^-(f_i)}{1 + \sum_{k \in B_p^-} h_p^-(f_k)}, & \forall i \in B_p^-, \end{cases}$$

where

$h_p^+(f) = \exp[-\alpha(S(f, p) - \delta)]$  : Positive hardness metric

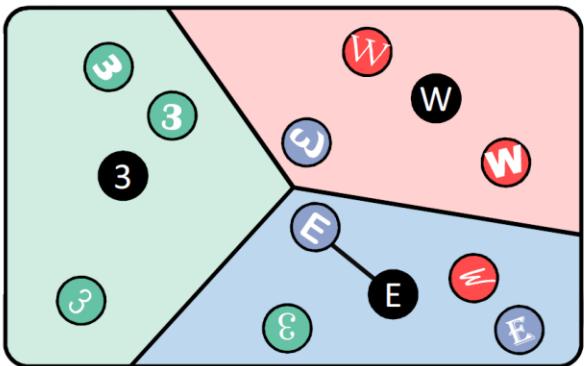
$h_p^-(f) = \exp[\alpha(S(f, p) + \delta)]$  : Negative hardness metric

The gradient w.r.t.  $f_i$  is affected by other examples in the batch.  
(The gradient becomes larger when  $f_i$  is harder than others.)

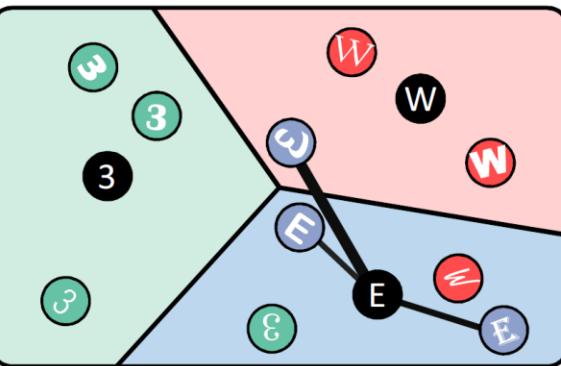
# Comparison to Proxy NCA

In the case of positive examples

Proxy NCA



Proxy Anchor

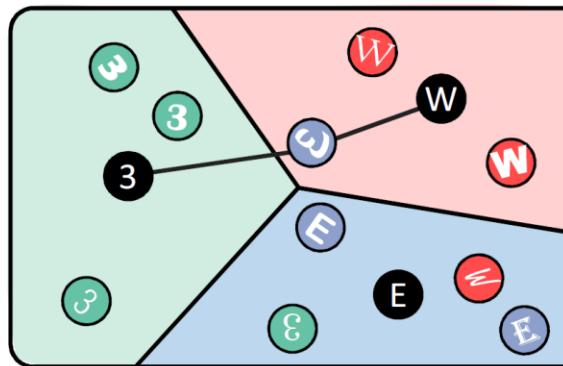


Uniform scale  
for all gradients

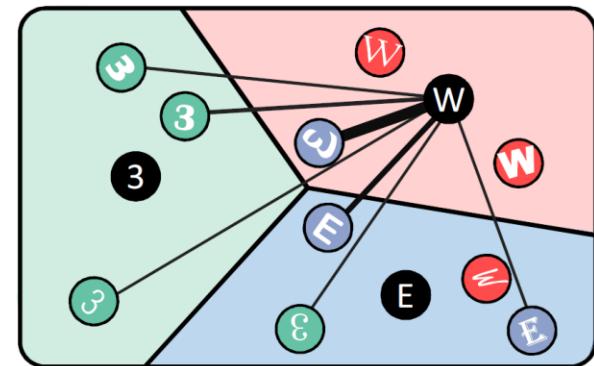
Scales weighted by  
relative hardness

In the case of negative examples

Proxy NCA



Proxy Anchor



Pushing only a small  
number of data with  
uniform strength

Pushing all data with  
consideration of their  
distribution

# Complexity Analysis

Type	Loss	Training Complexity
Proxy	Proxy Anchor	$O(MC)$
	Proxy NCA <sup>[6]</sup>	$O(MC)$
	SoftTriplet <sup>[8]</sup>	$O(MCU^2)$
Pair	Contrastive <sup>[4]</sup>	$O(M^2)$
	Triplet <sup>[1]</sup>	$O(M^3)$
	N-pair <sup>[5]</sup>	$O(M^3)$
	Lifted Structure <sup>[7]</sup>	$O(M^3)$

The same complexity, but Proxy Anchor converges faster & performs better since it considers relative hardness of data.

$M$ : # of data

$C$ : # of classes ( $C \ll M$ )

$U$ : # of proxies per class

[1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015

[4] Learning a similarity metric discriminatively with application to face verification, CVPR 2005

[5] Improved deep metric learning with multi-class N-pair loss objective, NeurIPS 2016

[6] No fuss distance metric learning using proxies, ICCV 2017

[7] Deep metric learning via lifted structured feature embedding, CVPR 2016

[8] Softtriplet loss: Deep metric learning without triplet sampling, ICCV 2019

# Experiments

- Evaluation on the 4 image retrieval benchmarks
  - Caltech-UCSD Bird 200 (CUB-200-2011)
  - Cars-196
  - Stanford Online Product (SOP)
  - In-Shop Clothes Retrieval (In-Shop)
- Proxy setting: 1 proxy per class
- Image setting
  - Default: 224 X 224 (as in most previous work)
  - Larger: 256 X 256 (for comparison to HORDE<sup>[9]</sup>)
- Hyper-parameters:  $\alpha = 32, \delta = 10^{-1}$

# Experiments

- Quantitative results on the CUB-200-2011 and Cars-196

Recall@K		CUB-200-2011				Cars-196			
		1	2	4	8	1	2	4	8
Clustering <sup>64</sup>	BN	48.2	61.4	71.8	81.9	58.1	70.6	80.3	87.8
Proxy-NCA <sup>64</sup>	BN	49.2	61.9	67.9	72.4	73.2	82.4	86.4	87.8
Smart Mining <sup>64</sup>	G	49.8	62.3	74.1	83.3	64.7	76.2	84.2	90.2
MS <sup>64</sup>	BN	57.4	69.8	80.0	87.8	77.3	85.3	90.5	94.2
SoftTriple <sup>64</sup>	BN	<u>60.1</u>	<u>71.9</u>	<u>81.2</u>	<u>88.5</u>	<u>78.6</u>	<u>86.6</u>	<u>91.8</u>	<u>95.4</u>
Proxy-Anchor <sup>64</sup>	BN	<b>61.7</b>	<b>73.0</b>	<b>81.8</b>	<b>88.8</b>	<b>78.8</b>	<b>87.0</b>	<b>92.2</b>	<b>95.5</b>
Margin <sup>128</sup>	R50	63.6	74.4	83.1	90.0	79.6	86.5	91.9	95.1
HDC <sup>384</sup>	G	53.6	65.7	77.0	85.6	73.7	83.2	89.5	93.8
A-BIER <sup>512</sup>	G	57.5	68.7	78.3	86.2	82.0	89.0	93.2	96.1
ABE <sup>512</sup>	G	60.6	71.5	79.8	87.4	<u>85.2</u>	90.5	94.0	96.1
HTL <sup>512</sup>	BN	57.1	68.8	78.7	86.5	81.4	88.0	92.7	95.7
RLL-H <sup>512</sup>	BN	57.4	69.7	79.2	86.9	74.0	83.6	90.1	94.1
MS <sup>512</sup>	BN	<u>65.7</u>	<u>77.0</u>	<u>86.3</u>	<u>91.2</u>	84.1	90.4	94.0	96.5
SoftTriple <sup>512</sup>	BN	65.4	76.4	84.5	90.4	84.5	<u>90.7</u>	<u>94.5</u>	<u>96.9</u>
Proxy-Anchor <sup>512</sup>	BN	<b>68.4</b>	<b>79.2</b>	<b>86.8</b>	<b>91.6</b>	<b>86.1</b>	<b>91.7</b>	<b>95.0</b>	<b>97.3</b>
<sup>†</sup> Contra+HORDE <sup>512</sup>	BN	66.3	76.7	84.7	90.6	83.9	90.3	94.1	96.3
<sup>†</sup> Proxy-Anchor <sup>512</sup>	BN	<b>71.1</b>	<b>80.4</b>	<b>87.4</b>	<b>92.5</b>	<b>88.3</b>	<b>93.1</b>	<b>95.7</b>	<b>97.5</b>

# Experiments

- Quantitative results on the SOP (*left*) and In-Shop (*right*)

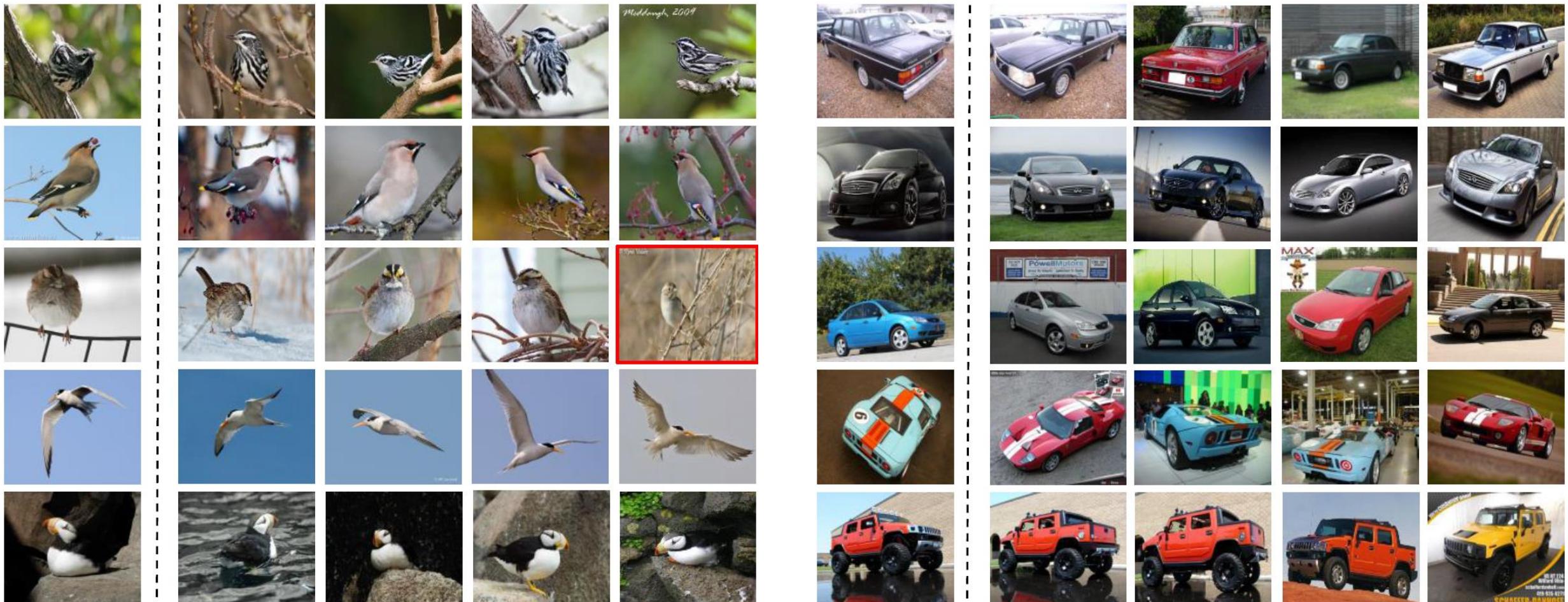
Recall@K	1	10	100	1000
Clustering <sup>64</sup>	67.0	83.7	93.2	-
Proxy-NCA <sup>64</sup>	73.7	-	-	-
MS <sup>64</sup>	74.1	87.8	94.7	<b>98.2</b>
SoftTriple <sup>64</sup>	<u>76.3</u>	<b>89.1</b>	<b>95.3</b>	-
Proxy-Anchor <sup>64</sup>	<b>76.5</b>	<u>89.0</u>	<u>95.1</u>	<b>98.2</b>
Margin <sup>128</sup>	72.7	86.2	93.8	98.0
HDC <sup>384</sup>	69.5	84.4	92.8	97.7
A-BIER <sup>512</sup>	74.2	86.9	94.0	97.8
ABE <sup>512</sup>	76.3	88.4	94.8	98.2
HTL <sup>512</sup>	74.8	88.3	94.8	98.4
RLL-H <sup>512</sup>	76.1	89.1	95.4	-
MS <sup>512</sup>	78.2	<u>90.5</u>	<u>96.0</u>	<b>98.7</b>
SoftTriple <sup>512</sup>	<u>78.3</u>	90.3	95.9	-
Proxy-Anchor <sup>512</sup>	<b>79.1</b>	<b>90.8</b>	<b>96.2</b>	<b>98.7</b>
<sup>†</sup> Contra+HORDE <sup>512</sup>	80.1	91.3	96.2	<b>98.7</b>
<sup>†</sup> Proxy-Anchor <sup>512</sup>	<b>80.3</b>	<b>91.4</b>	<b>96.4</b>	<b>98.7</b>

Recall@K	1	10	20	40
HDC <sup>384</sup>	62.1	84.9	89.0	92.3
HTL <sup>128</sup>	80.9	94.3	95.8	97.4
MS <sup>128</sup>	<u>88.0</u>	<u>97.2</u>	<u>98.1</u>	<u>98.7</u>
Proxy-Anchor <sup>128</sup>	<b>90.8</b>	<b>97.9</b>	<b>98.5</b>	<b>99.0</b>
FashionNet <sup>4096</sup>	53.0	73.0	76.0	79.0
A-BIER <sup>512</sup>	83.1	95.1	96.9	97.8
ABE <sup>512</sup>	87.3	96.7	97.9	98.5
MS <sup>512</sup>	<u>89.7</u>	<u>97.9</u>	<u>98.5</u>	<u>99.1</u>
Proxy-Anchor <sup>512</sup>	<b>91.5</b>	<b>98.1</b>	<b>98.8</b>	<b>99.1</b>
<sup>†</sup> Contra+HORDE <sup>512</sup>	90.4	97.8	98.4	98.9
<sup>†</sup> Proxy-Anchor <sup>512</sup>	<b>92.6</b>	<b>98.3</b>	<b>98.9</b>	<b>99.3</b>

Our method achieves state-of-the-art performance in almost all settings on the all 4 benchmarks.

# Experiments

- Qualitative results: Top 4 retrievals



CUB-200-2011

Cars-196

# Experiments

- Qualitative results: Top 4 retrievals



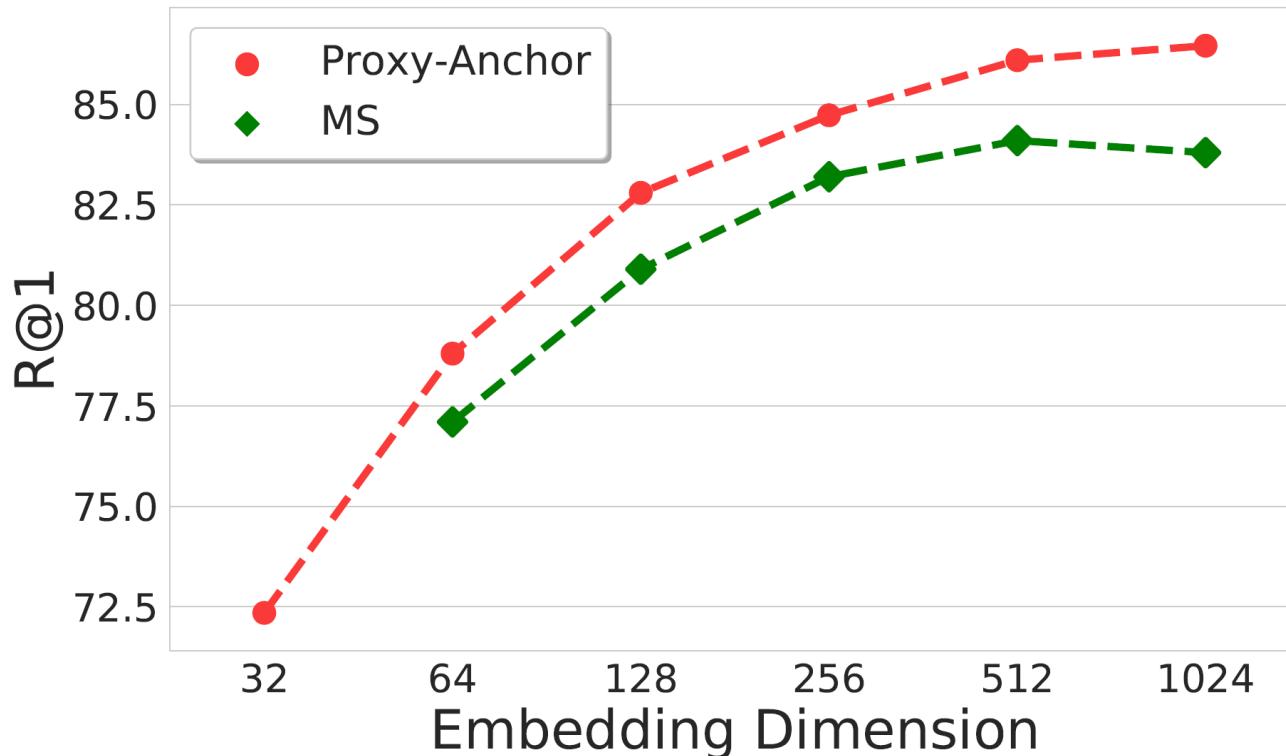
SOP



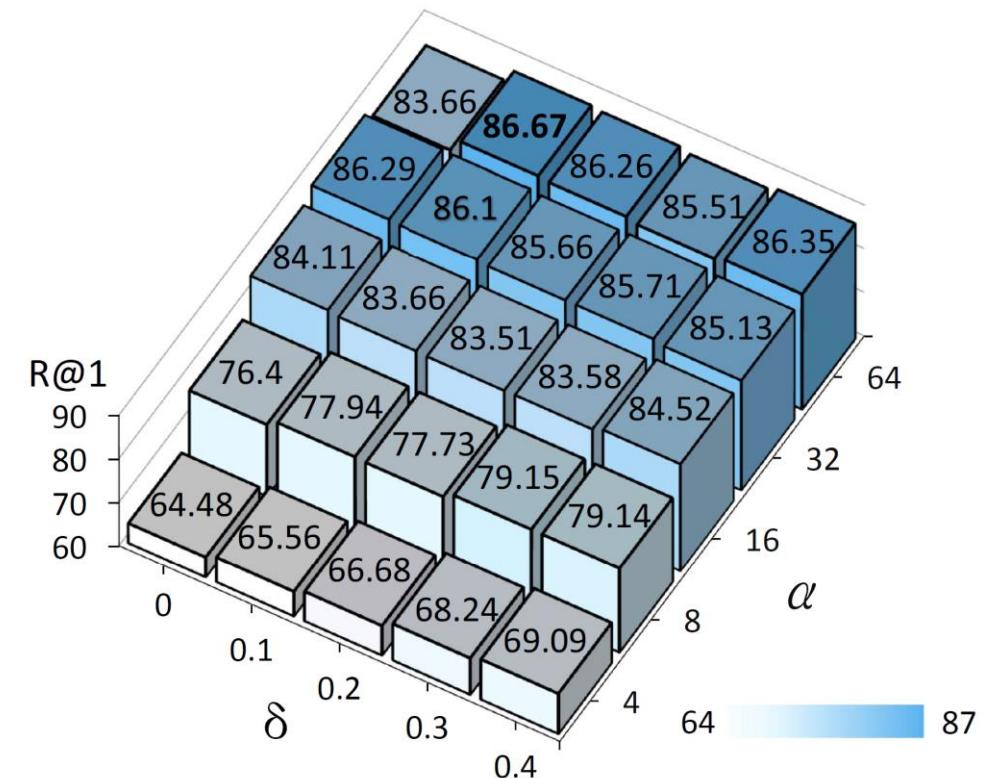
In-Shop

# Experiments

- Impact of hyper-parameters



Accuracy vs. embedding dimension



Accuracy vs.  $\alpha$  and  $\delta$

The performance is stable and high enough when the embedding dimension  $\geq 128$  and  $\alpha \geq 16$ .

# Experiments

- Ablation studies

Network	Image Size	CUB-200-2011				Cars-196			
		R@1	R@2	R@4	R@8	R@1	R@2	R@4	R@8
GoogleNet	224 × 224	63.8	74.4	83.6	90.4	84.3	90.4	94.1	96.7
Inception-BN		68.4	79.2	86.8	91.6	86.1	91.7	95.0	97.3
ResNet-50		69.7	80.0	87.0	92.4	87.7	92.9	95.8	97.9
ResNet-101		<b>70.8</b>	<b>81.0</b>	<b>88.1</b>	<b>93.0</b>	<b>87.9</b>	<b>93.0</b>	<b>96.1</b>	<b>97.9</b>
	256 × 256	71.1	80.4	87.4	92.5	88.3	93.1	95.7	97.5
Inception-BN	324 × 324	74.0	82.9	88.9	93.2	91.1	94.9	96.9	98.3
	448 × 448	<b>77.3</b>	<b>85.6</b>	<b>91.1</b>	<b>94.2</b>	<b>92.9</b>	<b>96.1</b>	<b>97.7</b>	<b>98.7</b>

Strong backbone and large input improve performance.

# Conclusion

- Contributions
  - A new metric learning loss based on proxy
  - Current state of the art on public benchmarks for image retrieval
  - Fastest convergence speed
- Future directions
  - Analysis on generalizability
  - Improving test time efficiency



# Deep Metric Learning Beyond Binary Supervision

Sungyeon Kim Minkyo Seo Ivan Laptev Minsu Cho Suha Kwak

{tjddus9597, mkseo, mscho, suha.kwak}@postech.ac.kr, ivan.laptev@inria.fr

**POSTECH**

*inria*

# Existing Losses in Deep Metric Learning

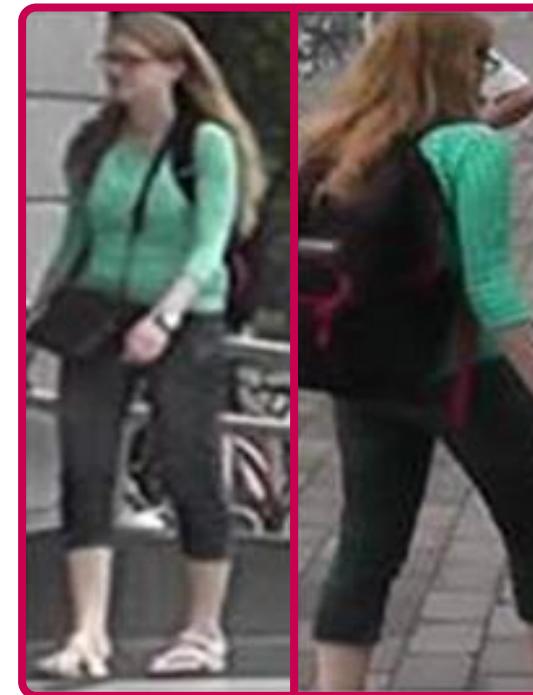
- A common issue
  - Existing (deep) metric learning approaches rely on binary relations between images: “*same*” or “*not*”.



Face verification



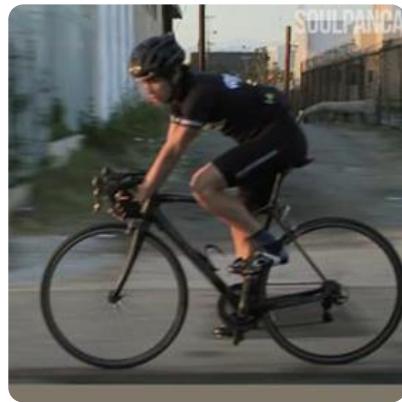
Content-based image retrieval



Person re-identification

# Existing Losses in Deep Metric Learning

- A common issue
  - However, relations between real world images are *not binary* but often represented as *continuous similarities*.



1.65



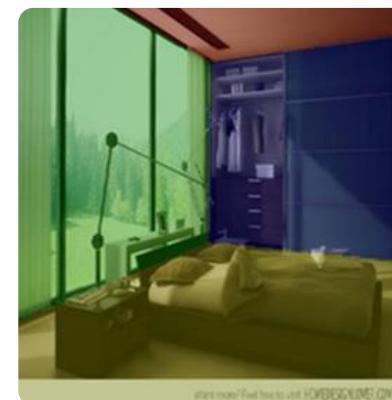
3.41



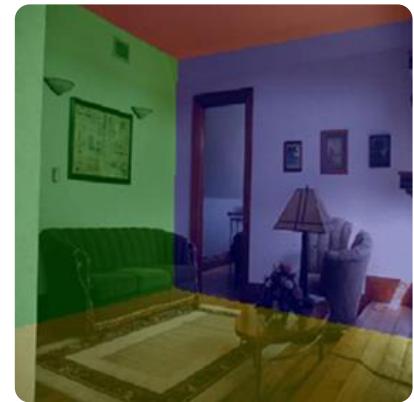
1.47



0.26



0.34



0.29



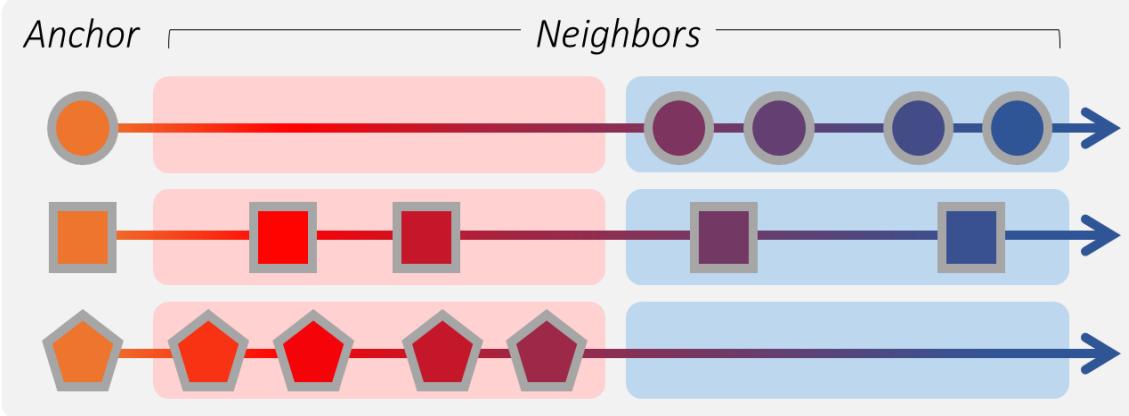
0.41

# Existing Losses in Deep Metric Learning

- Conventional methods to handle the issue
  - Existing metric learning loss + *similarity quantization*

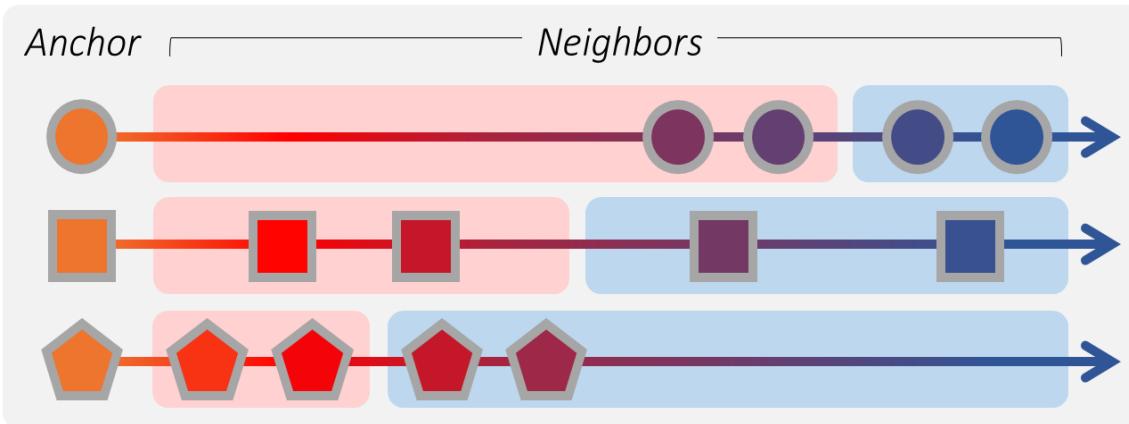
## *Binary thresholding*<sup>[9]</sup>

Populations of positive and negative examples would be significantly imbalanced.



## *Nearest neighbor search*<sup>[10]</sup>

Positive neighbors of a rare example would be dissimilar and negative neighbors of a common example would be too similar.



[9] Pose embeddings: A deep architecture for learning to match human poses, arXiv 2015

[10] Thin-slicing for pose: Learning to understand pose without explicit pose estimation, CVPR 2016

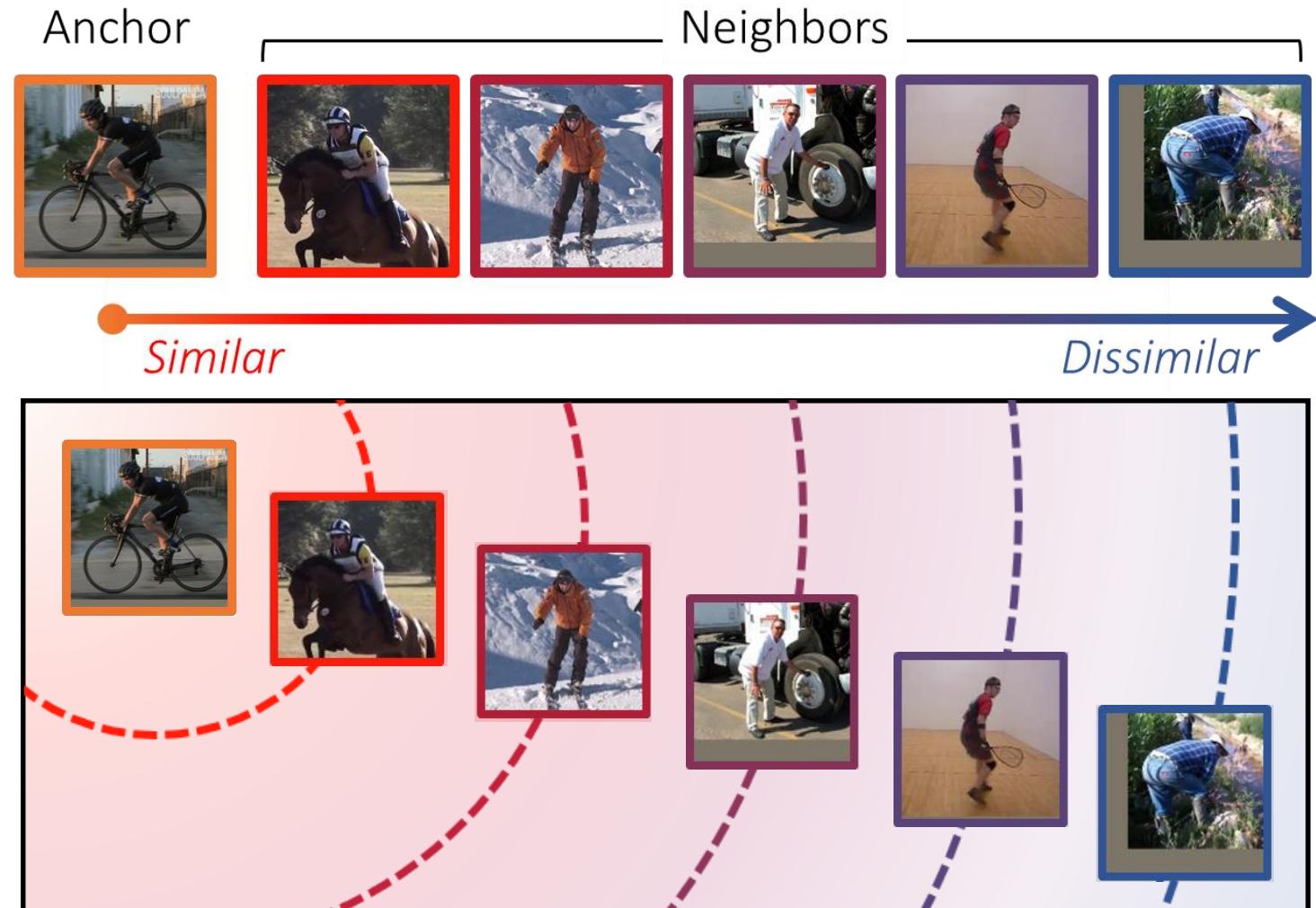
# Existing Losses in Deep Metric Learning

- Conventional methods to handle the issue
  - Degree of similarity is ignored in the learned embedding space.



# Our Method

- Our goal
  - Learning a metric space that reflects the degree of similarity directly



# Our Method

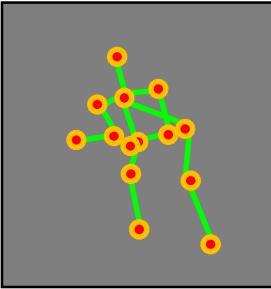
- Our goal
  - Learning a metric space that reflects the degree of similarity directly
- Contributions
  - A new triplet loss: *Log-ratio loss*
  - A new triplet sampling technique: *Dense triplet sampling*
  - Various applications
    - Human pose retrieval
    - Room layout retrieval
    - Caption-aware image retrieval
    - Representation learning for image captioning

# Log-ratio Loss

- Definition



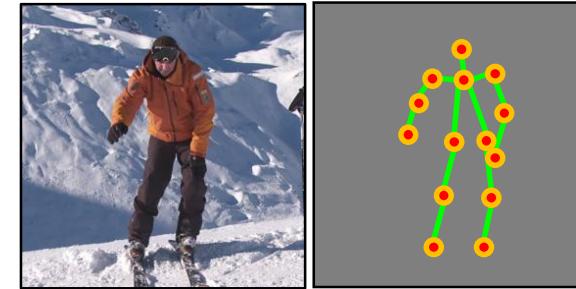
$\mathbf{x}_a$



$\mathbf{y}_a$



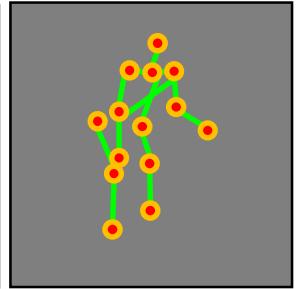
$\mathbf{x}_i$



$\mathbf{y}_i$



$\mathbf{x}_j$



$\mathbf{y}_j$

$$\ell_{\text{lr}}(a, i, j) = \left\{ \log \frac{D(f_a, f_i)}{D(f_a, f_j)} - \log \frac{D_y(\mathbf{y}_a, \mathbf{y}_i)}{D_y(\mathbf{y}_a, \mathbf{y}_j)} \right\}^2$$

where  $f_i := f(\mathbf{x}_i)$  is the embedding vector of image  $i$ ,  
and  $D(\cdot)$  denotes the squared Euclidean distance.

The distance between two images in the learned metric space  
will be proportional to their distance in the label space.

# Log-ratio Loss

- Analysis on its gradients

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_a} = -\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_i} - \frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_j}$$

Direction between  
the anchor and neighbors

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_i} = \frac{(f_i - f_a)}{D(f_a, f_i)} \cdot \ell'_{\text{lr}}(a, i, j)$$

Discrepancy between  
the label distance ratio and  
the embedding distance ratio

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_j} = \frac{(f_a - f_j)}{D(f_a, f_j)} \cdot \ell'_{\text{lr}}(a, i, j)$$

$$4 \left\{ \log \frac{D(f_a, f_i)}{D(f_a, f_j)} - \log \frac{D_y(\mathbf{y}_a, \mathbf{y}_i)}{D_y(\mathbf{y}_a, \mathbf{y}_j)} \right\}$$

# Log-ratio Loss

- Comparison to the triplet rank loss

*Log-ratio loss*

$$\ell_{\text{lr}}(a, i, j) = \left\{ \log \frac{D(f_a, f_i)}{D(f_a, f_j)} - \log \frac{D(y_a, y_i)}{D(y_a, y_j)} \right\}^2$$

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_a} = -\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_i} - \frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_j}$$

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_i} = \frac{(f_i - f_a)}{D(f_a, f_i)} \cdot \ell'_{\text{lr}}(a, i, j)$$

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_j} = \frac{(f_a - f_j)}{D(f_a, f_j)} \cdot \ell'_{\text{lr}}(a, i, j)$$

Although the rank constraint holds,  
the gradients' magnitudes could  
be significant if  $\ell'_{\text{lr}}(a, i, j)$  is large.

*Triplet rank loss*

$$\ell_{\text{tri}}(a, i, j) = [D(f_a, f_i) - D(f_a, f_j) + \delta]_+$$

$$\frac{\partial \ell_{\text{tri}}(a, i, j)}{\partial f_a} = -\frac{\partial \ell_{\text{tri}}(a, i, j)}{\partial f_i} - \frac{\partial \ell_{\text{tri}}(a, i, j)}{\partial f_j}$$

$$\frac{\partial \ell_{\text{tri}}(a, i, j)}{\partial f_i} = 2(f_i - f_a) \cdot \mathbb{I}(\ell_{\text{tri}}(a, i, j) > 0)$$

$$\frac{\partial \ell_{\text{tri}}(a, i, j)}{\partial f_j} = 2(f_a - f_j) \cdot \mathbb{I}(\ell_{\text{tri}}(a, i, j) > 0)$$

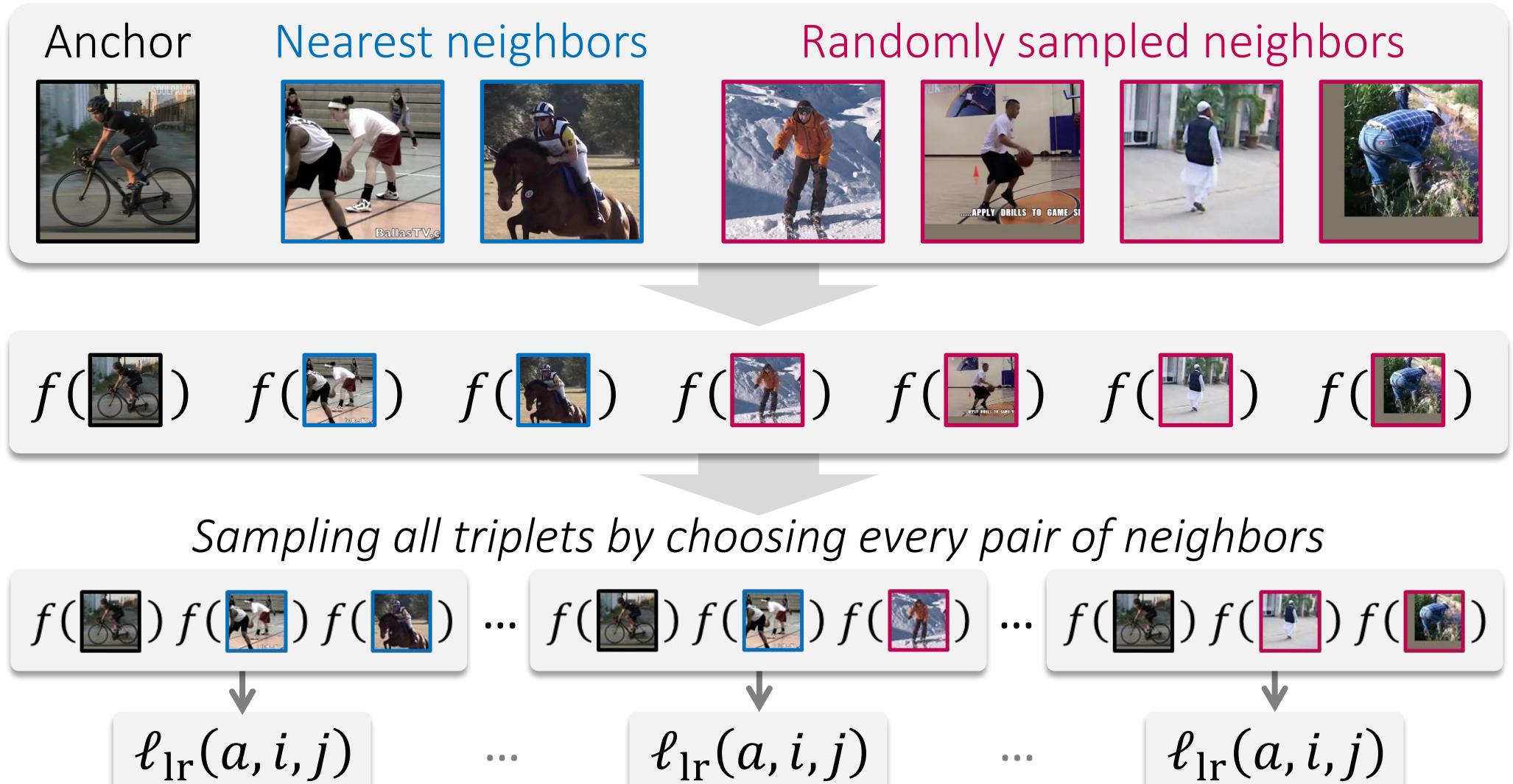
The gradients are zero if the triplet  
satisfies the rank constraint due to  
the indicator  $\mathbb{I}(\ell_{\text{tri}}(a, i, j) > 0)$ .

# Log-ratio Loss

- Compared to the triplet rank loss, our loss
  - Captures continuous similarities between images better, (the triplet rank loss focuses only on partial ranks of similarities.)
  - Does not require any hyperparameter, (for the triplet rank loss the margin should be tuned carefully.)
  - Does not demand  $L_2$  normalization of the embedding vectors, (such a normalization is essential for the triplet rank loss.)
  - Performs much better with a low embedding dimension.

# Dense Triplet Sampling

- Main idea: Using all triplets within a minibatch



# Dense Triplet Sampling

- Why not using existing sampling techniques<sup>[1,11]</sup>
  - They rely on binary relations between images.
  - They are designed to be combined with conventional triplet losses.
  - The notion of hardness is not clear in our setting.
- Our sampling strategy is well matched with the log-ratio loss.
  - The log-ratio loss enables every triplet to well contribute to training.

$$\frac{\partial \ell_{\text{lr}}(a, i, j)}{\partial f_i} = \frac{(f_i - f_a)}{D(f_a, f_i)} \cdot 4 \left\{ \log \frac{D(f_a, f_i)}{D(f_a, f_j)} - \log \frac{D_y(\mathbf{y}_a, \mathbf{y}_i)}{D_y(\mathbf{y}_a, \mathbf{y}_j)} \right\}$$

Non-trivial even if the triplet complies the rank constraint

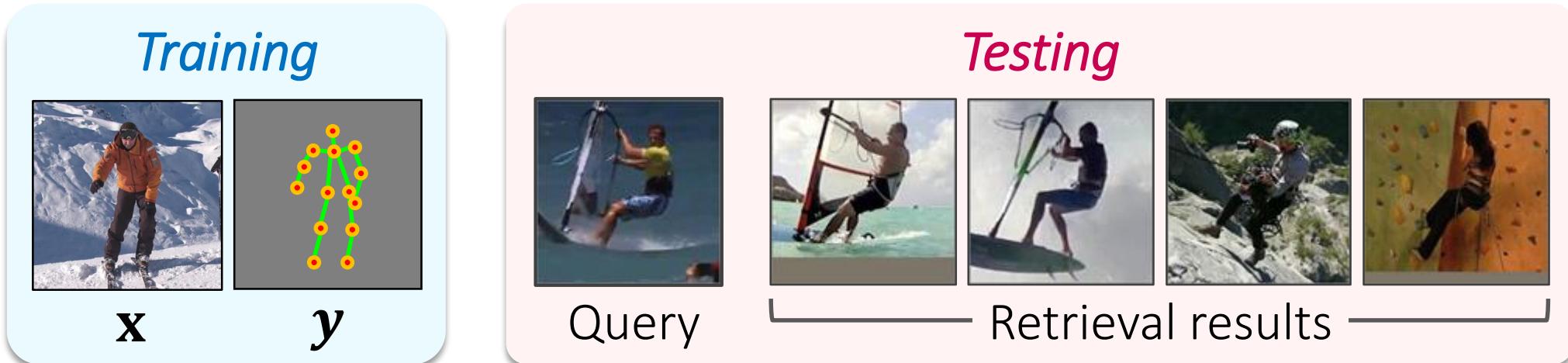
- *Exploiting all triplets improves embedding performance.*

[1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015

[11] Sampling matters in deep embedding learning, ICCV 2017

# Experiments – Three Retrieval Tasks

- Human pose retrieval

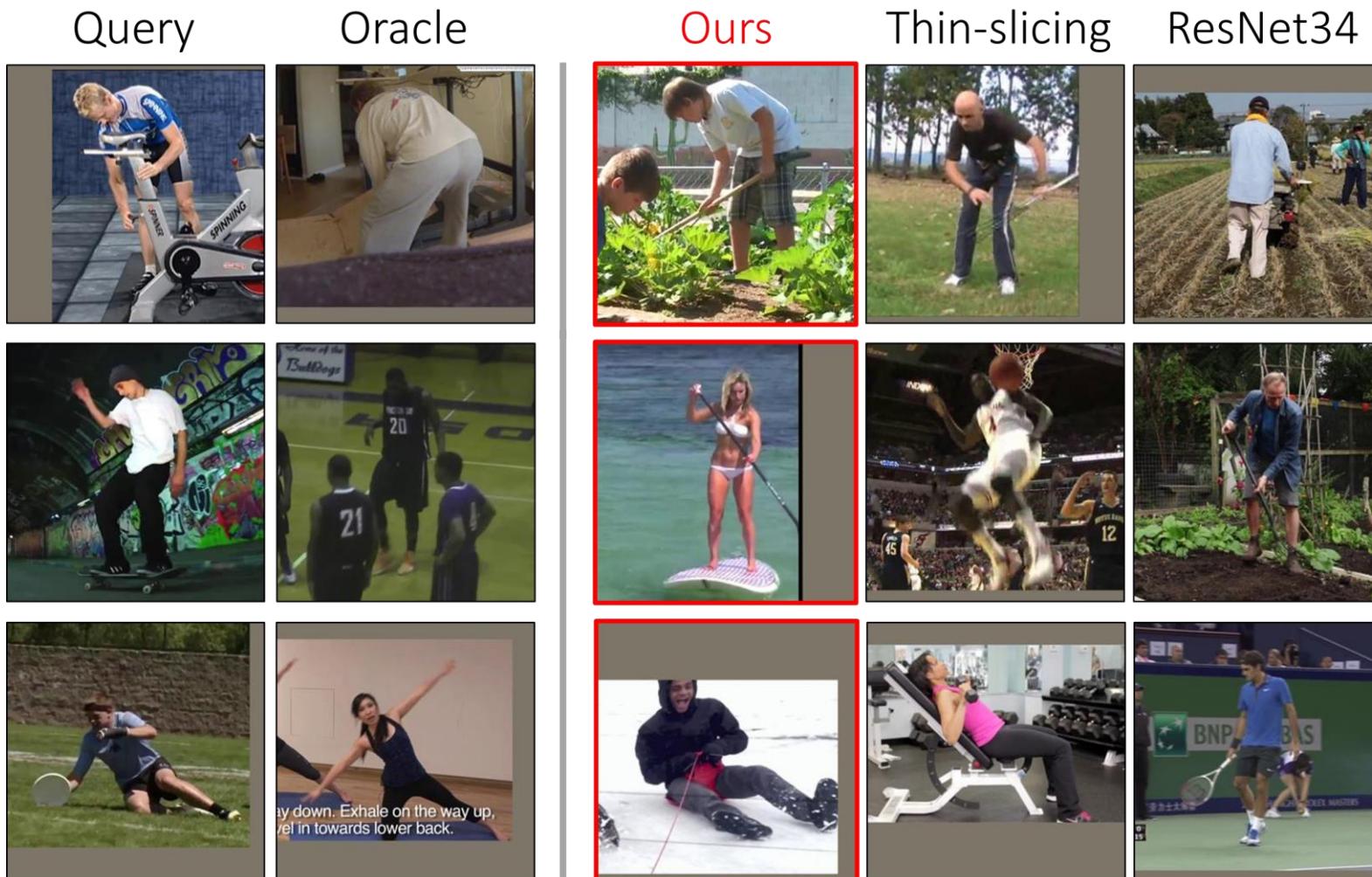


- Conducted on the *MPII human pose dataset*
- Application: *pose-aware representation for action recognition*
- Label distance between images:

$$D_y(y_i, y_j) = \|y_i - y_j\|_2^2.$$

# Experiments – Three Retrieval Tasks

- Human pose retrieval



ResNet34: ImageNet pre-trained network

Typically focuses on objects or background other than human poses.

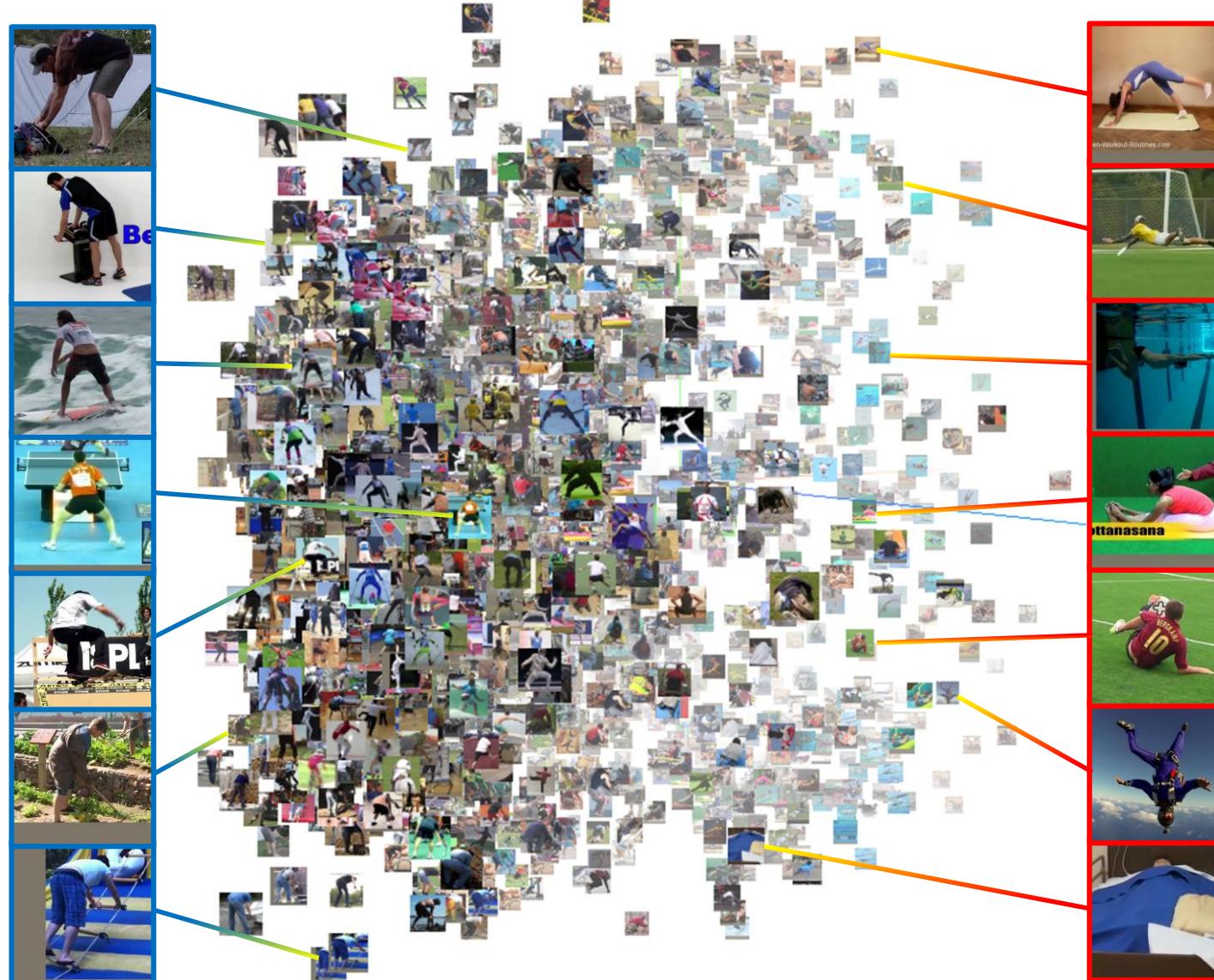
Thin-slicing<sup>[10]</sup>: A previous work on pose embedding

Often fails to address rare human poses.

[10] Thin-slicing for pose: Learning to understand pose without explicit pose estimation, CVPR 2016

# Experiments – Three Retrieval Tasks

- Human pose retrieval



# Experiments – Three Retrieval Tasks

- Room layout retrieval



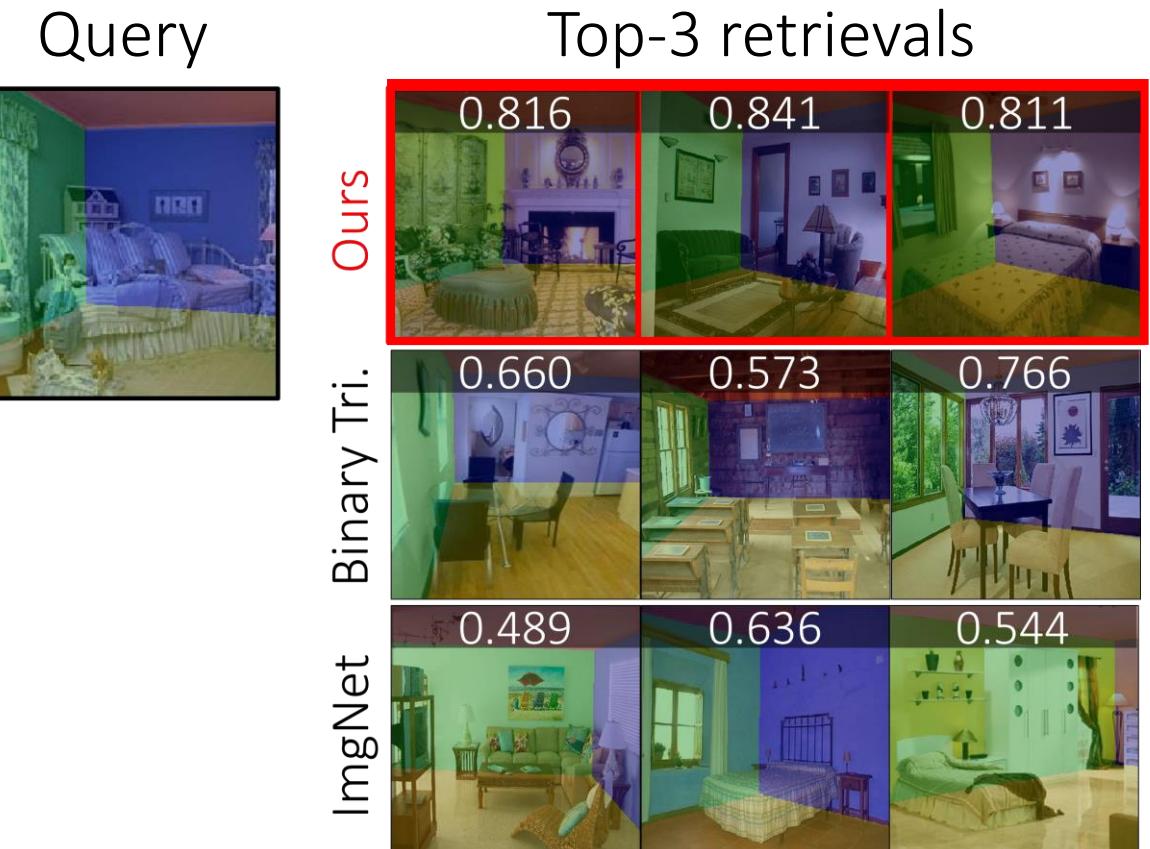
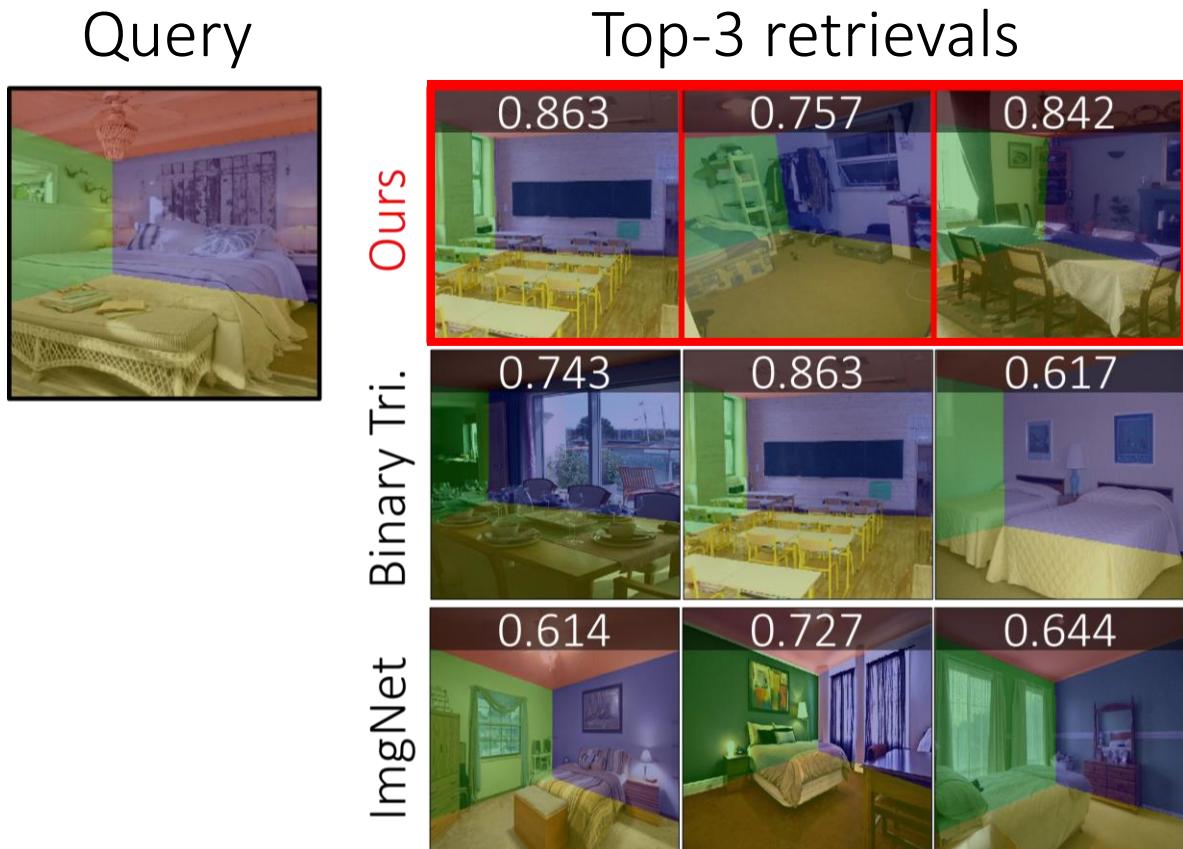
- Conducted on the *LSUN room layout dataset*
- Label distance between images:

$$D_y(\mathbf{y}_i, \mathbf{y}_j) = 1 - \text{mIoU}(\mathbf{y}_i, \mathbf{y}_j),$$

where  $\mathbf{y}_i$  and  $\mathbf{y}_j$  denote groundtruth room segmentations

# Experiments – Three Retrieval Tasks

- Room layout retrieval

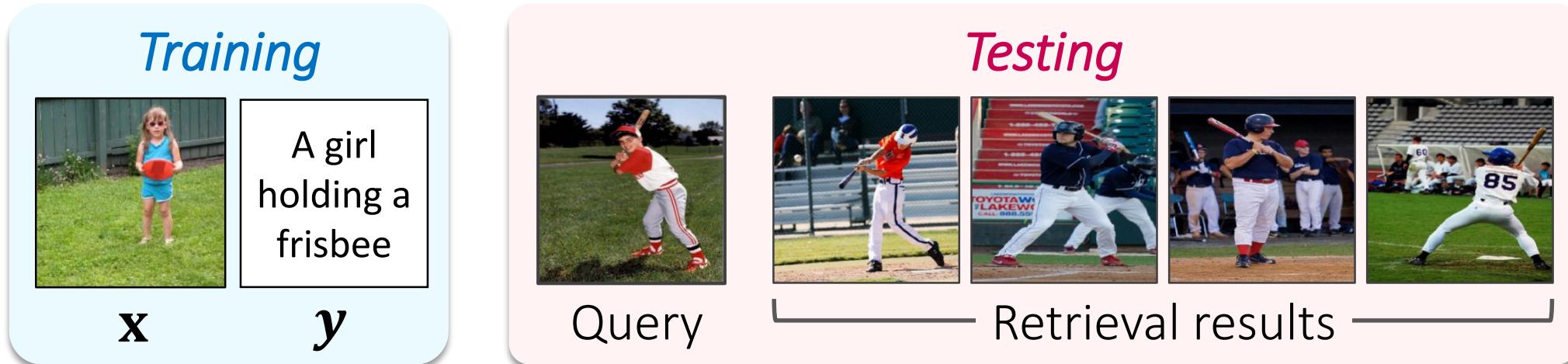


Binary Tri.: Triplet rank loss + Binary thresholding

ImgNet: ImageNet pre-trained ResNet101

# Experiments – Three Retrieval Tasks

- Caption-aware image retrieval



- Conducted on the *MS-COCO 2014 caption dataset*
- Label distance between images:

$$D_y(\mathbf{y}_i, \mathbf{y}_j) = \sum_{c_i \in \mathbf{y}_i} \min_{c_j \in \mathbf{y}_j} W(c_i, c_j) + \sum_{c_j \in \mathbf{y}_j} \min_{c_i \in \mathbf{y}_i} W(c_i, c_j),$$

where  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are sets of 5 captions and  $W(\cdot)$  is the WMD<sup>[12]</sup> between two captions

[12] From word embeddings to document distances, ICML 2015

# Experiments – Three Retrieval Tasks

- Caption-aware image retrieval

Query



Ours



Top-3 retrievals

Binary Tri.



ImgNet



Query



Ours



Top-3 retrievals

Binary Tri.



ImgNet



Binary Tri.: Triplet rank loss + Binary thresholding

ImgNet: ImageNet pre-trained ResNet101

# Experiments – Three Retrieval Tasks

- Caption-aware image retrieval

Query



Top-3 retrievals



Binary Tri.



ImgNet



Query



Ours



Binary Tri.



ImgNet

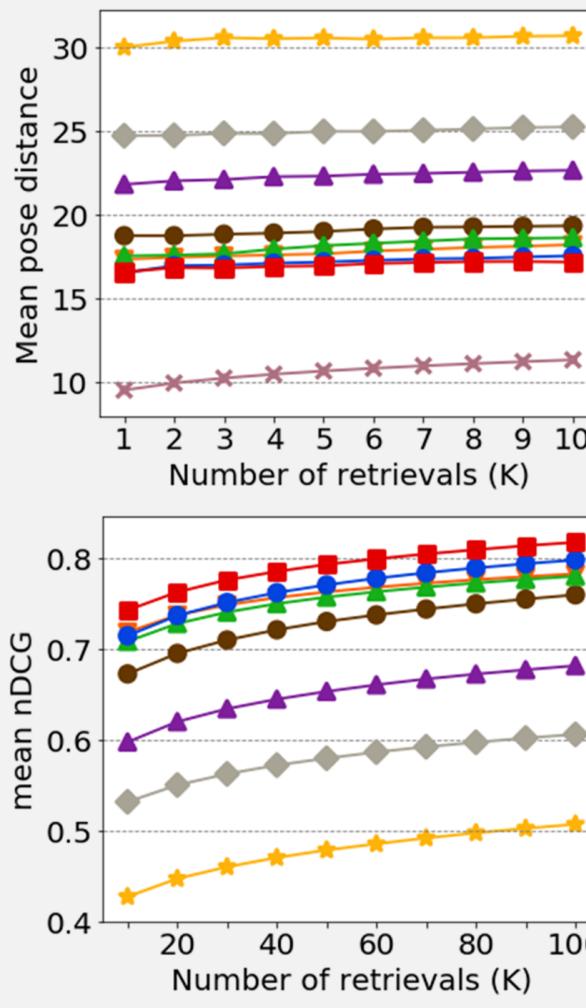


**Binary Tri.**: Triplet rank loss + Binary thresholding

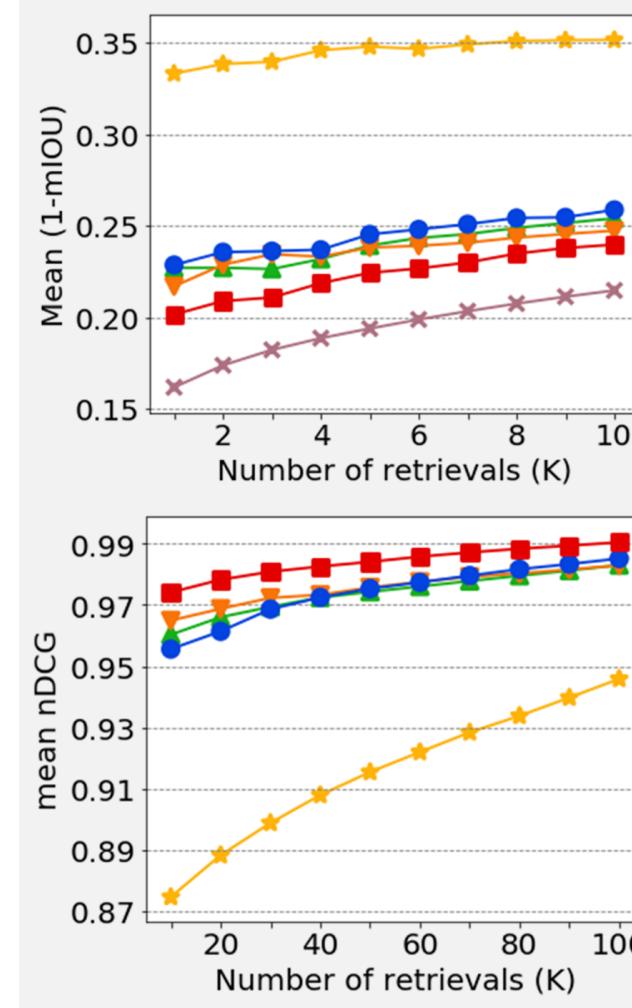
**ImgNet**: ImageNet pre-trained ResNet101

# Experiments – Three Retrieval Tasks

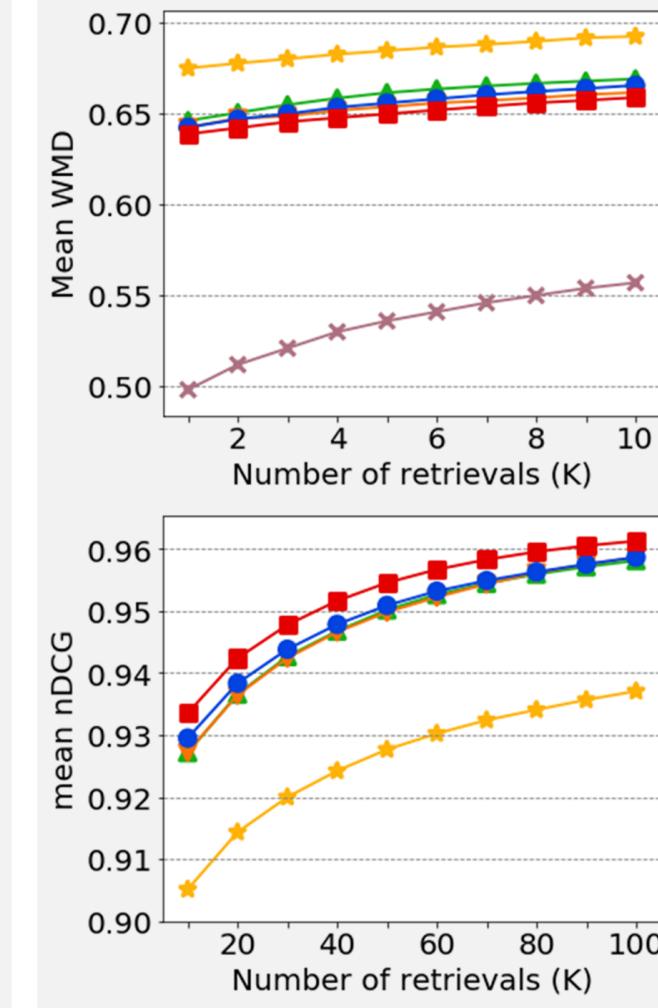
- Quantitative performance analysis



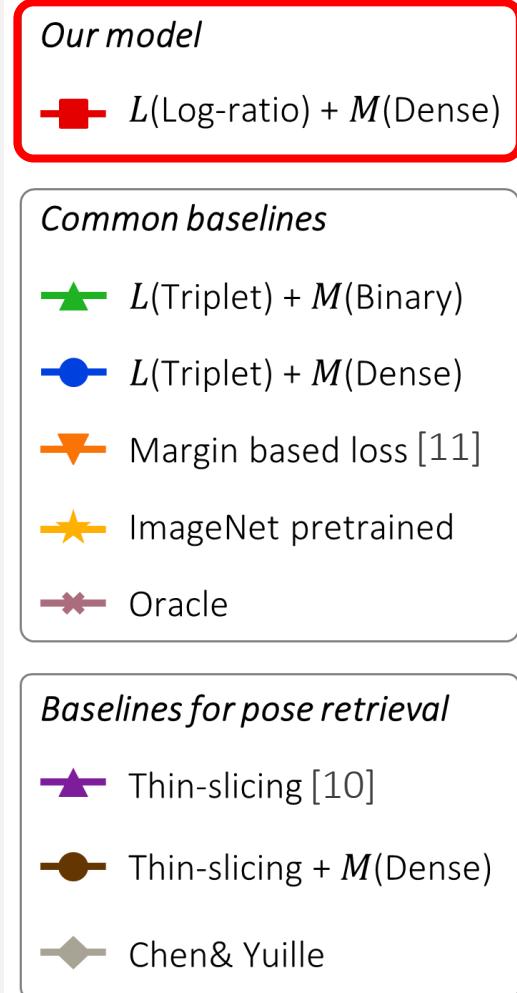
Human pose retrieval



Room layout retrieval

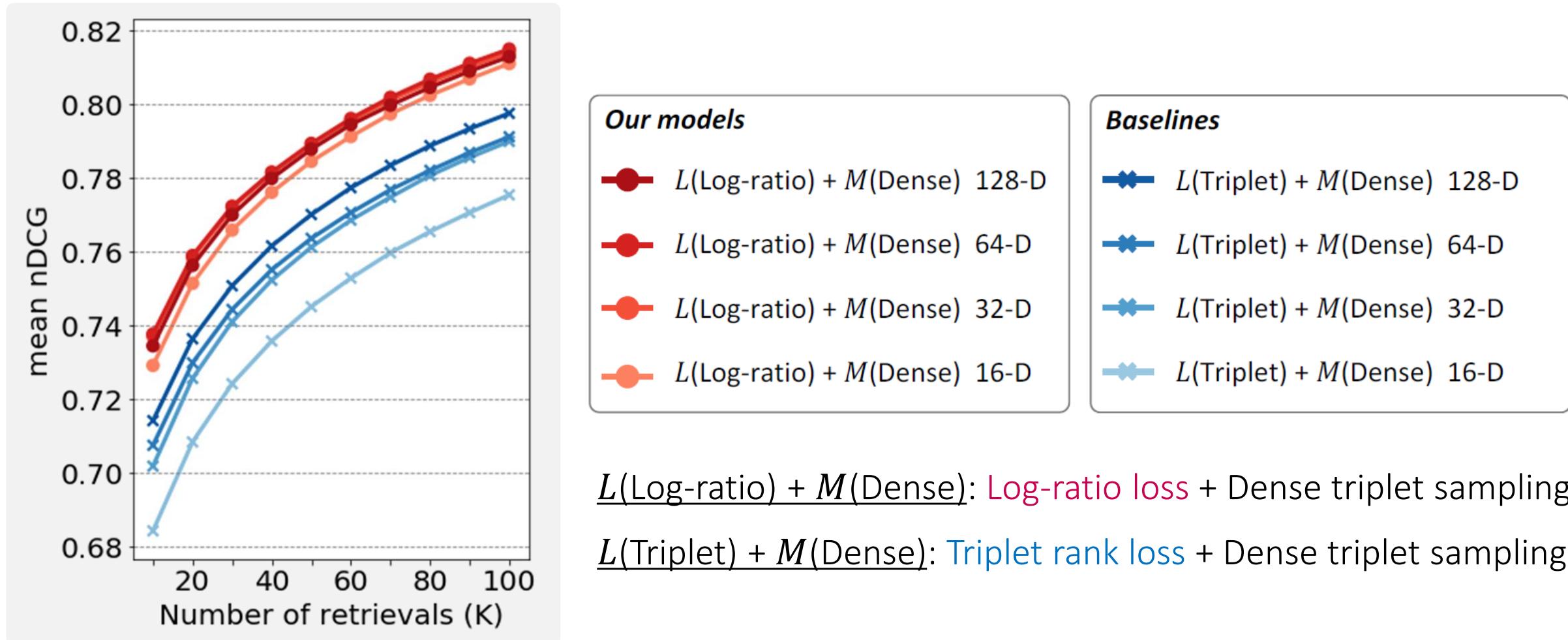


Caption-aware image retrieval



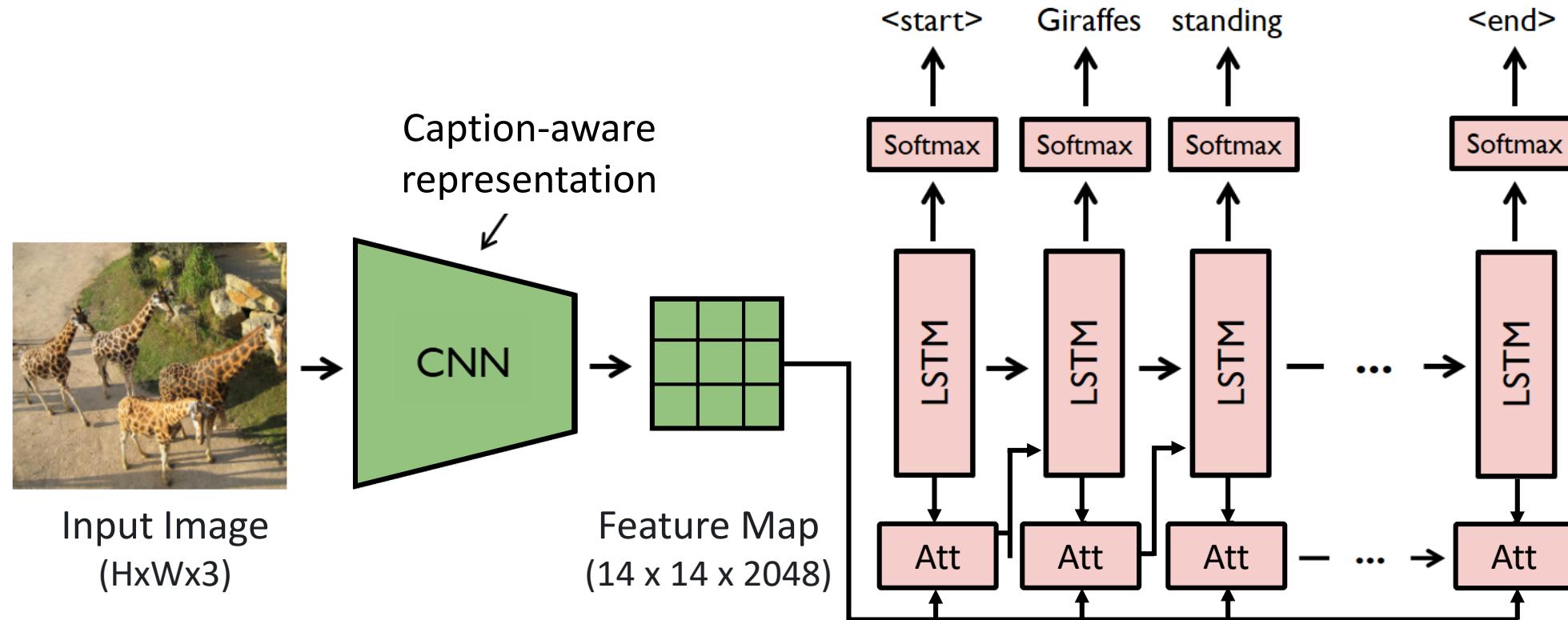
# Experiments – Three Retrieval Tasks

- Embedding dimension vs. retrieval performance



# Experiments – Representation Learning

- Representation learning for image captioning

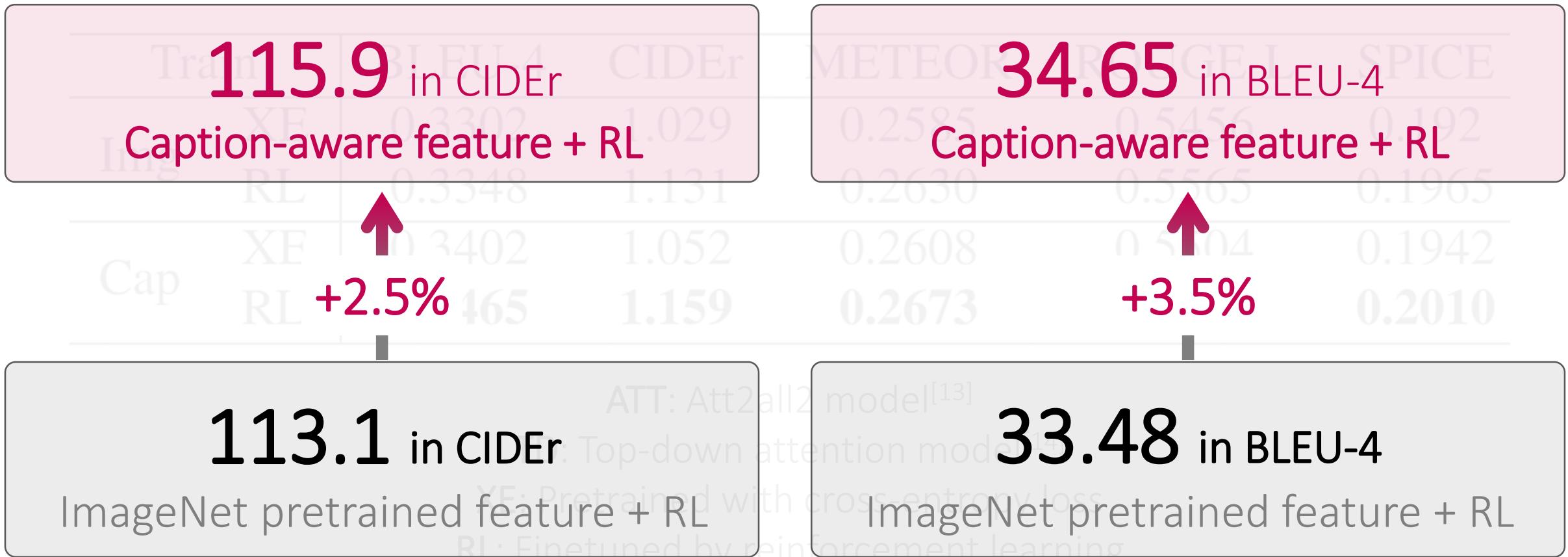


*Our approach*

Using the caption embedding network trained with caption similarities  
as an initial visual representation for image captioning

# Experiments – Representation Learning

- Quantitative results



[13] Self-critical sequence training for image captioning, CVPR 2017

[14] Bottom-up and top-down attention for image captioning and visual question answering, CVPR 2018

# Experiments – Representation Learning

- Qualitative results obtained by the top-down attention model



GT1	There are some zebras <b>standing</b> in a grassy field
GT2	A field with tall grass, bushes and trees, that has zebra <b>standing</b> in the field
Img XE	A group of zebras <b>grazing</b> in a field
Cap XE	Two zebras are <b>standing</b> in a grassy field
Img RL	A group of zebras are <b>grazing</b> in a field
Cap RL	A couple of zebras and a zebra <b>standing</b> in a field



GT1	A baseball batter <b>swinging</b> a bat over home plate
GT2	A baseball player <b>swings</b> a bat at a game
Img XE	A baseball player <b>holding</b> a bat on a field
Cap XE	A baseball player <b>swinging</b> a bat on top of a field
Img RL	A baseball player <b>holding</b> a bat on a field
Cap RL	A baseball player <b>swinging</b> a bat at a ball

# Conclusion

- Summary
  - A new framework for metric learning with continuous labels
  - Various applications including visual representation learning
  - Performance boost over existing approaches
- Future directions
  - A better distance metric for continuous and structured labels
  - A hard triplet mining technique for continuous metric learning
  - More applications of semantic nearest neighbor search
  - A new benchmark for continuous metric learning

# References

- [1] FaceNet: A unified embedding for face recognition and clustering, CVPR 2015
- [2] Beyond triplet loss: A deep quadruplet network for person re-identification, CVPR 2017
- [3] Learning to compare image patches via convolutional neural networks, CVPR 2015
- [4] Learning a similarity metric discriminatively with application to face verification, CVPR 2005
- [5] Improved deep metric learning with multi-class N-pair loss objective, NeurIPS 2016
- [6] No fuss distance metric learning using proxies, ICCV 2017
- [7] Deep metric learning via lifted structured feature embedding, CVPR 2016
- [8] Softtriple loss: Deep metric learning without triplet sampling, ICCV 2019
- [9] Pose embeddings: A deep architecture for learning to match human poses, arXiv 2015
- [10] Thin-slicing for pose: Learning to understand pose without explicit pose estimation, CVPR 2016
- [11] Sampling matters in deep embedding learning, ICCV 2017
- [12] From word embeddings to document distances, ICML 2015
- [13] Self-critical sequence training for image captioning, CVPR 2017
- [14] Bottom-up and top-down attention for image captioning and visual question answering, CVPR 2018

