

Curs 4 - Prima parte pg. 1-33
Transformări geometrice

Region props: Proprietăți de regiune: aria, perimetrul, ox, inclinarea, centru de greutate

Imagini BW (binare)

Grayscale (de nivele gri) $> \text{prag} = \begin{cases} \text{alb } 255/1, \text{ prag} > 128 \\ \text{negru } 0, \text{ altfel} \end{cases}$
threshold

Proprietățile geometrice ale imaginilor binare

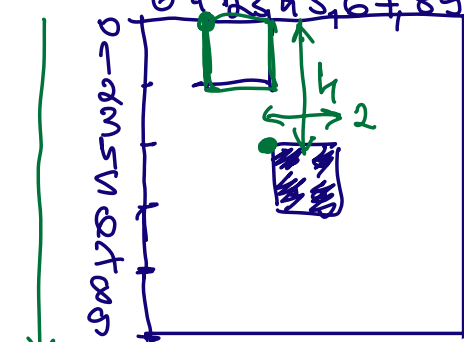
- Centrul de greutate (centrul de masă)

$$\bar{x} = \frac{\sum_{x=1}^w \sum_{y=1}^h x \cdot I(x,y)}{A}$$

$$\bar{y} = \frac{\sum_{x=1}^w \sum_{y=1}^h y \cdot I(x,y)}{A}$$

Transformări geometrice:

1. Translație $f(x,y) = I(x+a, y+b)$

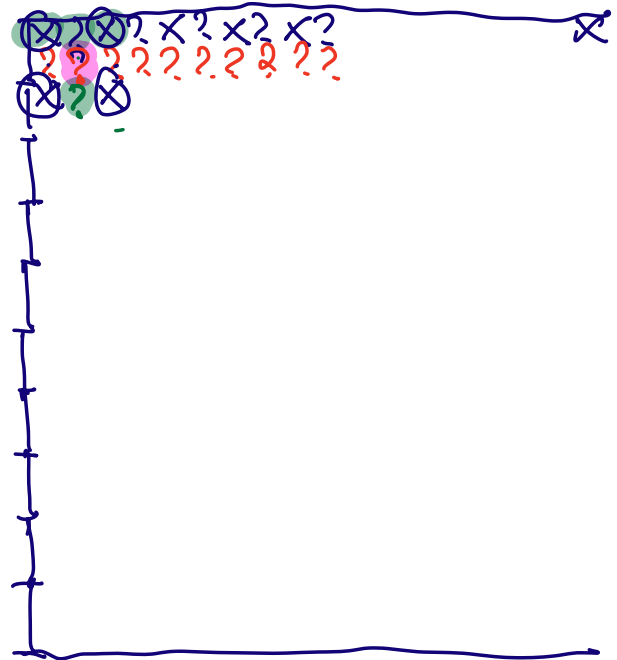
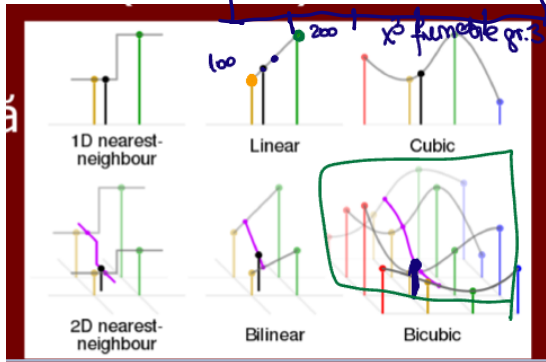


$$f(x,y) = I(x-4, y-2)$$

2. Scalare (zoom): $f(x,y) = I(a \cdot x, b \cdot y)$

factor de scalare a , pe axa x
 b , pe axa y

10x10: \Rightarrow 20x20



Pixeli lipsă se interpolatează prin metode matematice de interpolare: interp. liniară 1D ✓
2D (bilineară) ✓

interp. cubică

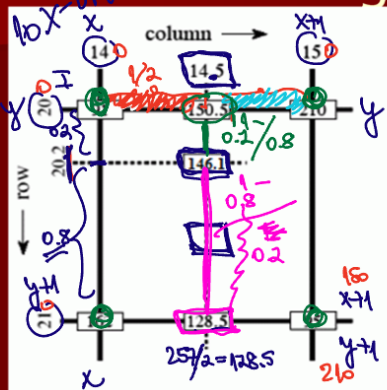
interp. bicubică

laminar

spline bicubic ??? spline

Matlab resi

Interpolarea biliniară în cazul imaginilor



$$I_{20.2, 14.5} = \frac{0.8}{21-20} \cdot 150.5 + \frac{0.2}{21-20} \cdot 128.5 = 146.1$$

$$I_{20.2, 14.5} = \frac{0.8}{1} \cdot 150.5 + \frac{0.2}{1} \cdot 128.5 = 146.1$$

$$I_{14.5, 20.2} = \frac{14.5-14}{14-15} \cdot 91 + \frac{15-14.5}{15-14} \cdot 210$$

Se cunosc 4 pixeli

$I(20, 14)=91$, $I(21, 14)=162$, $I(20, 15)=210$, $I(21, 15)=95$

Se obține pt. $I(14.5, 20.2)=146.1$

Interpolarea bicubică

- În acest caz se cunosc 4 puncte (0,0), (0,1), (1,0), (1,1)

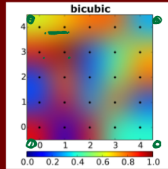
- Se calculează derivatele f_x, f_y, f_{xy} în

- fiecare dintre cele 4 puncte

$$p(x, y) = \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} x^i y^j$$

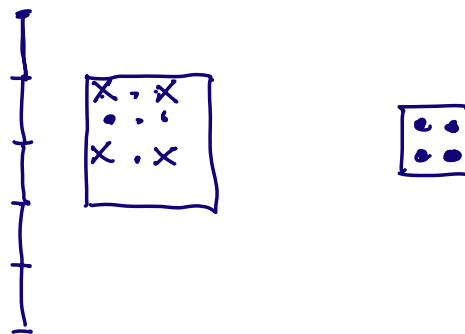
$$\begin{aligned} 1. f(0, 0) &= a_{00} \\ 2. f(1, 0) &= a_{00} + a_{10} + a_{20} + a_{30} \\ 3. f(0, 1) &= a_{00} + a_{01} + a_{02} + a_{03} \\ 4. f(1, 1) &= \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} \end{aligned}$$

https://en.wikipedia.org/wiki/Bicubic_interpolation



2. Rescale $1/2 = 0.5$

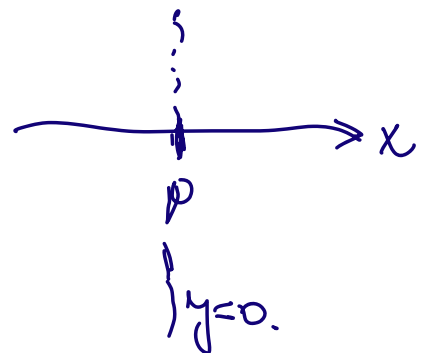
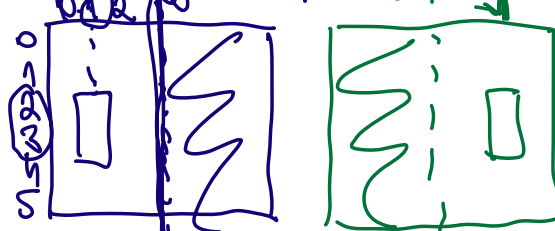
$30 \times 30 \Rightarrow 15 \times 15$



3. Oglinzire: Flip orizontal (retical)

$f(x', y') = I(-x, y)$ de la axa X.

$f(x', y') = I(x, -y)$ de la axa Y.



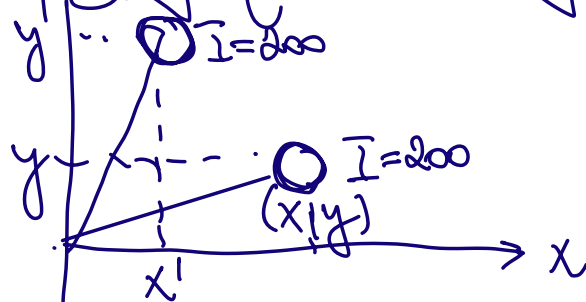
4. Rotatie: $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$ θ : direcția trigonometrică în sens acelor de ceasornic

Transformare (translatie, rotatie, scala)

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} x_0 \\ y_0 \end{bmatrix}$$

Translație
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} x_0 \\ y_0 \end{bmatrix}$$

Rotatie
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$



Scalare
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \alpha & 0 \\ 0 & \beta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \alpha x \\ \beta y \end{bmatrix}$$

Reflexie
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Transformare generică afină: se păstrează unghiurile

Transformare de împingere shear
distorsiune

$$\begin{bmatrix} 1 & 0 \\ m & 1 \end{bmatrix} \text{ y împingere } \begin{bmatrix} 1 & m \\ 0 & 1 \end{bmatrix} \text{ directoare } x$$

Transformare proiectivă: liniile nu se mențin paralele

Interpolarea celui mai apropiat vecin

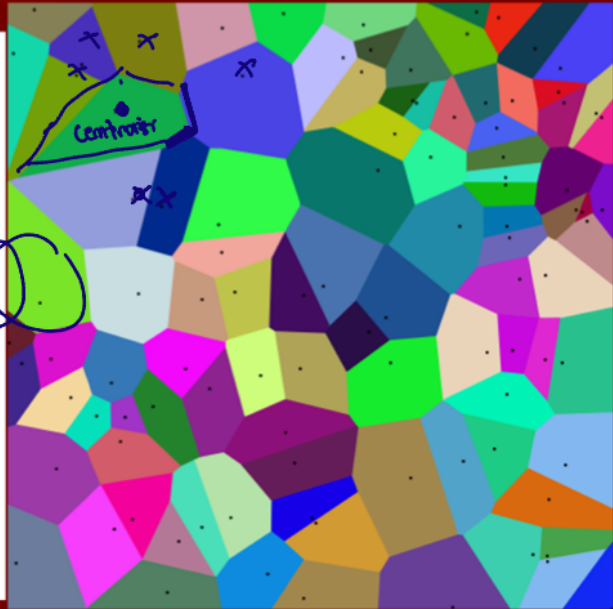
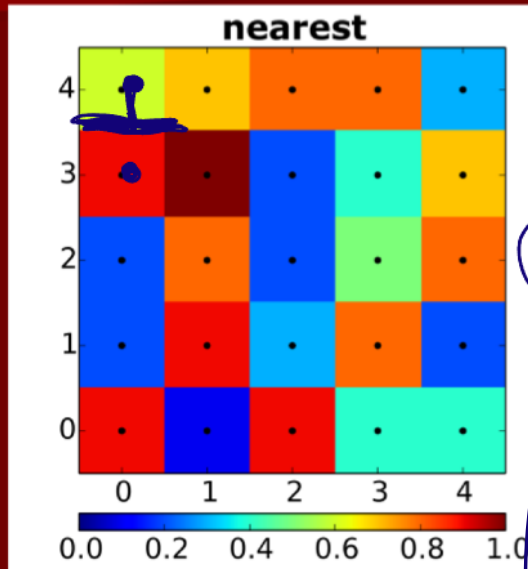


Diagrama Voronoi

antene tel. mobile
radio circulare

Termen finalizare proiect/tutoriale joi 26.10.2022
ora 23:59,
Prezentare marți ora 16/17/18/19.

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