

Jee 2022 shift-1 16-30

AI24BTECH11013-Geetha charani

I. SECTION - A

- 1) The area of the region $(x, y) : |x - 1| \leq y \leq \sqrt{5 - x^2}$ is equal to:
 - a) $\frac{5}{2} \sin^{-1}(\frac{3}{5}) - \frac{1}{2}$
 - b) $\frac{5\pi}{4} - \frac{3}{2}$
 - c) $\frac{3\pi}{4} + \frac{3}{2}$
 - d) $\frac{5\pi}{4} - \frac{1}{2}$
- 2) Let the focal chord of the parabola $P : y^2 = 4x$ along the line $L : y = mx + c, m > 0$ meet the parabola at the points M and N. Let the line L be the tangent to the hyperbola $H : x^2 + y^2 = 4$. If O is the vertex of P and F is the focus of H on the positive x-axis, then the area of the quadrilateral OMFN is :
 - a) $2\sqrt{6}$
 - b) $2\sqrt{14}$
 - c) $4\sqrt{6}$
 - d) $4\sqrt{14}$
- 3) The number of points, where the function $f : R \rightarrow R, f(x) = |x-1|\cos|x-2|\sin|x-1| + (x-3)|x^2-5x+4|$, is NOT differentiable, is :
 - a) 1
 - b) 2
 - c) 3
 - d) 4
- 4) Let $S = 1, 2, 3, \dots, 2022$. Then the probability, that a randomly chosen number n from the set S such that $\text{HCF}(n, 2022) = 1$, is :
 - a) $\frac{128}{1011}$
 - b) $\frac{166}{1011}$
 - c) $\frac{127}{1011}$
 - d) $\frac{112}{1011}$
- 5) Let $f(x) = 3^{(x^2-2)^3+4}, x \in R$. Then which of the following statements are true ?

P : $x = 0$ is a point of local minima of f

Q : $x + \sqrt{2}$ is a point of inflection of f

R : f' is increasing for $x > \sqrt{2}$

 - a) Only P and Q
 - b) Only P and R
 - c) Only Q and R
 - d) All P, Q and R

II. SECTION - B

- 6) Let $S = \theta \in (0, 2\pi) : 7\cos^2\theta - 3\sin^2\theta - 2\cos^2\theta = 2$. Then the sum of roots of all the equations $x^2 - 2(\tan^2\theta + \cot^2\theta)x + 6\sin^2\theta = 0, \theta \in S$, is :

- 7) Let the mean and the variance of 20 observations x_1, x_2, \dots, x_{20} be 15 and 9, respectively. For $\alpha \in R$, if the mean of $(x_1 + \alpha)^2, (x_2 + \alpha)^2, \dots, (x_{20} + \alpha)^2$ is 178, then the square of the maximum value of α is equal to :
- 8) Let a line with direction ratios $a, -4a, -7$ be perpendicular to the lines with direction ratios $3, -1, 2b$ and $b, a, -2$. If the point of intersection of the line $\frac{x+1}{a^2+b^2} = \frac{y-2}{a^2-b^2} = \frac{z}{1}$ and the plane $x - y + z = 0$ is (α, β, γ) , then $\alpha + \beta + \gamma$ is equal to
- 9) Let a_1, a_2, a_3, \dots be an A.P. If $\sum_{r=1}^{\infty} \frac{a_r}{2^r} = 4$, then $4a_2$ is equal to
- 10) Let the ratio of the fifth term from the beginning to the fifth term from the end in the binomial expansion of $\left(\sqrt[4]{2} + \frac{1}{\sqrt[4]{3}}\right)^n$, in the increasing powers of $\frac{1}{\sqrt[4]{3}}$ be $\sqrt[4]{6} : 1$. If the sixth term from the beginning is $\frac{\alpha}{\sqrt[4]{3}}$, then α is equal to
- 11) Let number of matrices of order 3×3 , whose entries are either 0 or 1 and the sum of all the entries is a prime number, is
- 12) Let p and $p + 2$ be prime numbers and let
- $$\Delta = \begin{vmatrix} p! & (p+1)! & (p+2)! \\ (p+1)! & (p+2)! & (p+3)! \\ (p+2)! & (p+3)! & (p+4)! \end{vmatrix}$$
- Then the sum of the maximum values of α and β , such that p^α and $(p+2)^\beta$ divide Δ , is
- 13) If $\frac{1}{2 \cdot 3 \cdot 4} + \frac{1}{3 \cdot 4 \cdot 5} + \frac{1}{4 \cdot 5 \cdot 6} + \dots + \frac{1}{100 \cdot 101 \cdot 102} = \frac{k}{101}$, then $34k$ is equal to
- 14) Let $S = 4, 6, 9$ and $T = 9, 10, 11, \dots, 1000$. If $A = a_1 + a_2 + \dots + a_k : K \in N, a_1, a_2, a_3, \dots, a_k \in S$, then the sum of all the elements in the set $T - A$ is equal to
- 15) Let the mirror image of a circle $c_1 : x^2 + y^2 - 2x - 6y + \alpha = 0$ in line $y = x + 1$ be $c_2 : 5x^2 + 5y^2 + 10gx + 10fy + 38 = 0$. If r is the radius of the circle c_2 , then $\alpha + 6r^2$ is equal to