

Jee 13 April Shift - 1 - 1-15

AI24BTECH11013-Geetha charani

I. SECTION - A

- 1) $\int_0^{\infty} \frac{6}{e^{3x} + 6e^{2x} + 11e^x + 6} dx$
 - a) $\log_e\left(\frac{32}{27}\right)$
 - b) $\log_e\left(\frac{256}{81}\right)$
 - c) $\log_e\left(\frac{512}{81}\right)$
 - d) $\log_e\left(\frac{64}{27}\right)$
- 2) Among
 - (S1) : $\lim_{n \rightarrow \infty} \frac{1}{n^2} (2 + 4 + 6 + \dots + 2n) = 1$
 - (S2) : $\lim_{n \rightarrow \infty} \frac{1}{n^{16}} (1^{15} + 2^{15} + 3^{15} + \dots + n^{15}) = \frac{1}{16}$
 - a) Only (S1) is true
 - b) Both (S1) and (S2) are true
 - c) Both (S1) and (S2) are false
 - d) Only (S2) is true
- 3) The number of symmetric matrices of order 3, with all the entries from the set 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, is
 - a) 10^9
 - b) 10^6
 - c) 9^{10}
 - d) 6^{10}
- 4) Let $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$, $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$ and $\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}$. If a vector \vec{d} satisfies $\vec{d} * \vec{b} = \vec{c} * \vec{b}$ and $\vec{d} \cdot \vec{a} = 24$, then $|\vec{d}|^2$ is equal to
- 5) A coin is biased so that the head is 3 times as likely to occur as tail. This coin is tossed until a head or three tails occur. If X denotes the number of tosses of the coin, then the mean of X is
 - a) $\frac{21}{16}$
 - b) $\frac{15}{16}$
 - c) $\frac{81}{16}$
 - d) $\frac{37}{16}$
- 6) $\max_0 \leq x \leq \pi x - 2\sin x \cos x + \frac{1}{3}\sin 3x =$
 - a) 0
 - b) π
 - c) $\frac{5\pi + 2 + 3\sqrt{3}}{6}$
 - d) $\frac{\pi + 2 - 3\sqrt{3}}{6}$
- 7) The set of all $a \in R$ for which the equation $x|x - 1| + |x + 2| = a = 0$ has exactly one real root, is
 - a) $(-\infty, -3)$
 - b) $(-\infty, \infty)$
 - c) $(-6, \infty)$
 - d) $(-6, -3)$
- 8) Let PQ be a focal chord of the parabola $y^2 = 36x$ of length 100, making an acute with the position x-axis. Let the ordinate of P be positive and M be the point on the line segment PQ such that

$PM : MQ = 3 : 1$. Then which of the following points does NOT lie on the line passing through M and perpendicular to the line PQ?

- a) (3, 33)
- b) (6, 29)
- c) (-6, 45)
- d) (-3, 43)

9) For the system of linear equations

$$2x + 4y + 2az = b$$

$$x + 2y + 3z = 4$$

$$2x - 5y + 2z = 8$$

which of the following is NOT correct?

- a) It has infinitely many solutions if $a = 3, b = 8$
- b) It has unique solution if $a = b = 8$
- c) It has unique solution if $a = b = 6$
- d) It has infinitely many solutions if $a = 3, b = 6$

10) Let $s_1, s_2, s_3, \dots, s_{10}$ respectively be the sum of 12 terms of 10 A.P.s whose first terms are 1, 2, ..., 10 and the common difference are 1, 3, 5, ..., 19 respectively. Then $\sum_{i=1}^{10} s_i$ is equal to

- a) 7260
- b) 7380
- c) 7220
- d) 7360

11) For the differentiable function $f : R - 0 \rightarrow R$, let $3f(x) + 2f\left(\frac{1}{x}\right) = \frac{1}{x} - 10$, then $|f(3) + f'\left(\frac{1}{4}\right)|$ is equal to

- a) 13
- b) $\frac{29}{5}$
- c) $\frac{33}{5}$
- d) 7

12) The negation of the statement $((A \wedge (B \vee C)) \Rightarrow (A \vee B)) \Rightarrow A$ is

- a) equivalent to $B \vee \sim C$
- b) a fallacy
- c) equivalent to $\sim C$
- d) equivalent to $\sim A$

13) Let the tangent and normal at the point $(3\sqrt{3}, 1)$ on the ellipse $\frac{x^2}{36} + \frac{y^2}{4} = 1$ meet the y-axis at the points A and B respectively. Let the circle C be drawn taking AB as a diameter and the line $x = 2\sqrt{5}$ intersect C at the points P and Q. If the tangents at the points P and Q on the circle intersect at the point (α, β) , then $\alpha^2 - \beta^2$ is equal to

- a) $\frac{304}{4}$
- b) 60
- c) $\frac{314}{5}$
- d) 61

14) The distance of the points $(-1, 2, 3)$ from the plane $\vec{r} \cdot (\hat{i} - 2\hat{j} + 3\hat{k}) = 10$ parallel to the line of the shortest distance between the lines $\vec{r} = (\hat{i} - \hat{j}) + \lambda(2\hat{i} + \hat{k})$ and $\vec{r} = (2\hat{i} - \hat{j} + \mu(\hat{i} - \hat{j} + \hat{k}))$ is

- a) $2\sqrt{5}$
- b) $3\sqrt{5}$
- c) $3\sqrt{6}$
- d) $2\sqrt{6}$

15) Let $B = \begin{bmatrix} 1 & 3 & \alpha \\ 1 & 2 & 3 \\ \alpha & \alpha & 4 \end{bmatrix}$, $\alpha > 2$ be the adjoint of matrix A and $|A| = 2$, then $\begin{bmatrix} \alpha & -2\alpha & \alpha \end{bmatrix} B \begin{bmatrix} \alpha \\ -2\alpha \\ \alpha \end{bmatrix}$ is equal to

- a) 16
- b) 32
- c) 0
- d) -16