



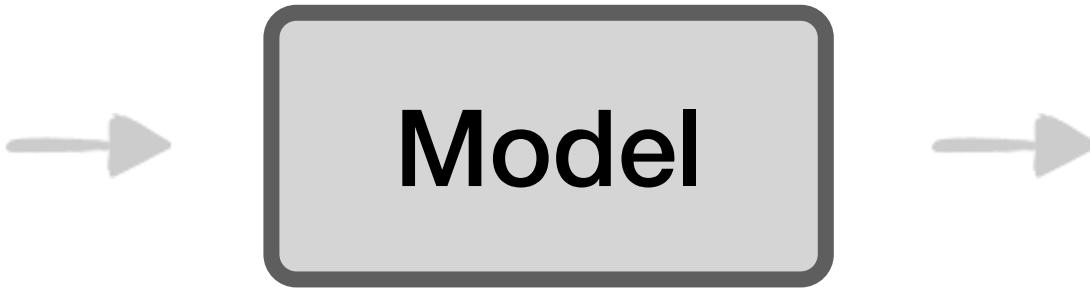
AIBridge

Lecture 6

Classification!

quick review
wine dataset

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol



White = 0
Red = 1

a class

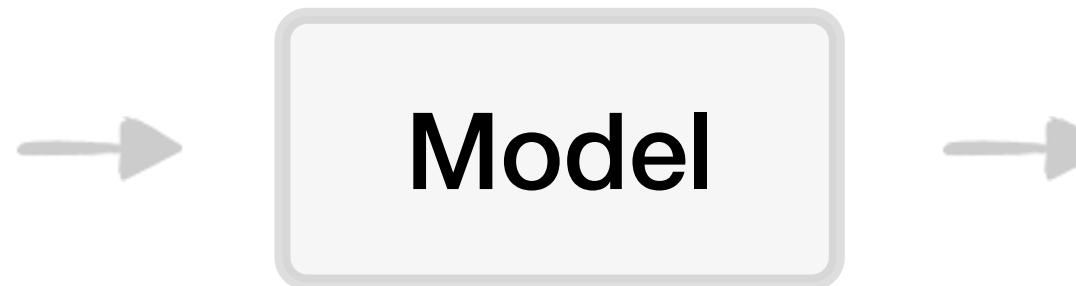
- categorical label outputs are named “classes”

Classification!

quick review
wine dataset

- Fixed acidity
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- Alcohol

that's a lot
of features!



White = 0
Red = 1

a class

- categorical label outputs are named “classes”

- Fixed acidity
 - Volatile acidity
 - Citric acid
 - Residual sugar
 - Chlorides
 - Free sulfur dioxide
 - Total sulfur dioxide
 - Density
 - pH
 - Sulphates
 - Alcohol
- Linear models might not be the best in some cases

Decision Trees

Decision Trees



Decision Trees



Can I afford it?

Decision Trees



Can I afford it?

Is it comfortable?

Decision Trees



Can I afford it?

Is it comfortable?

Is it fashionable?

Decision Trees

Can I afford it?

Is it comfortable?

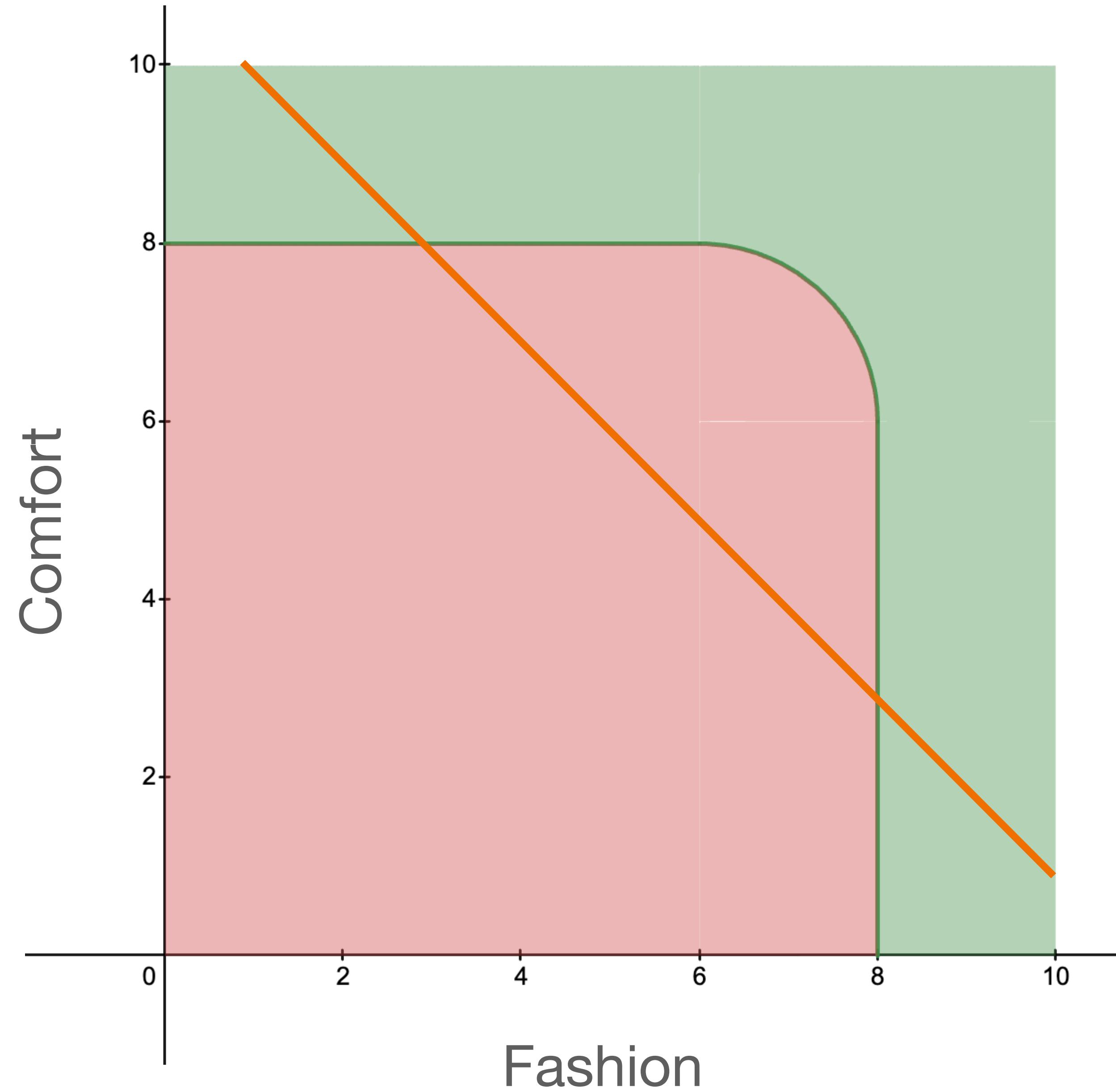
Is it fashionable?

Decision Trees

Can I afford it?

Is it comfortable?

Is it fashionable?



Decision Trees



Decision Trees

that seems awfully hard-coded!

- flowcharts of decisions can create an explainable and repeatable graph of predictions



Decision Trees

Price	Comfort	Fashion	Purchased?
\$70	4	6	No
\$120	5	8	No
\$20	4	4	No
\$60	1	8	Yes
\$60	6	3	No
\$80	8	8	Yes

Decision Trees

Purchased?

No

No

No

Yes

No

Yes

Decision Trees

No

No

No

Yes

No

Yes

Decision Trees

No	Yes
No	No
No	Yes

Decision Trees



Decision Trees

Gini impurity



- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.

Decision Trees

Gini impurity

Purchased?	
	No
0	No
	No
	Yes
0.44	No
	Yes
	No
	No
	Yes

- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.
- perfect groups => 0 **Gini Impurity** => 100% predictions

Decision Trees

Gini impurity

$$G = \sum_{i=1}^C P(i) \cdot (1 - P(i))$$

Fraction of that one class
in group Fraction of not that one
class in the group

The diagram illustrates the Gini impurity formula. It shows the formula $G = \sum_{i=1}^C P(i) \cdot (1 - P(i))$ with two orange arrows pointing down to the terms $P(i)$ and $(1 - P(i))$. Below the formula, an orange arrow points up to the summation symbol \sum , with the text "Add them up for all classes (in one side of the split)" written below it.

- **Gini impurity** measures the homogeneity in a group

Decision Trees

Purchased?

No

0

No

No

Yes

0.5

No

Yes

0.5

Decision Trees

Purchased?

No

No

0.38

No

Yes

No

0.5

Yes

0.88

Decision Trees

we gotta do better
than this, right?



Purchased?

No

No 0

No

Yes

No 0.44

Yes

0.44

Decision Trees

just split
again!

Purchased?

No

No 0

No

Yes

No 0.44

Yes

0.44

Decision Trees

1. Make splits (using features and thresholds)
2. Calculate Gini impurities
3. Select the split that results in the lowest Gini impurity sum
4. If unhappy, **just split again!**
5. Repeat 1-4 as much as needed



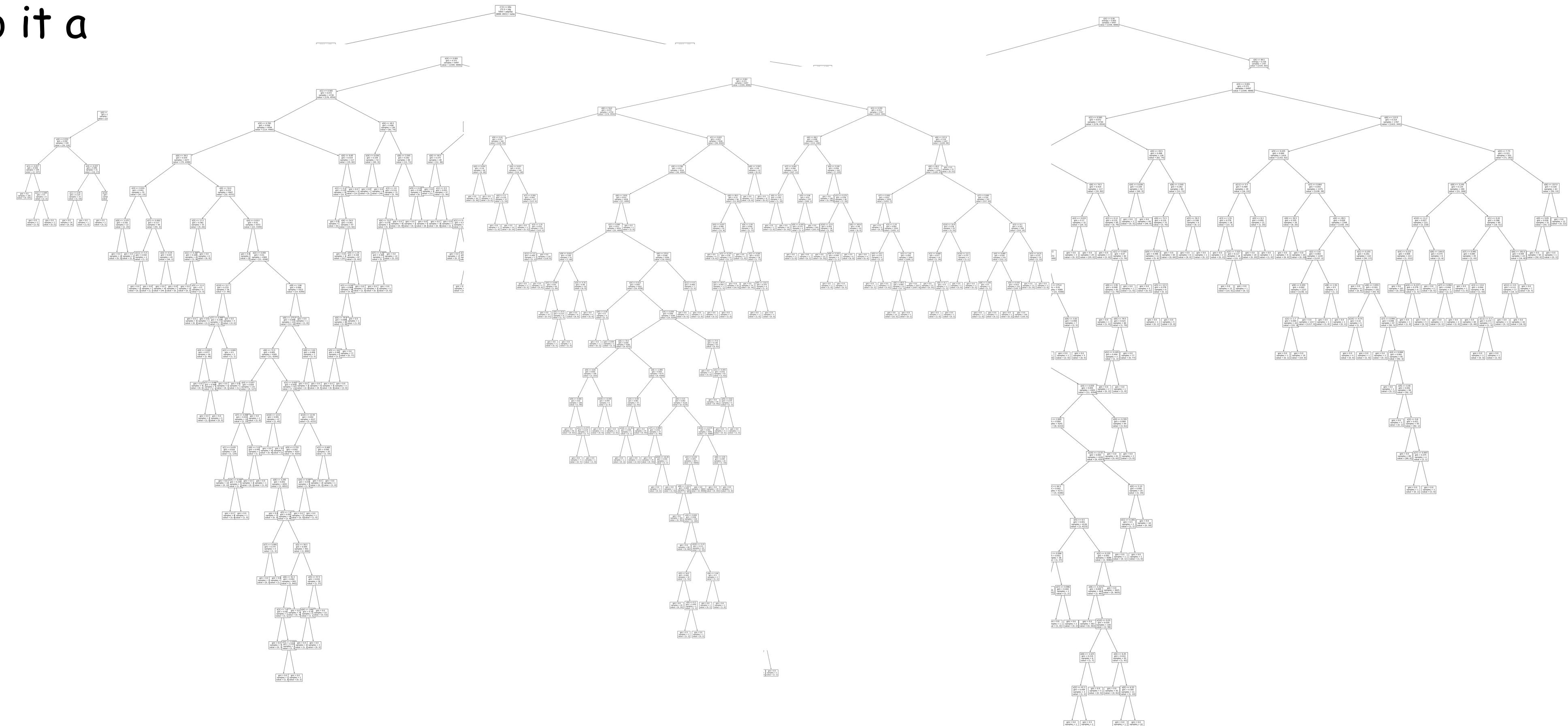
a hyperparameter

Decision Trees

What if we do it a lot?



diverse



Decision Trees

Random Forest



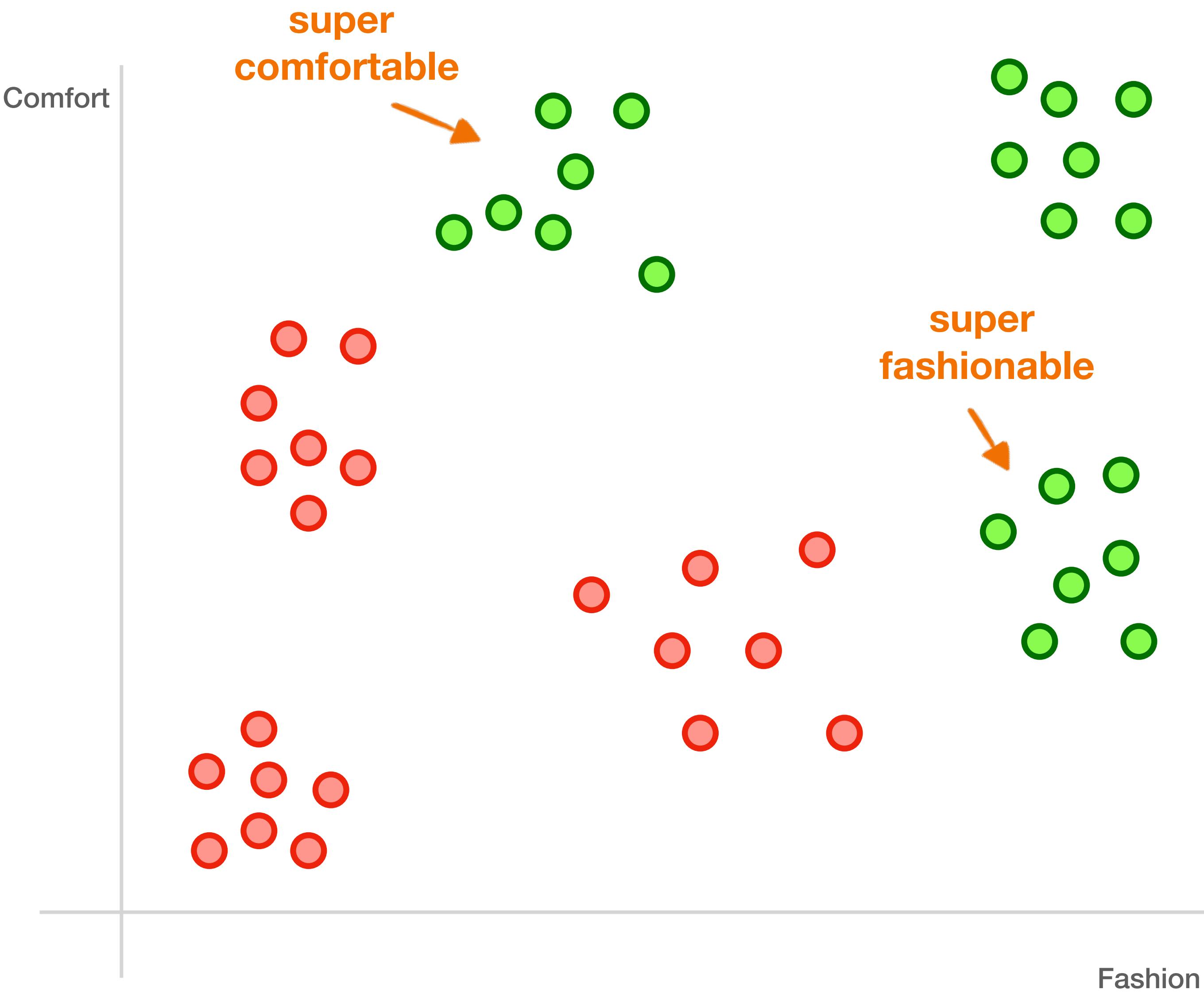
Decision Trees

Random Forest

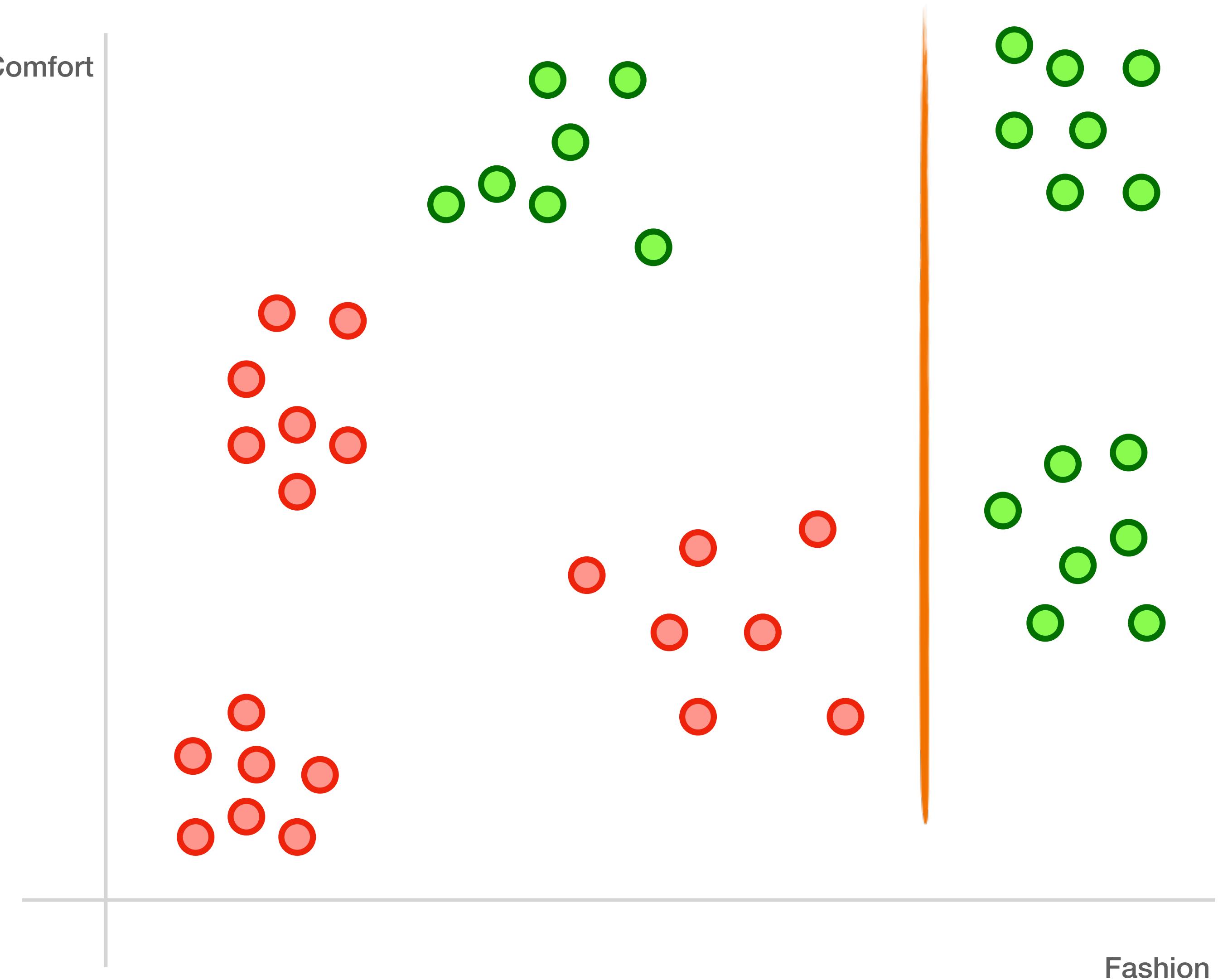
1. Make a lot of decision trees, on different portions of the data
2. For a new sample, run all of them
3. Combine their votes and take the majority

“split”

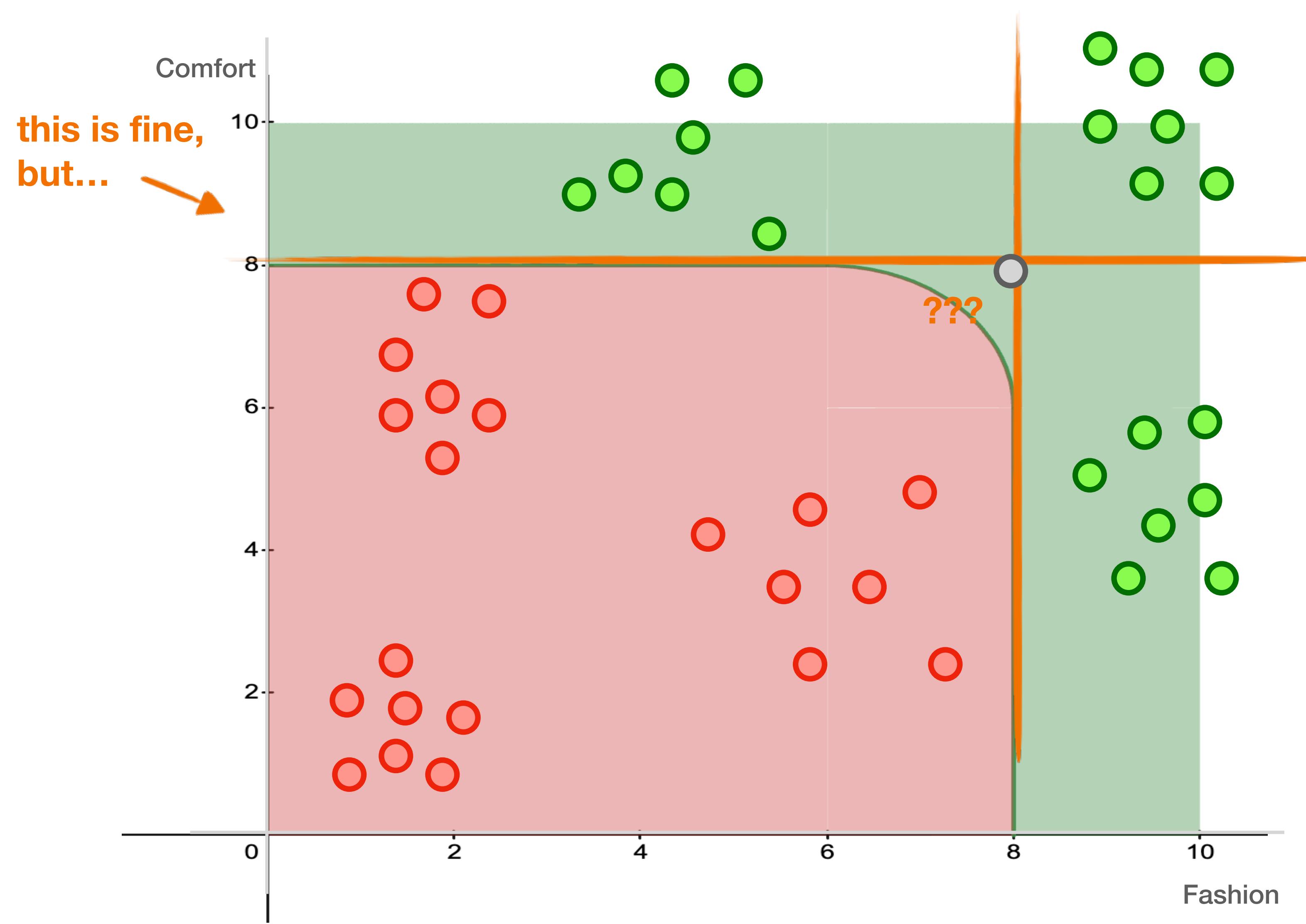
“split”



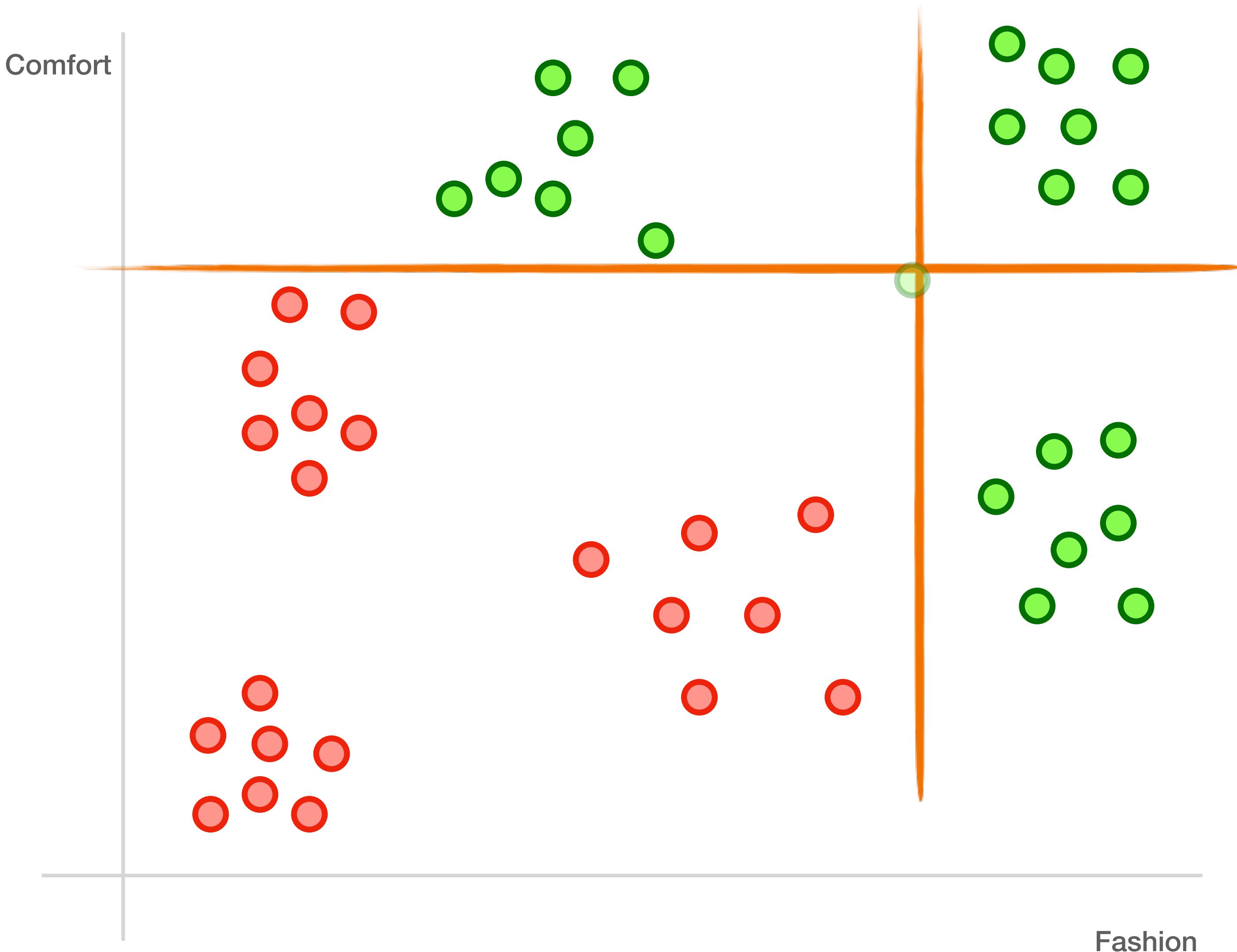
“split”



“split”

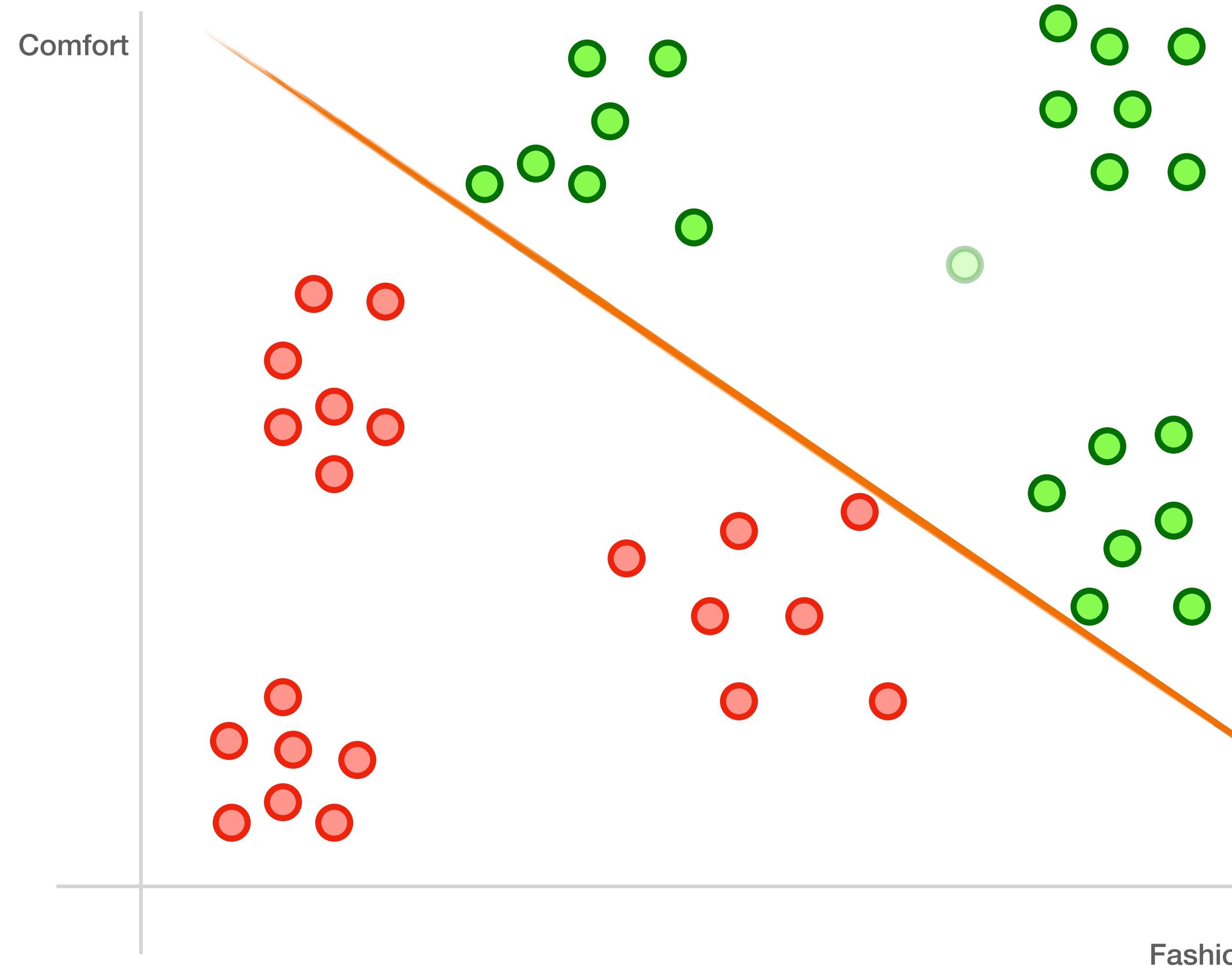


“split”

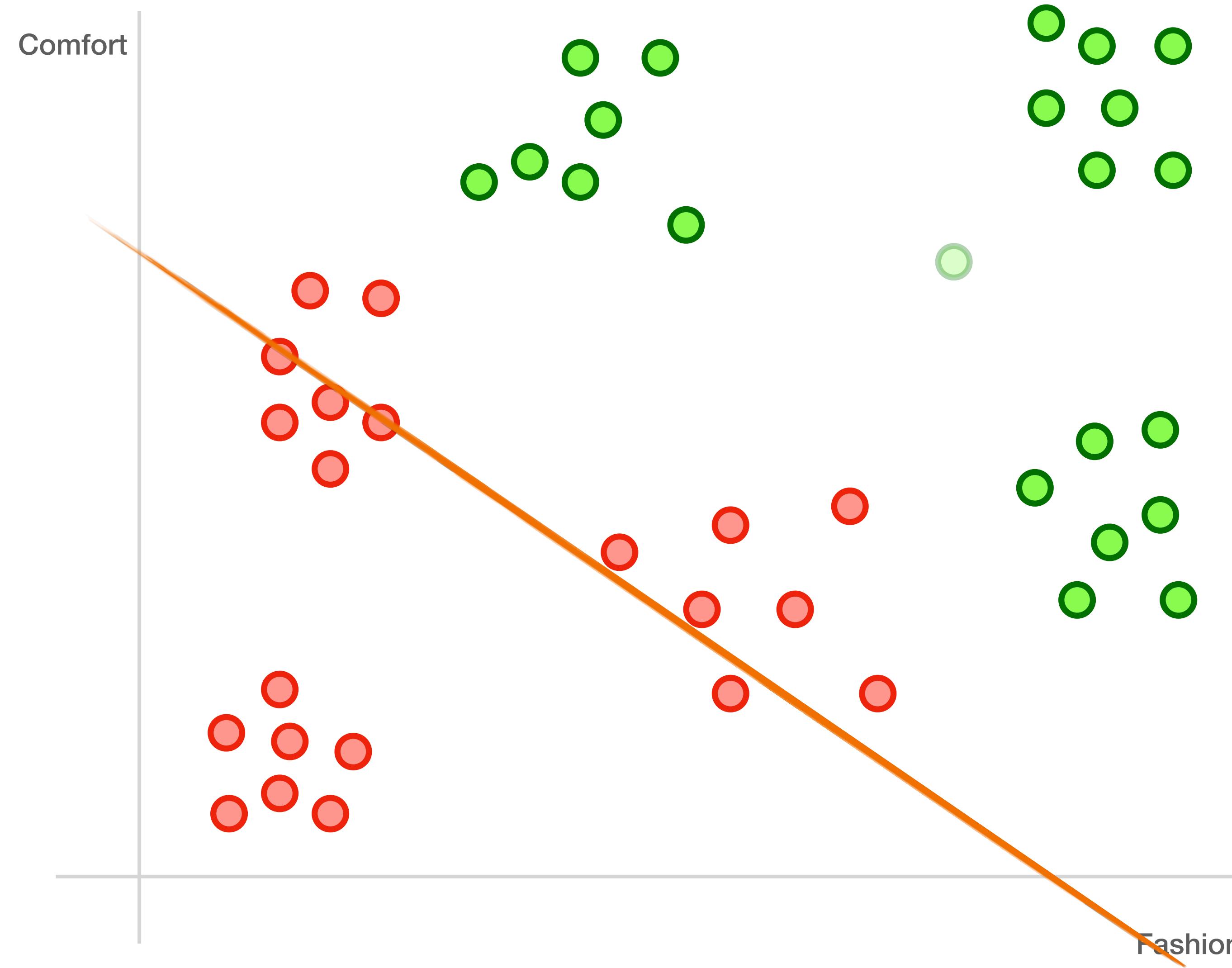


we need a more complex split
Support vector machines!

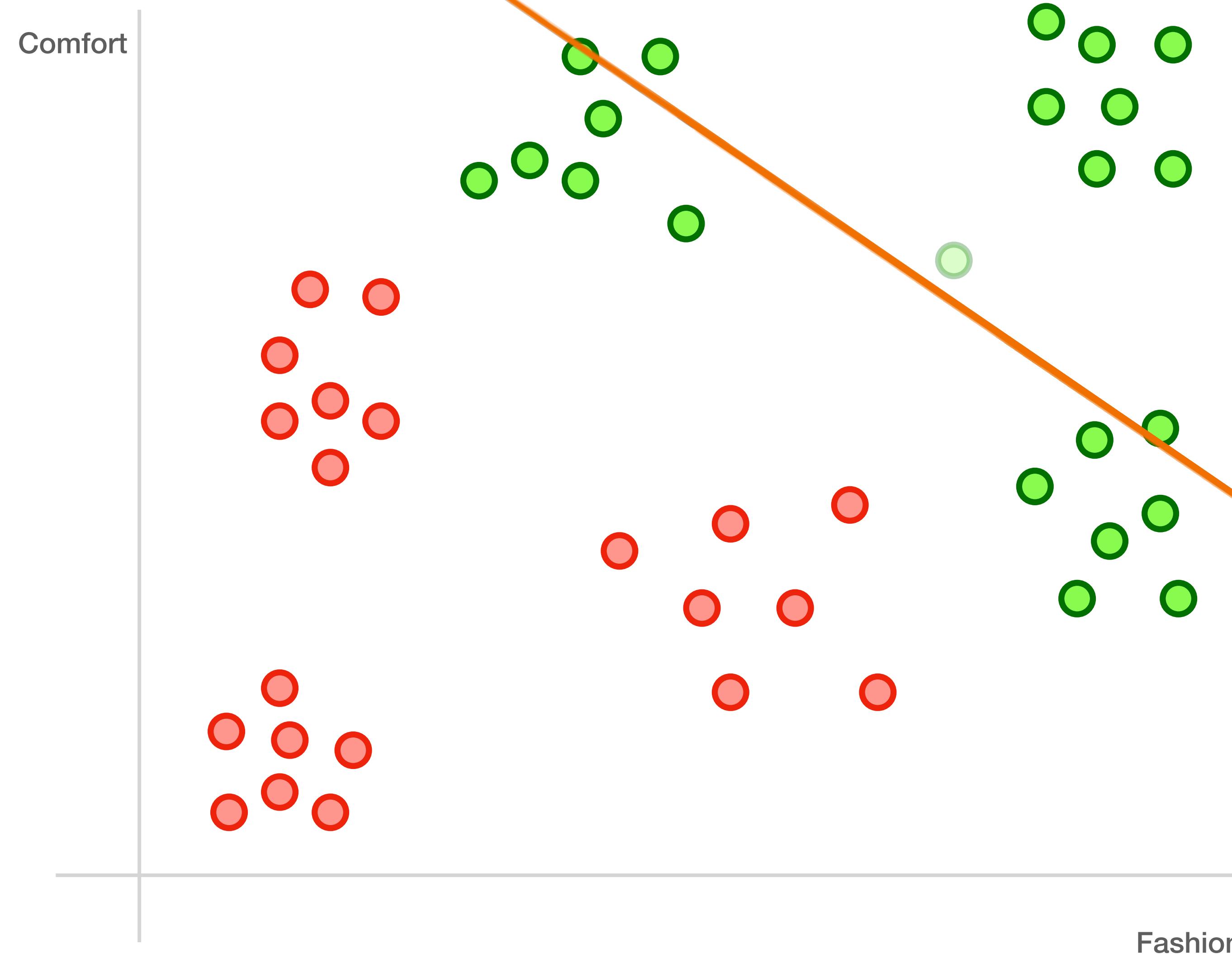
Support Vector Machines



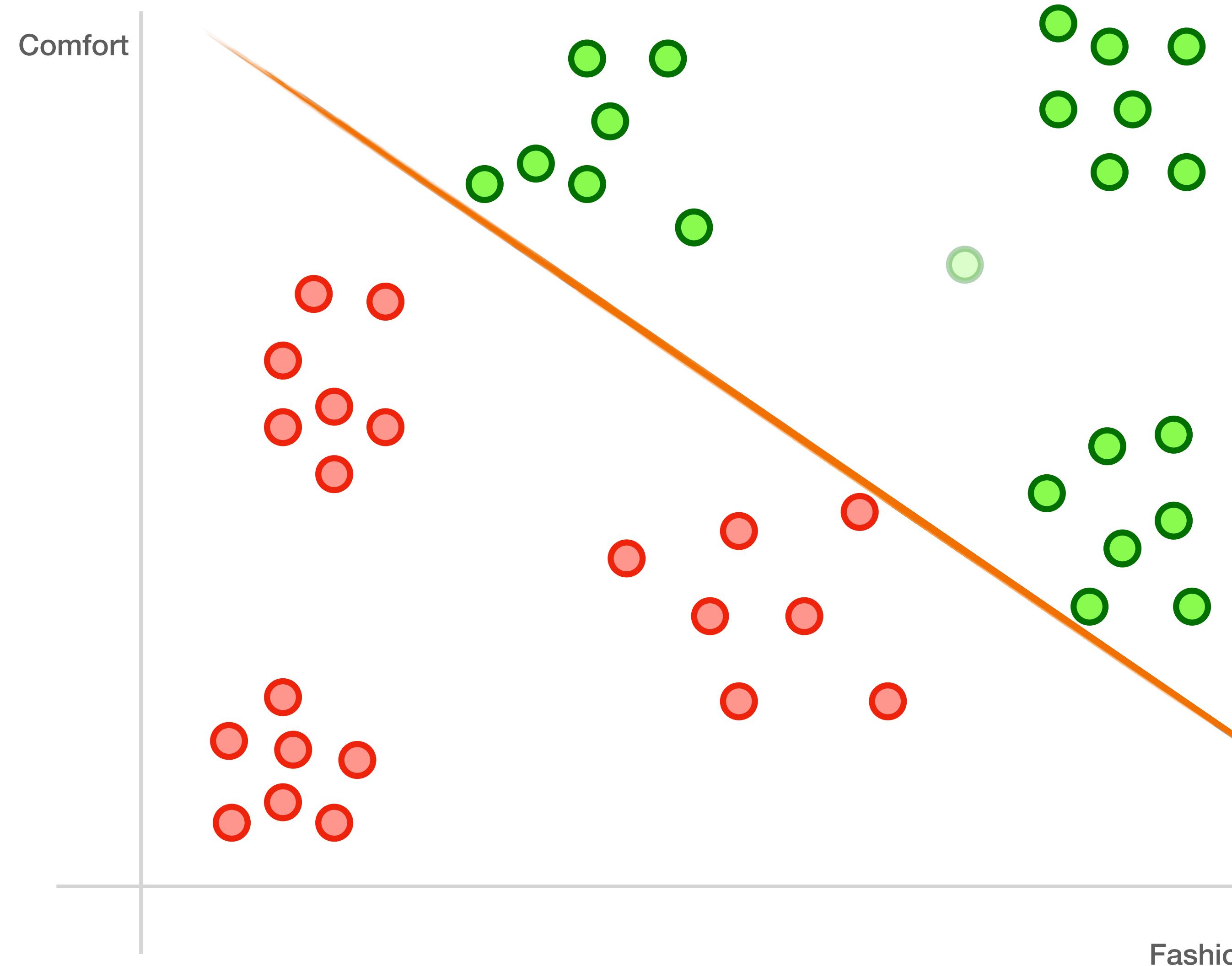
Support Vector Machines



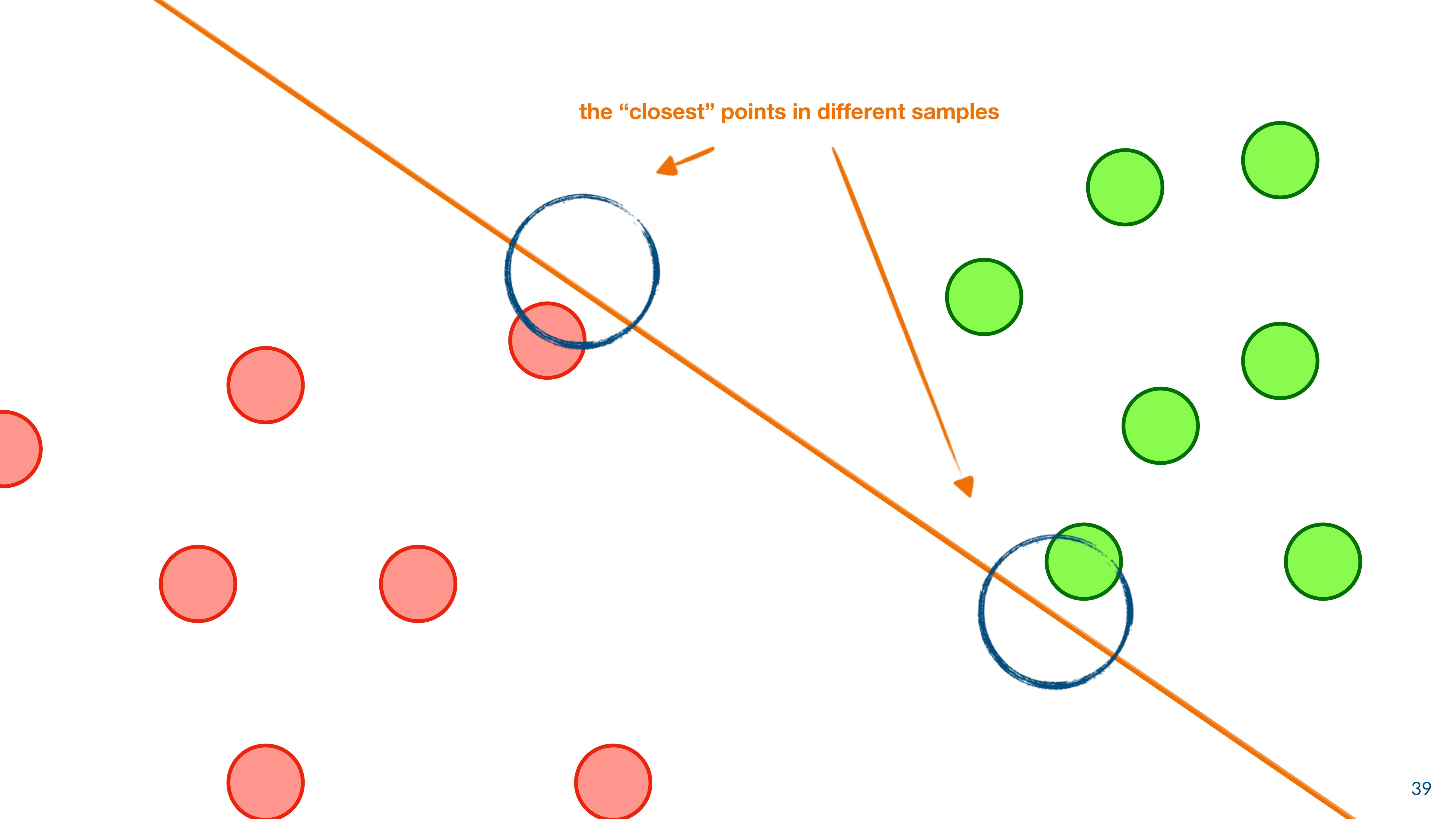
Support Vector Machines

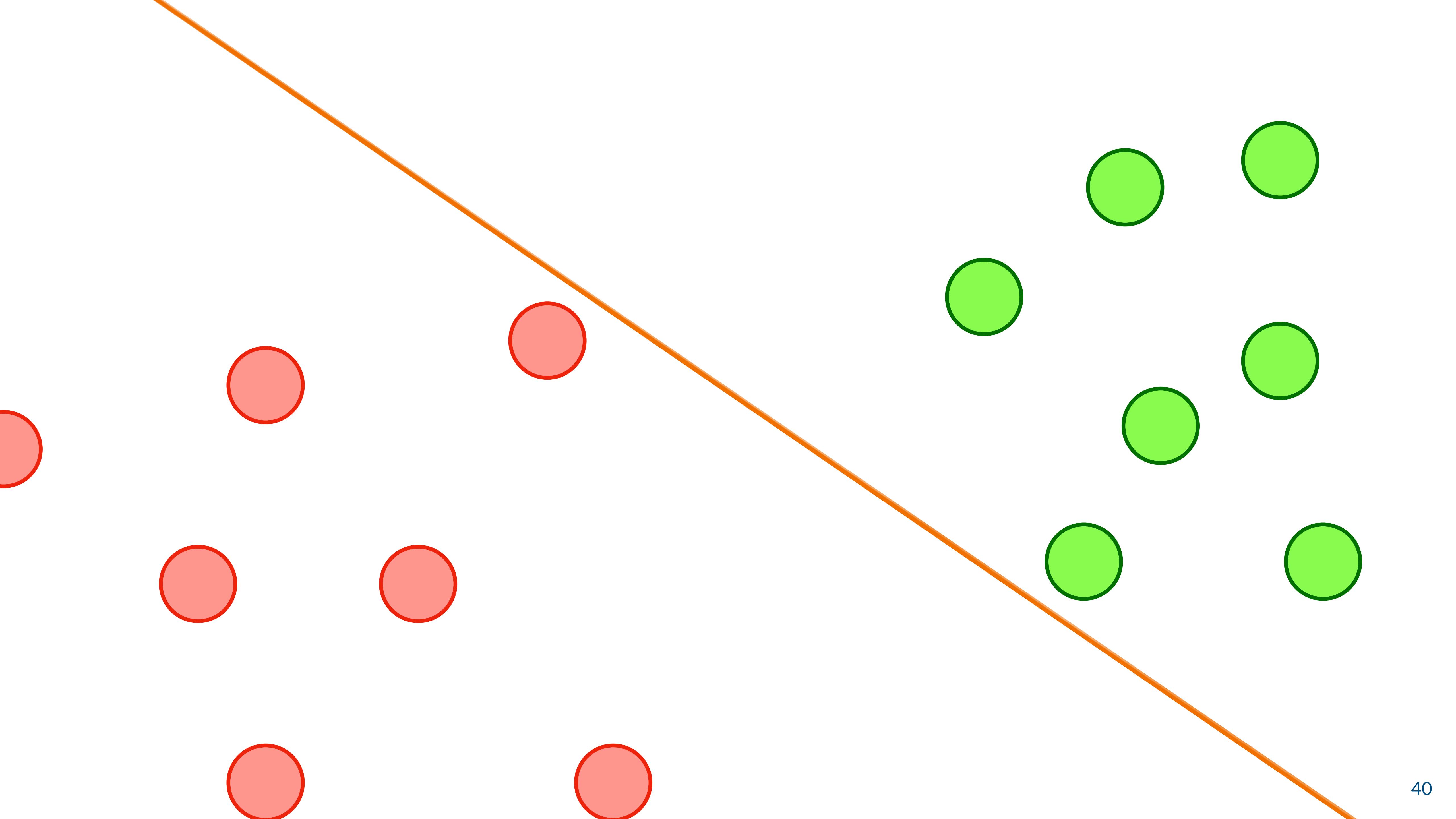


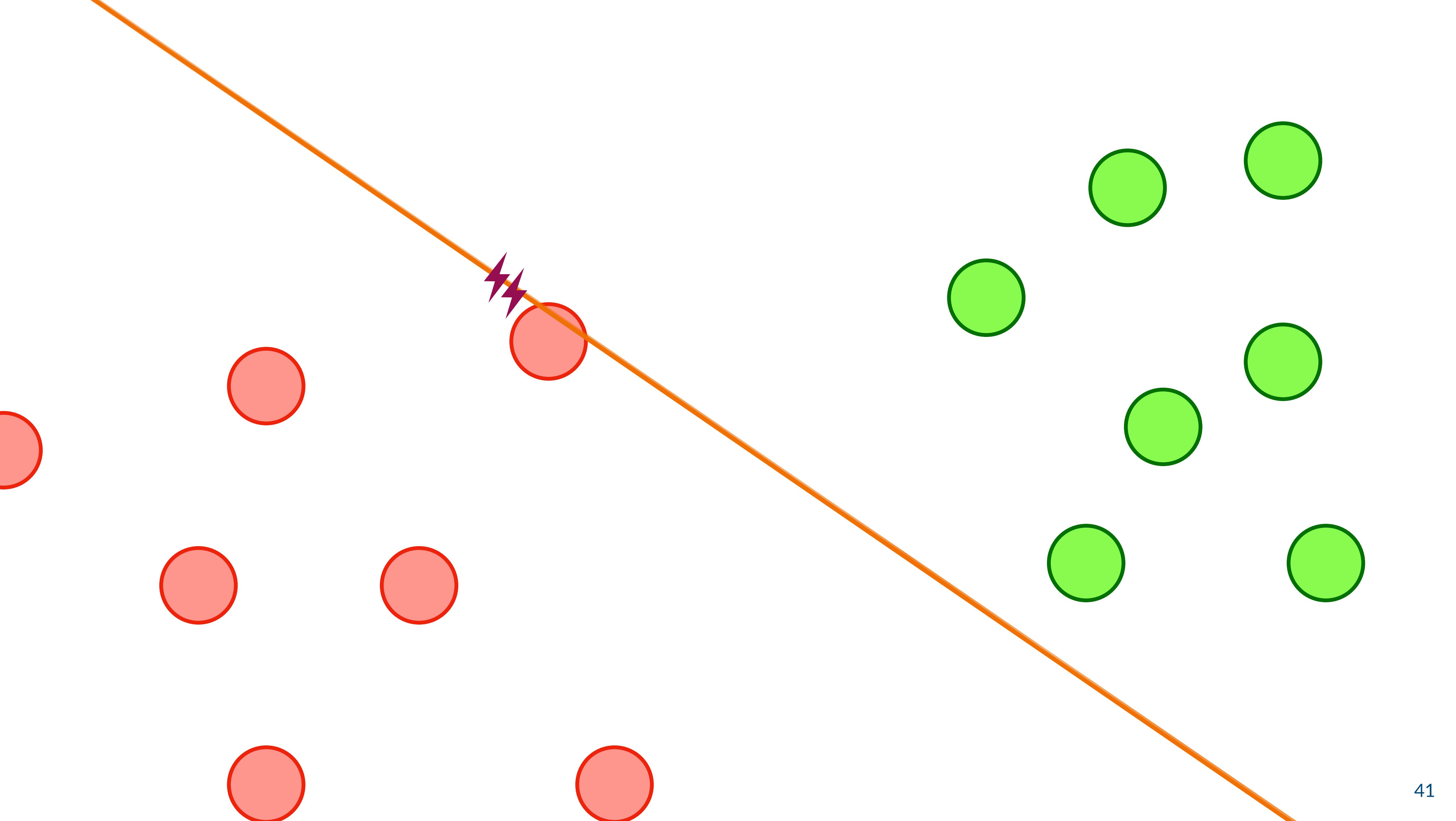
Support Vector Machines

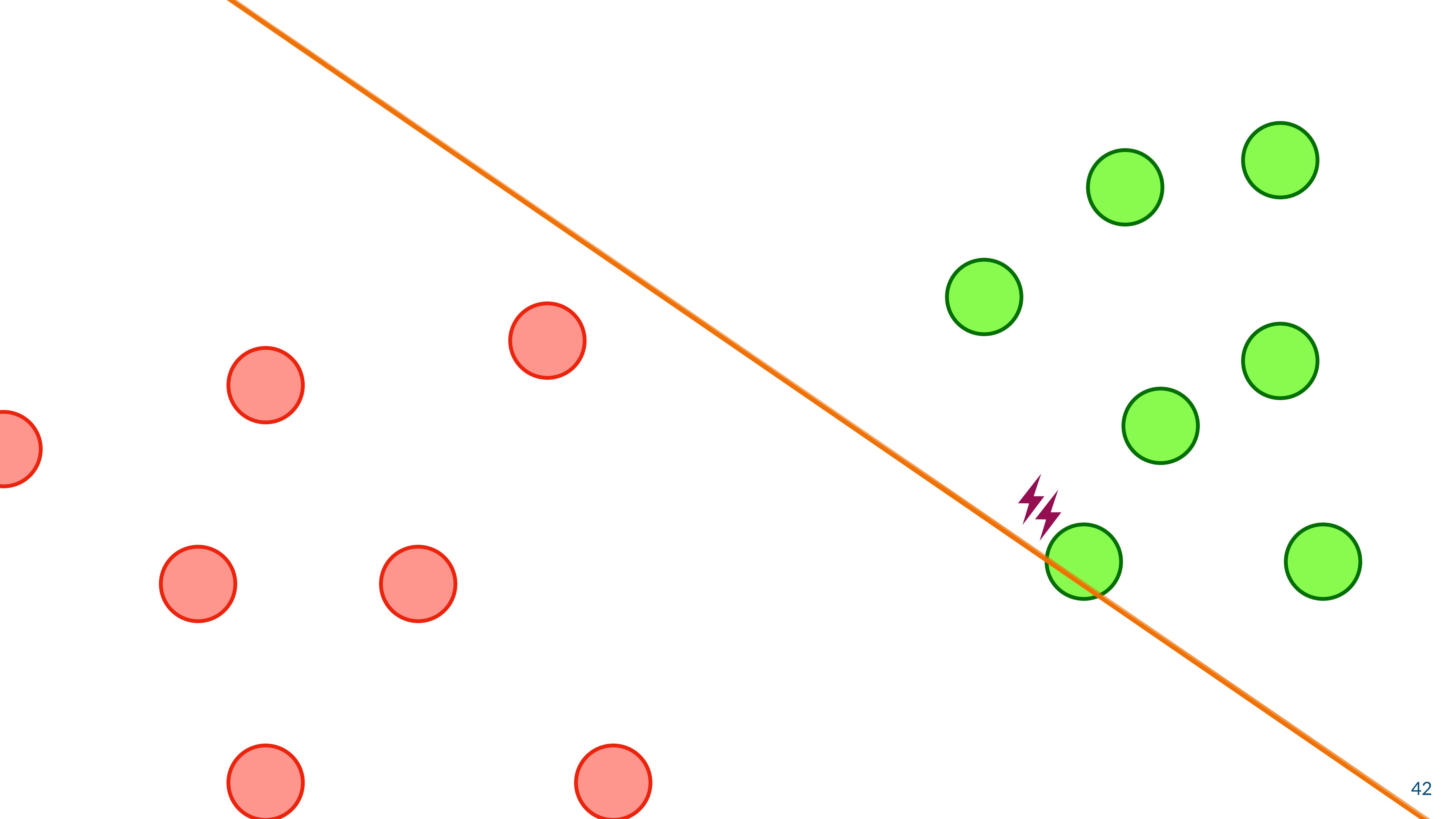


the “closest” points in different samples

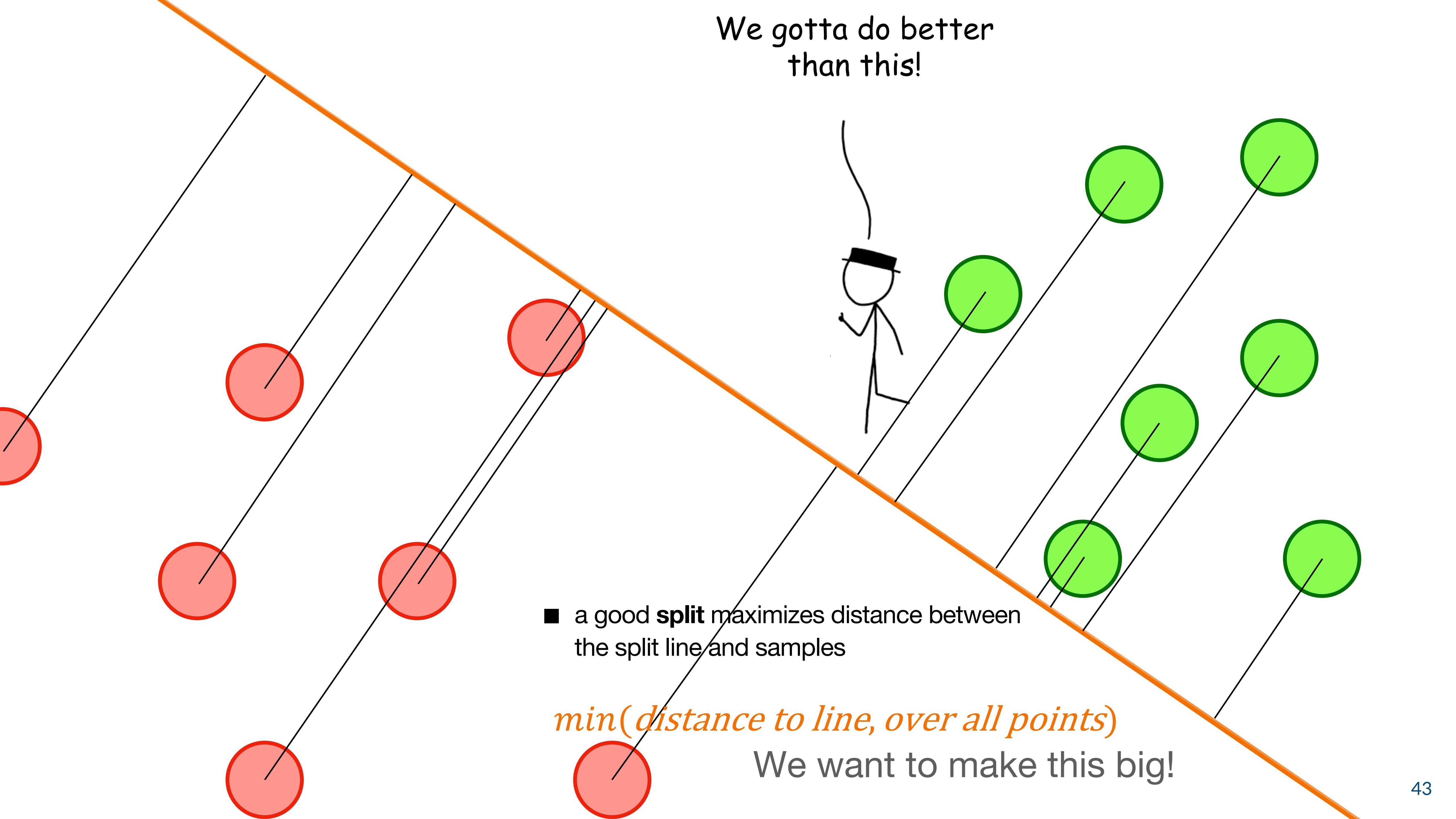








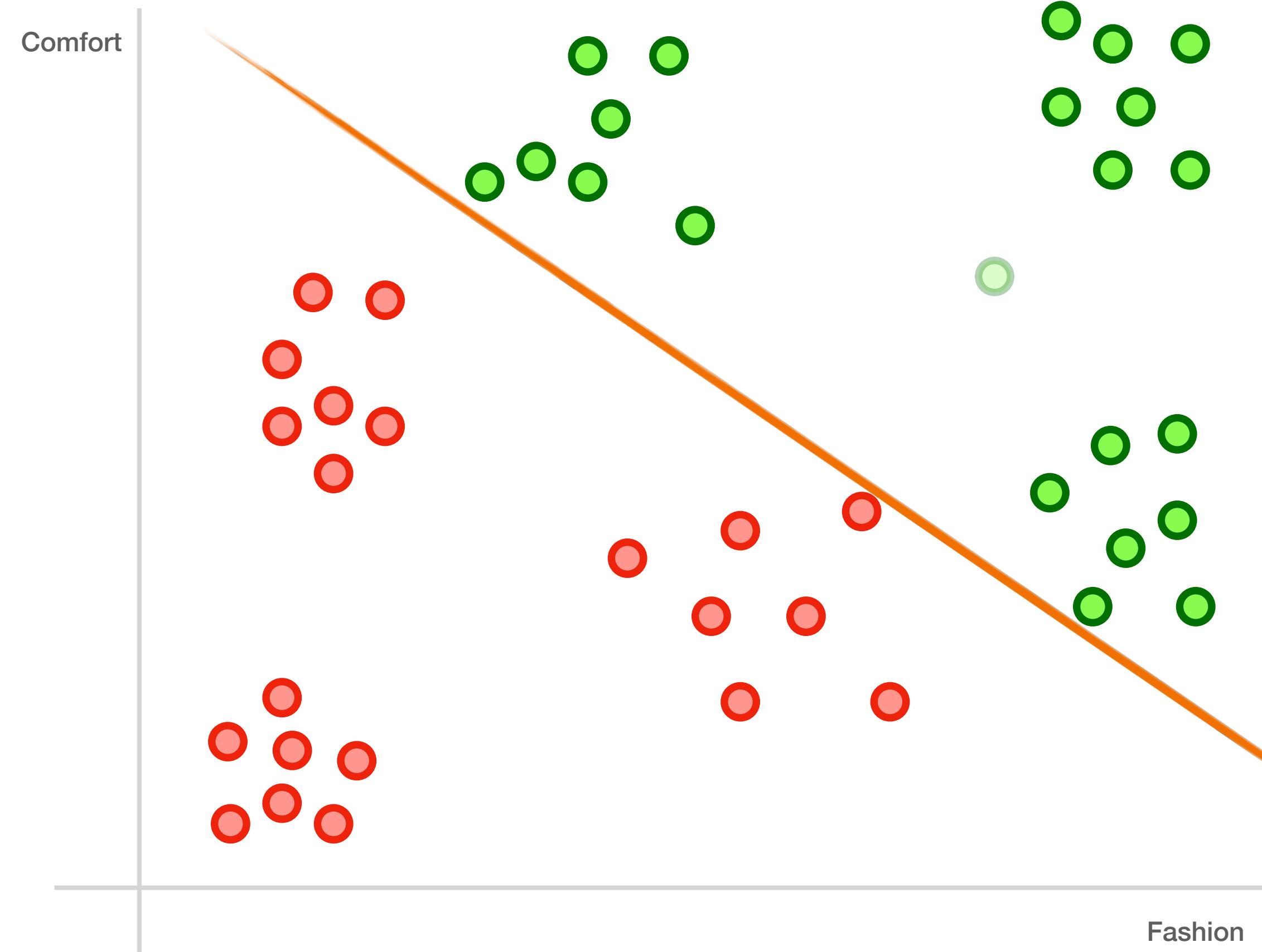
We gotta do better
than this!



Support Vector Machines

$\min(\text{distance to line, over all points})$

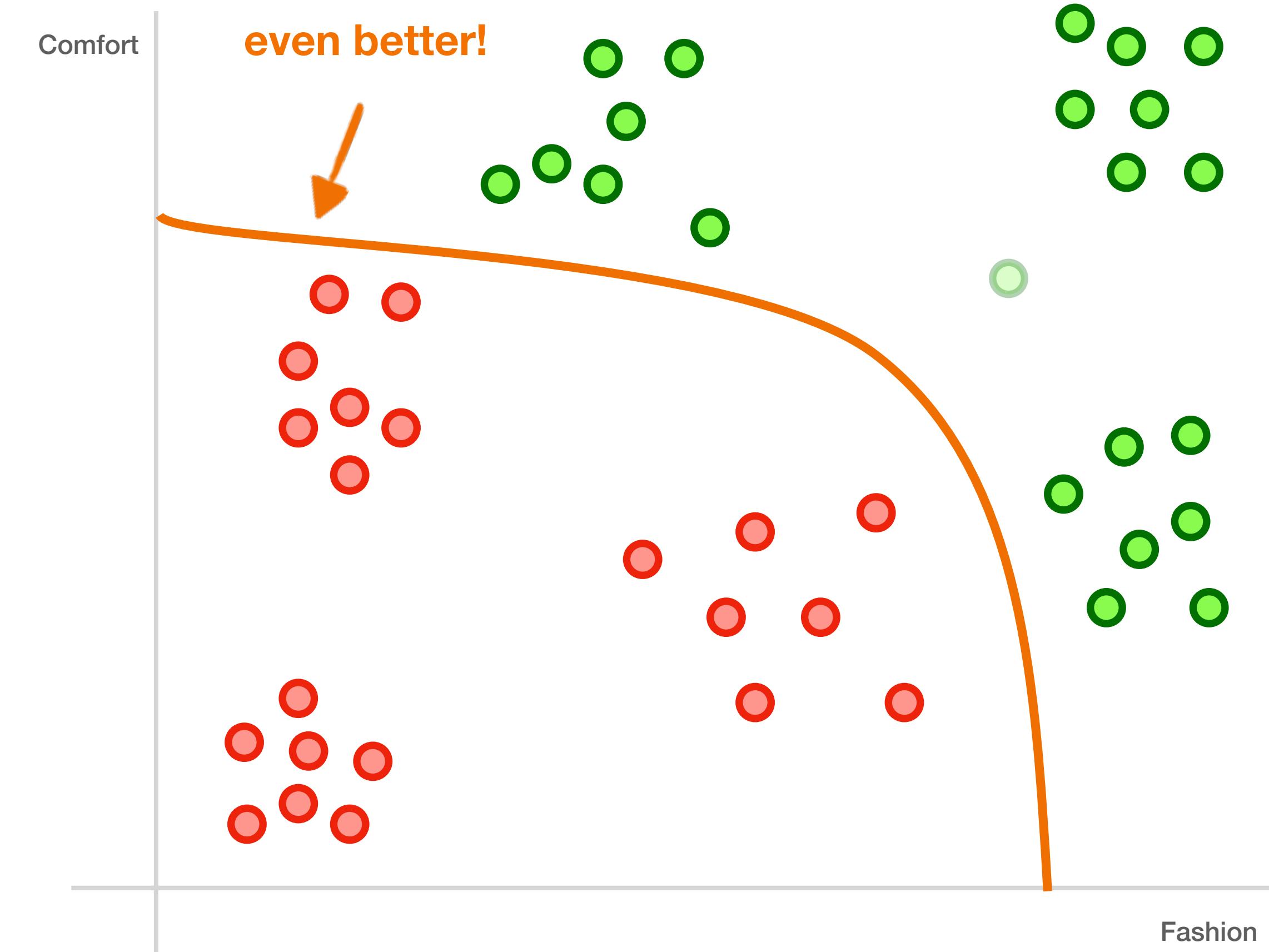
We want to make this big!



Support Vector Machines

$\min(\text{distance to line, over all points})$

We want to make this big!

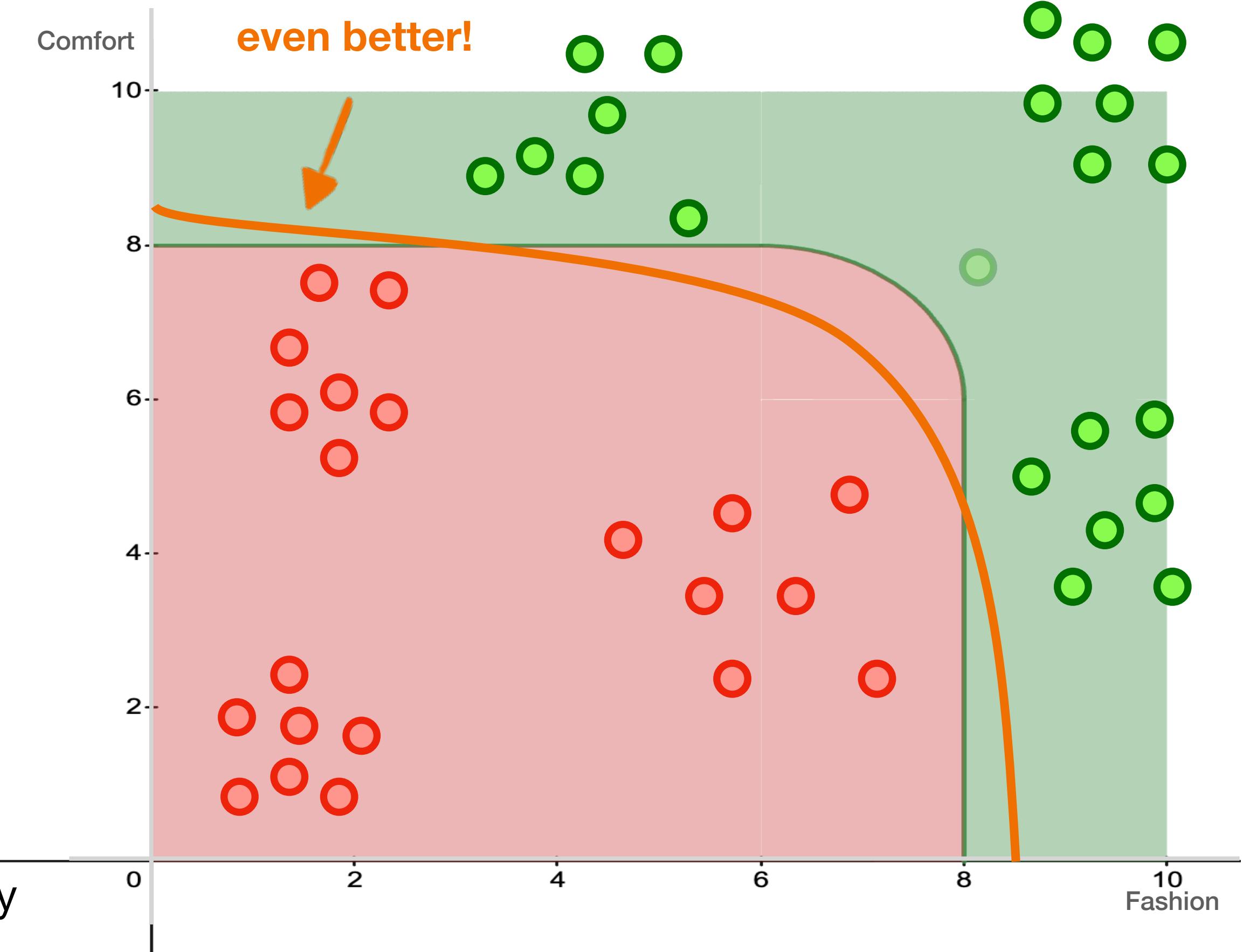


Support Vector Machines

$\min(\text{distance to line, over all points})$

We want to make this big!

- support-vector machines are classifiers that divide data by class, aiming to create a margin that's as wide as possible.
- They can use non-linear functions



Internal Memo:

**146 Hagley Road, Birmingham
Birmingham B3 3PJ**

**From the Desk of
Mr. Jerry Smith
Date: 13/01/14**

Attn: Sir/Madam,

I seize this opportunity to extend my unalloyed compliments of the new season to you and your family hoping that this year will bring more joy, happiness and prosperity into your house hold.

I am certain that by the time you read this letter I might have already gone back to my country **United Kingdom**. I visited South Africa during the New Year period and during my stay, I used the opportunity to send you this letter believing that it will reach you in good state.

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- | | | |
|-----------------------------------|---|-------------|
| “unalloyed complements” |  | Spam |
| “\$100,000 dollars” |  | Spam |
| “relative dying of cancer” |  | Spam |

IF we have this

“unalloyed complements”



we get this

Spam

“\$100,000 dollars”



Spam

“relative dying of cancer”



Spam

we get this IF we have this

we get this IF we have this

$$A | B$$

we get this IF we have this

$A | B$

- Is Spam
- “Nigerian Prince”

we get this IF we have this

spam|nigerianprince

we get this IF we have this

$$P(\text{spam} | \text{nigerianprince})$$

high? Nigerian prince  spam likely

low? Nigerian prince  not spam

- **conditional probabilities** can be used as a classifier!

Naïve Bayes

Bayes Equation

$$P(\text{spam}|\text{nigerianprince}) = \frac{P(\text{spam})P(\text{nigerianprince}|\text{spam})}{P(\text{nigerianprince})}$$

% of spam in
dataset

% of spam in
dataset that relates
to Nigerian prince

% of Nigerian
prince in dataset

Naïve Bayes

Classifier

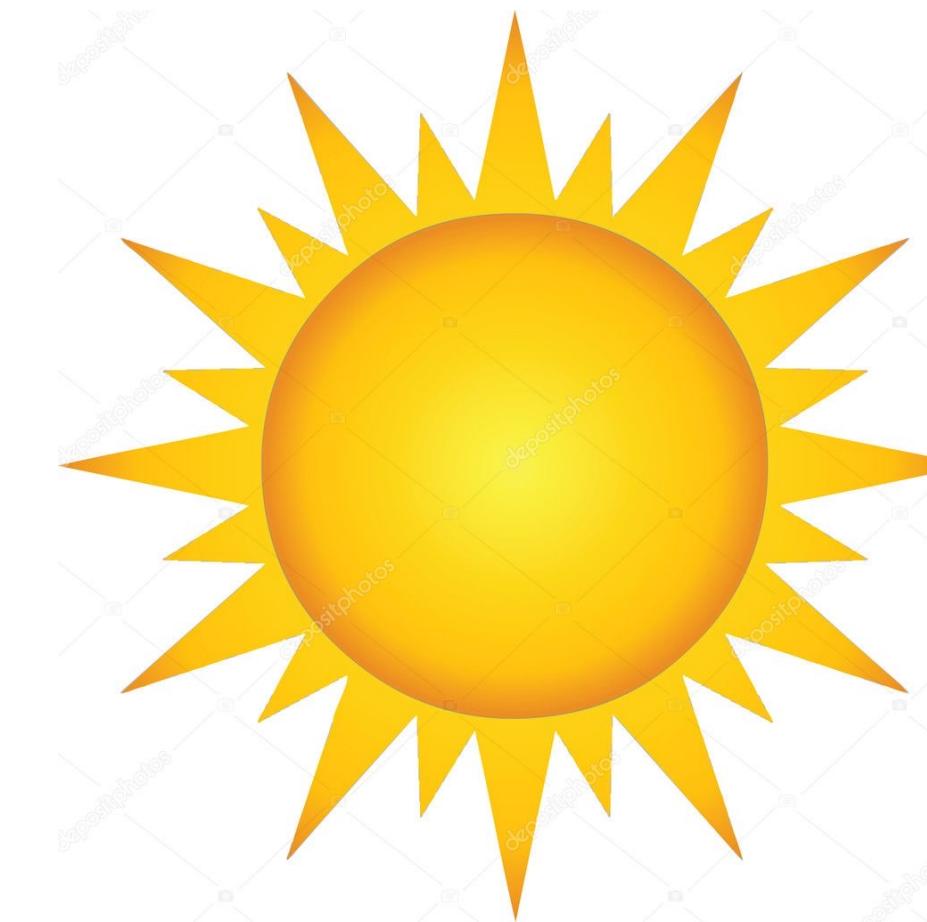
$$P(\text{spam}|\text{nigerianprince}, \text{offer}) = \frac{P(\text{spam})P(\text{nigerianprince}|\text{spam})P(\text{offer}|\text{spam})}{P(\text{nigerianprince})P(\text{offer})}$$



- **conditional probabilities** can be used as a classifier!
- a classifier made this way, however, is “**naïve**” when extended to multiple features

multiplication for AND assumes independence!
“naïve”

Naïve Bayes Independence



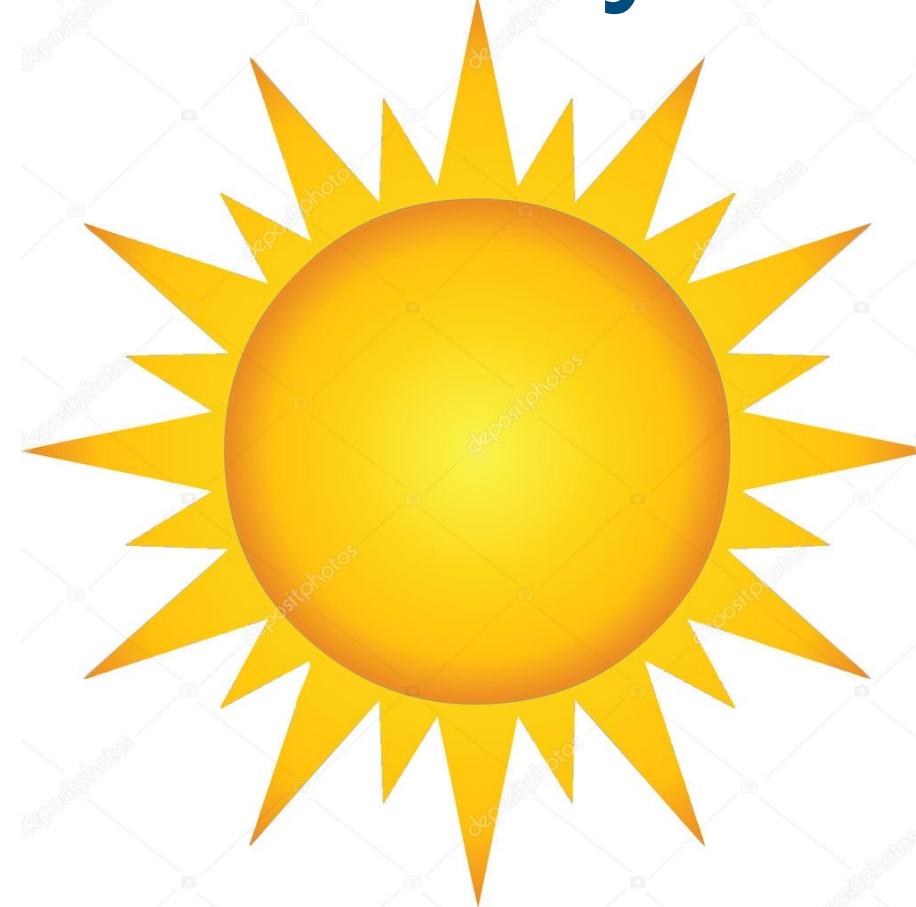
50%



50%

Naïve Bayes Independence

January 1st

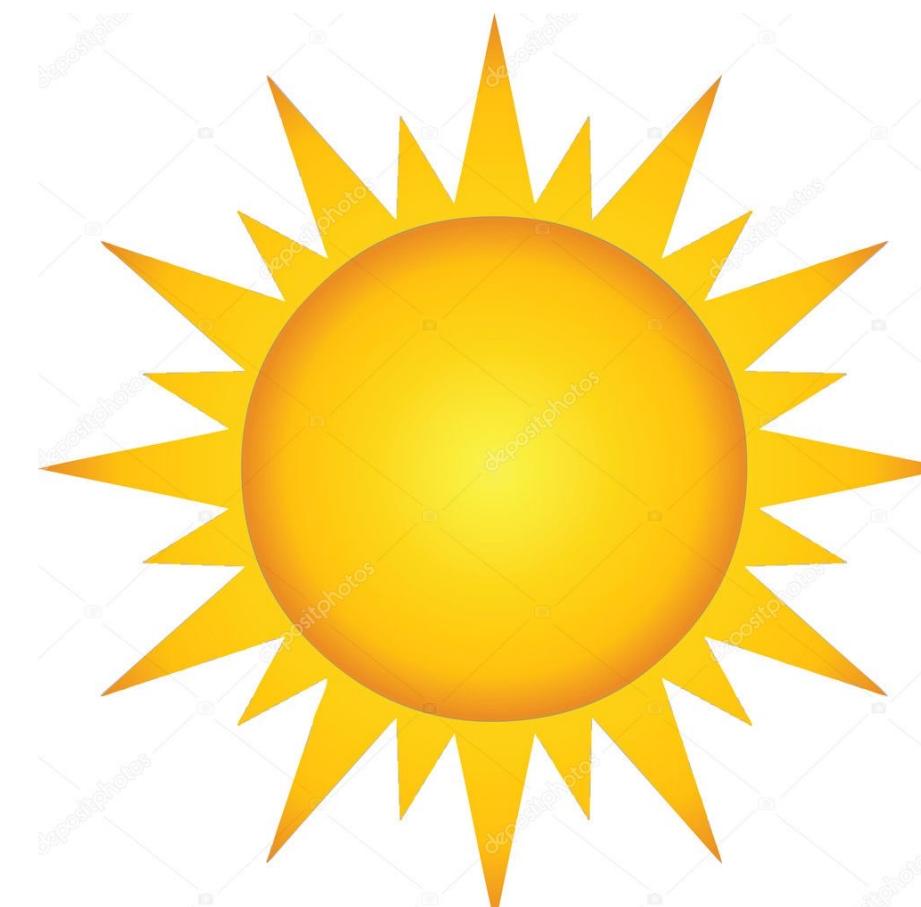


50%



50%

January 2nd



50%



50%

Naïve Bayes Independence

$P(\text{Rain} \mid \text{January } 1^{\text{st}})$

=50%

$P(\text{Rain} \mid \text{January } 2^{\text{nd}})$

=50%

Naïve Bayes Independence

$P(\text{Rain} \mid \text{January 1}^{\text{st}} \text{ AND Rain} \mid \text{January 2}^{\text{nd}}) = 45\%$

Is NOT

$P(\text{Rain} \mid \text{January 1}^{\text{st}}) * P(\text{Rain} \mid \text{January 2}^{\text{nd}})$
 $= 25\%$

Naïve Bayes Classifier

$$P(\text{spam}|\text{nigerianprince}, \text{offer}) = \frac{P(\text{spam})P(\text{nigerianprince}|\text{spam})P(\text{offer}|\text{spam})}{P(\text{nigerianprince})P(\text{offer})}$$



- **conditional probabilities** can be used as a classifier!
- a classifier made this way, however, is “**naïve**” when extended to multiple features

multiplication for AND assumes independence!
“naïve”



Buy?

Don't buy?

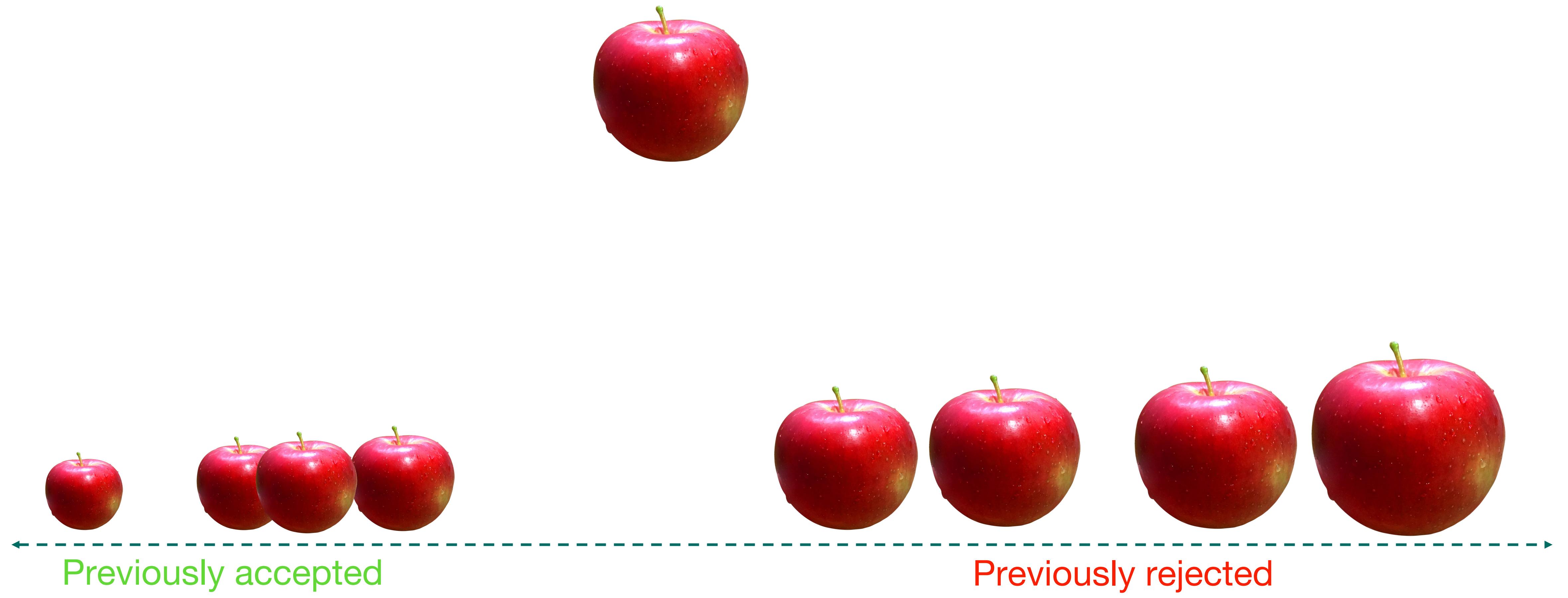


Did Buy



Rejected

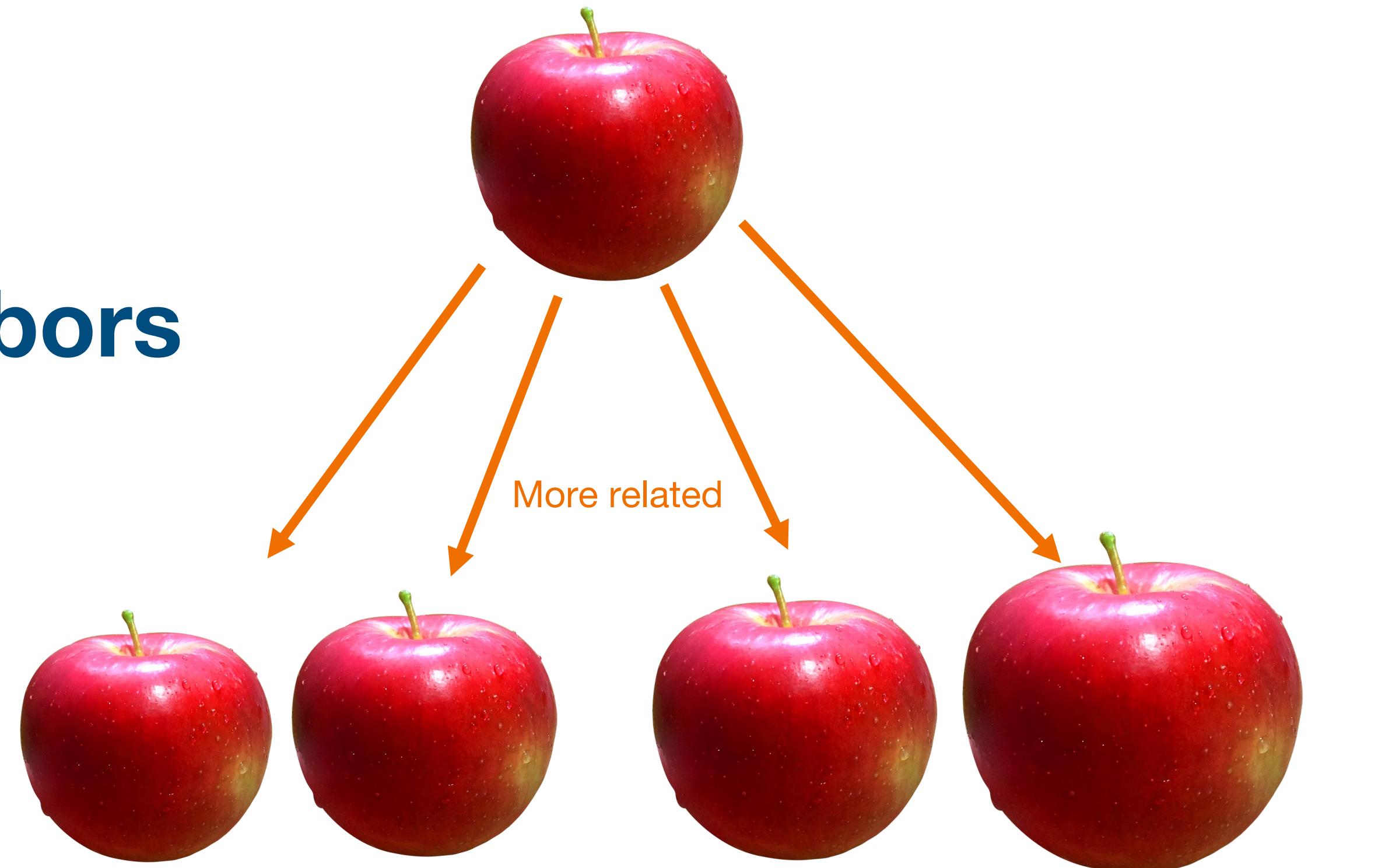




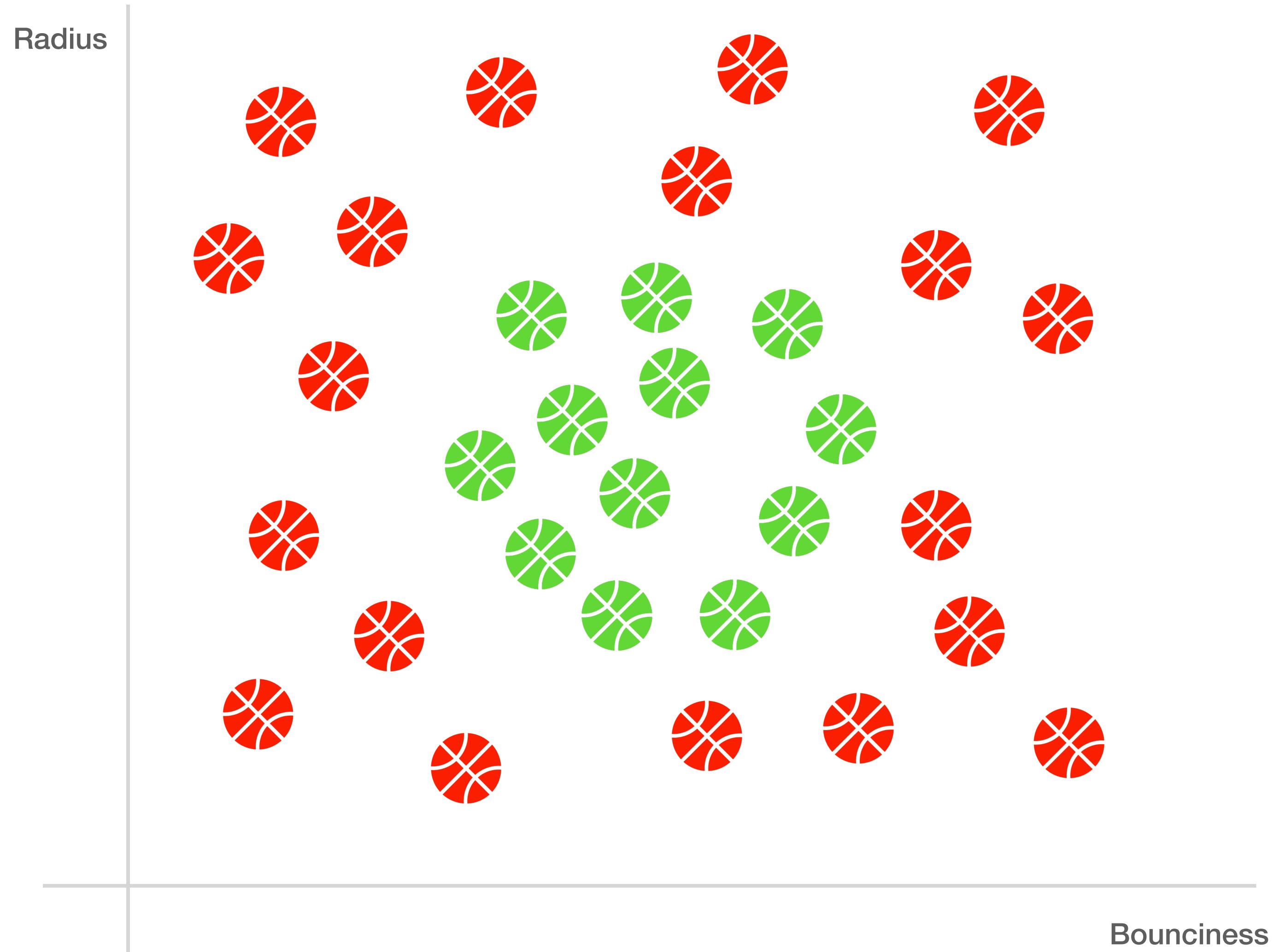
We find the **K Nearest Neighbors**



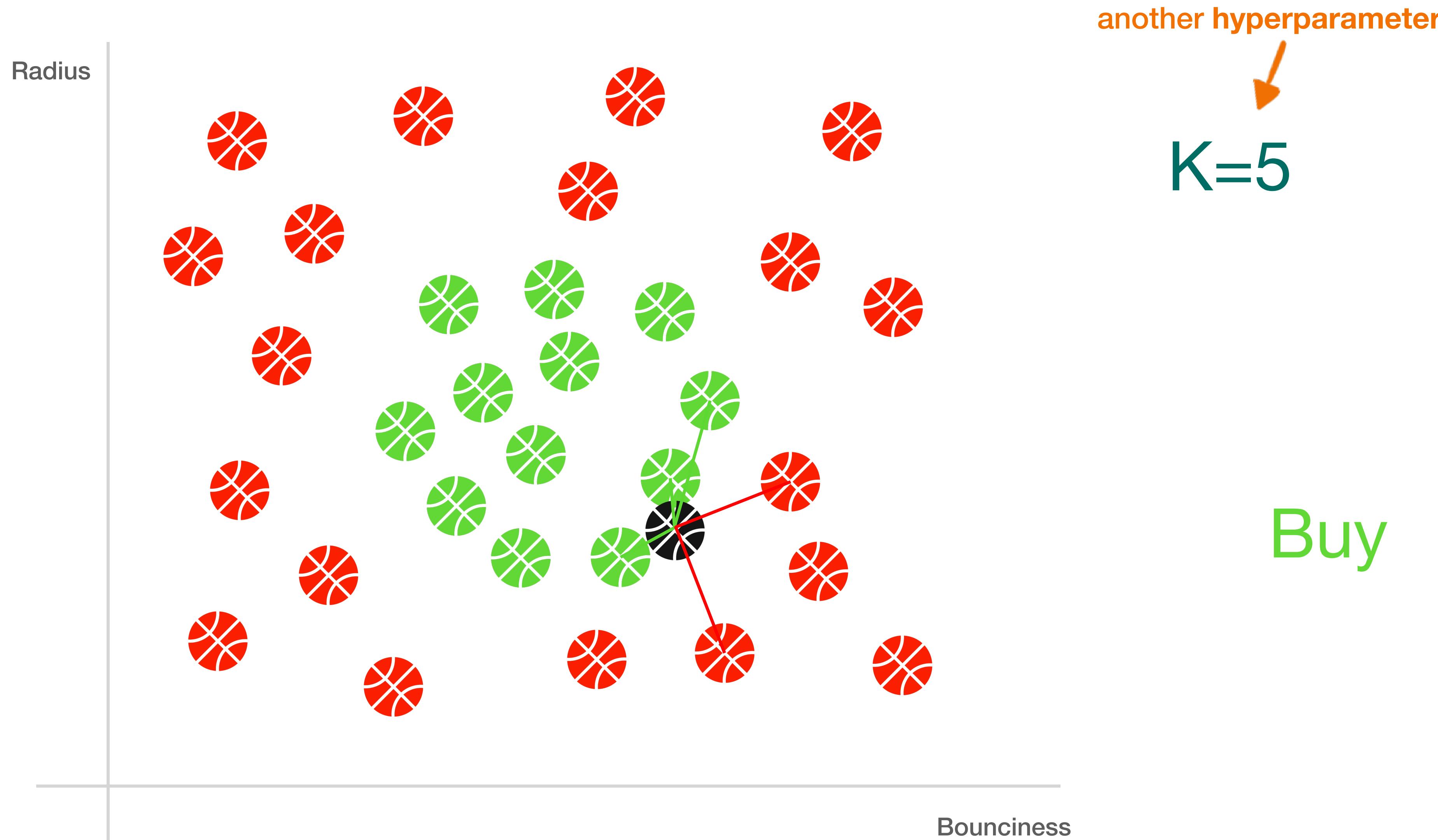
←————— Previously accepted —————→



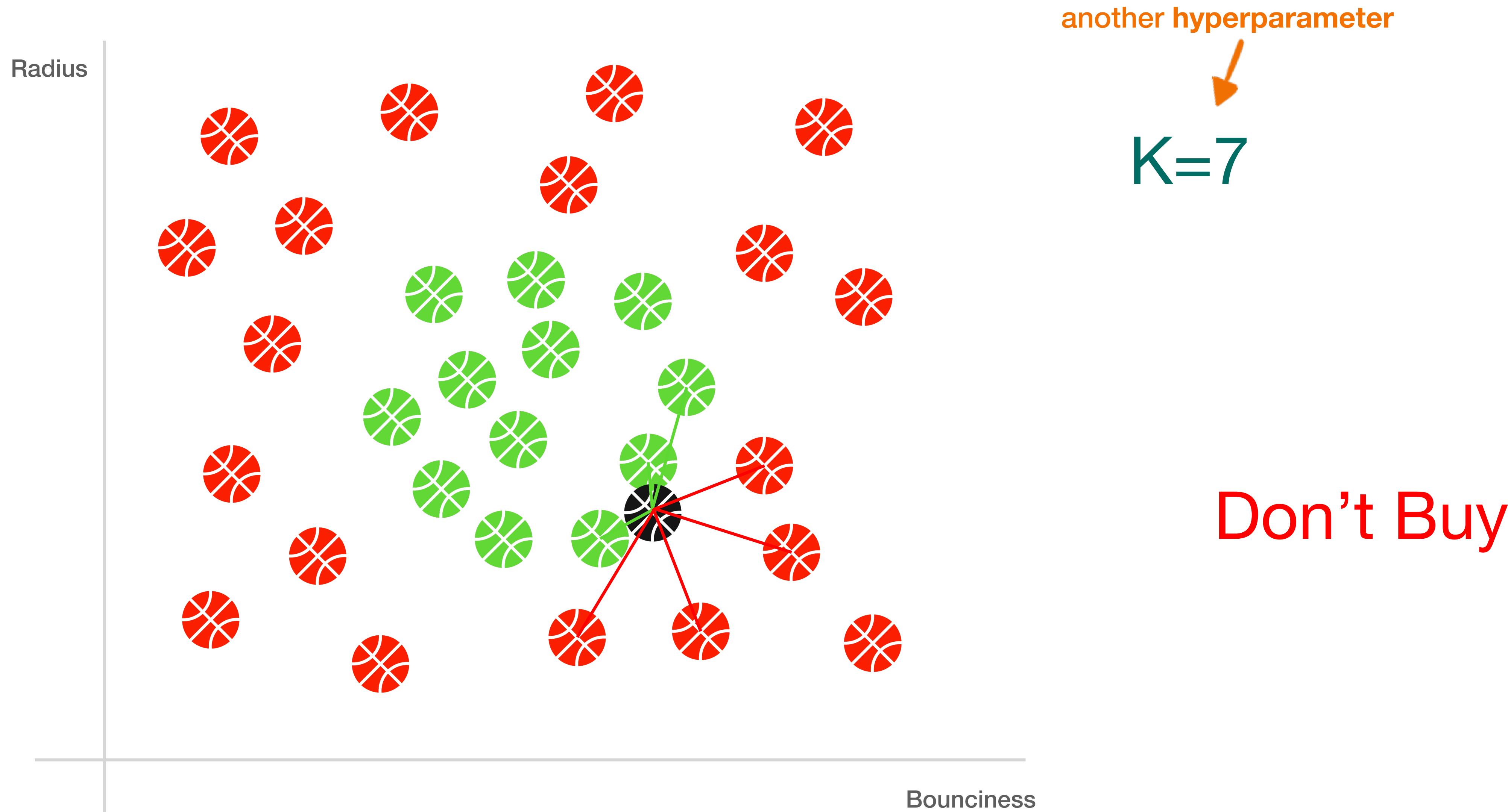
K Nearest Neighbors



K Nearest Neighbors



K Nearest Neighbors



Five classifiers! That's a lot.

Let's get to the lab!