

# Causal Inference for Earth System Science

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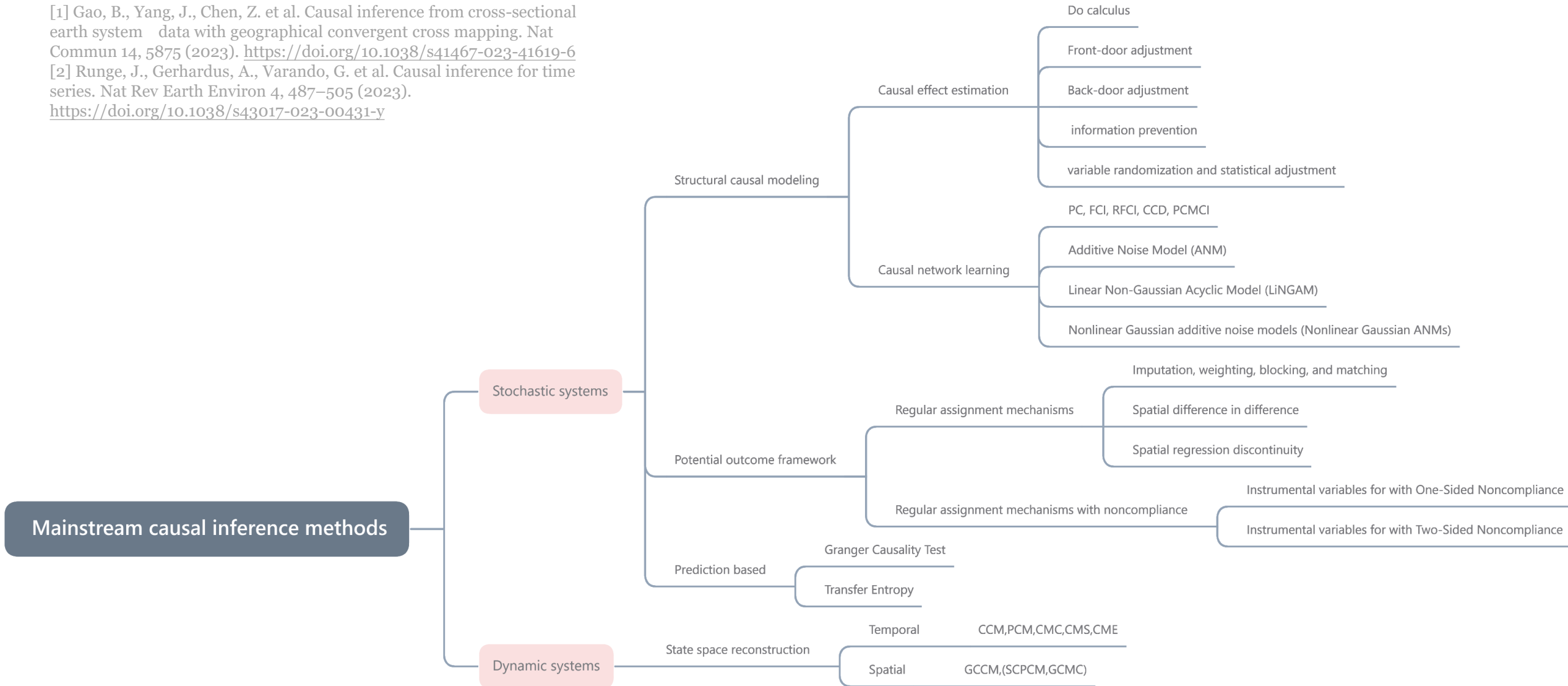
# Contents:

- **Data-driven algorithms vs. Earth system model simulations**
- **Inferring causation from time series**
- **Inferring causation from spatial cross sections**
- **Temporally or spatially?**
- **Spatial Empirical Dynamic Modeling**

	Data-driven algorithms	Earth system model simulations
Approach	Data-centric, based on statistical methods	Mechanistic, based on physical laws
Type	Correlation-based	Causality from system dynamics
Strengths	Flexibility, applicability to complex data	Deep understanding of system behavior
Limitations	May miss underlying causal mechanisms	Computationally expensive, requires high-quality data
Example	GCT(Granger Causality Test); CCM(Convergent Cross Mapping)	CESM(Community Earth System Model); WRF(Weather Research and Forecasting Model);

[1] Gao, B., Yang, J., Chen, Z. et al. Causal inference from cross-sectional earth system data with geographical convergent cross mapping. Nat Commun 14, 5875 (2023). <https://doi.org/10.1038/s41467-023-41619-6>

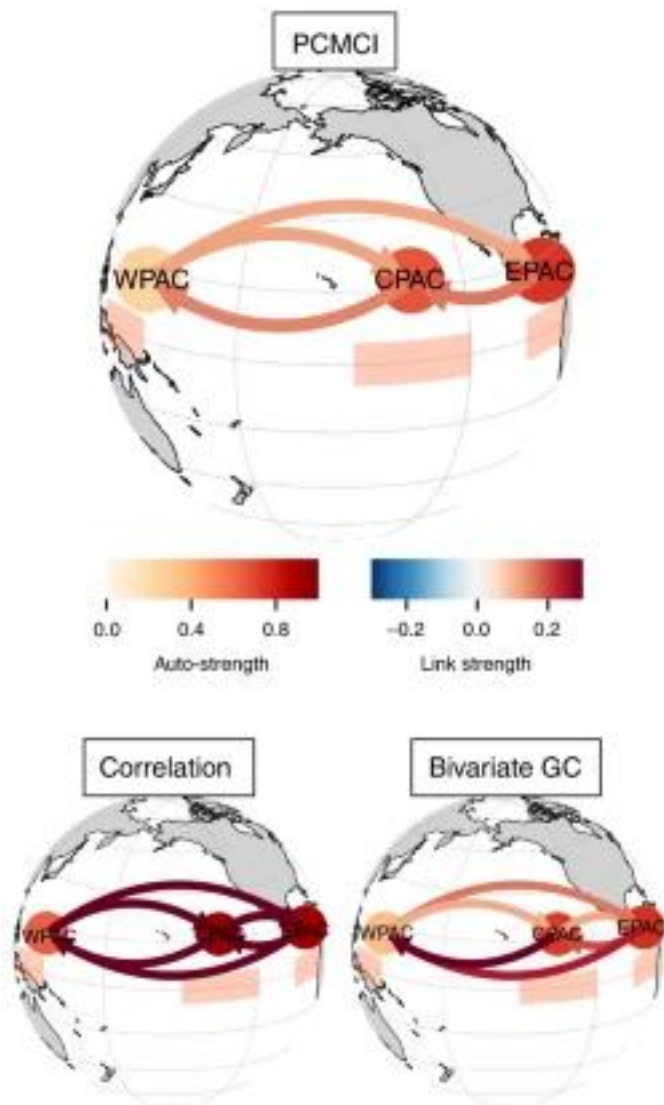
[2] Runge, J., Gerhardus, A., Varando, G. et al. Causal inference for time series. Nat Rev Earth Environ 4, 487–505 (2023). <https://doi.org/10.1038/s43017-023-00431-y>





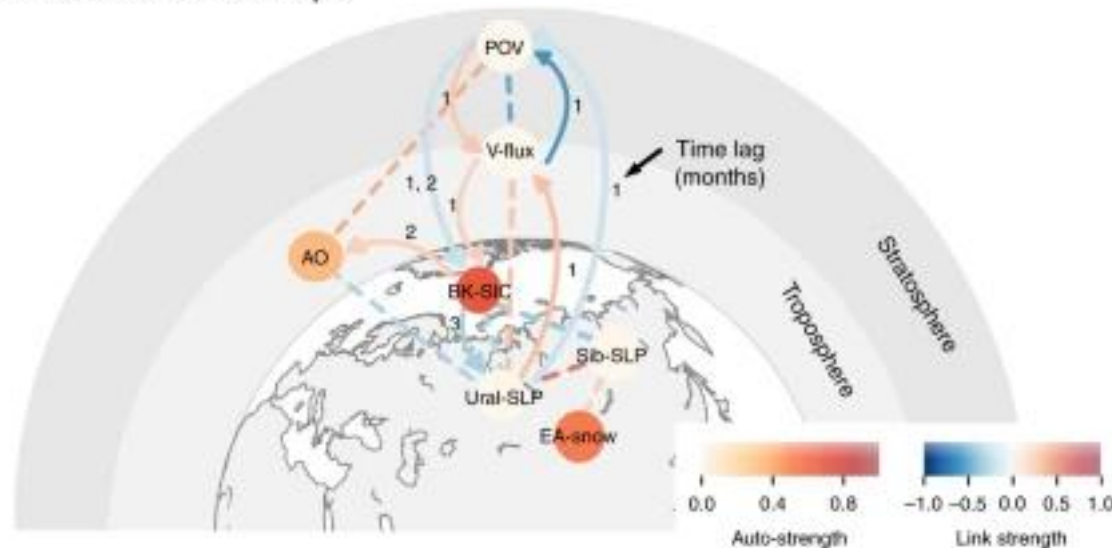
a

Tropical climate example



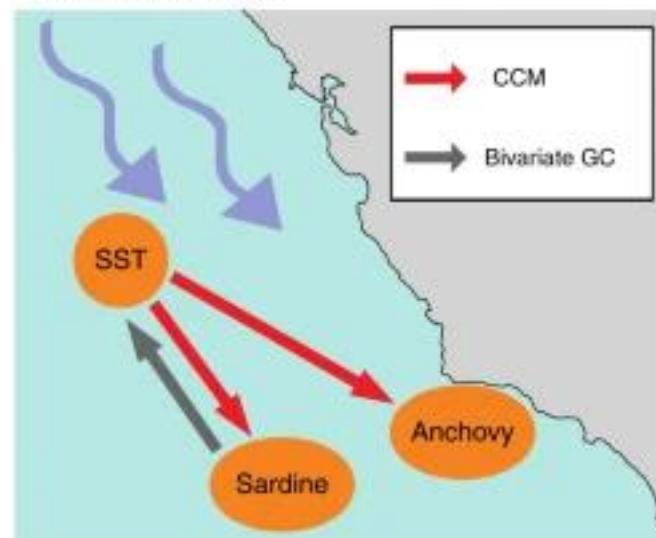
b

Arctic climate example



c

Ecology example



# Inferring causation from time series

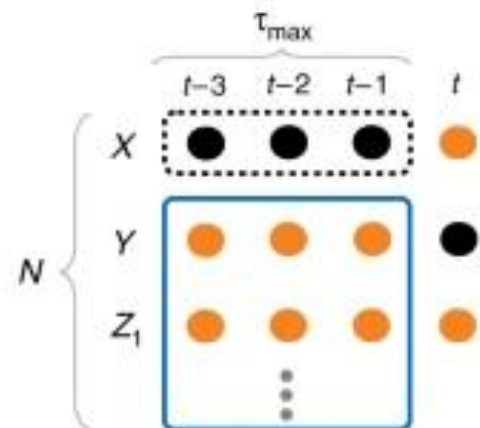
**a:** Tropical climate example showing dependencies between surface pressure anomalies in the West Pacific and temperature anomalies in the Central and East Pacific, with a multivariate causal method identifying the Walker circulation.

**b:** Arctic climate example highlighting how sea ice concentrations in the Barents and Kara seas influence the winter Arctic Oscillation via tropospheric mechanisms and the stratospheric Polar vortex.

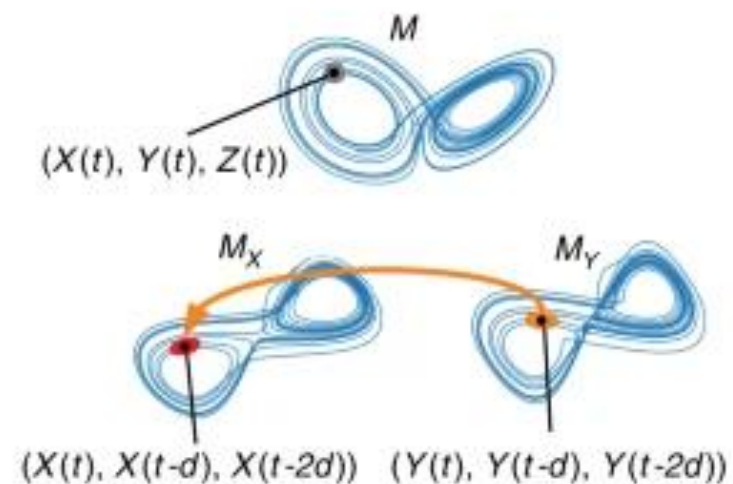
**c:** Ecology example showing that sardine and anchovy abundances are influenced by sea surface temperatures, with convergent cross mapping revealing a stronger causal relationship than Granger causality.

Runge, J., Bathiany, S., Bollt, E. *et al.* Inferring causation from time series in Earth system sciences. *Nat Commun* 10, 2553 (2019).  
<https://doi.org/10.1038/s41467-019-10105-3>

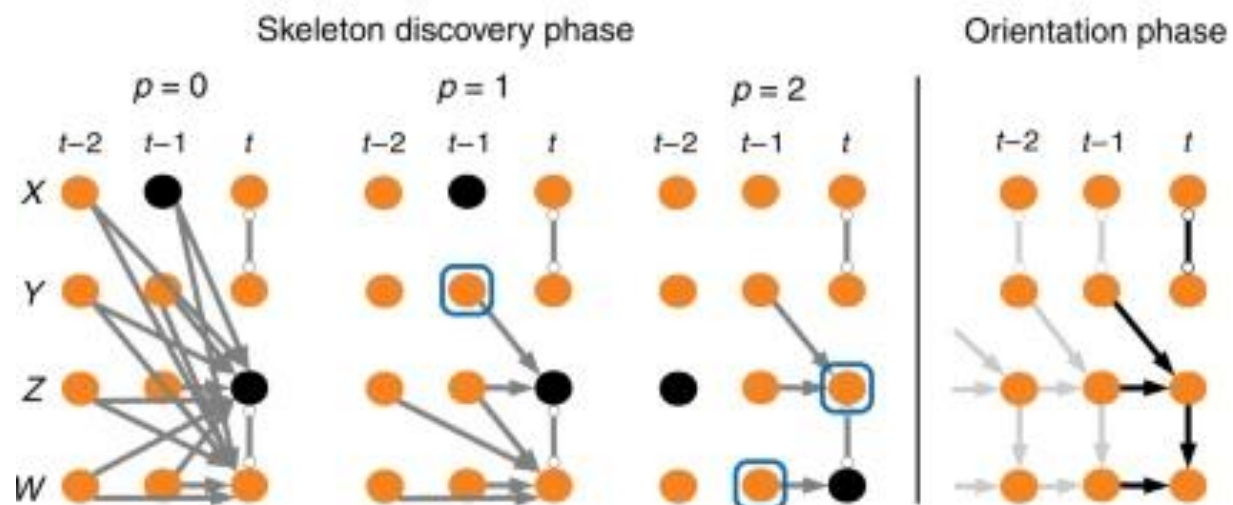
### a Granger causality



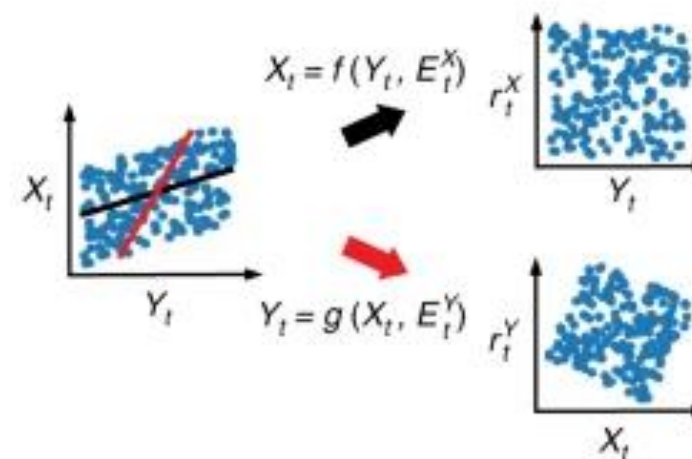
### b Nonlinear state-space methods



### c Causal network learning algorithms



### d Structural causal models

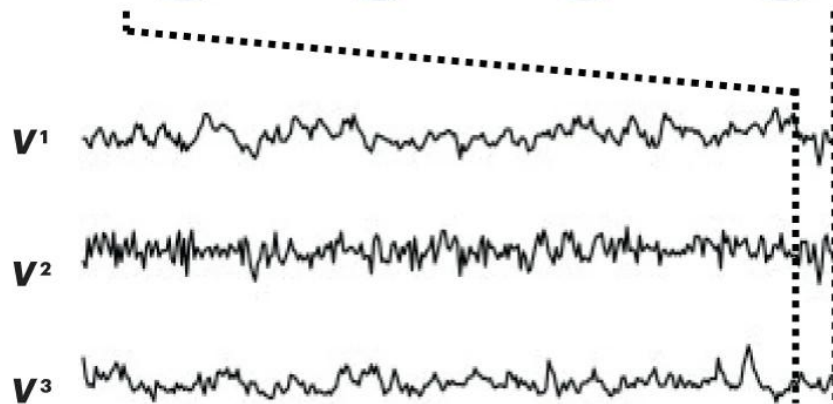
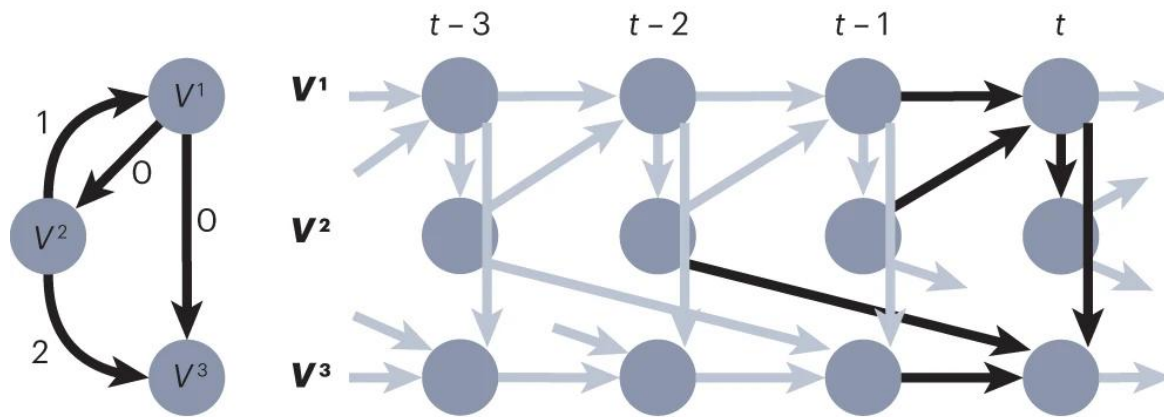
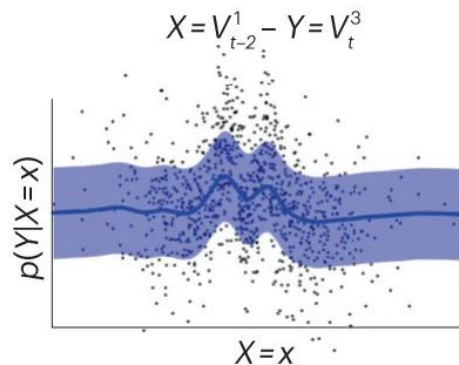


Runge, J., Bathiany, S., Boltt, E. *et al.* Inferring causation from time series in Earth system sciences. *Nat Commun* 10, 2553 (2019).  
<https://doi.org/10.1038/s41467-019-10105-3>



## a Observational SCM

$$\begin{aligned} V_t^1 &:= f^1(pa(V_t^1), \eta_t^1) \\ V_t^2 &:= f^2(pa(V_t^2), \eta_t^2) \\ V_t^3 &:= f^3(pa(V_t^3), \eta_t^3) \end{aligned}$$



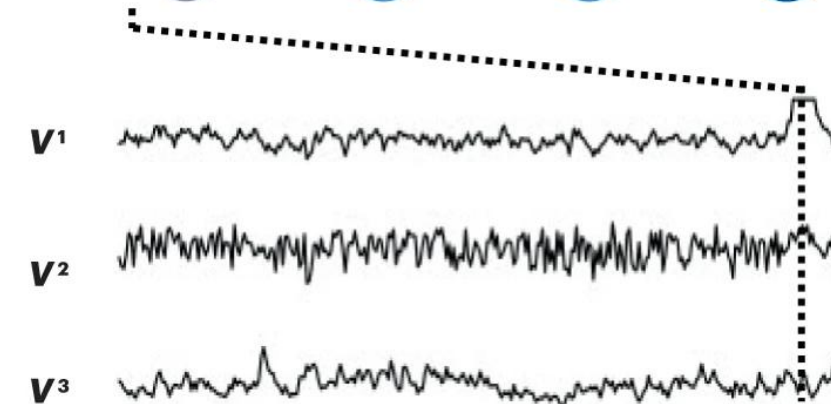
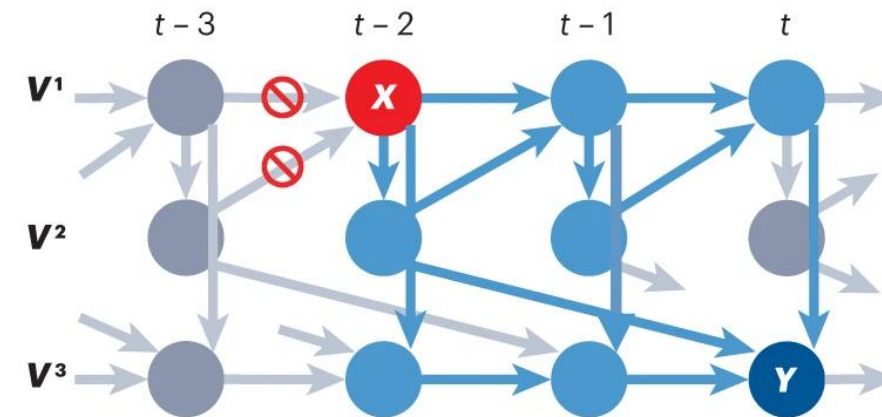
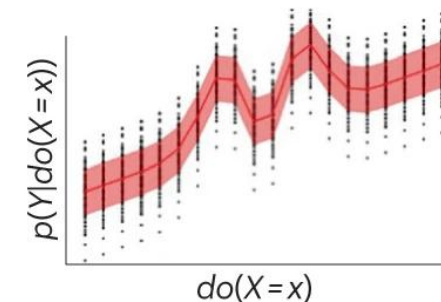
## b Intervened SCM

$$V_{t'}^1 := \begin{cases} v_{t'}^1, & \text{if } t' = t - 2 \\ f^1(pa(V_{t'}^1), \eta_{t'}^1) & \text{otherwise} \end{cases}$$

$$V_t^2 := f^2(pa(V_t^2), \eta_t^2)$$

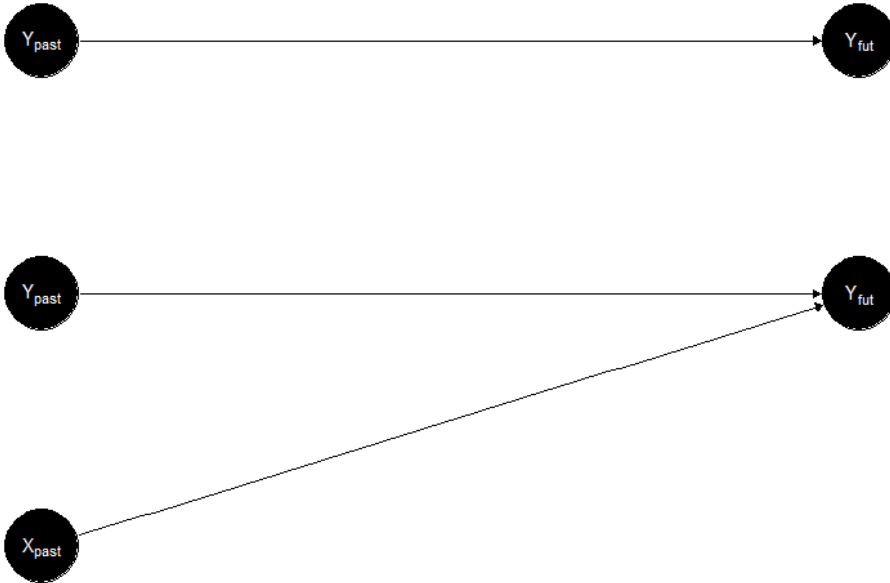
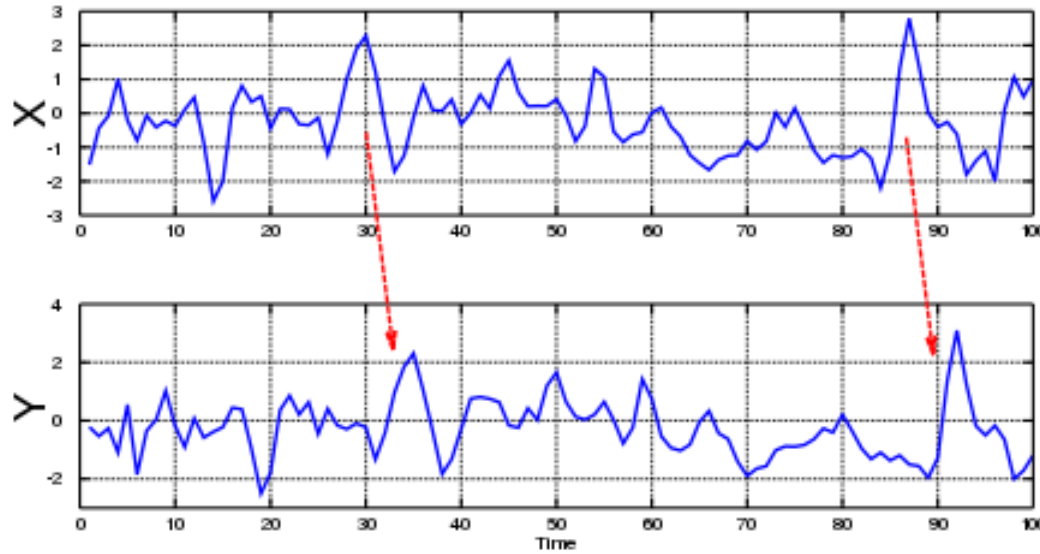
$$V_t^3 := f^3(pa(V_t^3), \eta_t^3)$$

$$X = V_{t-2}^1 \rightarrow Y = V_t^3$$



Runge, J., Gerhardus, A., Varando, G. et al. Causal inference for time series. Nat Rev Earth Environ 4, 487–505 (2023).  
<https://doi.org/10.1038/s43017-023-00431-y>

# Granger Causality



$$Y(t) = \alpha_1 Y(t-1) + error_1(t) \quad (1)$$

$$Y(t) = \alpha_1 Y(t-1) + \beta_1 X(t-1) + error_2(t) \quad (2)$$

- A F-test is performed with *the null hypothesis* of  $Y(t)$  equals to model (1) against *the alternative hypothesis* of  $Y(t)$  equals to model (2).
- We say that  $X$  Granger causes  $Y$  if we reject the null hypothesis.

$$Y(t) = \sum_{j=1}^p \alpha_j Y(t-j) + error_1(t)$$

$$Y(t) = \sum_{j=1}^p \alpha_j Y(t-j) + \sum_{j=1}^p \beta_j X(t-j) + error_2(t)$$



```
# Which came first: the chicken or the egg?  
# US chicken population and egg production  
# An annual time series from 1930 to 1983.  
df = as.data.frame(lmtest::ChickEgg)
```

```
head(df)
```

```
#>   chicken  egg  
#> 1  468491 3581  
#> 2  449743 3532  
#> 3  436815 3327  
#> 4  444523 3255  
#> 5  433937 3156  
#> 6  389958 3081
```

```
cor.test(df$chicken,df$egg)
```

```
#>
```

```
#> Pearson's product-moment correlation
```

```
#>
```

```
#> data: df$chicken and df$egg
```

```
#> t = -1.4327, df = 52, p-value = 0.1579
```

```
#> alternative hypothesis: true correlation  
is not equal to 0
```

```
#> 95 percent confidence interval:
```

```
#> -0.43969371  0.07689656
```

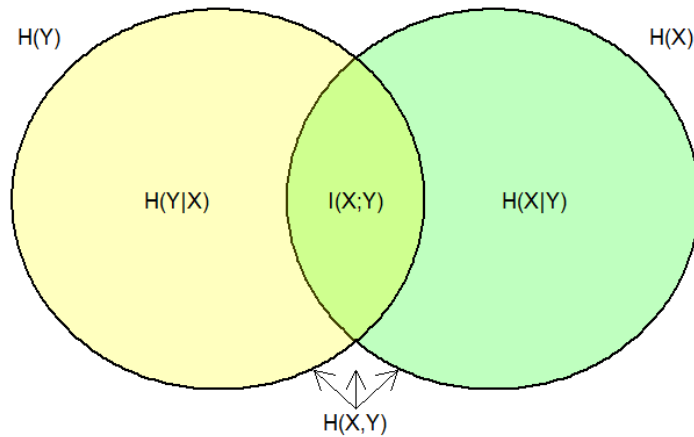
```
#> sample estimates:
```

```
#>          cor
```

```
#> -0.1948765
```

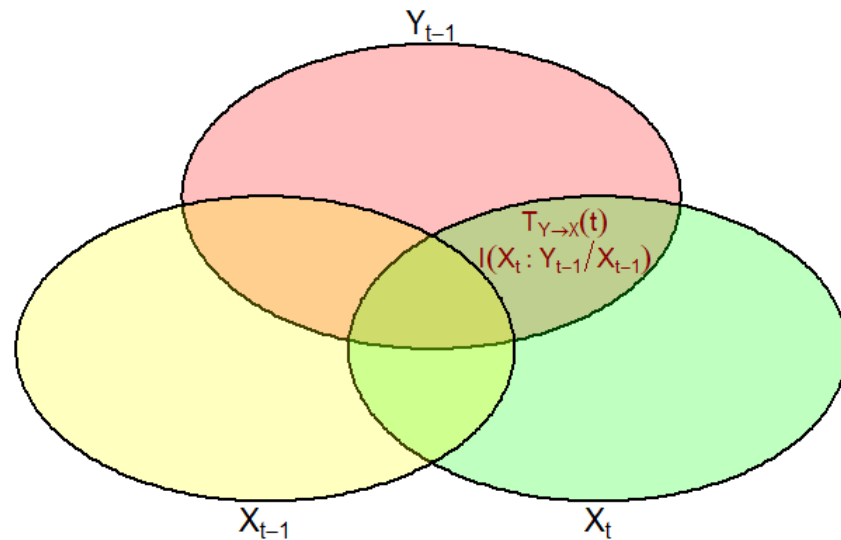
```
#----- Granger Causality Test -----
## chickens granger-cause eggs?
lmtest::grangertest(egg ~ chicken, order = 3, data = df)
#> Granger causality test
#>
#> Model 1: egg ~ Lags(egg, 1:3) + Lags(chicken, 1:3)
#> Model 2: egg ~ Lags(egg, 1:3)
#>   Res.Df Df       F Pr(>F)
#> 1      44
#> 2      47 -3 0.5916 0.6238
## eggs granger-cause chickens?
lmtest::grangertest(chicken ~ egg, order = 3, data = df)
#> Granger causality test
#>
#> Model 1: chicken ~ Lags(chicken, 1:3) + Lags(egg, 1:3)
#> Model 2: chicken ~ Lags(chicken, 1:3)
#>   Res.Df Df       F   Pr(>F)
#> 1      44
#> 2      47 -3 5.405 0.002966 **
#> ---
#> Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

# Transfer Entropy



$$H(X) = - \sum_{x \in X} p(x) \log_2 p(x)$$

$$\begin{aligned} T_{Y \rightarrow X}(t) &= I(X_t : Y_{t-1} | X_{t-1}) \\ &= H(X_t | X_{t-1}) - H(X_t | X_{t-1} Y_{t-1}) \\ &= \sum p(x_t, x_{t-1}, y_{t-1}) * \log_2 \frac{p(x_t | x_{t-1} y_{t-1})}{p(x_t | x_{t-1})} \end{aligned}$$



- Transfer entropy can be considered a **non-parametric equivalent** of Granger Causality (it also works for *nonlinear categorical variables*).
- The **mutual information** between both is **symmetric** (undirected), but the experimentally introduced **time delay** allows for establishing directionality.



## #----- Transfer Entropy -----

```
df = as.data.frame(lmtest::ChickEgg)
```

```
# Method1: Continuous Transfer Entropy using the Kraskov estimation
```

```
## TE: chickens -> eggs
```

```
NlinTS::te_cont(df$egg, df$chicken, p = 3, q = 3, k = 6, normalize = F)
```

```
#> [1] 0.007843137
```

```
## TE: eggs -> chickens
```

```
NlinTS::te_cont(df$chicken, df$egg, p = 3, q = 3, k = 6, normalize = F)
```

```
#> [1] 0.5748366
```

```
# Method2: Pre-discretization
```

```
chicken_disc = sdsfun::discretize_vector(df$chicken, n = 5, method = 'natural')
```

```
egg_disc = sdsfun::discretize_vector(df$egg, n = 5, method = 'natural')
```

```
## TE: chickens -> eggs
```

```
NlinTS::te_disc(egg_disc, chicken_disc, p = 3, q = 3, normalize = TRUE)
```

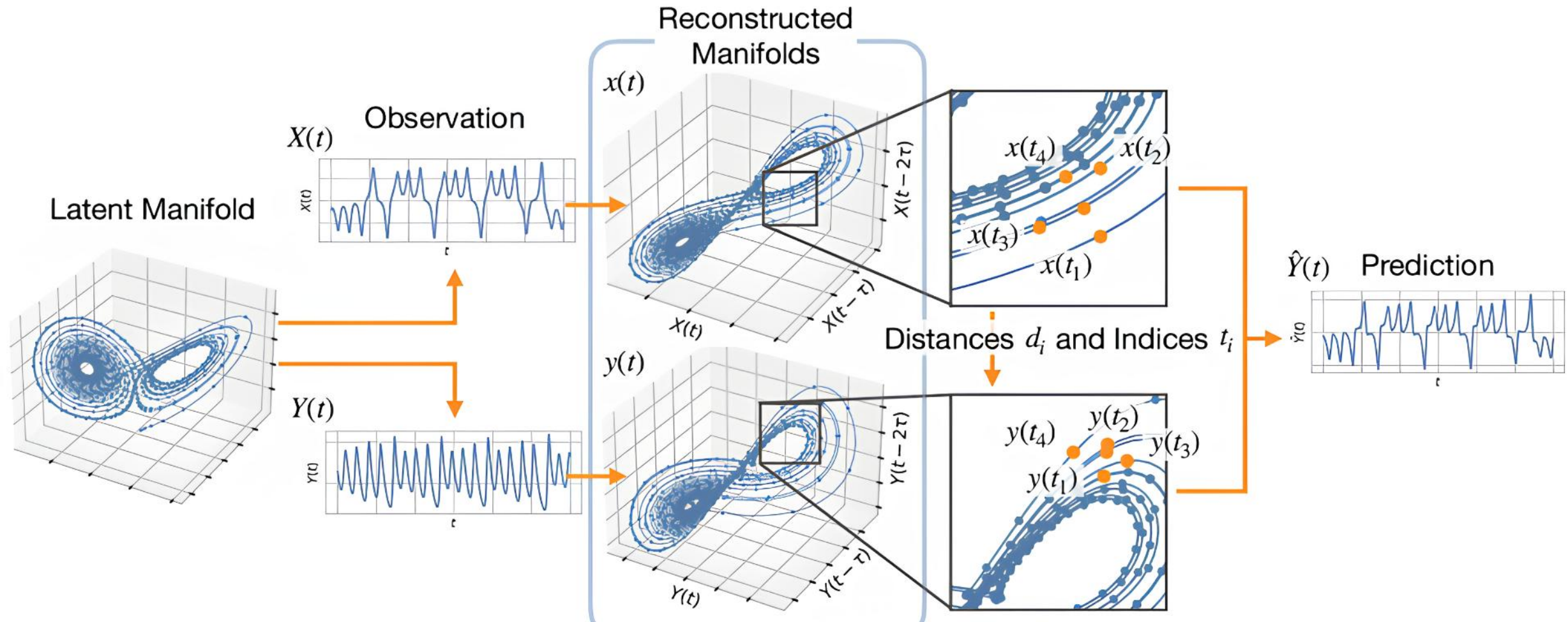
```
#> [1] 0.2670127
```

```
## TE: eggs -> chickens
```

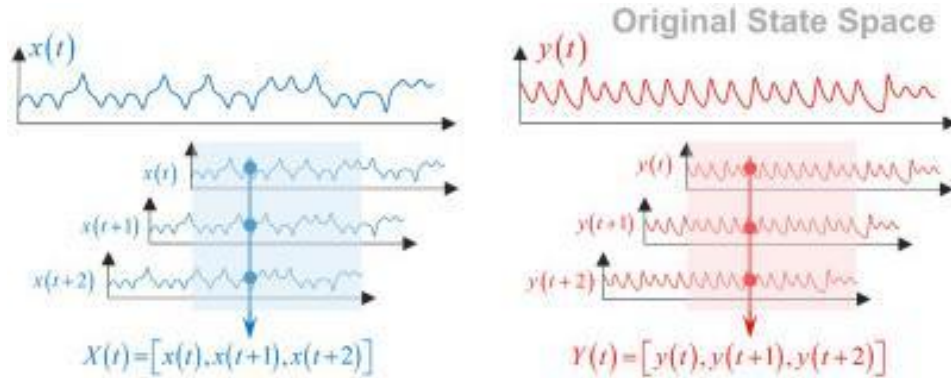
```
NlinTS::te_disc(chicken_disc, egg_disc, p = 3, q = 3, normalize = TRUE)
```

```
#> [1] 0.2745098
```

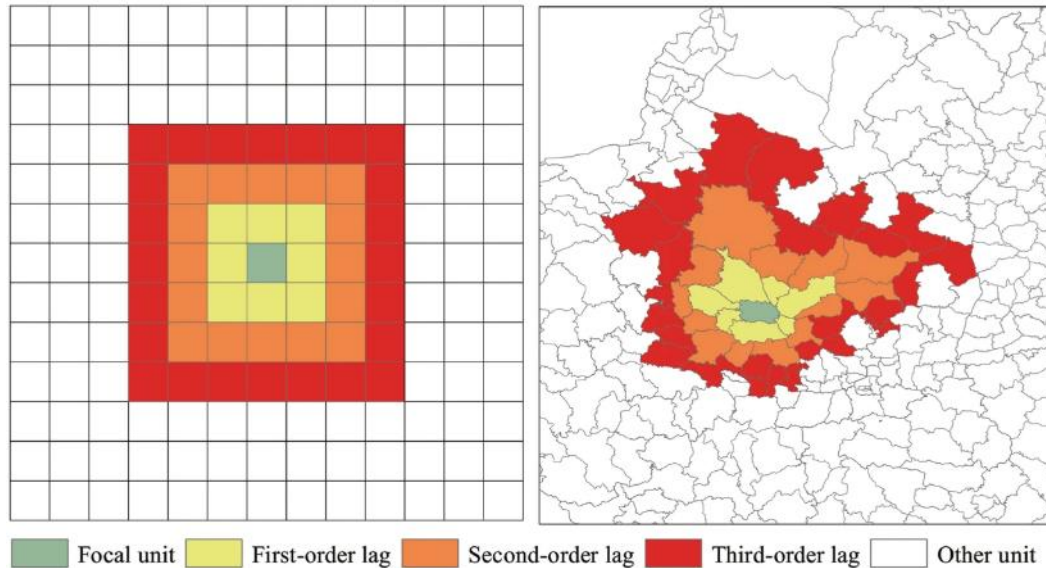
# Cross Mapping



# Time series and spatial cross-sectional embeddings



$$\mathbf{X} = \begin{bmatrix} x_1 & x_2 & \cdots & x_E \\ x_2 & x_3 & \cdots & x_{E+1} \\ \vdots & \vdots & \ddots & \vdots \\ x_{n-E+1} & x_{n-E+2} & \cdots & x_n \end{bmatrix}$$

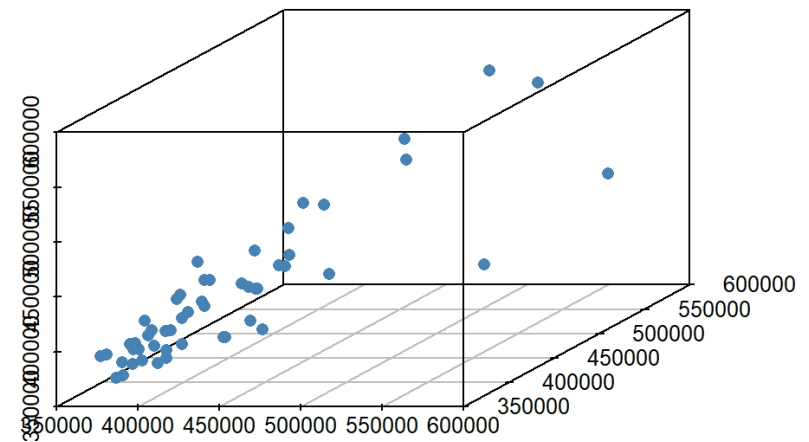


$$\mathbf{X} = \begin{bmatrix} \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j}^{(1)} & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j}^{(2)} & \cdots & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j}^{(k)} \\ \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j+1}^{(1)} & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j+1}^{(2)} & \cdots & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{i-j+1}^{(k)} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{n-m}^{(1)} & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{n-m}^{(2)} & \cdots & \frac{1}{m} \sum_{j=1}^m \mathbf{x}_{n-m}^{(k)} \end{bmatrix}$$



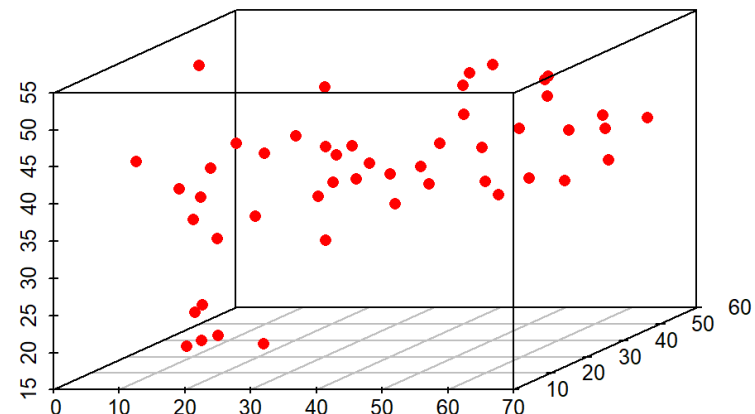
```
# temporal embeddings:
chickegg = as.data.frame(lmtest::ChickEgg)
m1 = stats::embed(chickegg$chicken,dimension = 3)
head(m1,5)
```

```
#>      [,1]    [,2]    [,3]
#> [1,] 436815 449743 468491
#> [2,] 444523 436815 449743
#> [3,] 433937 444523 436815
#> [4,] 389958 433937 444523
#> [5,] 403446 389958 433937
```



```
# spatial embeddings:
columbus = sf::read_sf(system.file("shapes/columbus.gpkg", package="spData"))
m2 = spEDM::embedded(columbus,target = "CRIME", E = 3, tau = 0)
head(m2,5)
```

```
#>      [,1]    [,2]    [,3]
#> [1,] 15.72598 24.71427 41.55964
#> [2,] 18.80175 26.24684 44.57868
#> [3,] 30.62678 29.41175 43.45135
#> [4,] 32.38776 34.64648 37.95647
#> [5,] 50.73151 40.46533 34.43484
```



# Simplex Projection

$$\text{distances}_j = \sqrt{\sum_{k=1}^E (x_{i+k-1} - x_{j+k-1})^2}$$

$$\text{neighbors} = \text{order}(\text{distances})[2:(E + 1)]$$

$$w_j = \exp\left(-\frac{\text{distance}_j}{\text{min.distance}}\right)$$

$$\hat{x}_{i+1} = \frac{\sum_{j \in \text{neighbors}} w_j \cdot x_{j+1}}{\sum_{j \in \text{neighbors}} w_j}$$

# S-Mapping

$$\text{distances}_j = \sqrt{\sum_{k=1}^E (x_{i+k-1} - x_{j+k-1})^2}$$

$$w_j = \exp\left(-\frac{\theta \cdot \text{distance}_j}{\text{distance}}\right)$$

$$\mathbf{A} = [\mathbf{X}, \mathbf{w}]$$

$$\mathbf{map} = \mathbf{V} \cdot \Sigma^{-1} \cdot \mathbf{U}^T$$

$$\hat{x}_{i+1} = \mathbf{map}^T \cdot [\mathbf{x}_i, 1]$$

```
# simplex proojection
spEDM:::RcppSimplexForecast(m2,columbus$CRIME,1:49,1:49,4)
#> [1] 17.70104 19.93840 30.16243 33.07348 52.18022 30.18953 13.01769 38.77808
#> [9] 32.23513 31.48435 59.09663 56.54921 52.37962 55.85027 45.97856 56.90080
#> [17] 32.00166 42.04745 57.18469 11.72599 40.22695 33.58007 19.03443 43.43395
#> [25] 61.19662 41.27700 47.49645 57.54308 60.16271 60.75822 16.88356 18.35503
#> [33] 38.45912 19.50335 36.89147 16.98435 42.51416 53.16424 17.19591 16.21441
#> [41] 17.43940 17.79455 35.36479 30.37855 27.84116 18.27504 18.16851 26.01435
#> [49] 22.38665
```

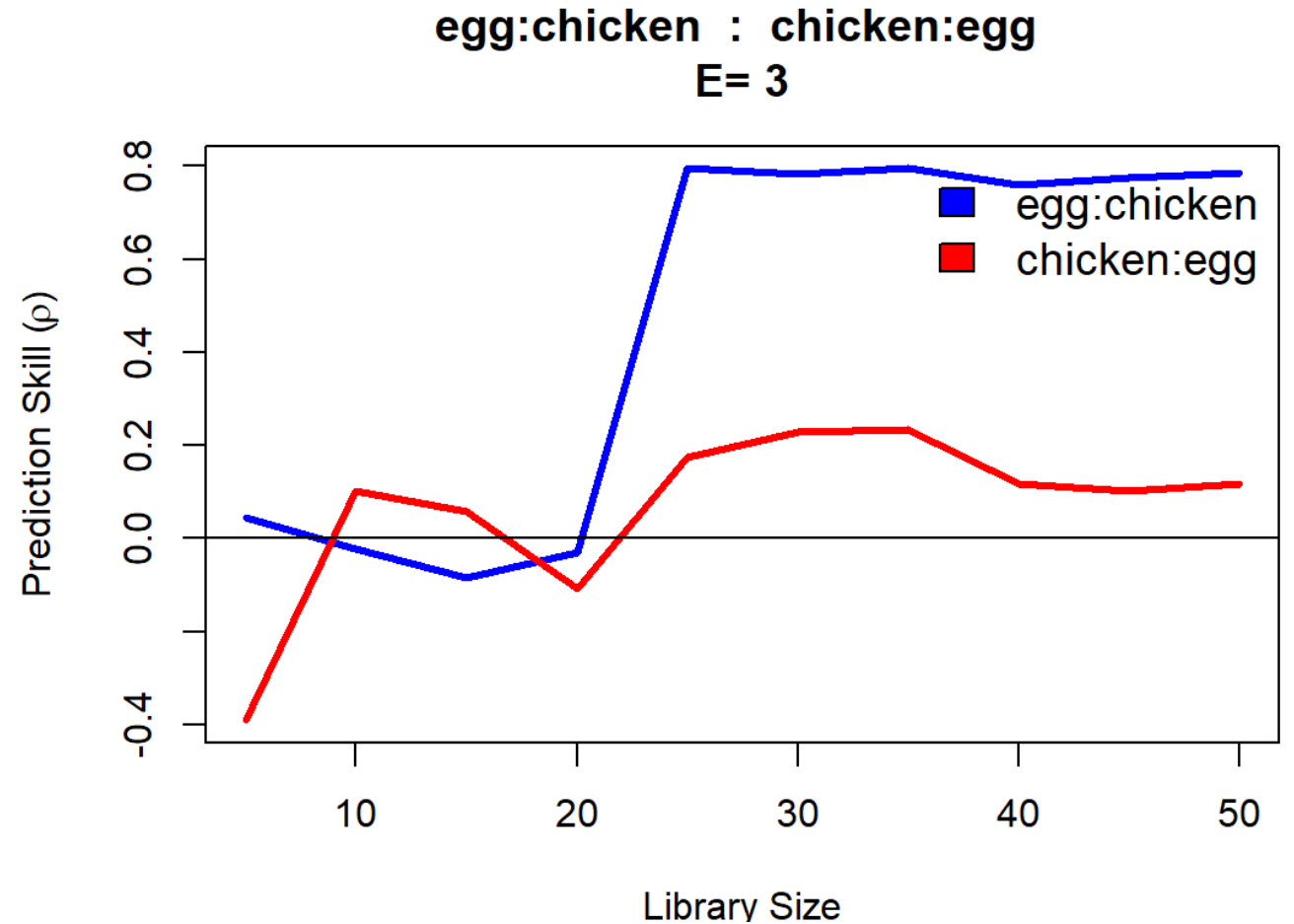
```
# s-mapping
spEDM:::RcppSMapForecast(m2,columbus$CRIME,1:49,1:49,4,theta = 0.1)
#> [1] 1.627749e+02 1.386350e+03 1.322136e+03 1.712858e+03 -3.264970e+03
#> [6] -4.801324e+02 4.574963e+02 -3.206982e+03 -1.089545e+03 3.597287e+02
#> [11] -6.972924e+01 4.814860e+03 -2.115798e+02 3.454839e+02 -1.318667e+03
#> [16] 6.773236e+02 -4.492509e+02 1.091786e+03 -2.059843e+02 2.330649e+02
#> [21] -1.940220e+02 7.405511e+02 -9.607234e+02 -9.933905e+02 3.984855e+03
#> [26] 4.145653e+02 -3.183077e+03 -1.776549e+03 8.340536e+02 2.323735e+03
#> [31] 3.861250e+02 -4.719258e+02 -1.072537e+03 2.790086e-02 5.645311e+03
#> [36] 2.159156e+02 2.532053e+03 -3.401927e+03 -4.756470e+02 -1.735974e+02
#> [41] 1.671329e+03 -3.355987e+01 -3.302869e+02 -1.042772e+03 9.089417e+02
#> [46] -5.821938e+02 -7.604911e+01 1.389021e+03 -1.093324e+04
```



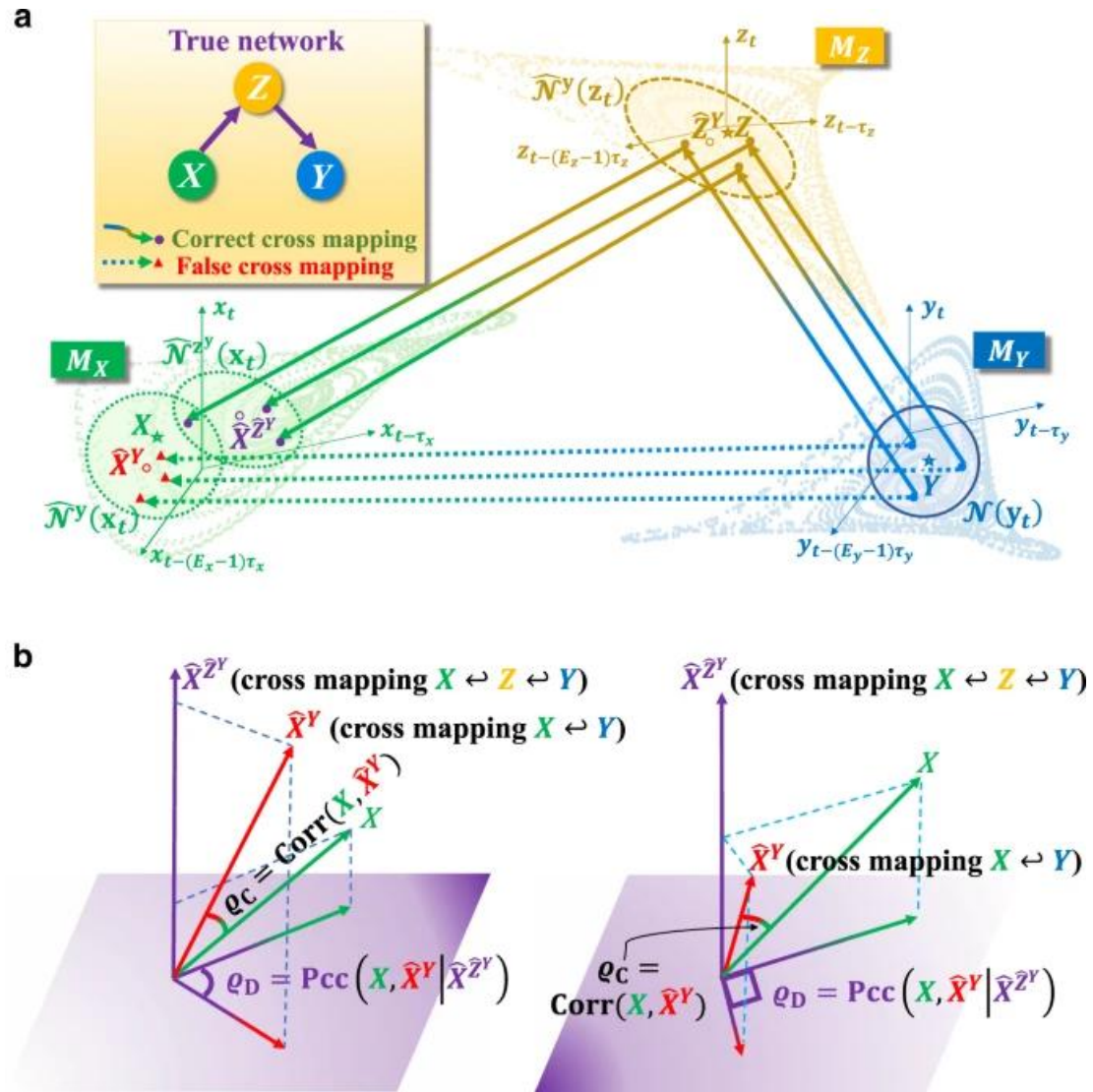
```
# convergent cross-mapping
chickegg = as.data.frame(lmtest::ChickEgg)
ccmres = rEDM::CCM(dataFrame = chickegg, E = 3, columns = "egg", target = "chicken",
                    libSizes = "5 50 5", random = FALSE, noTime = TRUE)
```

ccmres

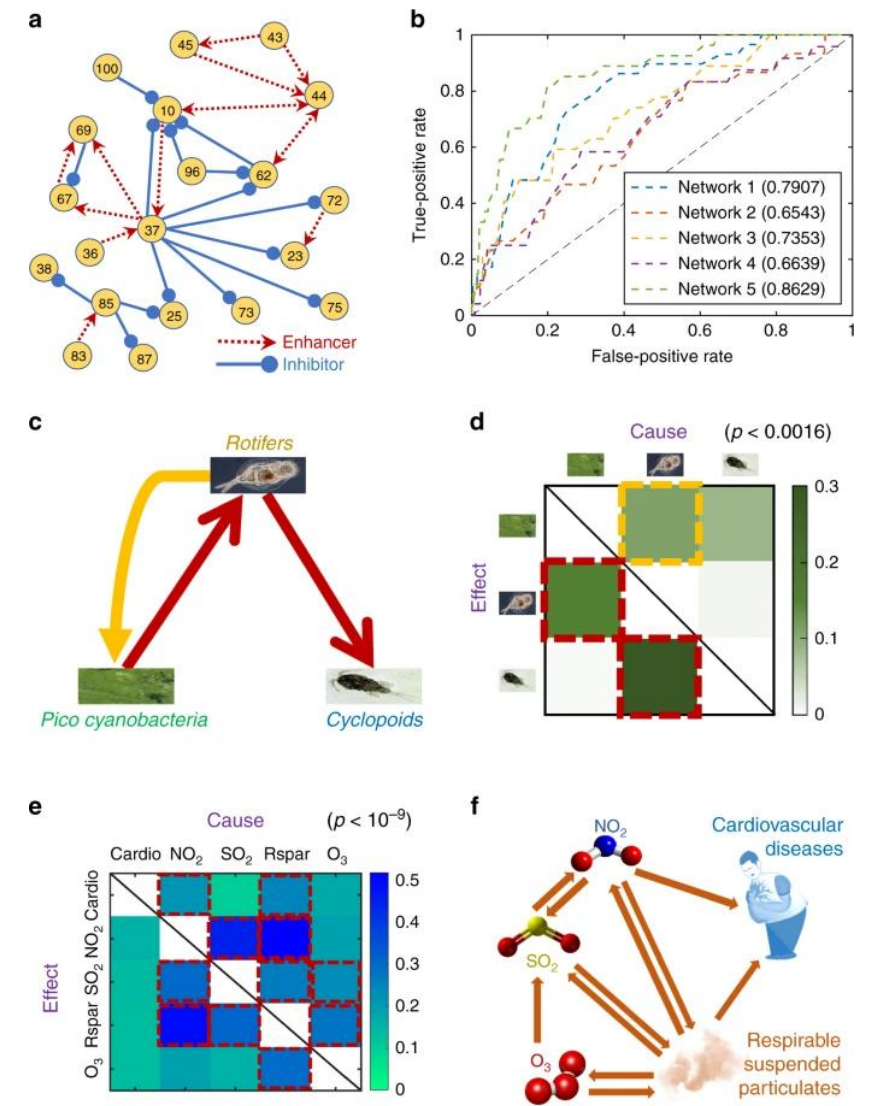
```
#>      LibSize egg:chicken chicken:egg
#> 1         5  0.04364260 -0.39121891
#> 2        10 -0.02381291  0.10223896
#> 3        15 -0.08433760  0.05800941
#> 4        20 -0.03005538 -0.10681737
#> 5        25  0.79516487  0.17436527
#> 6        30  0.78193136  0.22865146
#> 7        35  0.79522593  0.23369108
#> 8        40  0.75874122  0.11634096
#> 9        45  0.77645014  0.10142964
#> 10       50  0.78570387  0.11601891
```



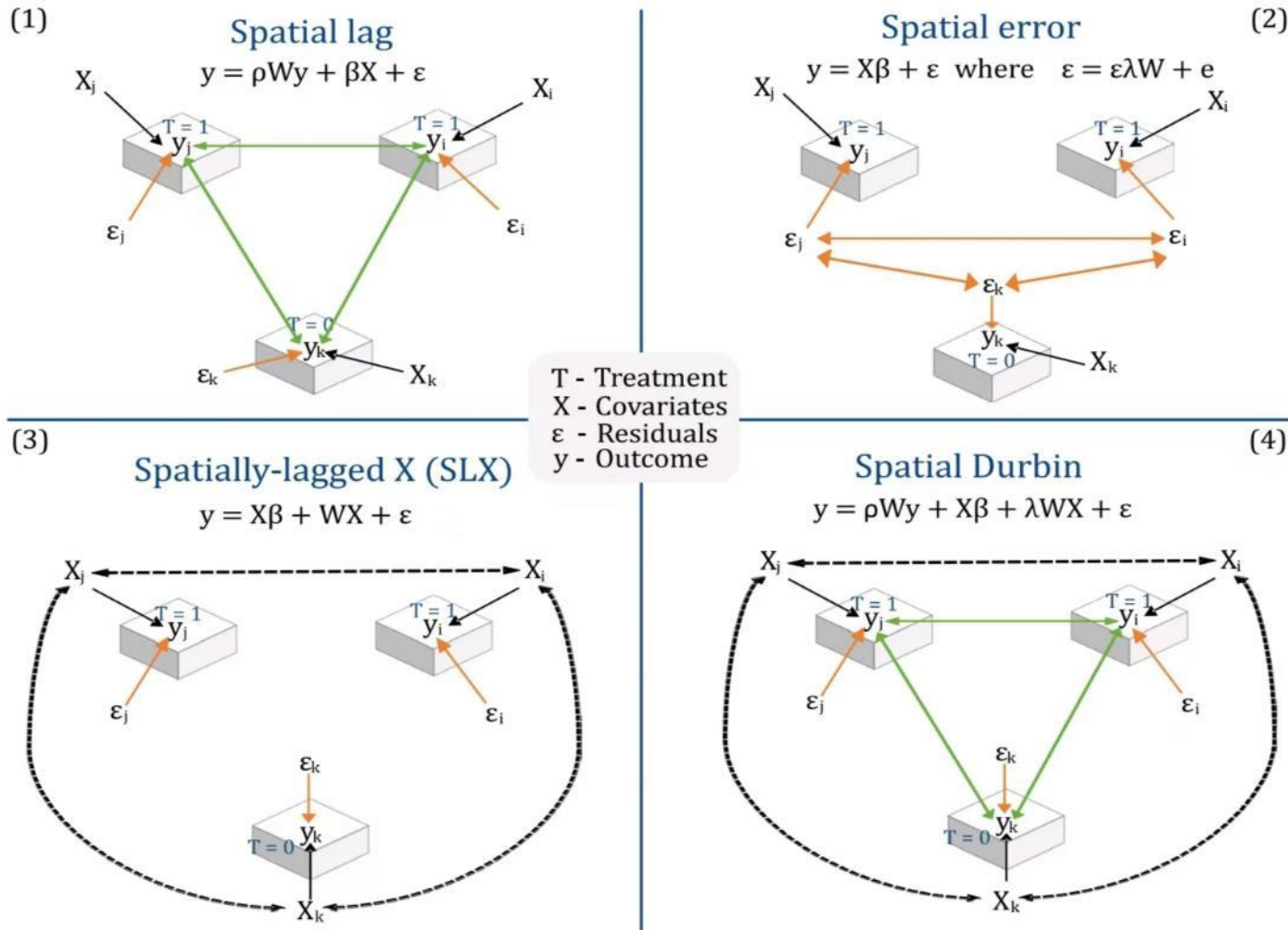
# Partial Cross Mapping



Leng, S., Ma, H., Kurths, J. *et al.* Partial cross mapping eliminates indirect causal influences. *Nat Commun* **11**, 2632 (2020). <https://doi.org/10.1038/s41467-020-16238-0>



# Inferring causation from spatial cross sections



## Spatial Difference-in-differences

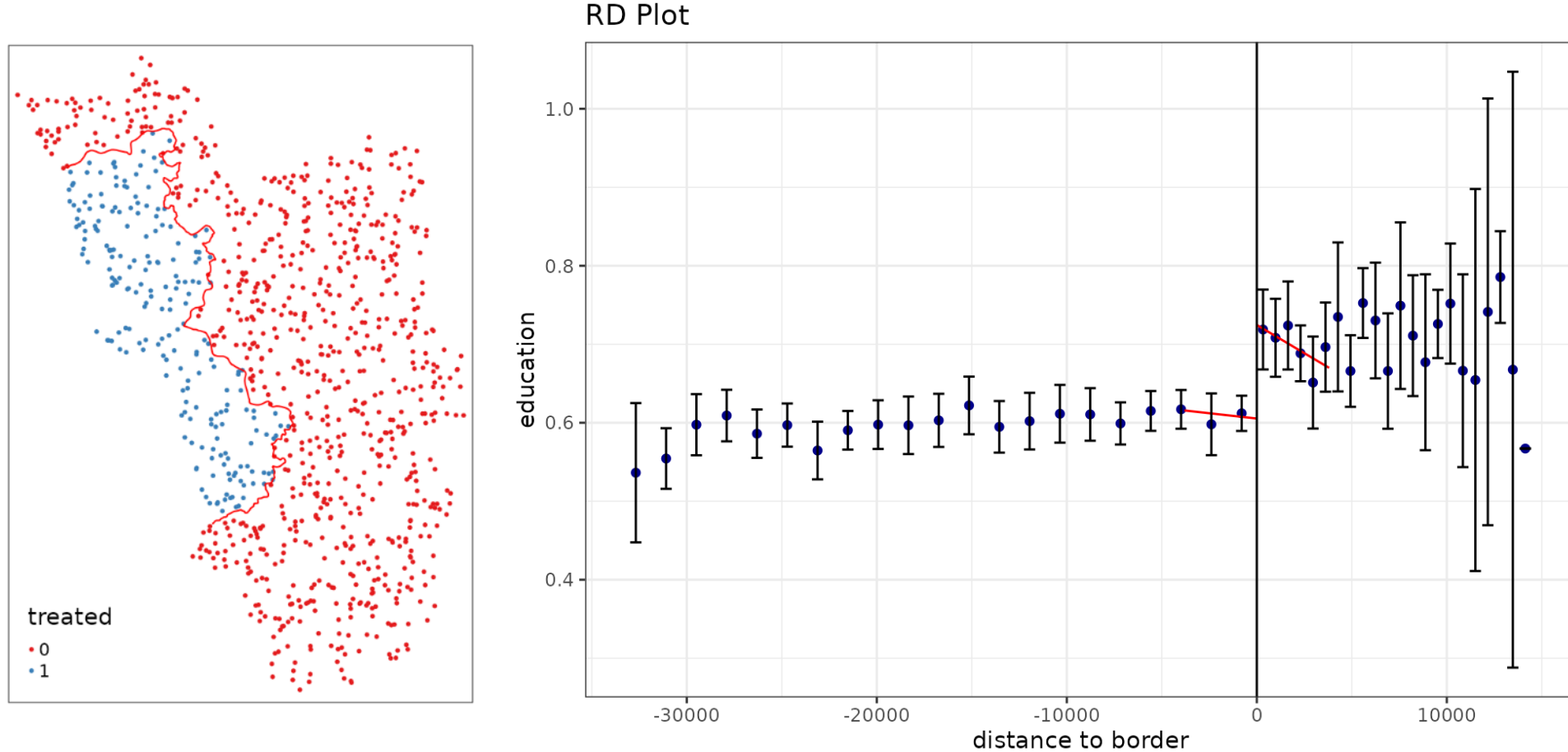
$$y_{it} = \alpha_0 + \alpha_1 X_{it} + \alpha_2 D_{it} + \alpha_3 T_{it} + \alpha_4 D_{it} T_{it} + \varepsilon_{it}$$

$$ATE(x) = E[y|X = x, D = 1, T = 1] - E[y|X = x, D = 0, T = 1] - E[y|X = x, D = 1, T = 0] + E[y|X = x, D = 0, T = 0].$$

Akbari, K., Winter, S. and Tomko, M. (2023), Spatial Causality: A Systematic Review on Spatial Causal Inference. *Geogr Anal*, 55: 56-89.  
<https://doi.org/10.1111/gean.12312>

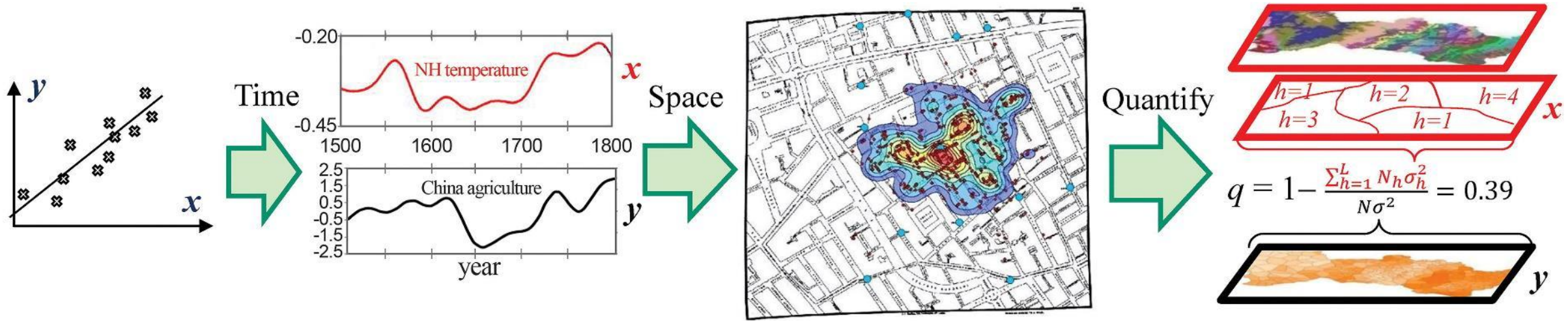


# Spatial Regression Discontinuity Designs



$$y_i = \beta_0 + \beta_1 D_i + \beta_2 \text{dist}_i + \beta_3 D_i \times \text{dist}_i + \sum_{s=1}^S \gamma_b \text{seg}_i^s + v_i' \phi + \epsilon_i$$

# Spatial Stratified Heterogeneity

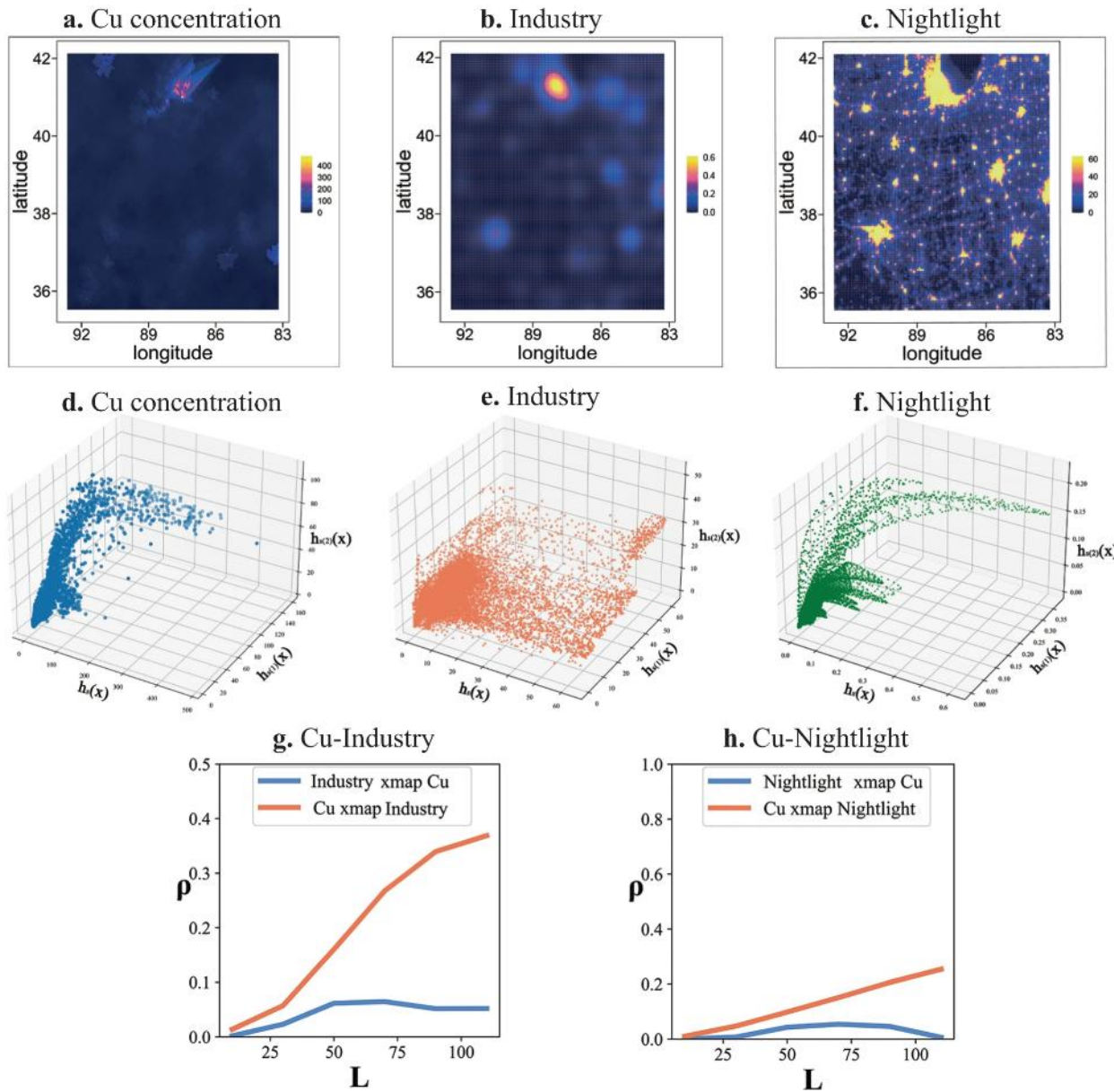


Wang, J., Haining, R., Zhang, T., Xu, C., Hu, M., Yin, Q., ... Chen, H. (2024). Statistical Modeling of Spatially Stratified Heterogeneous Data. *Annals of the American Association of Geographers*, 114(3), 499–519. <https://doi.org/10.1080/24694452.2023.2289982>

```

# geographical detector
columbus = sf::read_sf(system.file("shapes/columbus.gpkg", package="spData"))
gdverse::opgd("HOVAL ~ CRIME", data = columbus, discnum = 3:15)
#> ***      Optimal Parameters-based Geographical Detector
#>
#>
#> | variable | Q-statistic | P-value |
#> | :-----: | :-----: | :-----: |
#> |  CRIME   |  0.5885002 | 0.03009555 |
gdverse::opgd("CRIME ~ HOVAL", data = columbus, discnum = 3:15)
#> ***      Optimal Parameters-based Geographical Detector
#>
#>
#> | variable | Q-statistic | P-value |
#> | :-----: | :-----: | :-----: |
#> |  HOVAL   |  0.627518  | 0.001022616 |

```



# Geographical Convergent Cross Mapping

$$\hat{Y}_s | M_x = \sum_{i=1}^{L+1} (\omega_{si} Y_{si} | M_x)$$

$$\begin{aligned} & \text{dis}(\psi(x, s_i), \psi(x, s)) \\ &= \frac{1}{L} \left( |h_{si}(x) - h_s(x)| + \sum_{k=1}^{L-1} \text{abs}[h_{si(k)}(x), h_{s(k)}(x)] \right) \end{aligned}$$

$$\text{weight}(\psi(x, s_i), \psi(x, s)) = \exp \left( - \frac{\text{dis}(\psi(x, s_i), \psi(x, s))}{\text{dis}(\psi(x, s_1), \psi(x, s))} \right)$$

$$\omega_{si} | M_x = \frac{\text{weight}(\psi(x, s_i), \psi(x, s))}{\sum_{i=1}^{L+1} \text{weight}(\psi(x, s_i), \psi(x, s))}$$

$$\rho = \frac{\text{Cov}(Y, \hat{Y})}{\sqrt{\text{Var}(Y) \text{Var}(\hat{Y})}}$$

Gao, B., Yang, J., Chen, Z. et al. Causal inference from cross-sectional earth system data with geographical convergent cross mapping. Nat Commun 14, 5875 (2023).  
<https://doi.org/10.1038/s41467-023-41619-6>



```
# geographical convergent cross mapping
columbus = sf::read_sf(system.file(
  "shapes/columbus.gpkg", package="spData"))
spEDM::simplex(columbus,target = "HOVAL",
  lib = 1:49)
```

#> The suggested embedding dimension E for variable HOVAL is 6

#>		E	rho	mae	rmse
#>	[1,]	1	0.02078897	17.72059	23.91022
#>	[2,]	2	0.13227442	14.94268	21.20952
#>	[3,]	3	0.30246001	13.70158	18.66540
#>	[4,]	4	0.14412367	15.07788	20.40852
#>	[5,]	5	0.17810605	15.14727	20.34214
#>	[6,]	6	0.33371524	13.96825	18.88074
#>	[7,]	7	0.30107433	13.43619	19.09429
#>	[8,]	8	0.29861812	13.51815	19.13343
#>	[9,]	9	0.29555999	13.55432	19.17256
#>	[10,]	10	0.29555999	13.55432	19.17256

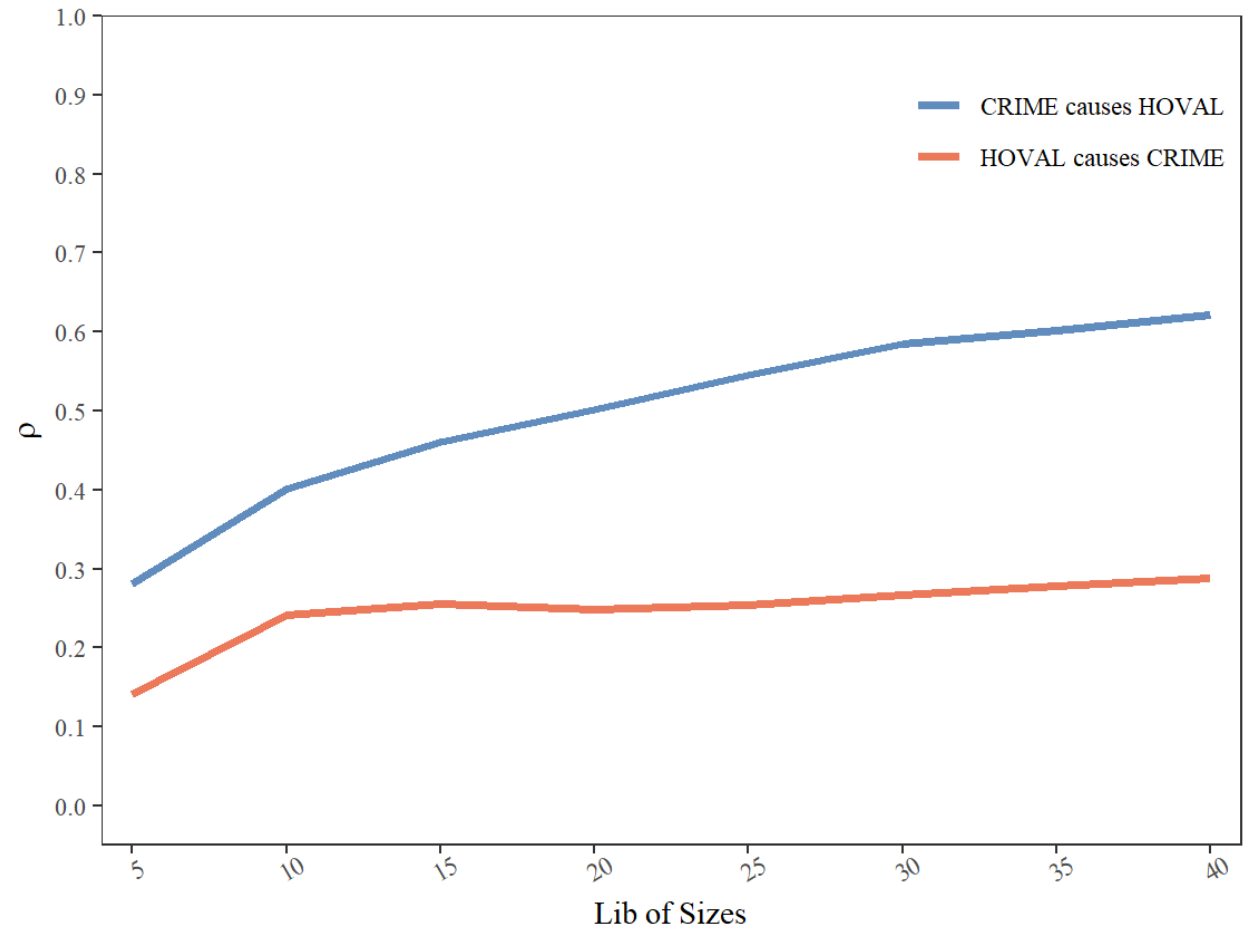
```
spEDM::simplex(columbus,target = "CRIME",
  lib = 1:49)
```

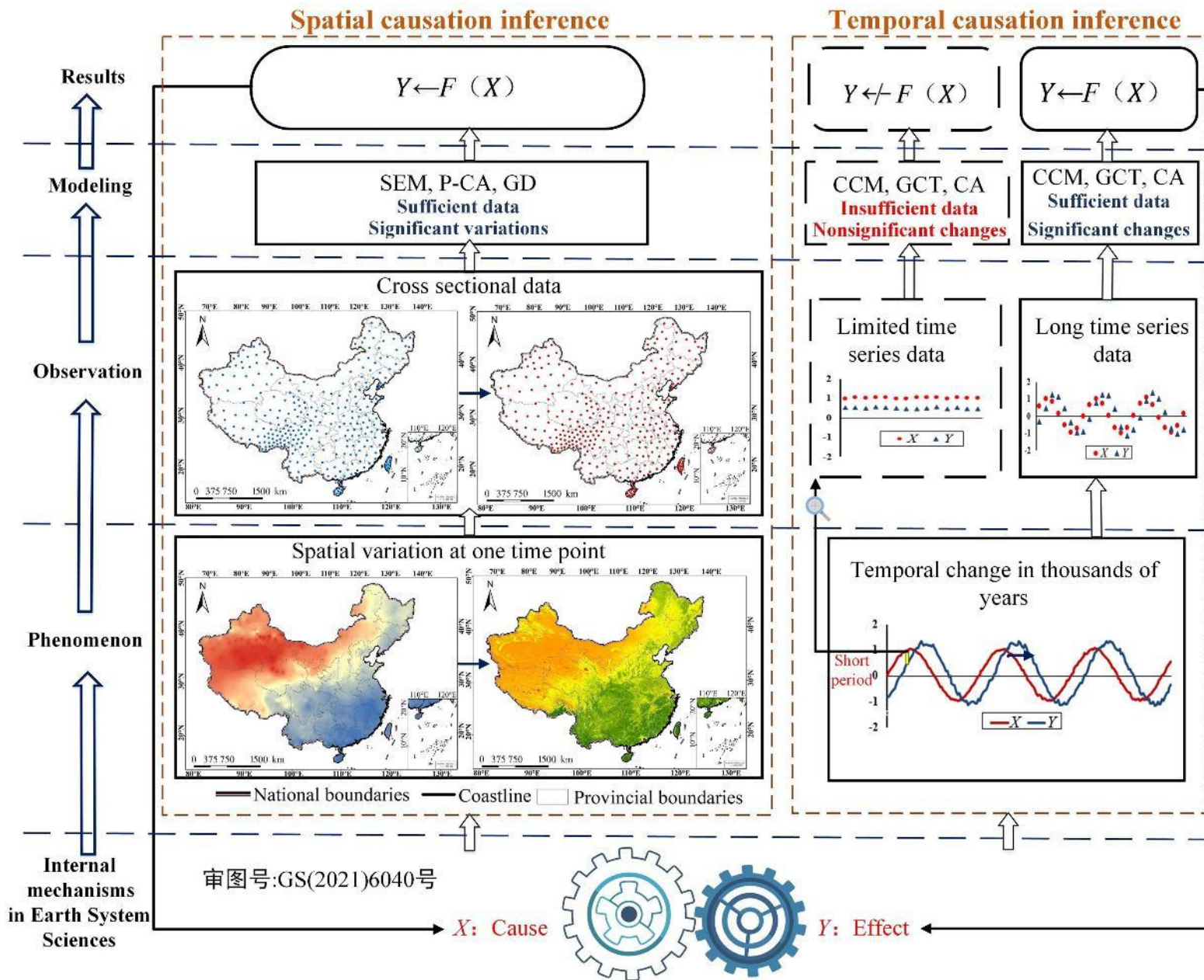
#> The suggested embedding dimension E for variable CRIME is 5

#>		E	rho	mae	rmse
#>	[1,]	1	0.5064332	10.752317	15.45595
#>	[2,]	2	0.5832484	9.753875	14.06003
#>	[3,]	3	0.6026672	10.093884	13.82248
#>	[4,]	4	0.6174598	10.269995	13.71842
#>	[5,]	5	0.6313140	9.808677	13.45584
#>	[6,]	6	0.6285516	9.832107	13.58268
#>	[7,]	7	0.6299036	9.787748	13.55552
#>	[8,]	8	0.6304351	9.769181	13.54919
#>	[9,]	9	0.6303645	9.770848	13.55023
#>	[10,]	10	0.6303645	9.770848	13.55023

```
g = spEDM::gccm(columbus, "HOVAL", "CRIME",
                libsizes = seq(5,40,5), E = c(6,5))
#> Computing: [=====] 100% (done)
#> Computing: [=====] 100% (done)
```

```
g
#>   libsizes HOVAL->CRIME CRIME->HOVAL
#> 1         5    0.1405456    0.2804058
#> 2        10    0.2413240    0.4006664
#> 3        15    0.2554682    0.4609814
#> 4        20    0.2482281    0.5019578
#> 5        25    0.2541110    0.5452084
#> 6        30    0.2671786    0.5847262
#> 7        35    0.2783446    0.6019328
#> 8        40    0.2876909    0.6217028
...`
```





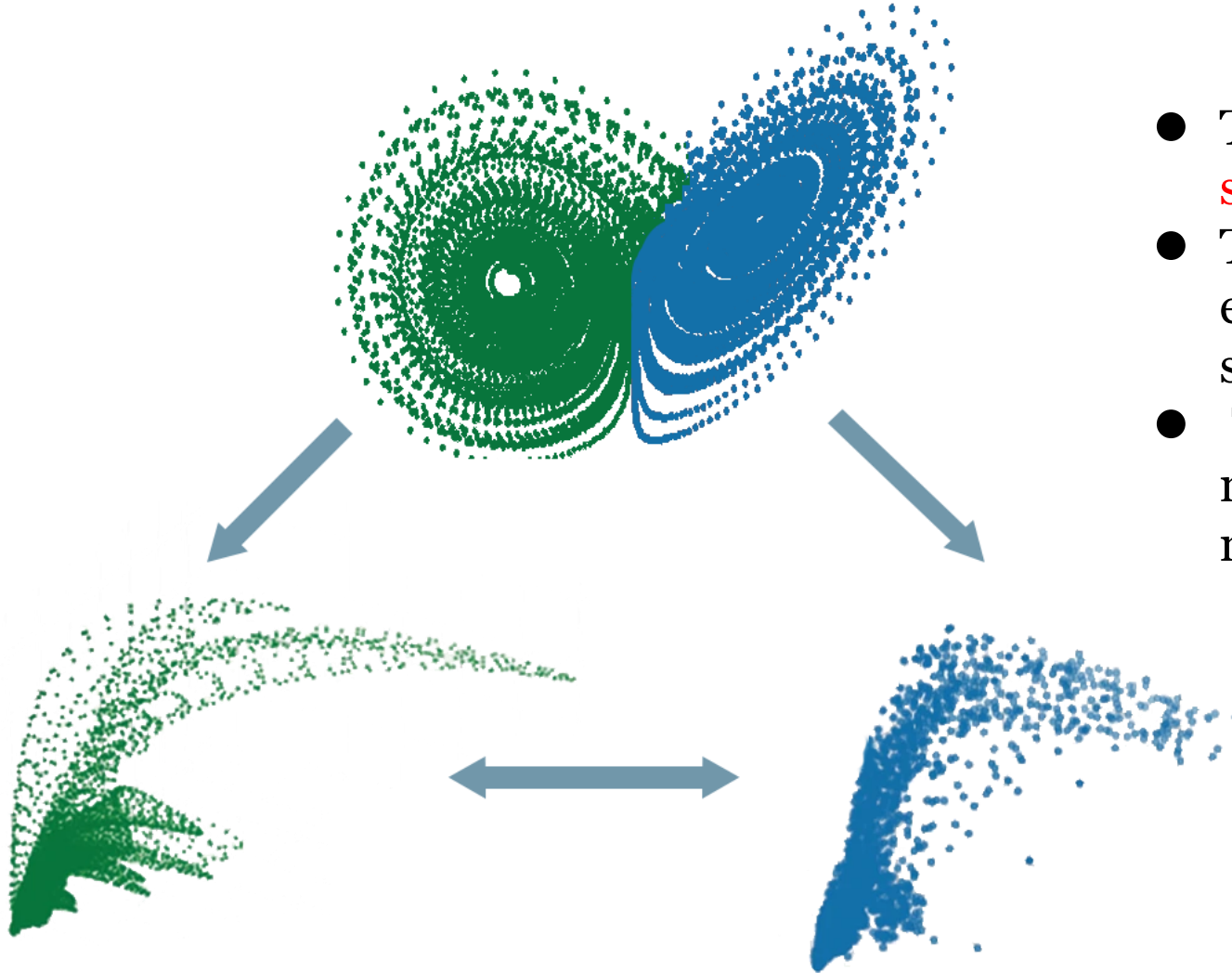
# Temporally or spatially?

- Capture causality through **temporal variations** reflected in *time series data*.
- Capture causality through **spatial variations** reflected in *spatial cross-sectional data*.
- When changes are **insufficient** in time or space, **incorporate information** from the other dimension to capture causality.
- Jointly model causality using both spatial and temporal information.

Gao, B., Li, M., Wang, J., & Chen, Z. (2022). Temporally or spatially? Causation inference in earth system sciences. *Sci. Bull*, 67(3).



# Spatial Empirical Dynamic Modeling



- The Earth is a highly interconnected **dynamical system**.
- The **state space reconstruction** method can be effectively applied to causal inference in dynamic systems.
- There are many state space reconstruction models oriented towards time series, but similar models in the **spatial domain** are relatively few.

[1]George Sugihara et al. ,Detecting Causality in Complex Ecosystems.Science338,496-500(2012).DOI:10.1126/science.1227079

- [2]Runge, J., Gerhardus, A., Varando, G. et al. Causal inference for time series. Nat Rev Earth Environ 4, 487–505 (2023).

<https://doi.org/10.1038/s43017-023-00431-y>

[3]Gao, B., Yang, J., Chen, Z. et al. Causal inference from cross-sectional earth system data with geographical convergent cross mapping. Nat Commun 14, 5875 (2023). <https://doi.org/10.1038/s41467-023-41619-6>





## spEDM: Spatial Empirical Dynamic Modeling

*Inferring causal associations in cross-sectional earth system data through empirical dynamic modeling (EDM), with extensions to convergent cross mapping from Sugihara et al. (2012) <[doi:10.1126/science.1227079](https://doi.org/10.1126/science.1227079)>, partial cross mapping as outlined in Leng et al. (2020) <[doi:10.1038/s41467-020-16238-0](https://doi.org/10.1038/s41467-020-16238-0)>, and cross mapping cardinality as described in Tao et al. (2023) <[doi:10.1016/j.fmre.2023.01.007](https://doi.org/10.1016/j.fmre.2023.01.007)>.*






Wenbo Lv



Authors: Wenbo Lv [aut, cre, cph]


 [spEDM\\_1.5.tar.gz](#)

 [spEDM\\_1.5.zip](#) (r-4.5) [spEDM\\_1.5.zip](#) (r-4.4) [spEDM\\_1.5.zip](#) (r-4.3)

 [spEDM\\_1.5.tgz](#) (r-4.5-x86\_64) [spEDM\\_1.4.tgz](#) (r-4.5-arm64) [spEDM\\_1.5.tgz](#) (r-4.4-x86\_64) [spEDM\\_1.5.tgz](#) (r-4.4-arm64) [spEDM\\_1.5.tgz](#) (r-4.3-x86\_64) [spEDM\\_1.5.tgz](#) (r-4.3-arm64)

 [spEDM\\_1.5.tar.gz](#) (r-4.5-noble) [spEDM\\_1.5.tar.gz](#) (r-4.4-noble) 

 [spEDM\\_1.5.tgz](#) (r-4.4-emsripten) [spEDM\\_1.5.tgz](#) (r-4.3-emsripten) 

 [spEDM.pdf](#) | [spEDM.html](#) ✨

 [spEDM/json](#) (API)

 [NEWS](#)

# Install 'spEDM' in R:

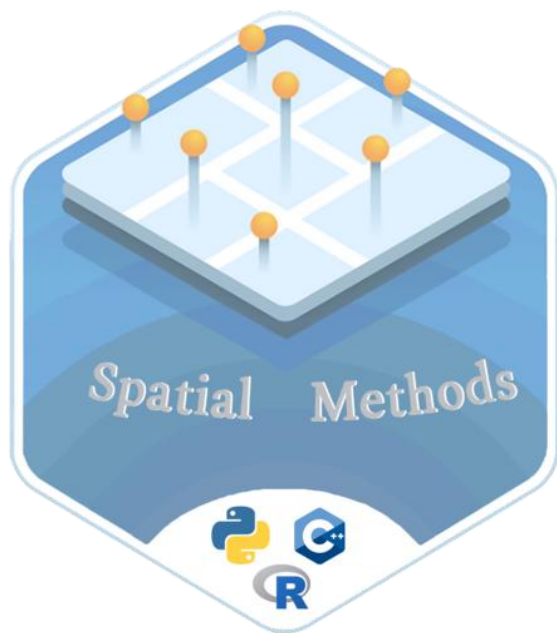
```
install.packages('spEDM', repos = c('https://stsc1.r-universe.dev', 'https://cloud.r-project.org'))
```



# Thanks.

[https://github.com/ai4city-hkust/geocausality\\_workshop](https://github.com/ai4city-hkust/geocausality_workshop)

[https://ai4city-hkust.github.io/workshop/geocausality/geocausality\\_workshop.html](https://ai4city-hkust.github.io/workshop/geocausality/geocausality_workshop.html)



Wenbo Lv

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Spatial Statistics; Causality;  
Geoinformatics; R; C++;

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SpatLyu / README.md

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Total PRs: 290  
Total Issues: 99  
Contributed to (last year): 52

A



I use these R packages a lot:



I authored and maintain these R packages:



About

- I am currently an undergraduate majoring in *Geographic Information Science* at *Shaanxi Normal University*, while also serving as a research assistant at *The Hong Kong Polytechnic University* and *The Hong Kong University of Science and Technology (Guangzhou)*.
- My research interests focus on **developing innovative spatial analysis methods** that leverage **spatial relationships**, such as *spatial dependence*, *spatial heterogeneity*, and *geographical similarity*, to advance *urban sustainability* and *climate change mitigation* efforts, and also include **developing the corresponding open source softwares**.
- I look forward to working with friends of all backgrounds to explore the fun of **statistics** and **programming**!
- How to reach me: message me at [zhihu](#) and [mastodon](#)!
- Ping me about #Geoinformatics, #Statistics, #R, #C++, #Python and anything you like!