### Client frequencies:

```
client_ 0 freq: [1357 1480 1603 1726 1850 1973 2096 2220 2343 2466]
client_ 1 freq: [243 265 287 309 331 353 375 397 419 441]
client_ 2 freq: [3135 3420 3705 3990 4275 4560 4845 5130 5415 5700]
client_ 3 freq: [1970 2149 2328 2507 2686 2865 3045 3224 3403 3582]
```

	Accuracy	Loss
Norm	<pre>for i in range(len(pdfs)):     for j in range(i+1,len(pdfs)):         print(i," and ", j , stats.was</pre>	<pre>for i in range(len(pdfs)):     for j in range(i+1,len(pdfs)):         print(i," and ", j , stats.wasserst</pre>
	0 and 1 1.1316950932567083 0 and 2 16.789943005620493 0 and 3 9.708723438735062 1 and 2 17.892796430680484 1 and 3 10.80858591890214 2 and 3 7.084210511778343	0 and 1 1.589712839613521 0 and 2 2.4618447346270234 0 and 3 1.2872063294604323 1 and 2 4.051557574240545 1 and 3 2.872169320055356 2 and 3 1.1793882541851883
	<pre>shape, loc, scale = stats.gamma.fit(gl pdf_global = stats.gamma.pdf(global_lo  for i in range(len(pdfs)):</pre>	<pre>shape, loc, scale = stats.gamma.fit(global_ pdf_global = stats.gamma.pdf(global_loss_li  for i in range(len(pdfs)):</pre>
	print(i," and global: ", stats.wa  0 and global: 1751631362.9410932  1 and global: 1751631362.5086415  2 and global: 1751631376.031605  3 and global: 1751631370.533872	print(i," and global: ", stats.wassers  0 and global: 1751631362.639029  1 and global: 1751631363.1257498  2 and global: 1751631364.5361264  3 and global: 1751631363.6473703
Gamma	print(i, "and ", j , stats.wasserstein_C  0 and 1 54717527503560.66 0 and 2 2619302465.973565 0 and 3 32223122.089287713 1 and 2 54714908201097.61 1 and 3 54717495280441.984 2 and 3 2587079344.469823	0 and 1 23293.67582116507 0 and 2 2642966087.701834 0 and 3 86836338.94386089 1 and 2 2642989381.0476484 1 and 3 86859632.27898744 2 and 3 2556129748.768661
	<pre>shape, loc, scale = stats.gamma.fit(global_loss_pdf_global = stats.gamma.pdf(global_loss_list, s) for i in range(len(pdfs)):     print(i," and global: " , stats.wasserstein 0 and global: 1751631312.3499918 1 and global: 54715775872251.2 2 and global: 867671153.9460524 3 and global: 1719408190.8830602</pre>	<pre>shape, loc, scale = stats.gamma.fit(global_ pdf_global = stats.gamma.pdf(global_loss_li  for i in range(len(pdfs)):     print(i," and global: ", stats.wassers  0 and global: 1751608069.7465165 1 and global: 1751631363.2008057 2 and global: 891358018.1219131 3 and global: 1664771762.0599706</pre>
Lognorm	<pre>for i in range(len(pdfs)):     for j in range(i+1,len(pdfs)):         print(i," and ", j, stats.wasserste  0    and 1 55254380325754.164 0    and 2 16.07790006404852 0    and 3 9.049841030666352 1    and 2 55254380325751.23</pre>	0 and 1 1.5962046520864261 0 and 2 1152032554.6114473 0 and 3 828319716.0062158 1 and 2 1152032555.8887386 1 and 3 828319717.1620903 2 and 3 323712838.75998193
	<pre>1  and 3 55254380325752.18 2  and 3 7.04678114945583  shape, loc, scale = stats.gamma.fit(global l pdf_global = stats.gamma.pdf(global_loss_lis)  for i in range(len(pdfs)):     print(i," and global: ", stats.wasserst  0  and global: 1751631363.2840414 1  and global: 55252628694393.89 2  and global: 1751631376.009677 3  and global: 1751631370.5441334</pre>	<pre>shape, loc, scale = stats.gamma.fit(global_loss pdf_global = stats.gamma.pdf(global_loss_list, ); for i in range(len(pdfs)):     print(i," and global: " , stats.wasserstein  0 and global: 1751631362.6457176 1 and global: 1751631363.124102 2 and global: 599598829.1823409 3 and global: 923311661.1644437</pre>

```
for i in range(len(pdfs)):
    for j in range(i+1,len(pdfs)):
        print(i," and ", j , stats.wasserste
Beta
                                                                                                           0 and 1 1326423760265.2085
                                                                                                           0 and 2 2797271921268.4023
                                                                                                           0 and 3 4987275998778.207
                                                                                                          1 and 2 1470848161004.5254
                                                0 and 1 472447182945.1053
                                                0 and 2 1633923312858.529
                                                                                                          1 and 3 3660852238514.3296
                                               0 and 3 30858645448885.793
1 and 2 1161476130514.6243
                                                                                                           2 and 3 2190004078257.9138
                                               1 and 3 30386198265965.234
2 and 3 29224722136028.8
                                                                                                           shape, loc, scale = stats.gamma.fit(global_lc
                                                                                                           pdf_global = stats.gamma.pdf(global_loss_list
                                                shape, loc, scale = stats.gamma.fit(global_l
                                                pdf_global = stats.gamma.pdf(global_loss_lis
                                                                                                          for i in range(len(pdfs)):
    print(i," and global: " , stats.wasserste
                                               for i in range(len(pdfs)):
    print(i," and global: " , stats.wasserst
                                                                                                           0 and global: 17268452031.729095
                                                0 and global: 1751371635.8632
1 and global: 470695811311.50385
2 and global: 1632171941224.898
                                                                                                          1 and global: 1343692212296.3552
2 and global: 2814540373299.788
3 and global: 5004544450809.597
                                                3 and global: 30856894077252.176
Burr
                                                0 and 1 472447182945.1053
                                                                                                          0 and 1 1326423760265.2085
                                                                                                          0 and 2 2797271921268.4023
                                                0 and 2 1633923312858.529
                                                0 and 3 30858645448885.793
                                                                                                          0 and 3 4987275998778.207
                                                1 and 2 1161476130514.6243
                                                                                                         1 and 2 1470848161004.5254
                                                1 and 3 30386198265965.234
                                                                                                          1 and 3 3660852238514.3296
                                                2 and 3 29224722136028.8
                                                                                                          2 and 3 2190004078257.9138
                                                                                                         shape, loc, scale = stats.gamma.fit(global_lo
pdf_global = stats.gamma.pdf(global_loss_list
                                                shape, loc, scale = stats.gamma.fit(global
                                                pdf_global = stats.gamma.pdf(global_loss_l
                                                                                                         for i in range(len(pdfs)):
    print(i," and global: " , stats.wasserste
                                                for i in range(len(pdfs)):
    print(i," and global: " , stats.wasser
                                                                                                          0 and global: 17268452031.729095
                                                0 and global: 1751371635.8632
                                                                                                         1 and global: 1343692212296.3552
                                                1 and global: 470695811311.50385
                                                                                                          2 and global: 2814540373299.788
                                                2 and global: 1632171941224.898
                                                                                                          3 and global: 5004544450809.597
                                                3 and global: 30856894077252.176
```

t e			
loss st,			
ein			

# NON\_IID DISTRIBUTIONS (4 clients : gender-income)

```
client_ 0 freq: [1973 2096 2220 2343 2466 2589 2713 2836 2959 3083]
```

client\_ 1 freq: [353 375 397 419 441 463 485 507 529 551]
client\_ 2 freq: [4560 4845 5130 5415 5700 5985 6270 6555 6840 7125]

client\_ 3 freq: [2865 3045 3224 3403 3582 3761 3940 4119 4298 4477]

Distribution	frequency	accuracy	Loss
Gamma	<pre>0 and 1 0.0034349427373413384 0 and 2 0.00042332799344532235 0 and 3 0.00023232772854376901 1 and 2 0.003858270730786661 1 and 3 0.003667270465885108 2 and 3 0.00019100026490155328  0 and global: 0.0005951170688163395 1 and global: 0.004030059806157678 2 and global: 0.00017178907537101712 3 and global: 0.00036278934027257045</pre>	<pre>0 and 1 96611745126.51799 0 and 2 26331468952.791576 0 and 3 10325938315.564121 1 and 2 70280276178.07014 1 and 3 86285806815.72081 2 and 3 16005530637.711647  0 and global: 71717033119.61592 1 and global: 24894712009.077194 2 and global: 45385564169.90277 3 and global: 61391094807.61442</pre>	<pre>0 and 1 3571334.6290192525 0 and 2 3527876.6556697614 0 and 3 3375884237.1164727 1 and 2 43488.81355166581 1 and 3 3379455571.689611 2 and 3 3379412087.511244  0 and global: 100025094.95119059 1 and global: 103596429.5762785 2 and global: 103552956.95220673 3 and global: 3275859142.165282</pre>
Norm	<pre>0 and 1 0.003434916180979071 0 and 2 0.00042333433612756695 0 and 3 0.00023233377600585708 1 and 2 0.0038582505171066376 1 and 3 0.003667249956984929 2 and 3 0.00019100056012170982  0 and global: 0.0005951218430858042 1 and global: 0.004030038024064876 2 and global: 0.00017178750695823704 3 and global: 0.00036278806707994697</pre>	<pre>0 and 1 1.8533511277924637 0 and 2 12.550186731287384 0 and 3 8.844801561217773 1 and 2 14.389581675430298 1 and 3 10.680811536495323 2 and 3 3.7087701389349754  0 and global: 45.57258011544753 1 and global: 47.41197505959046 2 and global: 33.02239338416016 3 and global: 36.73116352309513</pre>	<pre>0 and 1 1.9439247483985005 0 and 2 2.2940469778074366 0 and 3 1.3069255004588132 1 and 2 4.237971726205937 1 and 3 3.2498012081393775 2 and 3 0.9881705180665596  0 and global: 4.964483702557023 1 and global: 6.908408450955523 2 and global: 2.7417408911300143 3 and global: 3.658607242816146</pre>

Lognorm	<pre>0 and 1 5660592.193859114 0 and 2 58726.068773617095 0 and 3 58834.618926491945 1 and 2 5719318.262632731 1 and 3 5719426.812785607 2 and 3 108.55021695542531  0 and global: 59708.31306807256 1 and global: 5720300.506927187 2 and global: 982.244294455473 3 and global: 873.6941415806158</pre>	<pre>0 and 1 3463538508071.1514 0 and 2 11.92890537244354 0 and 3 8.301989770435537 1 and 2 3463538508076.3716 1 and 3 3463538508074.5317 2 and 3 3.637997000153498  0 and global: 45.35031292556467 1 and global: 3463538508096.0435 2 and global: 33.440059079099576 3 and global: 37.078056079253074</pre>	<pre>0 and 1 1.9443768895059936 0 and 2 42.594144025410536 0 and 3 198758847484.76242 1 and 2 44.479917786526045 1 and 3 198758847485.8803 2 and 3 198758847476.48886  0 and global: 6.273941466842511 1 and global: 8.218318356348504 2 and global: 36.908357975239106 3 and global: 198758847483.9256</pre>
Beta	<pre>0 and 1 0.0037600727311337865 0 and 2 0.0010872173535729818 0 and 3 0.0007812811823525462 1 and 2 0.004730229869492611 1 and 3 0.004424293698272176 2 and 3 0.0003059361712204356  0 and global: 0.0013583023787272718 1 and global: 0.0050013148946469015 2 and global: 0.00027108502515429 3 and global: 0.0005770211963747256</pre>	<pre>0 and 1 854113097152899.4 0 and 2 23350576942951.473 0 and 3 28716477394886.68 1 and 2 830762520209948.1 1 and 3 825396619758256.6 2 and 3 5365900451935.387  0 and global: 142560324721048.28 1 and global: 711552772431869.8 2 and global: 119209747778098.02 3 and global: 113843847326399.7</pre>	<pre>0 and 1 1668988051430.631 0 and 2 33993429924.851116 0 and 3 5102665534436.631 1 and 2 1702981481355.2244 1 and 3 3433677483008.0156 2 and 3 5136658964360.713  0 and global: 36162306096.86395 1 and global: 1705150357527.4949 2 and global: 2168876172.2707167 3 and global: 5138827840527.401</pre>
Burr	<pre>0 and 1 0.0033262394877202617 0 and 2 0.00040832023076190096 0 and 3 0.00022358570628453592 1 and 2 0.003734559718482163 1 and 3 0.003549825194004798 2 and 3 0.00018473452447736509  0 and global: 0.0005744299617219128 1 and global: 0.0039006694494421747 2 and global: 0.00016610973096001176 3 and global: 0.0003508442554373769</pre>	<pre>0 and 1 802754617320.8098 0 and 2 40.223243866821676 0 and 3 45.69219771091308 1 and 2 802754617348.5286 1 and 3 802754617351.9719 2 and 3 7.6786916197144635  0 and global: 43.05023143195532 1 and global: 802754617350.6935 2 and global: 3.4811377511131445 3 and global: 5.862382991576778</pre>	<pre>0 and 1 0.972495068914641 0 and 2 29.11436567242299 0 and 3 24.301778376477447 1 and 2 29.84226937755347 1 and 3 24.928362496047953 2 and 3 4.9139068815055165  0 and global: 4.580701327257708 1 and global: 5.459503317743751 2 and global: 25.287826120400084 3 and global: 20.688757770350925</pre>

#### **Single-Batch Distributions**

#### client 0

loss: [0.04675943 0.22334448 0.3253662 0.3327828 0.32753864 0.30964363 0.30064547 0.2881389 0.30844659 0.29107651]

acc [0.99366689 0.91247624 0.87321091 0.86865103 0.87473083 0.8781507 0.88081062 0.88777709 0.87941736 0.88448387]

#### client 1

acc [0.89128917 0.49756098 0.37770036 0.50522649 0.44808361 0.43135887 0.47804877 0.47456446 0.50662023 0.48989546]

#### client 2

loss: [0.03972216 0.02067855 0.01909248 0.02059607 0.02184644 0.02210405 0.0240159 0.02484704 0.02478325 0.02511534]

freq: [18259 18259 18259 18259 18259 18259 18259 18259 18259 18259]

acc [0.99611151 0.99989045 1. 1. 1. 0.99994522 0.99994522 0.99989045 0.999984522]

#### client\_ 3

loss: [0.10719391 0.02389912 0.0262641 0.02447494 0.02615622 0.02859946 0.0283988 0.02978892 0.03104771 0.03117665] freq: [11484 11484 11484 11484 11484 11484 11484 11484 11484]

acc [0.98885405 0.99965167 0.99982584 0.99991292 0.99991292 0.99991292 0.99982584 0.99982584 0.99973875 0.99973875]

Distribution	Accuracy	Loss	
Gamma	<pre>0 and 1 5052963785.6386385 0 and 2 110213288418.12776 0 and 3 107785490295.07877 1 and 2 105160324655.85822 1 and 3 102732526518.81839 2 and 3 2427798137.039818  0 and global: 2170527.9642331777 1 and global: 5050793767.680869 2 and global: 110211118394.07294 3 and global: 107783320275.70663</pre>	<pre>0 and 1 9.308714649162779 0 and 2 11341.601002166437 0 and 3 4854633.798060776 1 and 2 11337.843632987884 1 and 3 4854630.040691596 2 and 3 4843350.173976158  0 and global: 6.269837293033752 1 and global: 13.414506742209406 2 and global: 11335.51733712475 3 and global: 4854628.48416662</pre>	
Norm	<pre>0 and 1 6.675711374677921 0 and 2 286.15857542033956 0 and 3 94.18641588484508 1 and 2 292.8342867950175 1 and 3 100.86212725952299 2 and 3 191.97215953549448 0 and global: 1091.4961367516255 1 and global: 1098.1718481263035 2 and global: 805.337561331286 3 and global: 997.3097208667805</pre>	<pre>0 and 1 2.4057410423621155 0 and 2 54.555577640223106 0 and 3 10.220130044593963 1 and 2 56.96131868258523 1 and 3 12.62587108695608 2 and 3 44.33544759562915 0 and global: 6.002736887598183 1 and global: 8.408477929960299 2 and global: 49.369079300209755 3 and global: 5.281169731086335</pre>	

Lognorm		
	<pre>0 and 1 20.848571350665924 0 and 2 68.43472489365098 0 and 3 78.13086556288947 1 and 2 89.2832962443169 1 and 3 98.97943691355539 2 and 3 84.68423389603093  0 and global: 1078.2990797532764 1 and global: 1099.1476511039423 2 and global: 1015.7192759065204 3 and global: 1000.1682141903868</pre>	<pre>0 and 1 2.396580615537854 0 and 2 88.29790770059965 0 and 3 79.39303651314505 1 and 2 90.69448831613751 1 and 3 81.7896171286829 2 and 3 32.77755483496762  0 and global: 6.029857038491165 1 and global: 8.426437654029018 2 and global: 82.74258355514098 3 and global: 74.39622381424006</pre>
Beta	<pre>0 and 1 1521748664975.6758 0 and 2 210969340692530.25 0 and 3 30110798953388.42 1 and 2 212491089357505.84 1 and 3 31632547618362.84 2 and 3 180858541739143.1  0 and global: 308744075720725.44 1 and global: 310265824385701.06 2 and global: 385995910701328.75 3 and global: 325709730121620.6</pre>	<pre>0 and 1 2314866766485.9023 0 and 2 10624594890126.223 0 and 3 4839861950005.761 1 and 2 12939461656612.125 1 and 3 7154728716486.841 2 and 3 5784732940125.554  0 and global: 4391291160872.917 1 and global: 2076424394391.9973 2 and global: 15015886050987.99 3 and global: 9231153110878.678</pre>
Burr	<pre>0 and 1 12.557451473326129 0 and 2 73.81034375812625 0 and 3 58.98077024145226 1 and 2 86.36779523145239 1 and 3 71.5382217147784 2 and 3 14.82957351667399  0 and global: 37.68286544026416 1 and global: 50.24031691359029 2 and global: 36.12747831786209 3 and global: 30.816360768026254</pre>	<pre>0 and 1 5.9800054838741215 0 and 2 85.11174054509708 0 and 3 14009025718706.021 1 and 2 91.09174602897119 1 and 3 14009025718712.0 2 and 3 14009025718739.184  0 and global: 2.2096049476649746 1 and global: 7.564232292959562 2 and global: 83.77601115000714 3 and global: 14009025718705.12</pre>

# NON\_IID DISTRIBUTIONS (8 clients : gender-race(white/black)-income)

```
client_ 0  freq: [154 173 193 212 231 250 270 289 308 327]
client_ 1  freq: [12 13 15 16 17 19 20 22 23 24]
client_ 2  freq: [1148 1291 1435 1578 1722 1865 2009 2152 2295 2439]
client_ 3  freq: [214 241 268 294 321 348 375 401 428 455]
client_ 4  freq: [ 900 1013 1125 1238 1350 1463 1575 1688 1800 1913]
client_ 5  freq: [42 47 52 57 62 68 73 78 83 88]
client_ 6  freq: [1921 2168 2415 2661 2908 3154 3401 3647 3894 4140]
client_ 7  freq: [1504 1529 1553 1577 1602 1626 1650 1675 1699 1724]
```

Distribution	frequency	accuracy	Loss
Distribution Gamma	frequency  0 and 1 0.061555536385285624  0 and 2 0.0041382116829178405  0 and 3 0.0013400631914867798  0 and 4 0.003961905318923298  0 and 5 0.013010983461184001  0 and 6 0.004406344593409131  0 and 7 0.00100519614650254  1 and 2 0.06569374806820347  1 and 3 0.0628955995767724	accuracy  0 and 1 3.5001817549856585e+23 0 and 2 7869143271.861214 0 and 3 357034.07862304547 0 and 4 518126.9362475103 0 and 5 165104.89760287738 0 and 6 19103681246.857594 0 and 7 392016643.4018573 1 and 2 3.50018175498558e+23 1 and 3 3.5001817549856585e+23	Loss  0 and 1 0.22051657214227194 0 and 2 14774694.28399596 0 and 3 4717296587.966944 0 and 4 1661033.0837199779 0 and 5 0.1598046861121252 0 and 6 31.63787434757529 0 and 7 4686093.701512583 1 and 2 14774694.504512532 1 and 3 4717296588.187131
	1 and 3 0.0628955995767724 1 and 4 0.06551744170420892 1 and 5 0.048544552924101626 1 and 6 0.06596188097869476 1 and 7 0.06256073253178818 2 and 3 0.0027981484914310598 2 and 4 0.00017630636399454234 2 and 5 0.01714919514410184 2 and 6 0.0002681329104912907 2 and 7 0.0031330155364153 3 and 4 0.002621842127436518 3 and 5 0.014351046652670783 3 and 6 0.00306628140192235 3 and 7 0.00033486704498423994 4 and 5 0.016972888780107297 4 and 6 0.0004444392744858331 4 and 7 0.002956709172420758 5 and 6 0.017417328054593128 5 and 7 0.014016179607686542	1 and 3 3.5001817549856585e+23 1 and 4 3.5001817549856585e+23 1 and 5 3.5001817549856585e+23 1 and 6 3.500181754985467e+23 1 and 7 3.500181754985655e+23 2 and 3 7868786239.209446 2 and 4 7868625147.615849 2 and 5 7869231109.581604 2 and 6 11234537976.059536 2 and 7 7477126628.530401 3 and 4 161100.1784975285 3 and 5 444871.7990126755 3 and 6 19103324215.268982 3 and 7 391659611.30970186 4 and 6 19103163122.99236 4 and 7 391498519.3510584 5 and 6 19103769084.577984 5 and 7 392104481.1222469	1 and 3 4717296588.187131 1 and 4 1661033.0432750282 1 and 5 0.06072497058341592 1 and 6 31.858060977126417 1 and 7 4686093.921699212 2 and 3 4702521897.798205 2 and 4 13113661.556582669 2 and 5 14774694.443800645 2 and 6 14774665.688301405 2 and 7 10088608.07593358 3 and 4 4715635555.235035 3 and 5 4717296588.126406 3 and 6 4717296562.071834 3 and 7 4712610502.249417 4 and 5 1661033.0135691038 4 and 6 1661030.5133884917 4 and 7 3025060.9600235075 5 and 6 31.797336006543002 5 and 7 4686093.860974241
	and 7 0.014016179607686342 and 7 0.003401148446906591  0 and global: 0.004620694721391866 1 and global: 0.0661762311066775 2 and global: 0.00048248303847402575 3 and global: 0.0032806315299050855 4 and global: 0.000658789402468568 5 and global: 0.017631678182575862 6 and global: 0.00021435012798273496 7 and global: 0.003615498574889326	and 7 392104481.1222469 and 7 18711664603.959282  0 and global: 41259533824.28781 1 and global: 3.5001817549852465e+23 2 and global: 33390390564.280167 3 and global: 41259176803.48961 4 and global: 41259015707.19073 5 and global: 41259621663.250084 6 and global: 22155852588.220627 7 and global: 40867517192.17992	and 7 4686093.860974241 and 7 4686093.860974241  0 and global: 7654705523.434952 1 and global: 7654705523.655138 2 and global: 7639930862.044109 3 and global: 2937408981.9449573 4 and global: 7653044490.611863 5 and global: 7654705523.594413 6 and global: 7654705517.384555 7 and global: 7650019469.851103

Norm	0 and 1 0.06155314818732709	0 and 1 0.8325300686638157	0 and 1 0.2263963719578554
	0 and 2 0.0041382495420010145	0 and 2 10.459736423104237	0 and 2 2.4129205474004163
	0 and 3 0.0013401049330001278	0 and 3 1.698031063319809	0 and 3 1.2704907536330314
	0 and 4 0.003961938678467752	0 and 4 0.6592378845059876	0 and 4 1.4787686693468602
	0 and 5 0.013011209351361921	0 and 5 0.42290213571143564	0 and 5 0.16566362160853892
		0 and 6 18.528715177097837	
	0 and 7 0.001005243975558933	0 and 7 13.219825443615902	0 and 7 2.9819330218239486
	1 and 2 0.06569139772932811	1 and 2 9.627206354440421	1 and 2 2.6393169193582717
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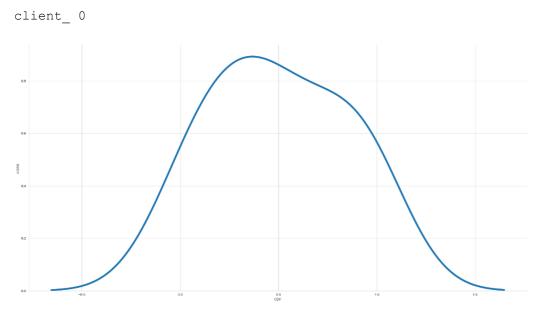
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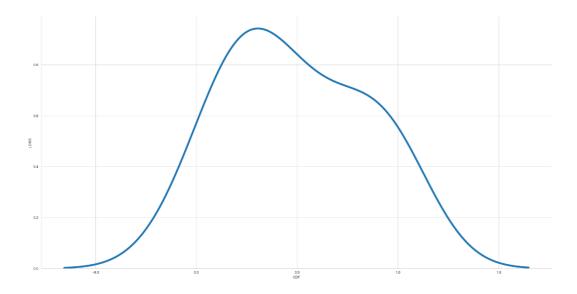
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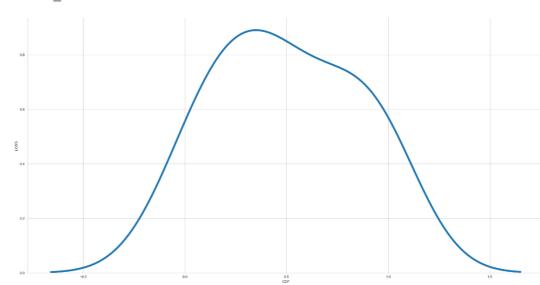
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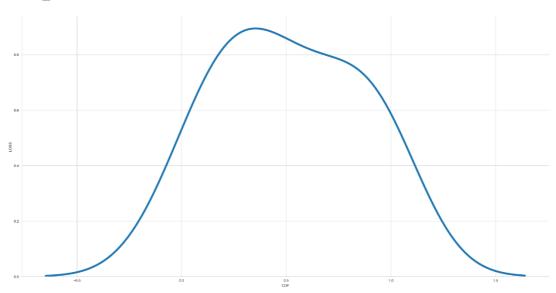


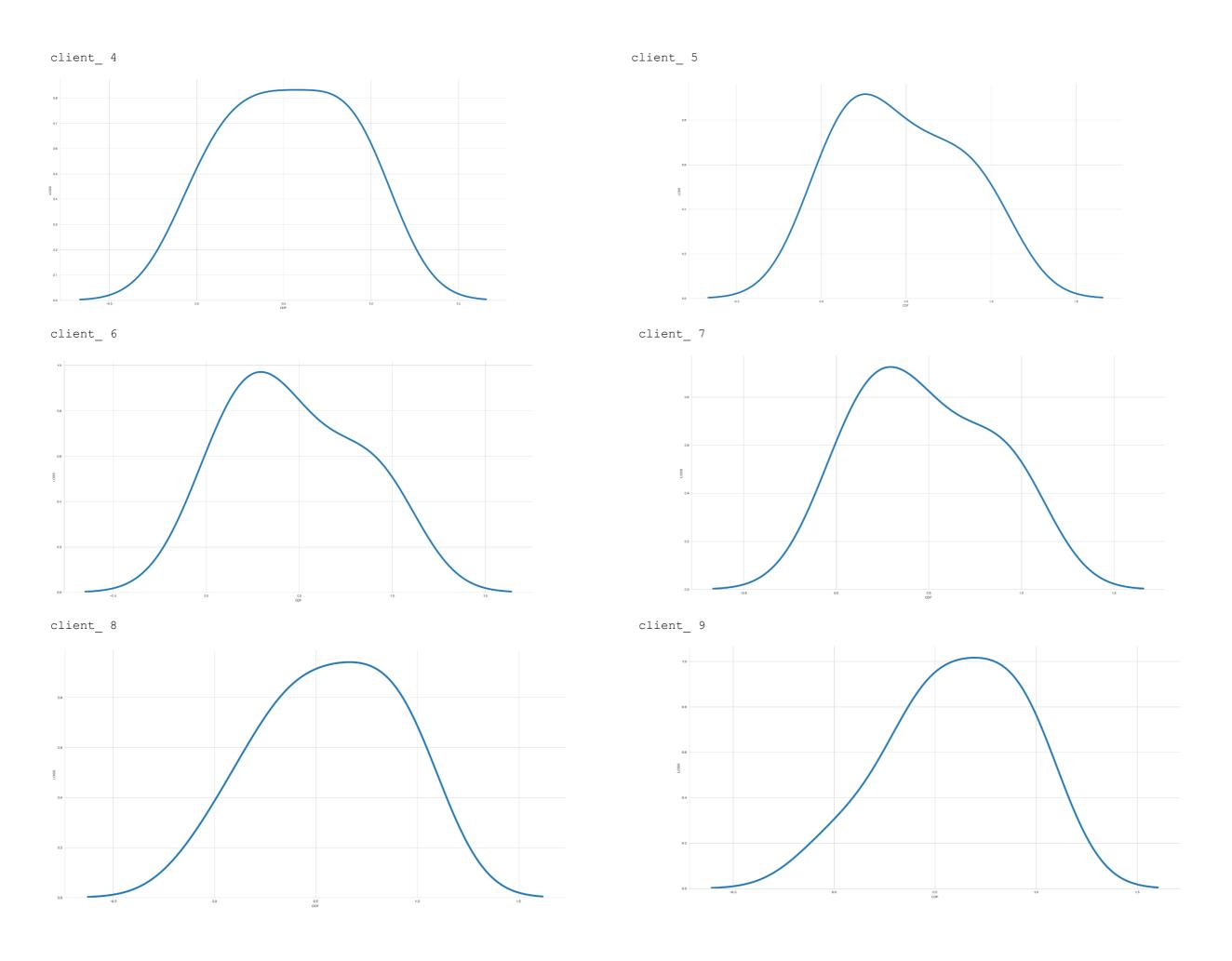


### client\_ 1



# client\_ 3





#### Statistics:

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