

Established in collaboration with MIT

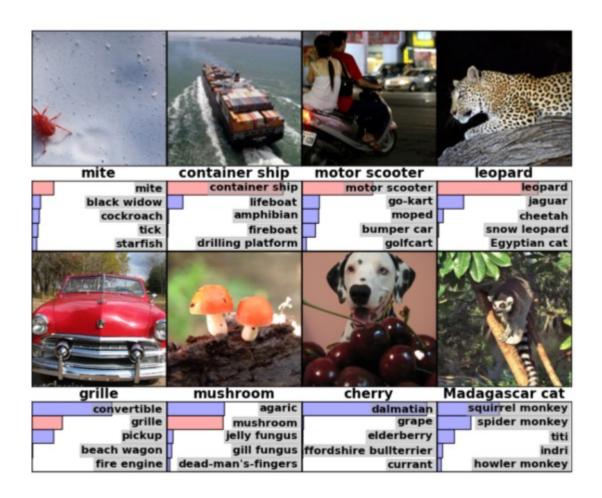
Introduction to Deep Learning

Soujanya Poria

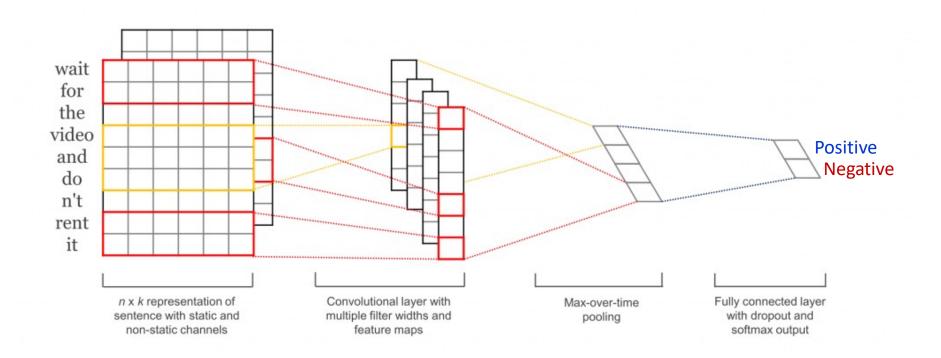
Objectives

- Understand the basic structure of a neural network, particularly a Multi-layer Perceptron
- Understand the various steps in training a neural network

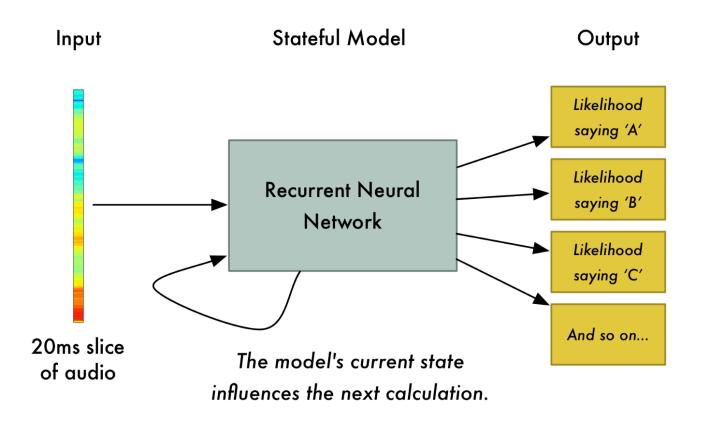
Examples: Images



Examples: Text



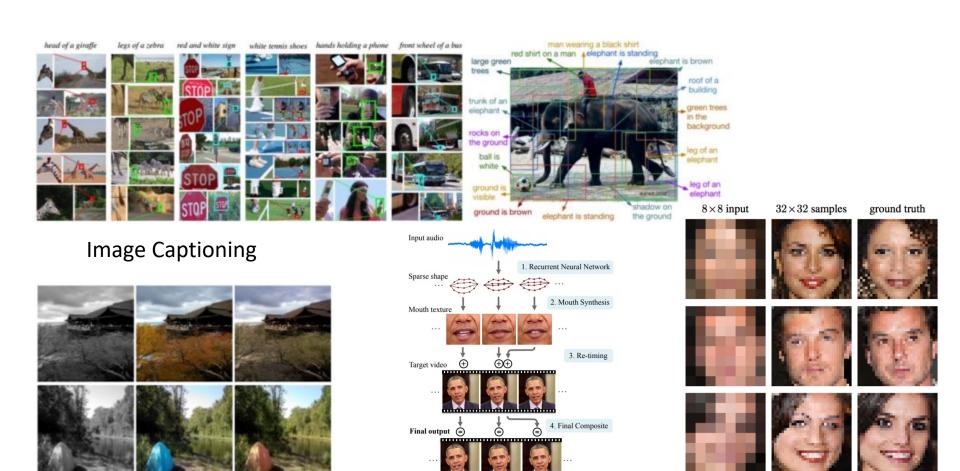
Examples: Audio



https://medium.com/@ageitgey/machine-learning-is-fun-part-6-how-to-do-speech-recognition-with-deep-learning-28293c162f7a

Various other examples

Colouring B&W Photos



Synthesizing Speech Image Super-resolution

Why Deep Learning?

1952 1958 • • • • • • • • • • •

Stochastic Gradient Descent

Perceptron

Learnable Weights

Backpropagation

• Multi-Layer Perceptron

Deep Convolutional NN

Digit Recognition

Neural Networks date back decades, so why the resurgence?

I. Big Data

- Larger Datasets
- Easier
 Collection &
 Storage







2. Hardware

- Graphics
 Processing Units
 (GPUs)
- Massively Parallelizable



3. Software

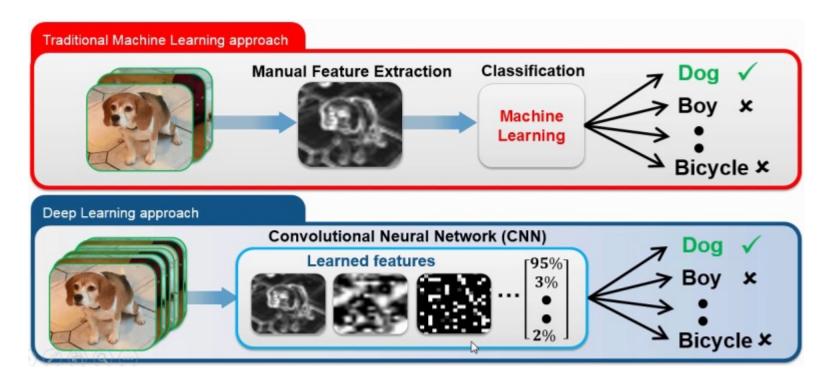
- Improved Techniques
- New Models
- Toolboxes



Why Deep Learning?

Accuracy neural networks other approaches Scale (data size, model size)

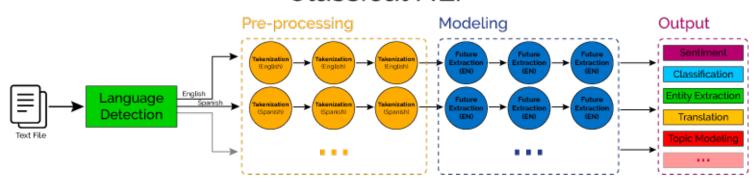
Differences

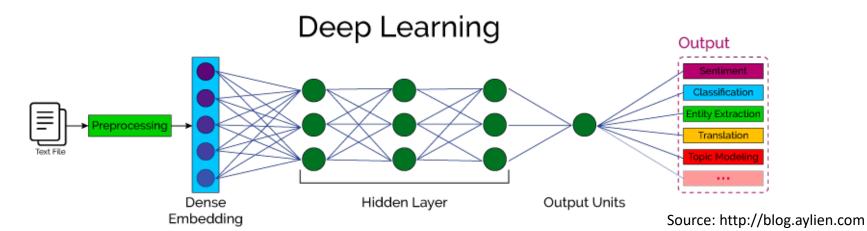


https://leonardoaraujosantos.gitbooks.io/artificial-inteligence/content/deep learning.html

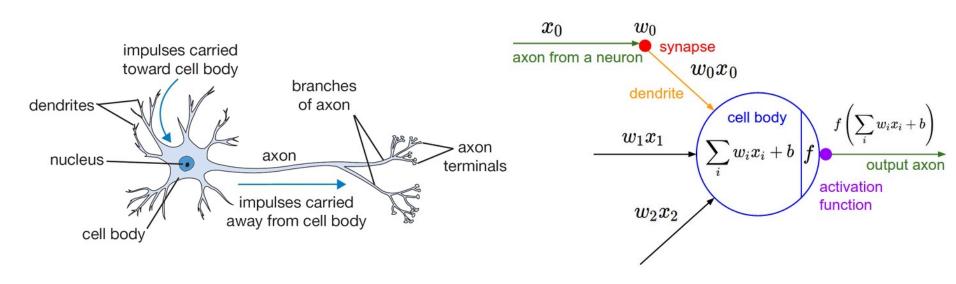
Differences

Classical NLP



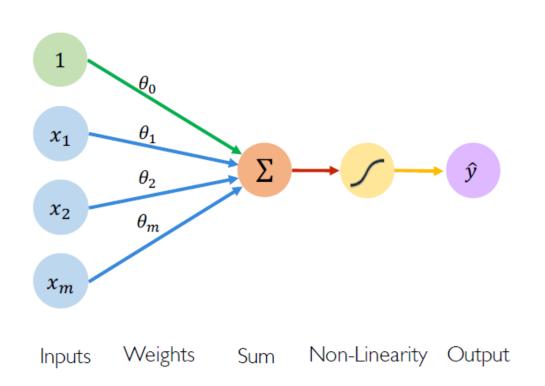


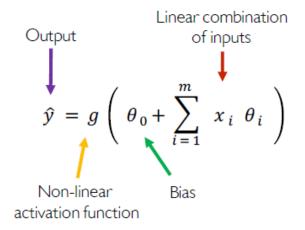
Inspiration behind Neural Networks



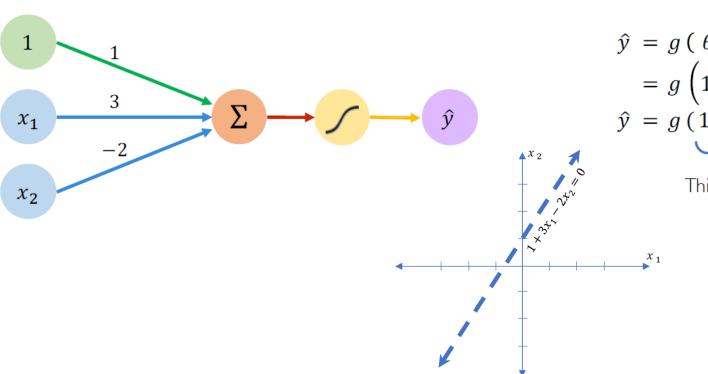
http://cs231n.github.io/neural-networks-1/

Perceptron





Why Non-linear Activation?



We have:
$$\theta_0 = 1$$
 and $\boldsymbol{\theta} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$

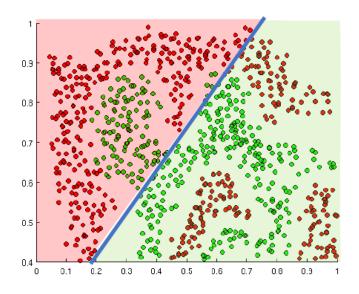
$$\hat{y} = g \left(\theta_0 + X^T \theta \right)$$

$$= g \left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 3 \\ -2 \end{bmatrix} \right)$$

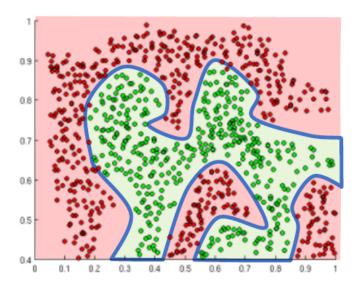
$$\hat{y} = g \left(1 + 3x_1 - 2x_2 \right)$$

This is just a line in 2D!

Why Non-linear Activation?



Linear Activation functions produce linear decisions no matter the network size

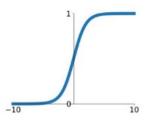


Non-linearities allow us to approximate arbitrarily complex functions

Activation Functions

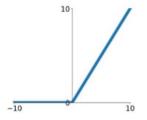
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



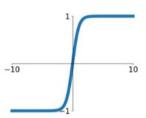
ReLU

 $\max(0, x)$



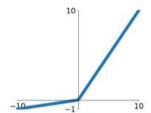
tanh

tanh(x)



Leaky ReLU

 $\max(0.1x, x)$



Activation Functions

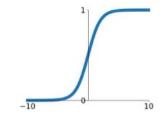
Main problem with Sigmoid and tanh activation

Vanishing gradient problem

- Issue of exceeding small gradients when training neural networks
- Worse with multiple layers in a NN

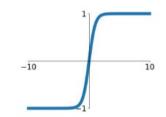
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



Additional problem with Sigmoid Slower convergence than tanh

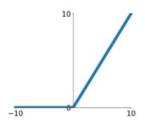
tanh



Activation Functions

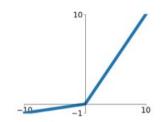
- Rectified Linear Units (ReLU)
 - Developed to overcome the vanishing gradient problem
 - However, some neuron may "die"

ReLU $\max(0, x)$

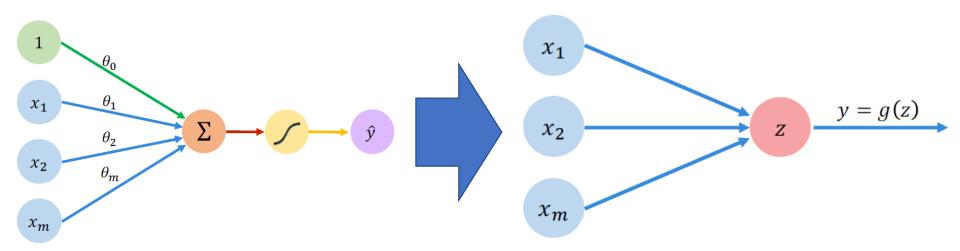


- Leaky ReLU
 - Prevents neurons from "dying" by using a small negative slope

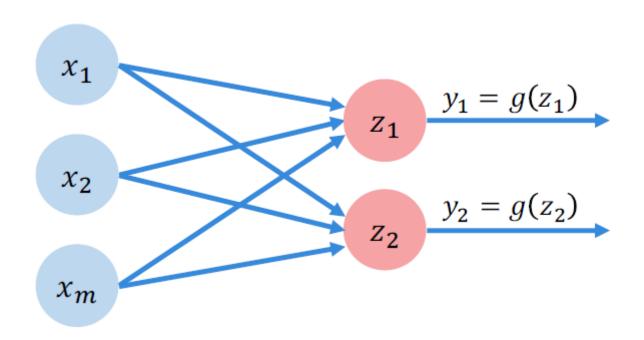
Leaky ReLU max(0.1x, x)



Simplifying the Perceptron

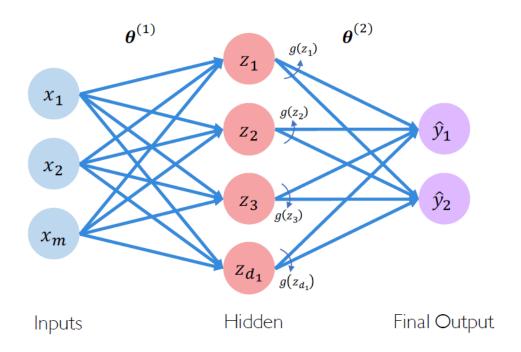


Multiple Perceptron



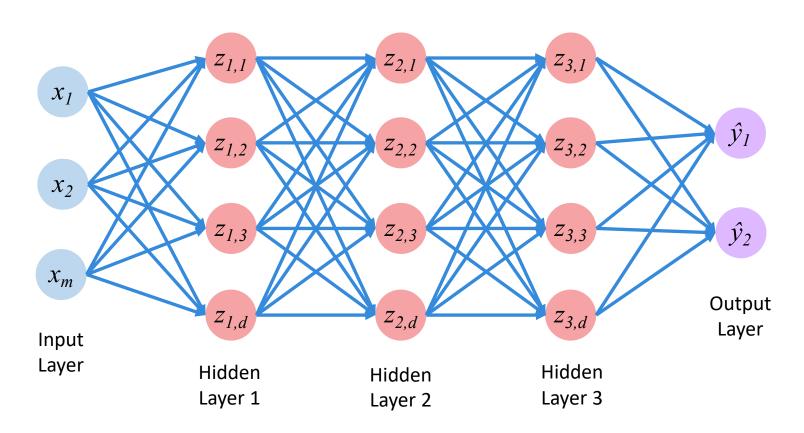
Neural Network

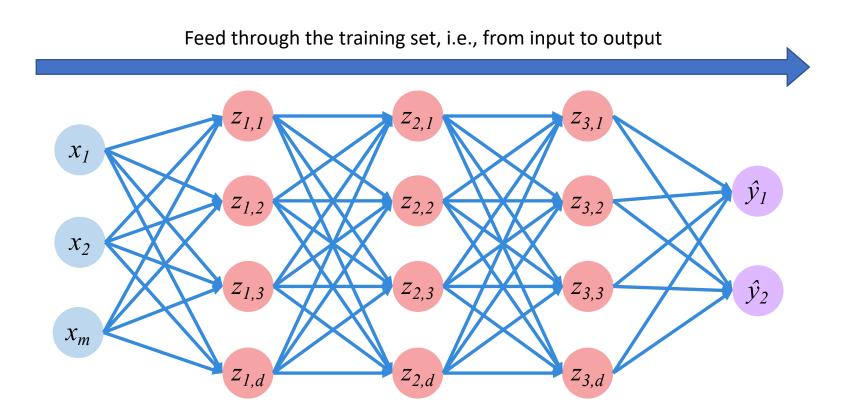
• Multiple perceptrons, aka a Multi-layer Perceptron (MLP)

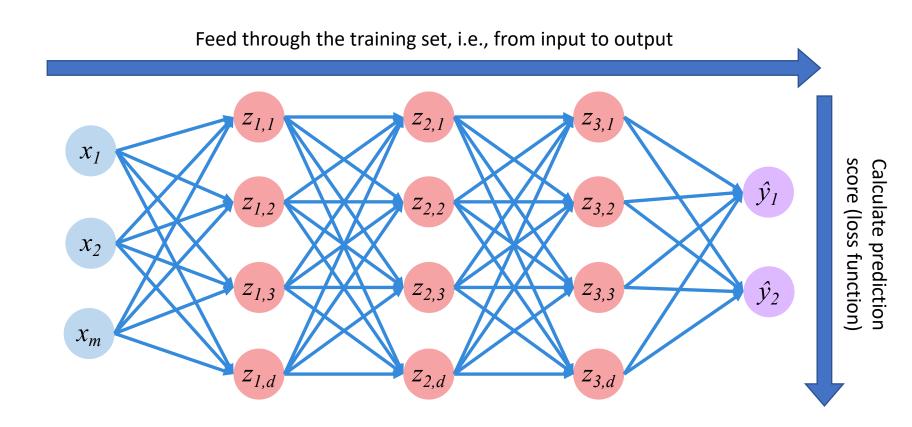


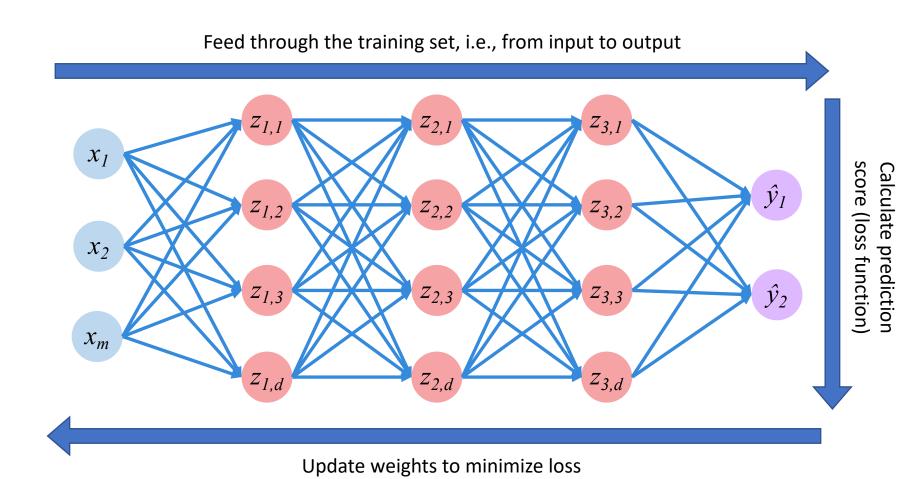
Deep Neural Network

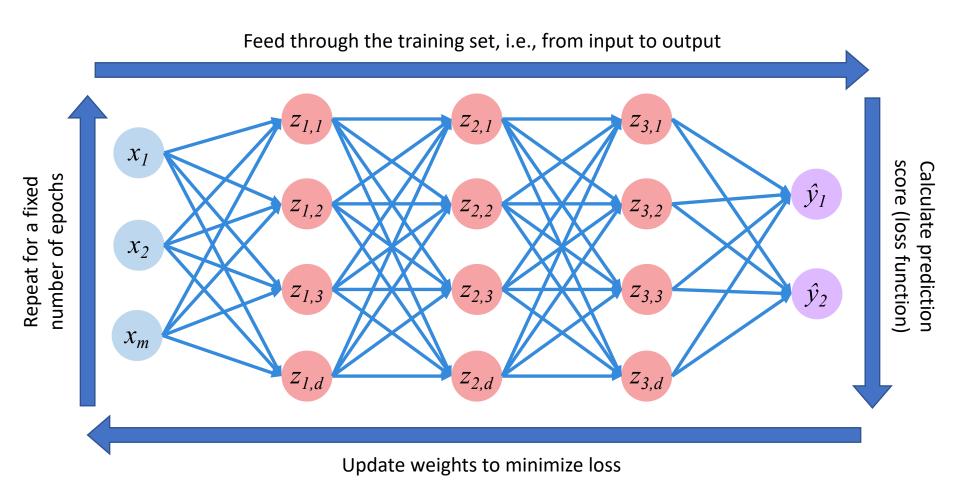
Adding on multiple hidden layers









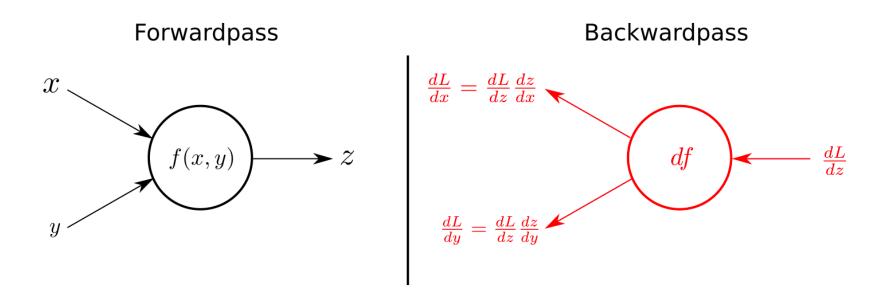


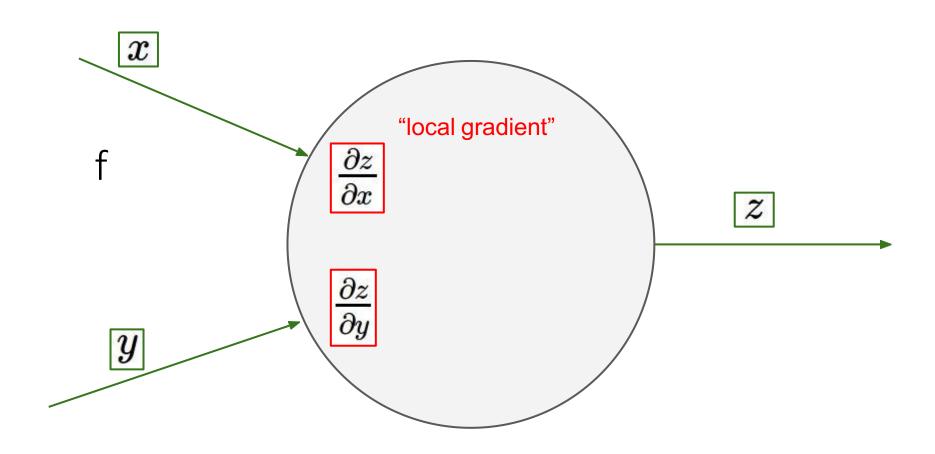
- What type of loss function?
- How to learn and update weights?
- How much training data to use?

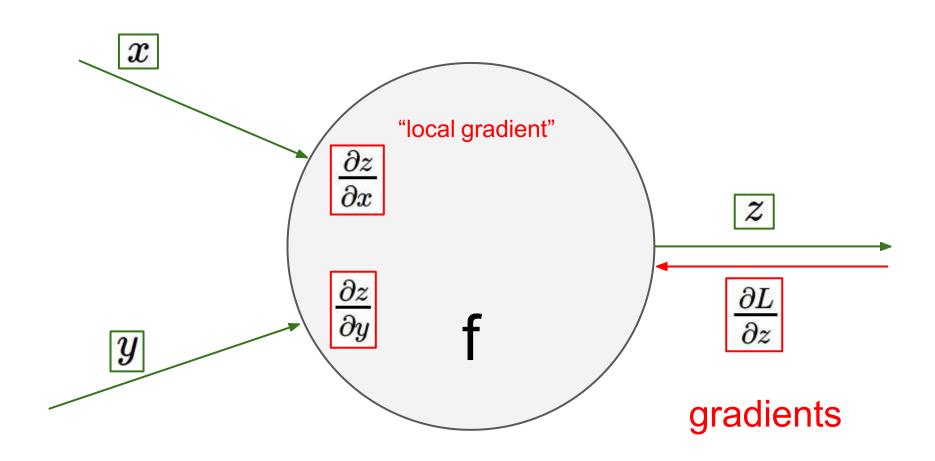
Forward propagation and Backpropagation

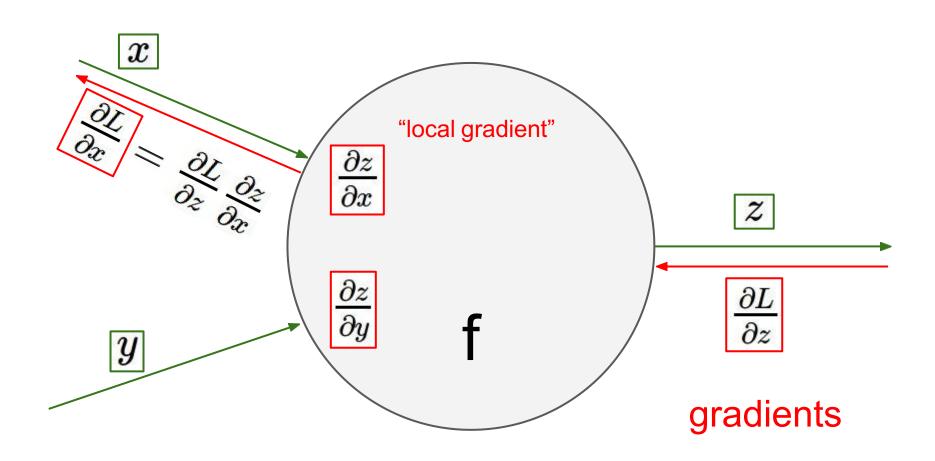
- 1. Given inputs and the labels first do forward propagation through the network. It is done by feeding the input to the network. Finally, we will get an output from the last layer. This process is called forward propagation.
- 2. Calculate the error/loss and gradients of the loss with respect to each of the parameters in the network. The error/loss is the difference between the network generated output and the actual output in the training dataset.
- 3. Backpropagate the gradients and update/tune the weights using gradient descent technique. This process is called backpropagation.

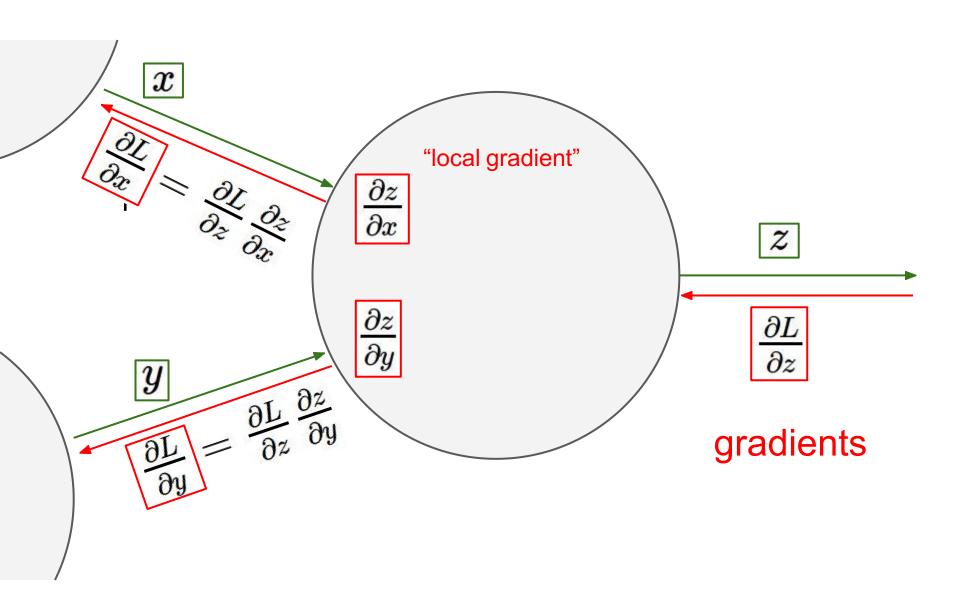
Forward propagation and Backpropagation



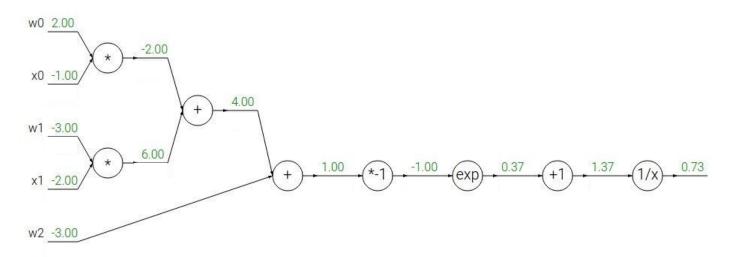








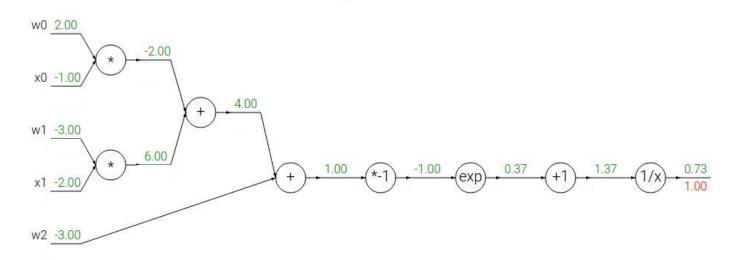
$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



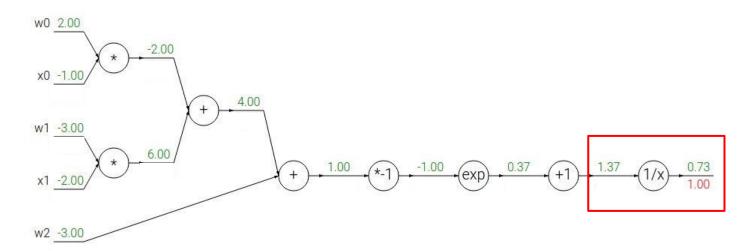
Calculate the gradient of the LOSS with respect to w0, x0, w1, x1 and w2.

Another example:

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



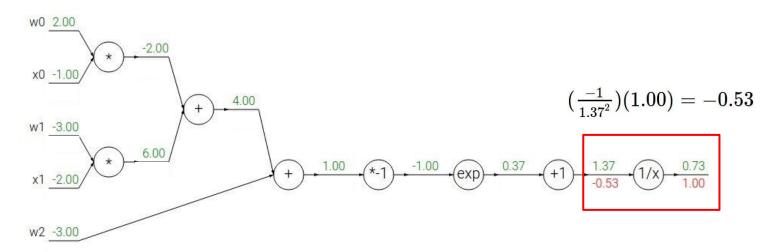
$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x) = e^x \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx} = e^x \hspace{1cm} f(x) = rac{1}{x} \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx} = -1/x^2 \hspace{1cm} f_c(x) = ax \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx} = a \hspace{1cm} f_c(x) = c + x \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx} = 1$$

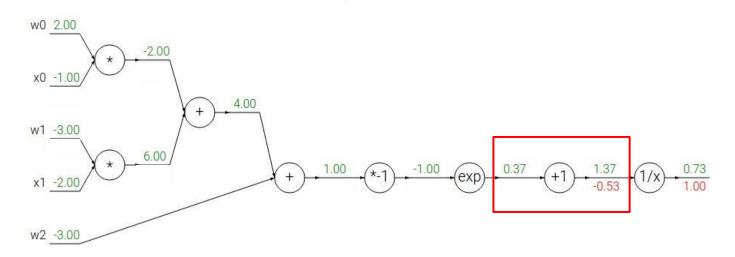
Another example:

$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x)=e^x \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx}=e^x \hspace{1cm} f(x)=rac{1}{x} \hspace{1cm}
ightarrow \hspace{1cm} rac{df}{dx}=-1/x^2 \hspace{1cm} f_c(x)=ax \hspace{1cm}
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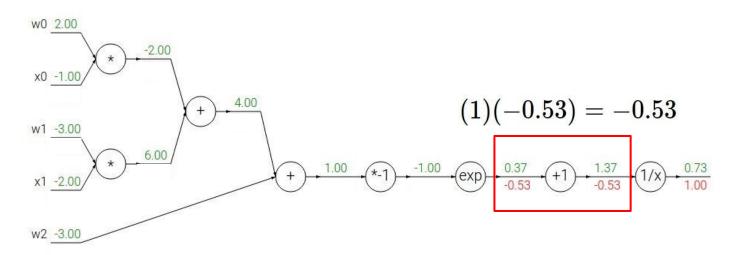
$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x \hspace{1cm} o \hspace{1cm} rac{df}{dx} = e^x \hspace{1cm} f(x) = rac{1}{x} \hspace{1cm} o \hspace{1cm} rac{df}{dx} = -1/x^2 \ f_a(x) = ax \hspace{1cm} o \hspace{1cm} rac{df}{dx} = a \hspace{1cm} f(x) = c + x \hspace{1cm} o \hspace{1cm} rac{df}{dx} = 1$$

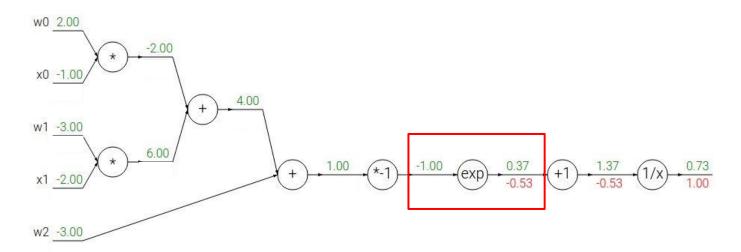
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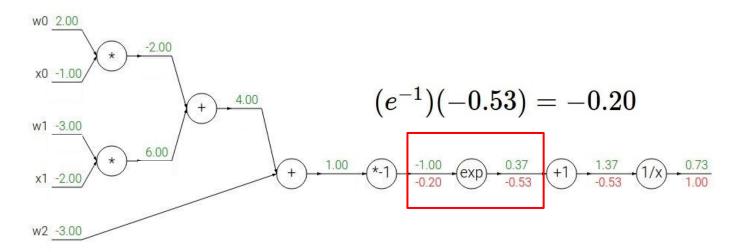
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$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$

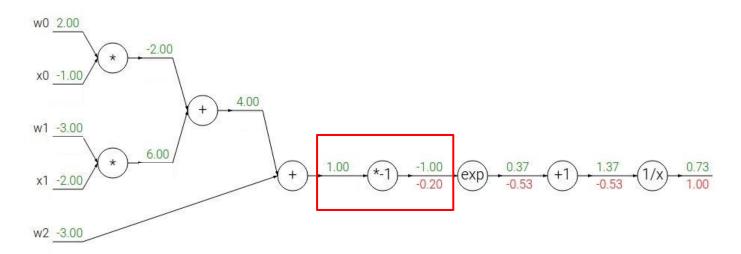


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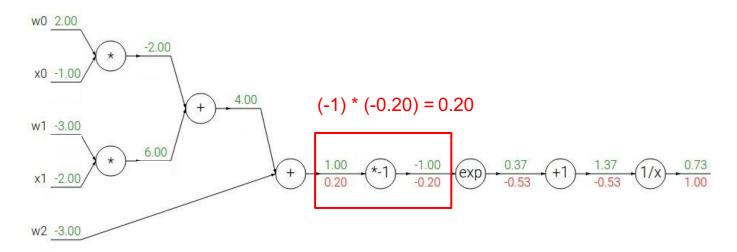
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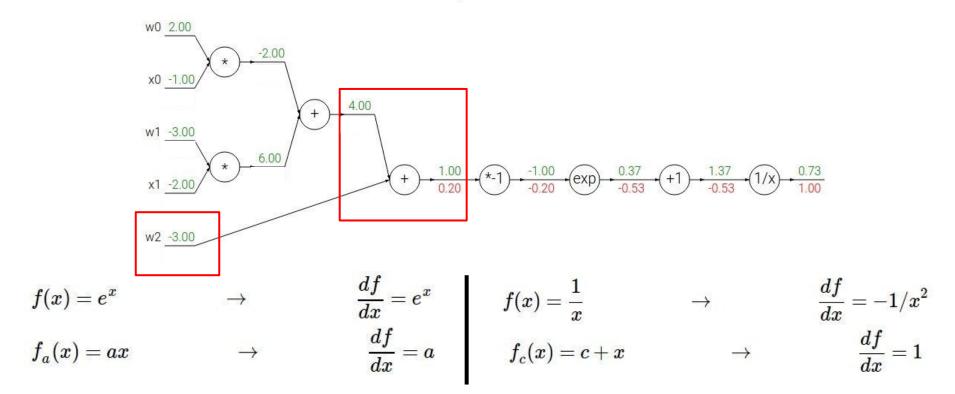
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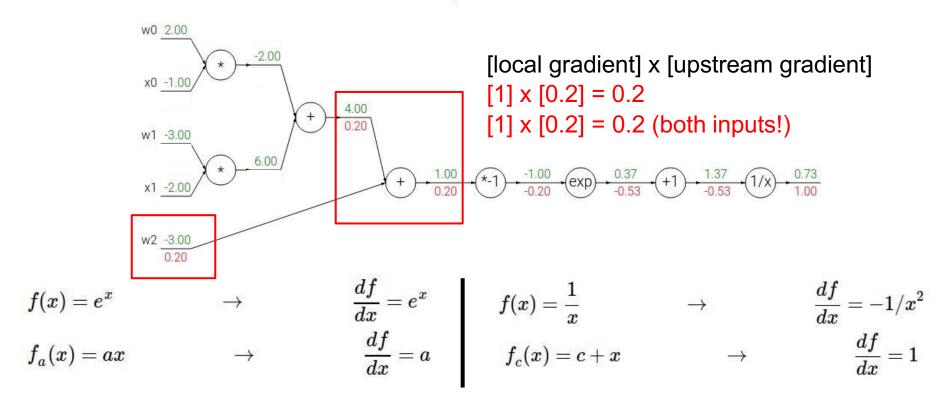
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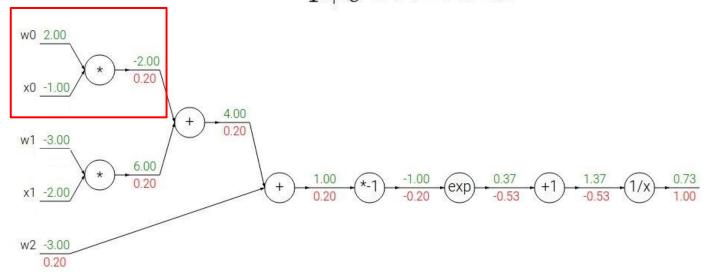


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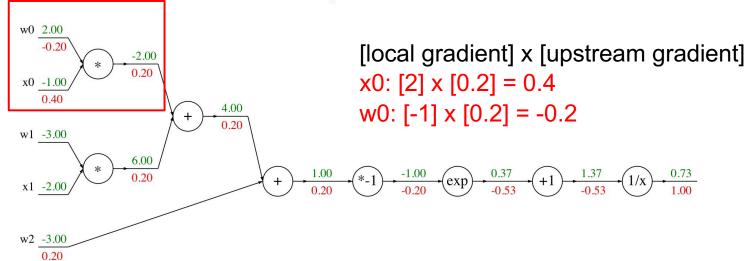
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$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



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$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$

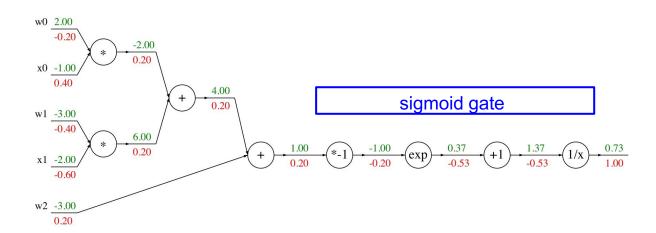


$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$

$$\sigma(x) = rac{1}{1+e^{-x}}$$

sigmoid function

$$rac{d\sigma(x)}{dx} = rac{e^{-x}}{(1+e^{-x})^2} = \left(rac{1+e^{-x}-1}{1+e^{-x}}
ight) \left(rac{1}{1+e^{-x}}
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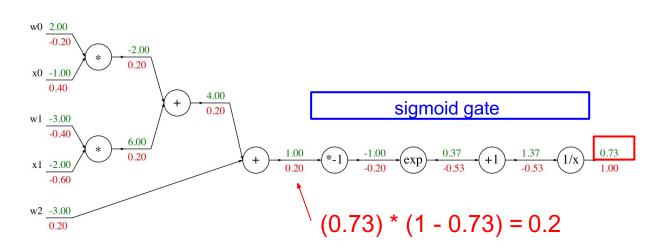


$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$

$$\sigma(x) = \frac{1}{1+e^{-x}}$$

sigmoid function

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ight)\sigma(x)$$



Logistic regression: binary classification

The loss function is -

$$: L(w) = -\frac{1}{m} \sum_{i=1}^{m} [y^{(i)} logh(x^{(i)}) + (1 - y^{(i)}) log(1 - h(x^{(i)}))]$$

 $x^{(i)}$ is a vector for all x_i (j=0,1,...,n), and $y^{(i)}$ is the target value for this example.

$$h(x) = \frac{1}{1 + e^{-w^T x}}$$

Softmax

- Use softmax for multi-class classification
 - K is the number classes

$$P(y = j \mid z^{(i)}) = \phi_{softmax}(z^{(i)}) = \frac{e^{z^{(i)}}}{\sum_{j=0}^{k} e^{z_k^{(i)}}},$$

where we define the net input z as

$$z = w_0 x_0 + w_1 x_1 + \ldots + w_m x_m = \sum_{l=0}^m w_l x_l = \mathbf{w}^T \mathbf{x}.$$

The loss function is
$$H(y,p) = -\sum_i y_i log(p_i)$$

Softmax vs Sigmoid function in Logistic classifier?

• In the two-class logistic regression, the predicted probabilities are as follows, using the sigmoid function:

$$Pr(Y_i = 0) = \frac{e^{-\beta \cdot X_i}}{1 + e^{-\beta_0 \cdot X_i}}$$

$$Pr(Y_i = 1) = 1 - Pr(Y_i = 0) = \frac{1}{1 + e^{-\beta \cdot X_i}}$$

In the multiclass logistic regression, with K classes, the predicted probabilities are as follows, using the softmax function:

$$Pr(Y_i = k) = \frac{e^{\beta_k \cdot X_i}}{\sum_{0 < c < K} e^{\beta_c \cdot X_i}}$$

Softmax vs Sigmoid function in Logistic classifier?

• One can observe that the softmax function is an extension of the sigmoid function to the multiclass case, as explained below. Let's look at the multiclass logistic regression, with K=2 classes:

$$\Pr(Y_i = 0) = \frac{e^{\beta_0 \cdot X_i}}{\sum_{0 < c < K} e^{\beta_c \cdot X_i}} = \frac{e^{\beta_0 \cdot X_i}}{e^{\beta_0 \cdot X_i} + e^{\beta_1 \cdot X_i}} = \frac{e^{(\beta_0 - \beta_1) \cdot X_i}}{e^{(\beta_0 - \beta_1) \cdot X_i} + 1} = \frac{e^{-\beta_1 X_i}}{1 + e^{-\beta_1 X_i}}$$

$$\Pr(Y_i = 1) = \frac{e^{\beta_1 \cdot X_i}}{\sum_{0 < c < K} e^{\beta_c \cdot X_i}} = \frac{e^{\beta_1 \cdot X_i}}{e^{\beta_0 \cdot X_i} + e^{\beta_1 \cdot X_i}} = \frac{1}{e^{(\beta_0 - \beta_1) \cdot X_i} + 1} = \frac{1}{1 + e^{-\beta_i X_i}}$$

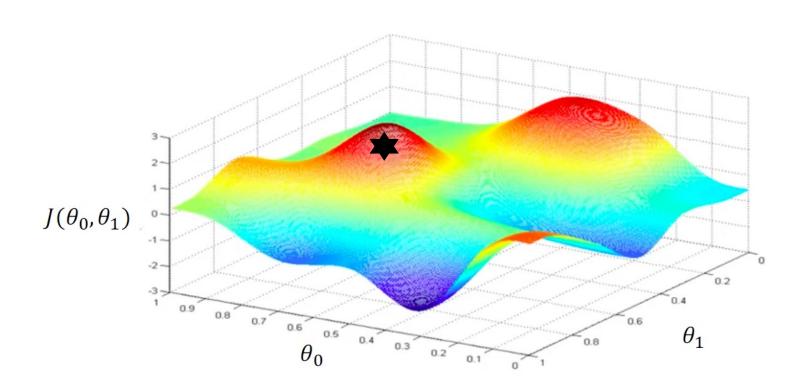
where
$$\beta = -(\beta_0 - \beta_1)$$

Types of Loss Functions

- For Regression tasks (continuous values)
 - Mean Absolute Error
 - Mean Squared Error
- For Classification tasks (discrete categories)
 - Categorical Cross Entropy
 - Binary Cross Entropy
- And various others in Keras

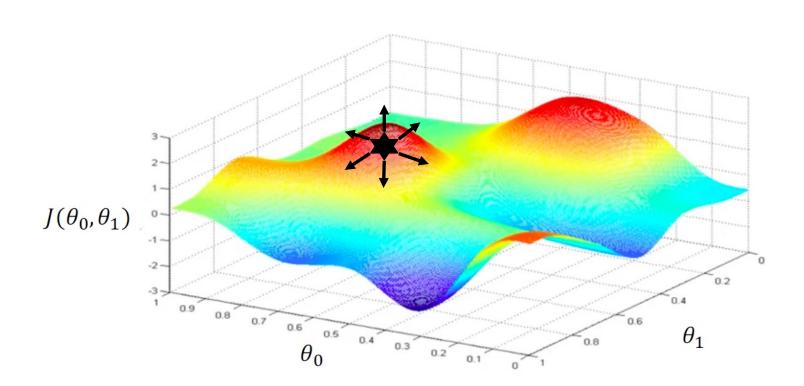
Gradient Descent

Standard approach for learning weights



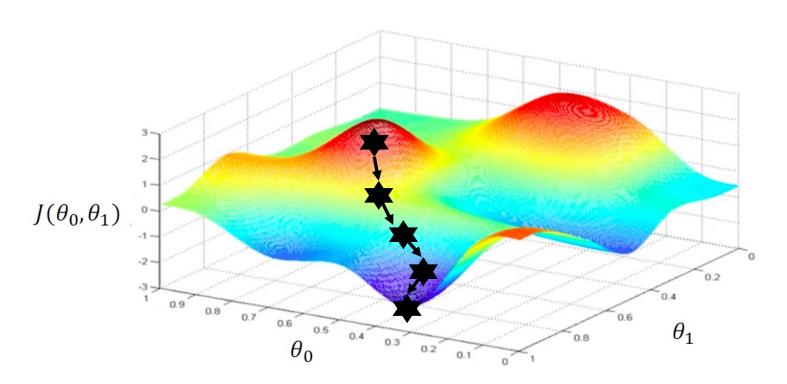
Gradient Descent

Standard approach for learning weights



Gradient Descent

- Standard approach for learning weights
 - What about the learning rate?



Exercise 1: Gradient Descent

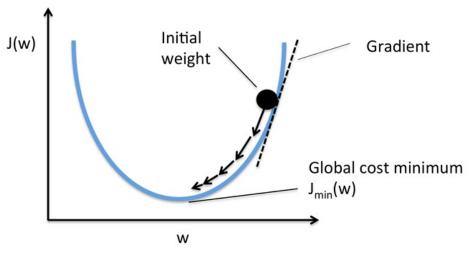
What are the effects of learning rates on gradient descent?

Mini-batch Training

- Batch gradient descent (BGD)
 - Compute weights using entire training set
- Stochastic gradient descent (SGD)
 - Compute weights using an instance at a time
- Mini-batch gradient descent
 - Compute weights using small batches (e.g., 32) from training set
- Typically, mini-batch is used in training neural networks
 - More robust convergence (avoid local minima) than BGD
 - Computationally more efficient than SGD
 - Parallelization to speed up computation

Adaptive Learning Rates

- Instead of fixed learning rates, use learning rates that change based on:
 - Value of gradient
 - Speed of learning
 - Sizes of weights

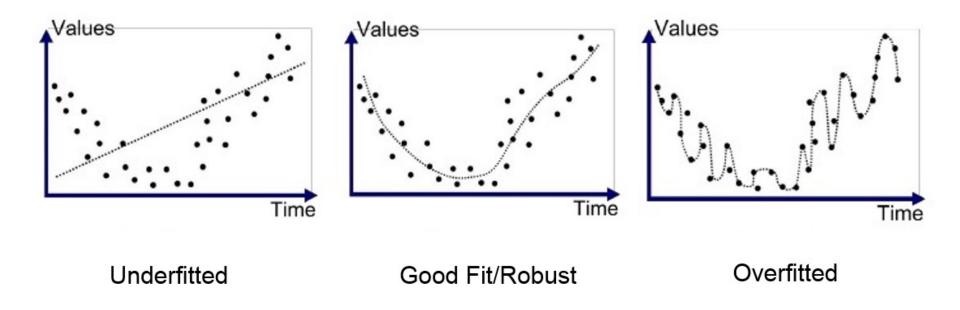


https://wiki.tum.de/display/lfdv/Adaptive+Learning+Rate+Method

Adaptive Learning Rates

- Various approaches available in Keras
 - Adagrad
 - Adadelta
 - Adam
 - Nadam
 - RMSprop

Under/Over-fitting Problem



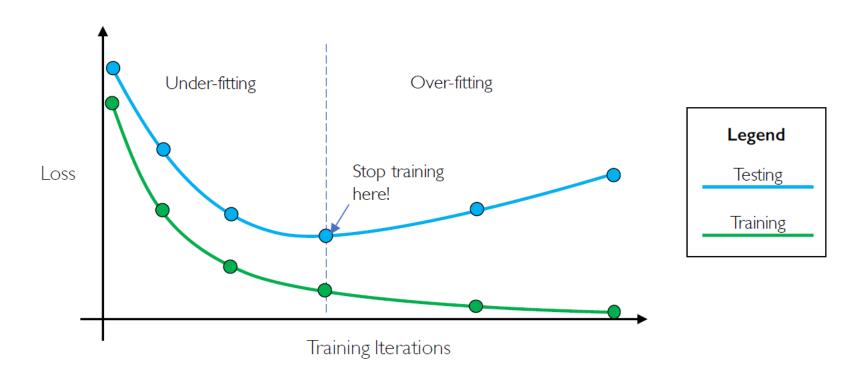
Source: https://medium.com/greyatom/what-is-underfitting-and-overfitting-in-machine-learning-and-how-to-deal-with-it-6803a989c76

Regularization

- Technique to help prevent overfitting on training data
 - Helps to generalize our model on unseen (testing) data
- Use
 - Early Stopping

Early Stopping

• Stop training of model before overfitting

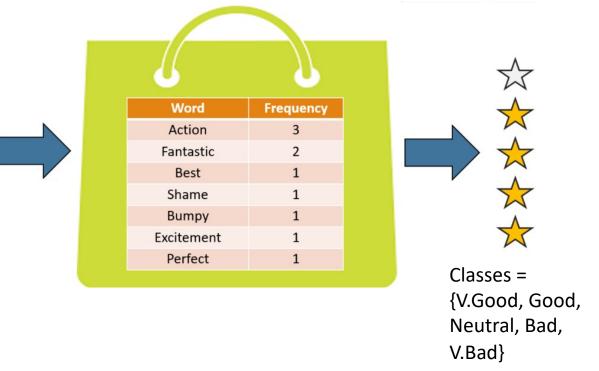


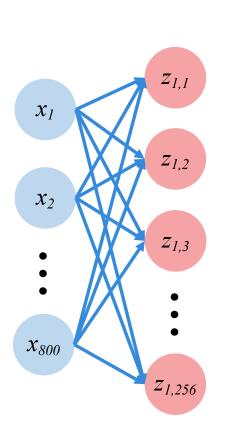
Exercise 2: Application to NLP

 What would your neural network architecture look like for the following sentiment analysis task?

Another fantastic entry to the best action franchise, putting James Bond films to shame once again. While the beginning is still a little bumpy, by the middle of the movie it is developing into a maelstrom of excitement and wonder about how action scenes are thought of, directed and performed. The Paris chase is already pretty fantastic but the last 30 minutes top it all off, pushing the envelope with every minute and twist. Cruise keeps risking his health for his audience, I know I am on board. Perfect action entertainment.

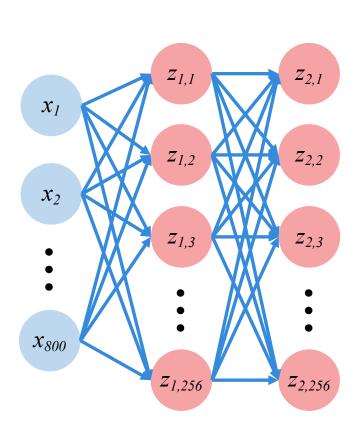
Vocabulary = 800 Words





```
model = Sequential()

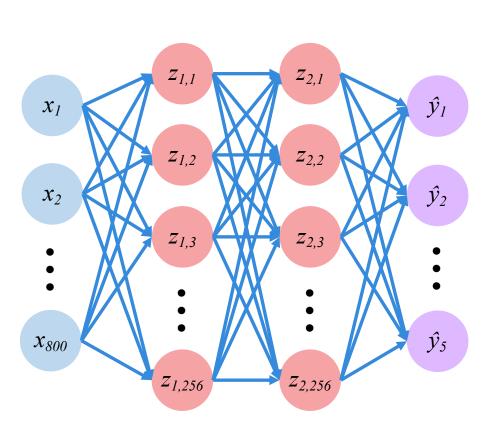
# input layer and hidden layer 1
model.add(Dense(256, activation='relu', input_dim=800))
model.add(Dropout(0.5))
```



```
model = Sequential()

# input layer and hidden layer 1
model.add(Dense(256, activation='relu', input_dim=800))
model.add(Dropout(0.5))

# hidden layer 2
model.add(Dense(256, activation='relu'))
model.add(Dropout(0.5))
```

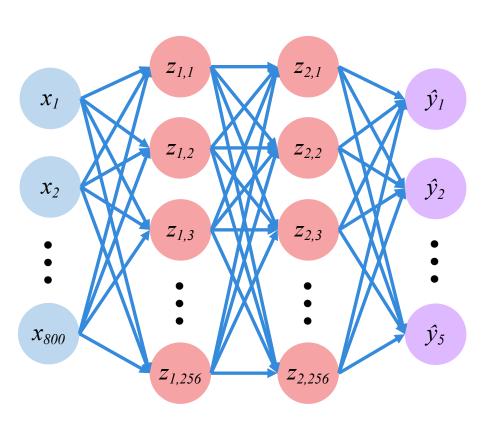


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model = Sequential()

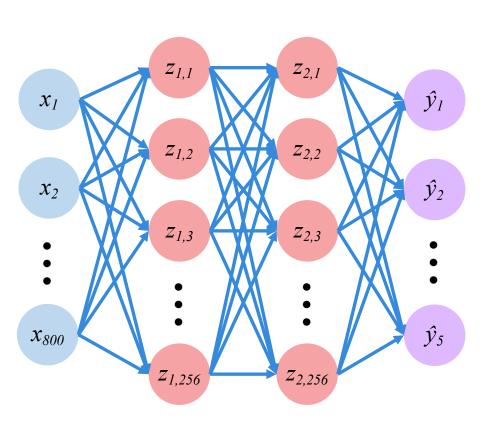
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model.add(Dropout(0.5))

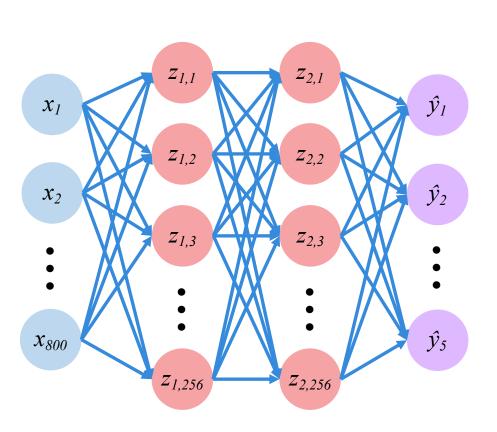
# output layer
model.add(Dense(5, activation='softmax'))
```



```
model = Sequential()
   # input layer and hidden layer 1
   model.add(Dense(256, activation='relu', input dim=800))
   model.add(Dropout(0.5))
 6
   # hidden layer 2
   model.add(Dense(256, activation='relu'))
   model.add(Dropout(0.5))
10
   # output layer
11
12
   model.add(Dense(5, activation='softmax'))
13
   # configure learning process
14
   model.compile(loss='categorical crossentropy',
16
                  optimizer='adam',
                  metrics=['accuracy'])
17
```



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   # input layer and hidden layer 1
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16
                  optimizer='adam',
                  metrics=['accuracy'])
17
18
19
   # train our model
   model.fit(x train, y train,
21
              epochs=50,
22
              batch size=128)
```



```
model = Sequential()
   # input layer and hidden layer 1
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20
21
              epochs=50,
22
              batch size=128)
23
   # test our model
25 | score = model.evaluate(x_test, y_test, batch_size=128)
```

Exercise 3: Discussion of Shortcomings

 What are the possible shortcomings of our previous Naïve Bayes and this MLP approach to sentiment classification?

