

Linear Algebra:

Branch of Mathematics



Vectors, Matrices, Eigen value, Eigen vectors



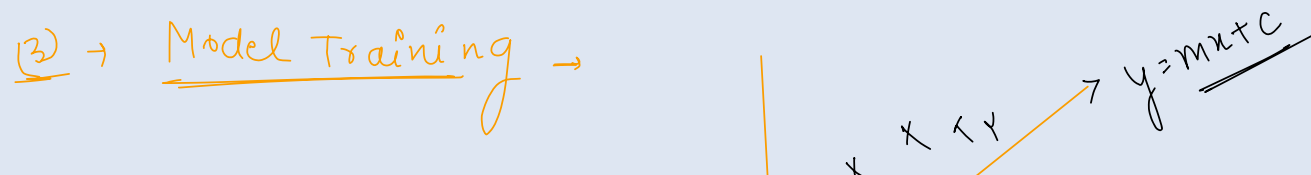
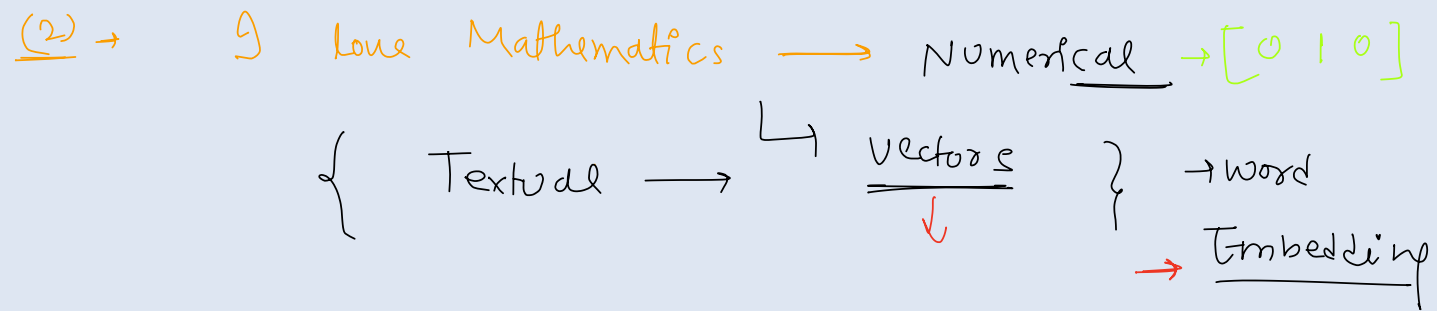
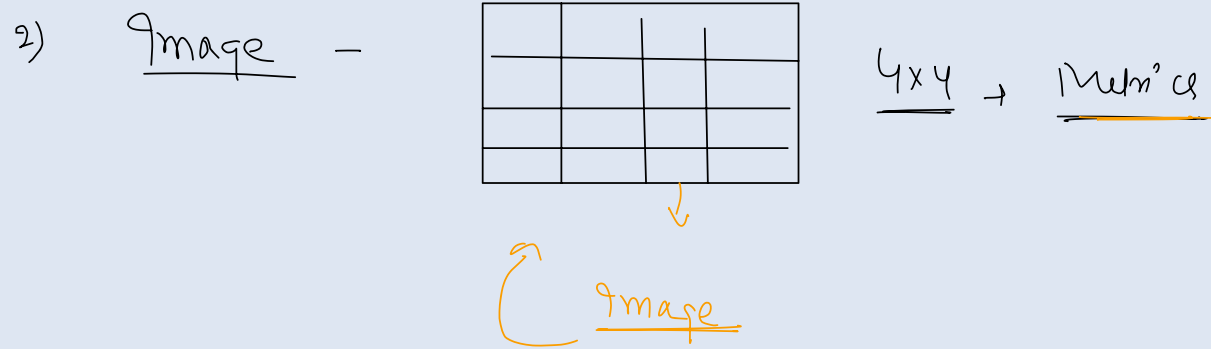
Linear Algebra

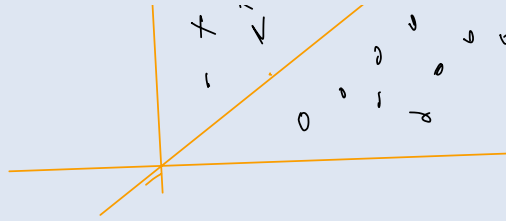
① Importance + Use Case → House (Data Representation)

1) Vectors → No Room Area Area Price

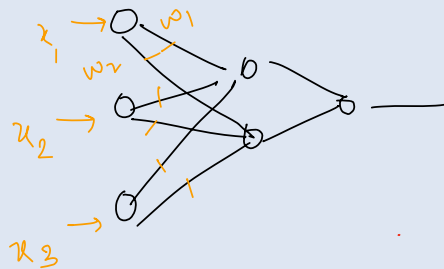
Data value 2 600sq 5ac 2100k

$[2 \quad 6 \quad 5 \quad 2100] \rightarrow \underline{\text{vector}}$





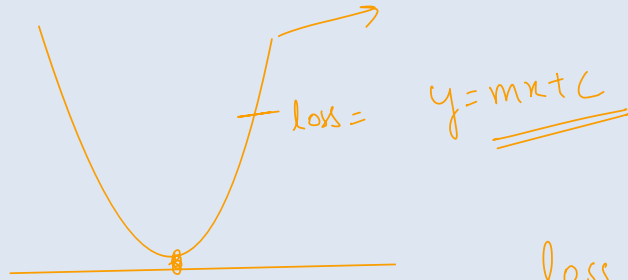
Neural Network →



$w_1, w_2, w_3, w_4, \dots$

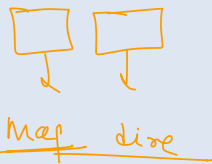
$$x_1 \times w_1 + w_2 \times x_2 \dots \dots$$

(4) Optimize →



loss / optimize .

(5) → Robotics → Movement →

Vector / 
map direction

6 → Data compression →

Dimensionality reduction →

Signal processing →

Recommendation Systems →

- vectors →
- 1) Vector
 - 2) Application
 - 3) operations → Sum, Sub,
 - 4) Data union.

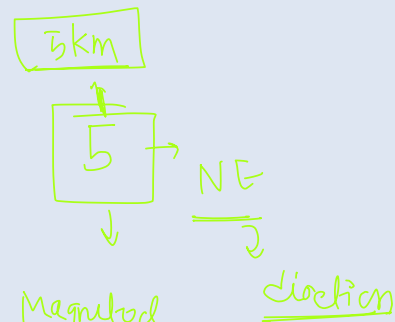
Day 2 \rightarrow Vectors -!

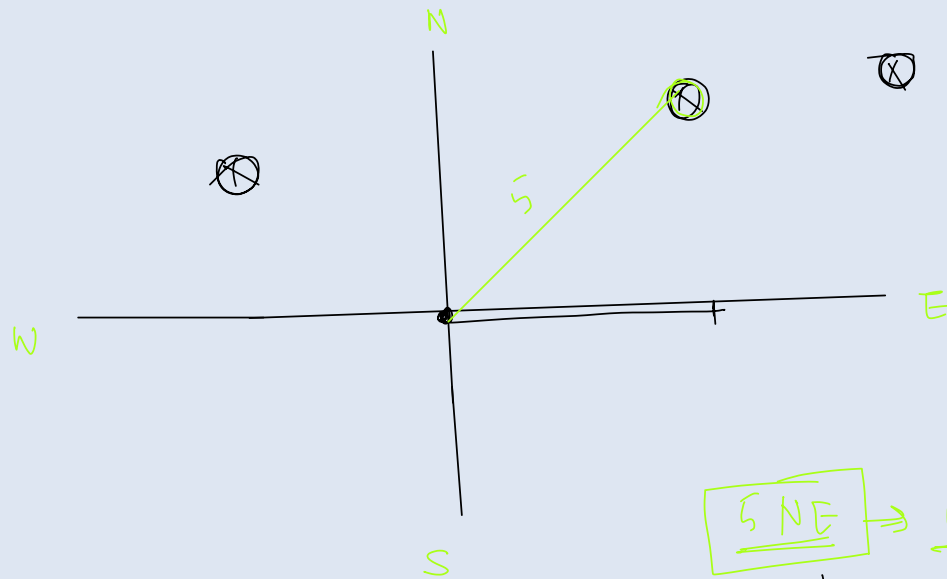
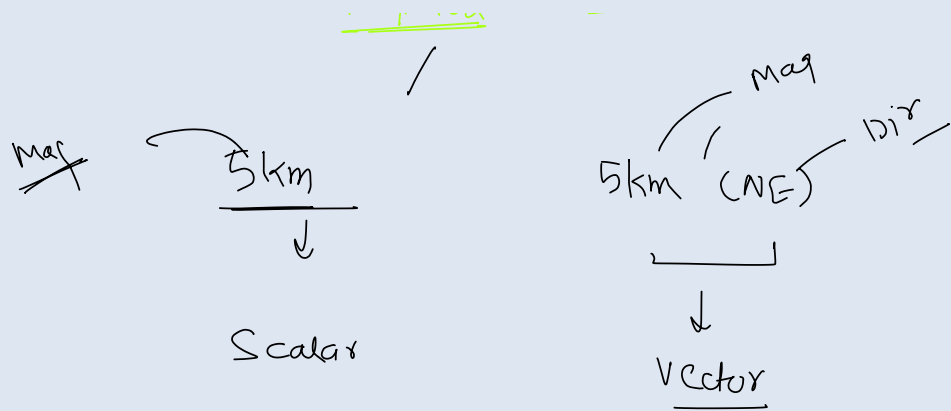
It is a collection of Number, representing data features, or data. It has both Magnitude & Direction

Scalar \Rightarrow Scalar has Magnitude but No direction (or dim)

Scalar (M)

Vector (D, M)





5 NE ⇒ Accurate.

Representation ⇒ $\begin{bmatrix} 5 \\ 1 \end{bmatrix}$

[5 1]

[5 1 3]

→

Multiple dimension

↓

Represent

Ex →

House → data features →

House ⇒

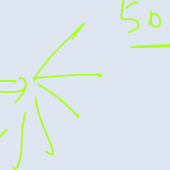
3 2 1
Rooms Bathroom Kitchen

↑ ↗ ↘
[3 2 1]

→

3 dimension

↓

Multiple feature ⇒  50

⊛

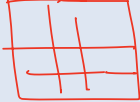
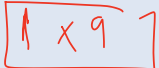
[1 2 3 50]

→

Multiple dimension

* Applications → Text Representation → NLP

I love Math → $\begin{bmatrix} [100] & [010] & [001] \end{bmatrix}$

(2) → Image processing →  → Matrix →
3x3
↓
 - vector

(3) → Recommendation System →

Day -3 →

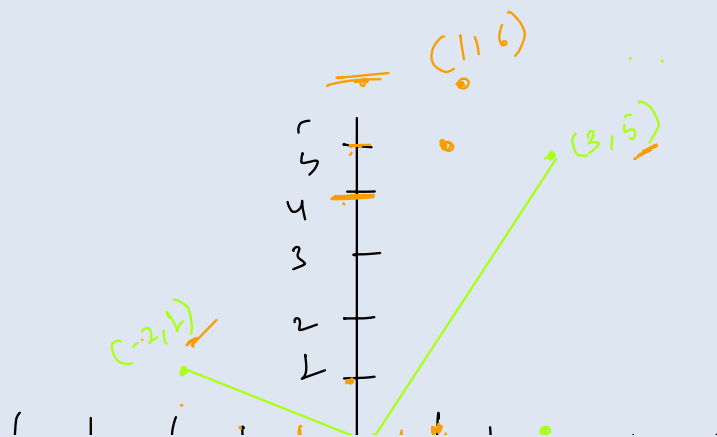
Adding of Vectors:

$$x = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$$

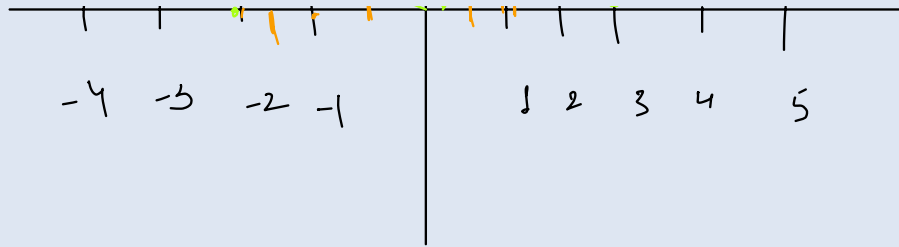
$$y = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

$$x + y =$$

$$x \begin{bmatrix} -2 \\ 1 \end{bmatrix} + \begin{bmatrix} 3 \\ 5 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 \\ 6 \end{bmatrix}$$



$$x \rightarrow -2 \dots \dots L$$



Machine

$$\textcircled{1} \rightarrow \begin{matrix} F_A = [-2, 5, 3] \\ F_B = [1, 2, 3] \end{matrix} \rightarrow \begin{matrix} F_C \\ [-1, 7, 6] \end{matrix}$$

$$\textcircled{2} \rightarrow \text{NLP} \rightarrow \begin{matrix} \text{good} \\ \downarrow \\ [1, 0, 0] \end{matrix} \quad \begin{matrix} \text{Movie} \\ \downarrow \\ [0, 1, 0] \end{matrix} \quad \begin{matrix} \text{'good movie'} \\ \rightarrow [1, 1, 0] \end{matrix}$$

(3) Recommendations \Rightarrow [History + Genre + Trends]

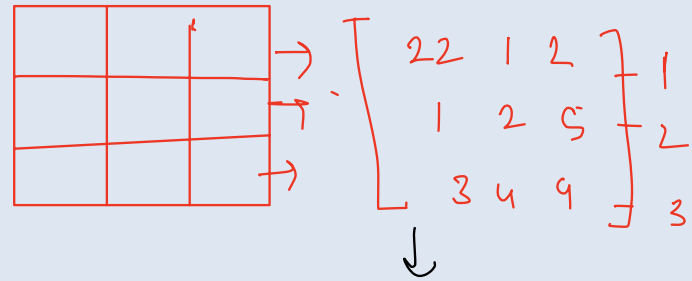
{ [] + [] + [] }

AI → Computer Vision →

RGB -



Grayscale



$$[22 + 1 + 3]$$

$$[1 + 2 + 4]$$

- 2) Dot product \cdot
- 3) cross product \otimes

KNN, SVM \rightarrow 2) Normalization of Vector

(3) \rightarrow projection of vector = $(P(A))$

(4) Euclidean (Distance formula) \rightarrow (NLP)

Scalar Multiplication

(1) \rightarrow

$$V = [2, 3]$$

k = scalar value = 5 learning (0.01)

$$\underline{kV} = k \cdot V = 2 \cdot [2, 3] \\ \downarrow \text{Scalar} \\ [2 \cdot 2, 2 \cdot 3] = [4, 6]$$

② →

$$V = [3, 4] \Rightarrow \frac{V}{|V|} = \underline{\text{Unit (direction)}}$$
$$|V| = 5$$

$$[3, 4]$$

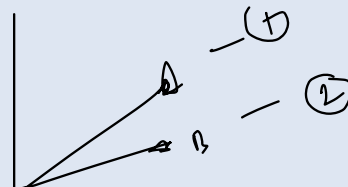
$$|V| \Rightarrow \sqrt{(3)^2 + (4)^2} = \sqrt{9+16} = \sqrt{25} = \underline{5}$$

$$= \left[\frac{3}{5}, \frac{4}{5} \right] \rightarrow \underline{\text{Normalized Vector}}$$

③ →

Vector projection →

$$\text{proj} \rightarrow \frac{10}{5} \rightarrow \underline{2}$$



$$V_1 = [3, 4]$$

$$V_2 = [1, 2]$$

$$P_{\text{proj } V_1 \text{ on } V_2} \Rightarrow P_{V_1} \Rightarrow \frac{V_1 \cdot V_2}{|V_2|^2} \cdot V_2$$

$$V_1 \cdot V_2 = (3 \times 1 + 4 \times 2) = [3, 8] = \underline{\underline{11}}$$

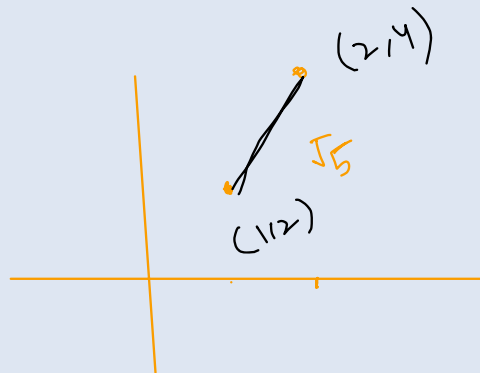
$$|V_2|^2 = [(1)^2 + (2)^2] = 1 + 4 = \underline{\underline{5}}$$

$$\Rightarrow \frac{11 \cdot (V_2)}{5} \quad 11 [1, 2]$$

$$= \begin{bmatrix} 11 & 22 \end{bmatrix}$$

Distance Calculation

$$\textcircled{*} \quad v_1 = \begin{matrix} x_1 & y_1 \\ [1, 2] \end{matrix}$$
$$v_2 = \begin{matrix} x_2 & y_2 \\ [2, 4] \end{matrix}$$



$$\text{Euclidean Formula} \Rightarrow \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\Rightarrow \sqrt{(2-1)^2 + (4-2)^2} \Rightarrow \sqrt{1^2 + 2^2}$$
$$\underline{\underline{\sqrt{5}}}$$