



AIBridge

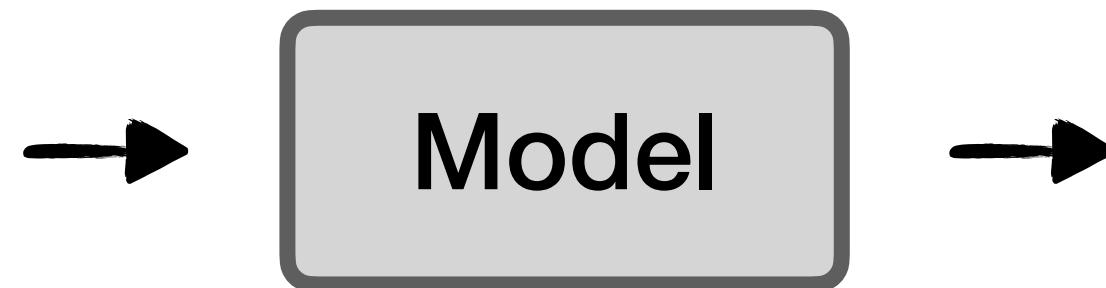
Lecture 6

Classification!

Classification!

quick review
wine dataset

- Fixed acidity
- Volatile acidity
- Citric acid
- Residual sugar
- Chlorides
- Free sulfur dioxide
- Total sulfur dioxide
- Density
- pH
- Sulphates
- Alcohol



White = 0
Red = 1

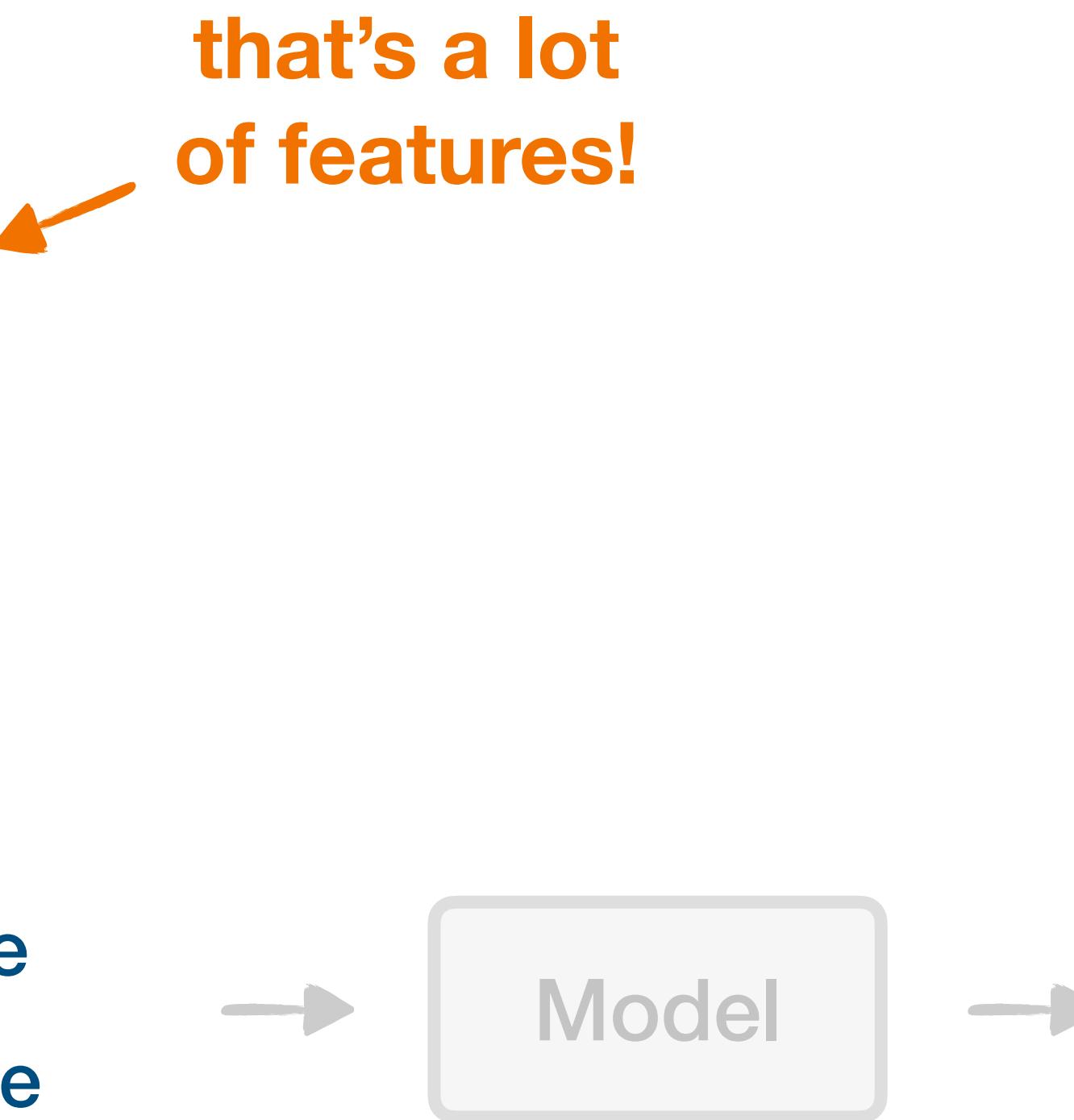
a class

- categorical label outputs are named “classes”

Classification!

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that's a lot
of features!

a class

- categorical label outputs are named “classes”

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that's a lot
of features!

can they really be linear?
even in high dimensions?

- as feature counts increase, and on complex data,
linear type model may not be the best model

as feature counts increase, and on complex data,
linear type models may not be the best model

we need a more complex model

Decision Trees

Decision Trees



Decision Trees



Can I afford it?

Decision Trees



Can I afford it?

Is it comfortable?

Decision Trees



Can I afford it?

Is it comfortable?

Is it fashionable?

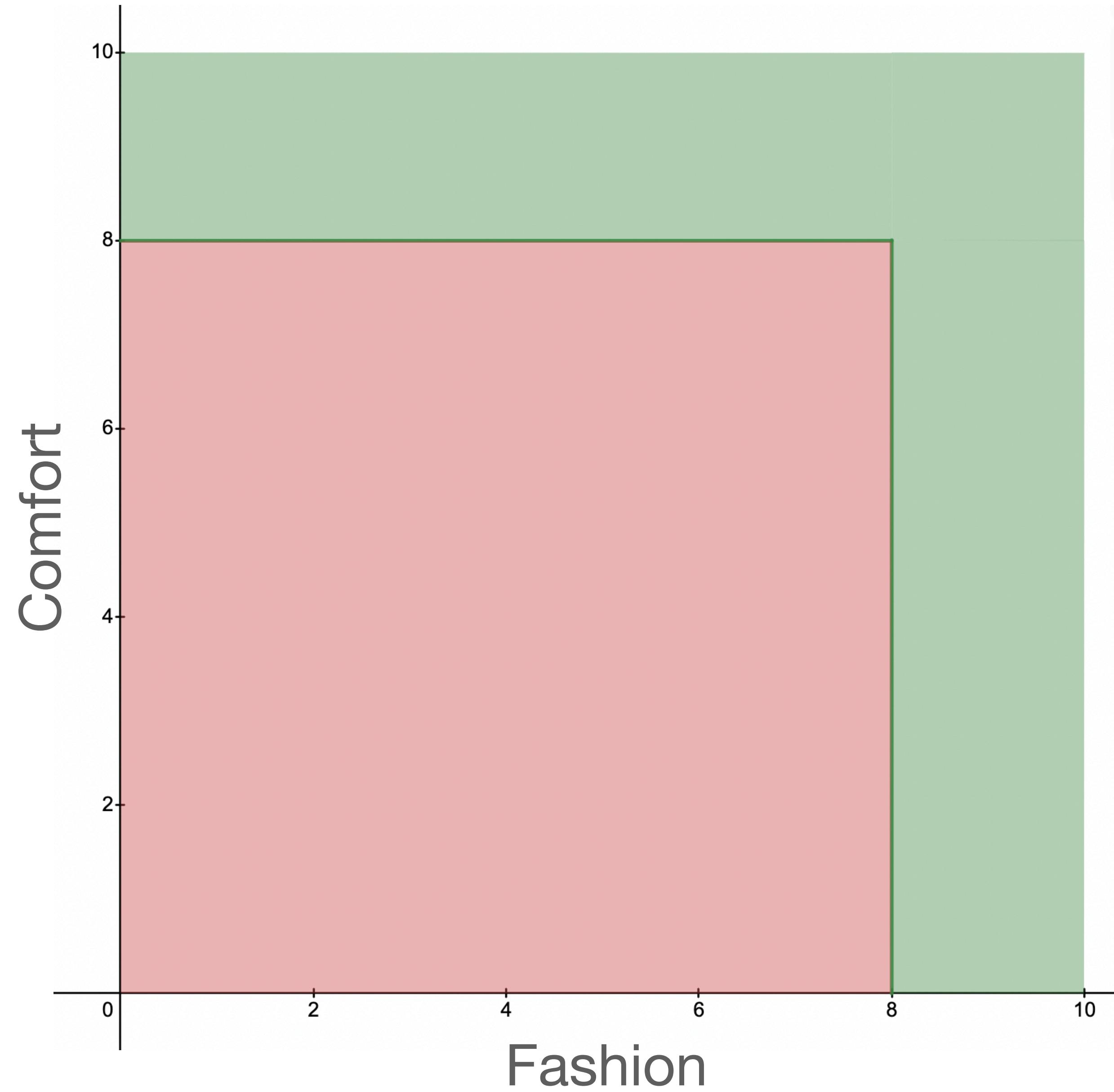
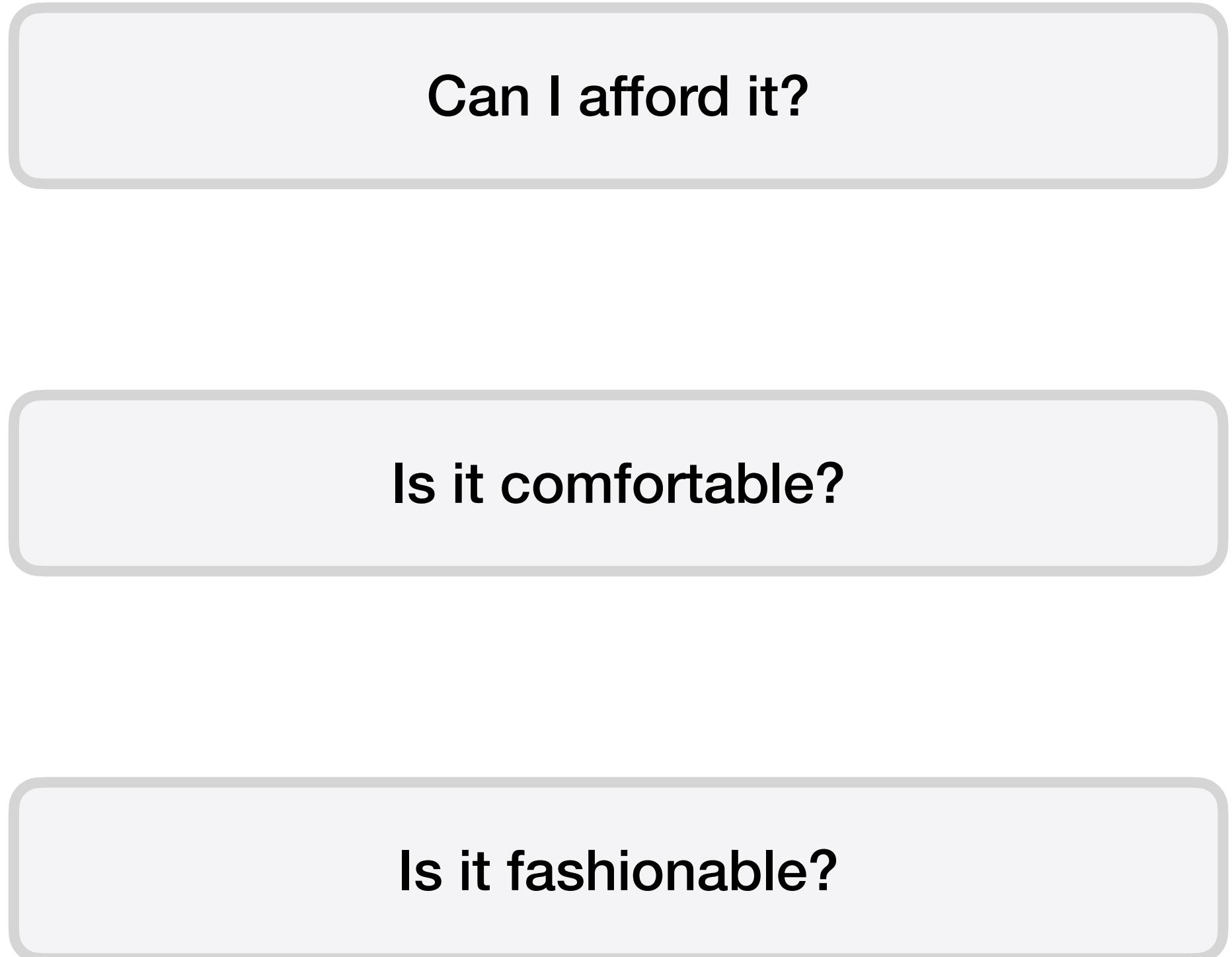
Decision Trees

Can I afford it?

Is it comfortable?

Is it fashionable?

Decision Trees



Decision Trees



Decision Trees

that seems awfully
hard-coded!

- flowcharts of decisions can create an explainable and repeatable graph of predictions



Decision Trees

Price	Comfort	Fashion	Purchased?
\$70	4	6	No
\$120	5	8	No
\$20	4	4	No
\$60	1	8	Yes
\$60	6	3	No
\$80	8	8	Yes

Decision Trees

Purchased?

No

No

No

Yes

No

Yes

Decision Trees

No

No

No

Yes

No

Yes

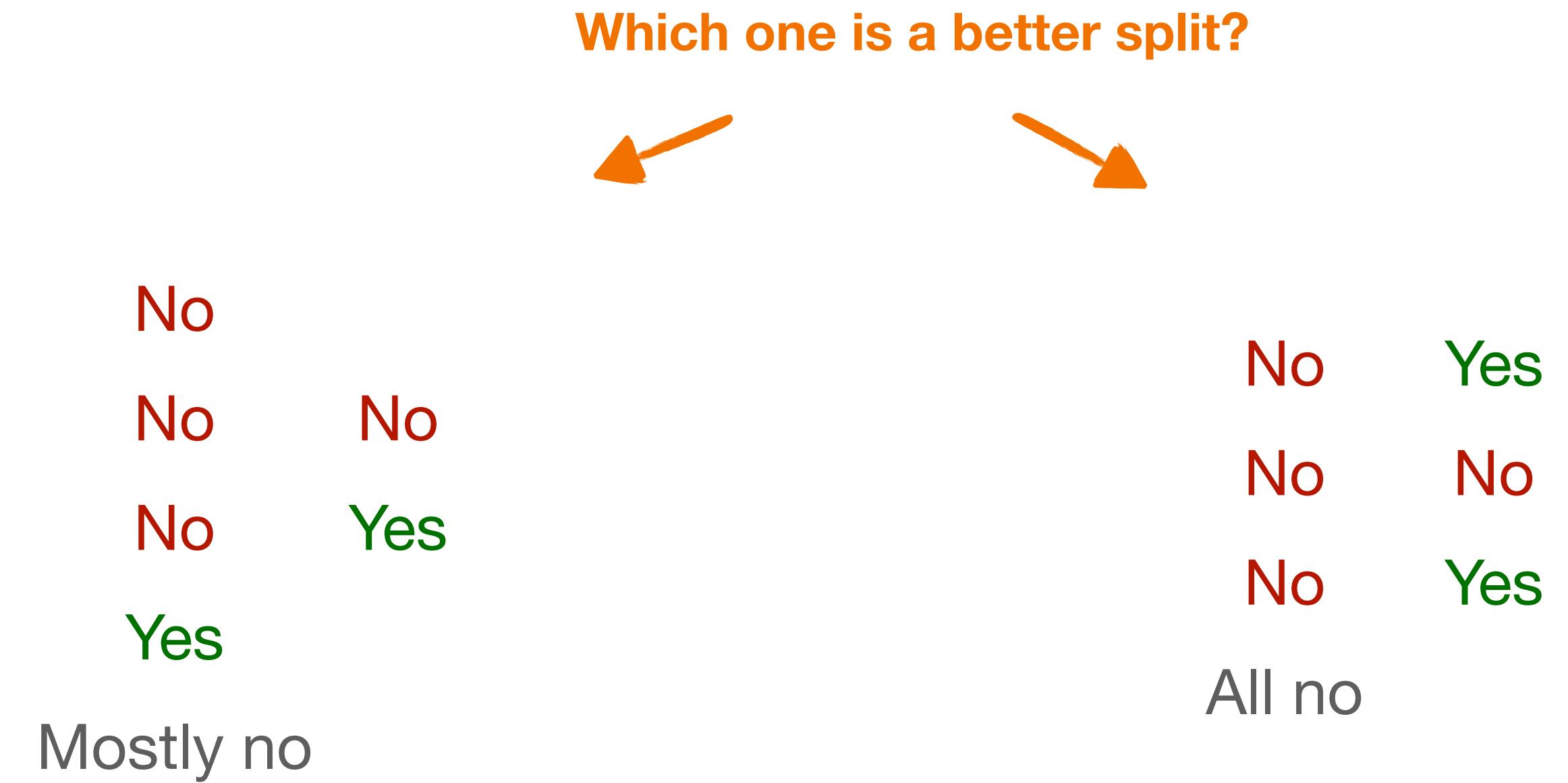
Decision Trees

No Yes

No No

No Yes

Decision Trees



Mostly
(Gini impurity)

Decision Trees

Gini impurity



- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.

Decision Trees

Gini impurity



- as a group becomes more **homogeneous**, its **Gini Impurity** decreases.
- perfect groups => 0 **Gini Impurity** => 100% predictions

$$G = \sum_{i=1}^C P(i) \cdot (1 - P(i)) \blacksquare$$

↑
Add them up for all groups

Portion of that one class in group Portion of not that one class in the group

The diagram illustrates the formula for Gini impurity. It shows the summation part of the formula with a large orange arrow pointing upwards from the 'i=1' term towards the summation symbol. Above the summation symbol, two orange arrows point downwards from the text 'Portion of that one class in group' and 'Portion of not that one class in the group' to the terms $P(i)$ and $(1 - P(i))$ respectively.

- **Gini impurity** measures the homogeneity in a group

Decision Trees

Purchased?

No

0

No

No

Yes

0.5

No

Yes

0.5

Decision Trees

Purchased?

No

No

0.38

No

Yes

No

0.5

Yes

0.88

Decision Trees

we gotta do better
than this, right?



Purchased?

No

No 0

No

Yes

No 0.44

Yes

0.44

Decision Trees

just split
again!

Purchased?

No

No 0

No

Yes

No 0.44

Yes

0.44

Decision Trees

1. Make splits and calculate Gini impurity
2. Select the split with the lowest Gini impurity
3. If unhappy, **just split again!**
4. Repeat 1-3 as much as needed

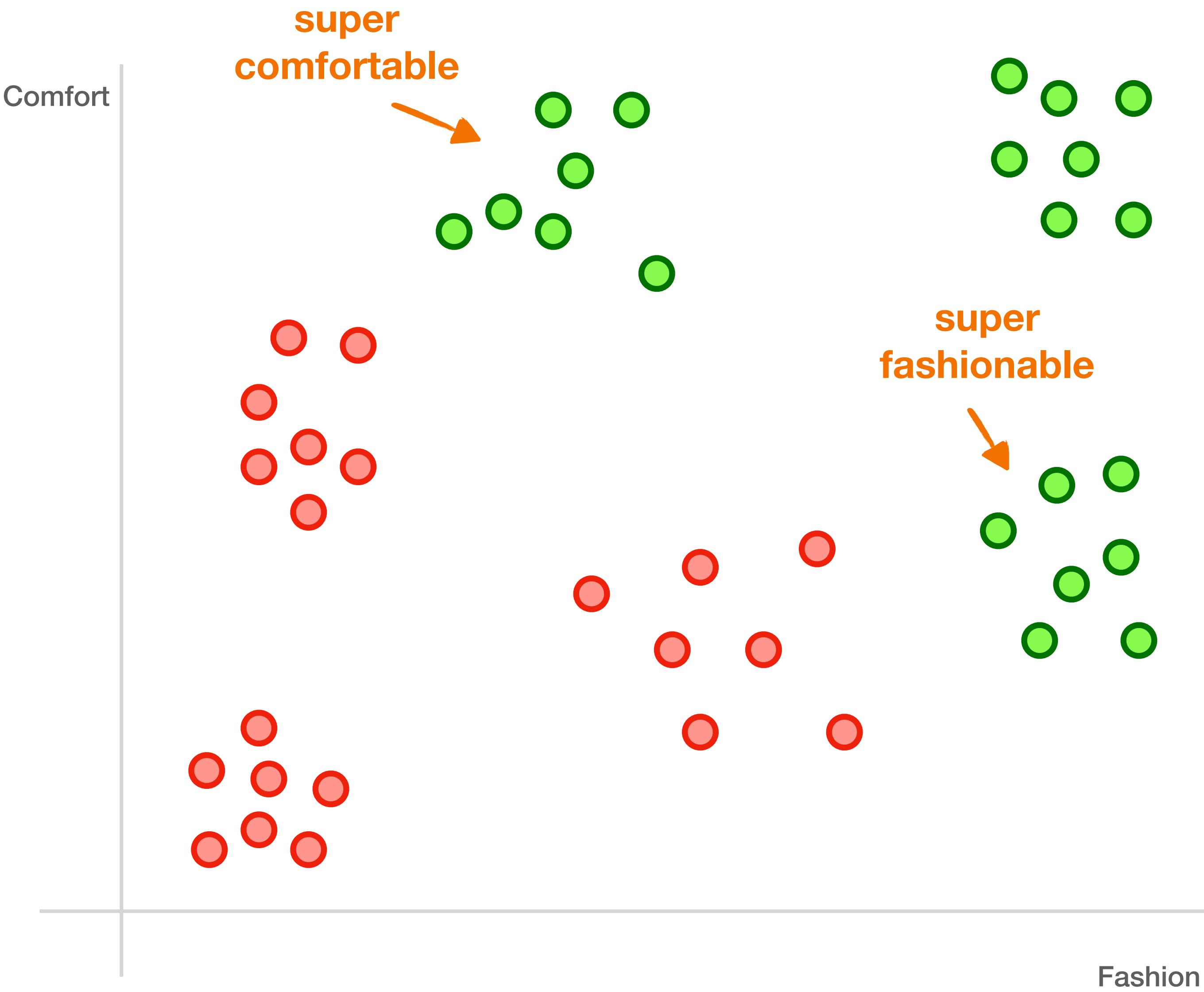


a hyperparameter

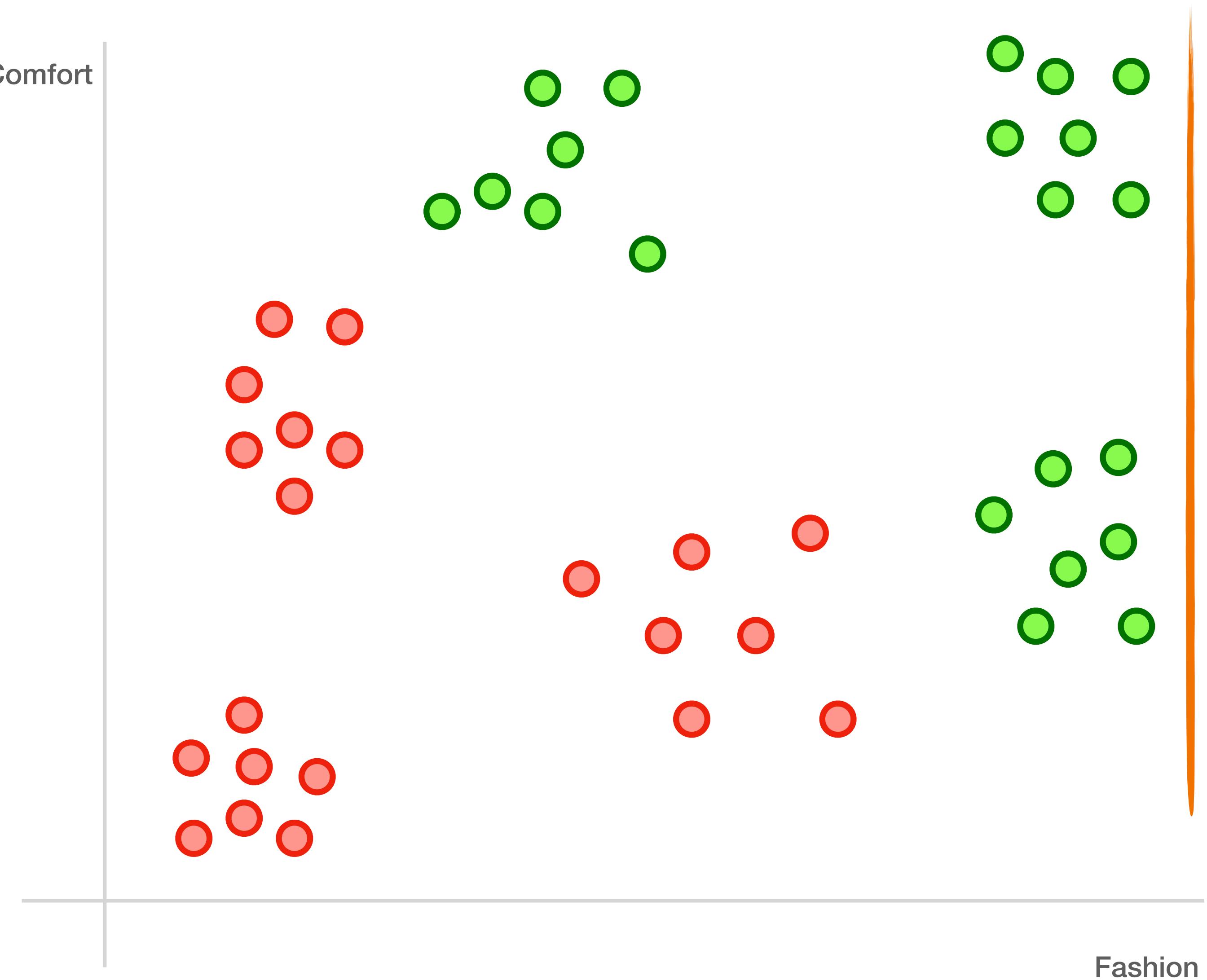


“split”

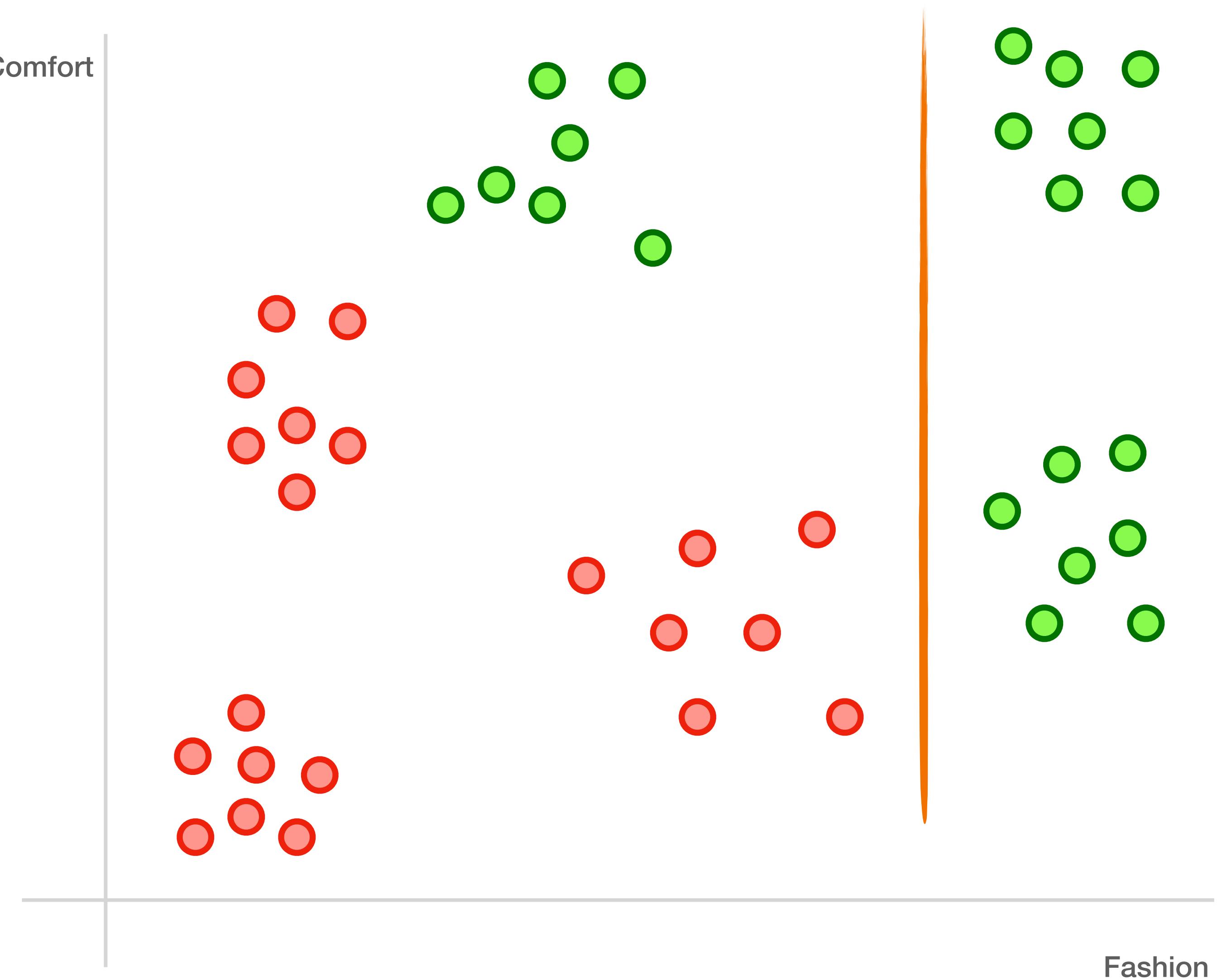
“split”



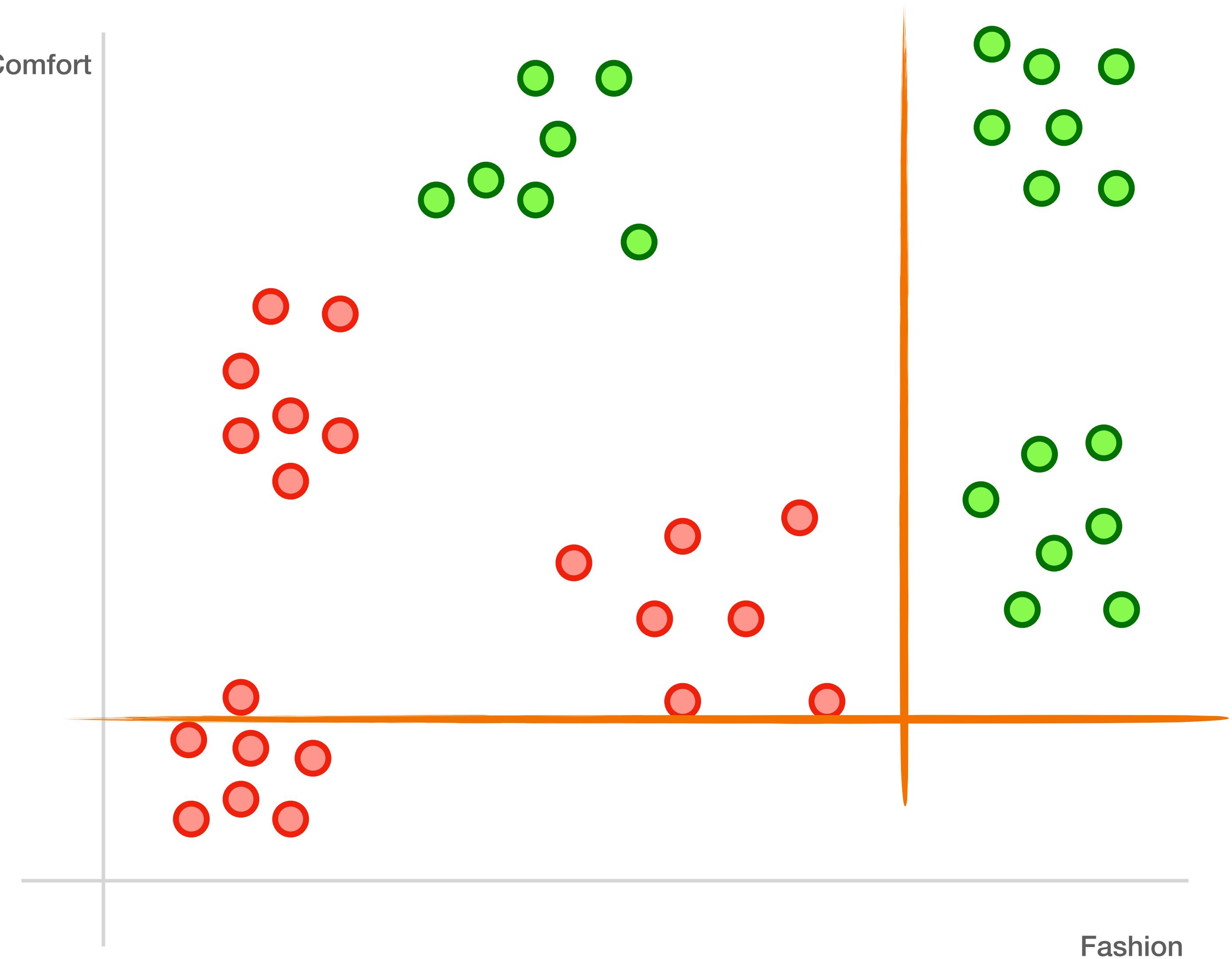
“split”



“split”

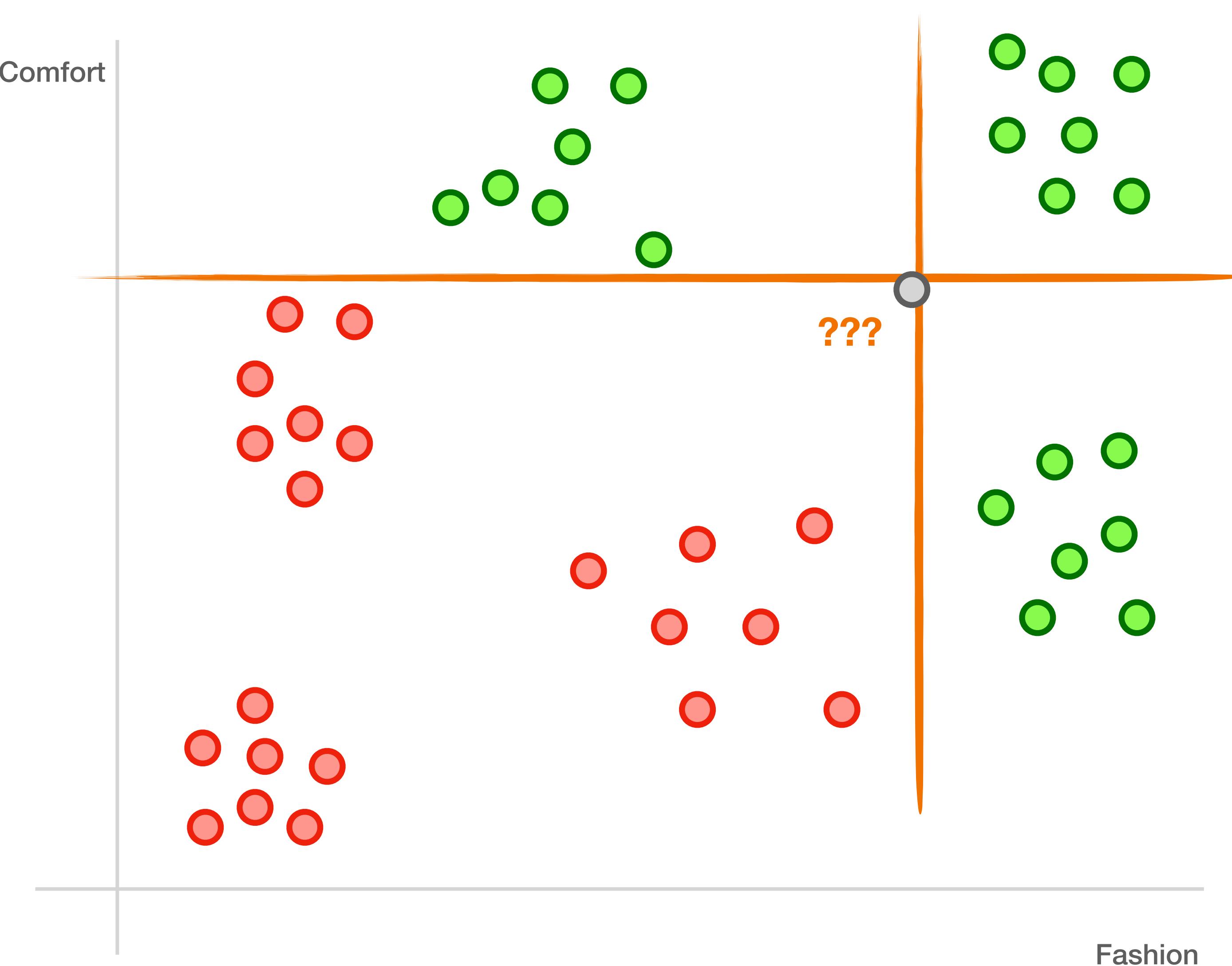


“split”



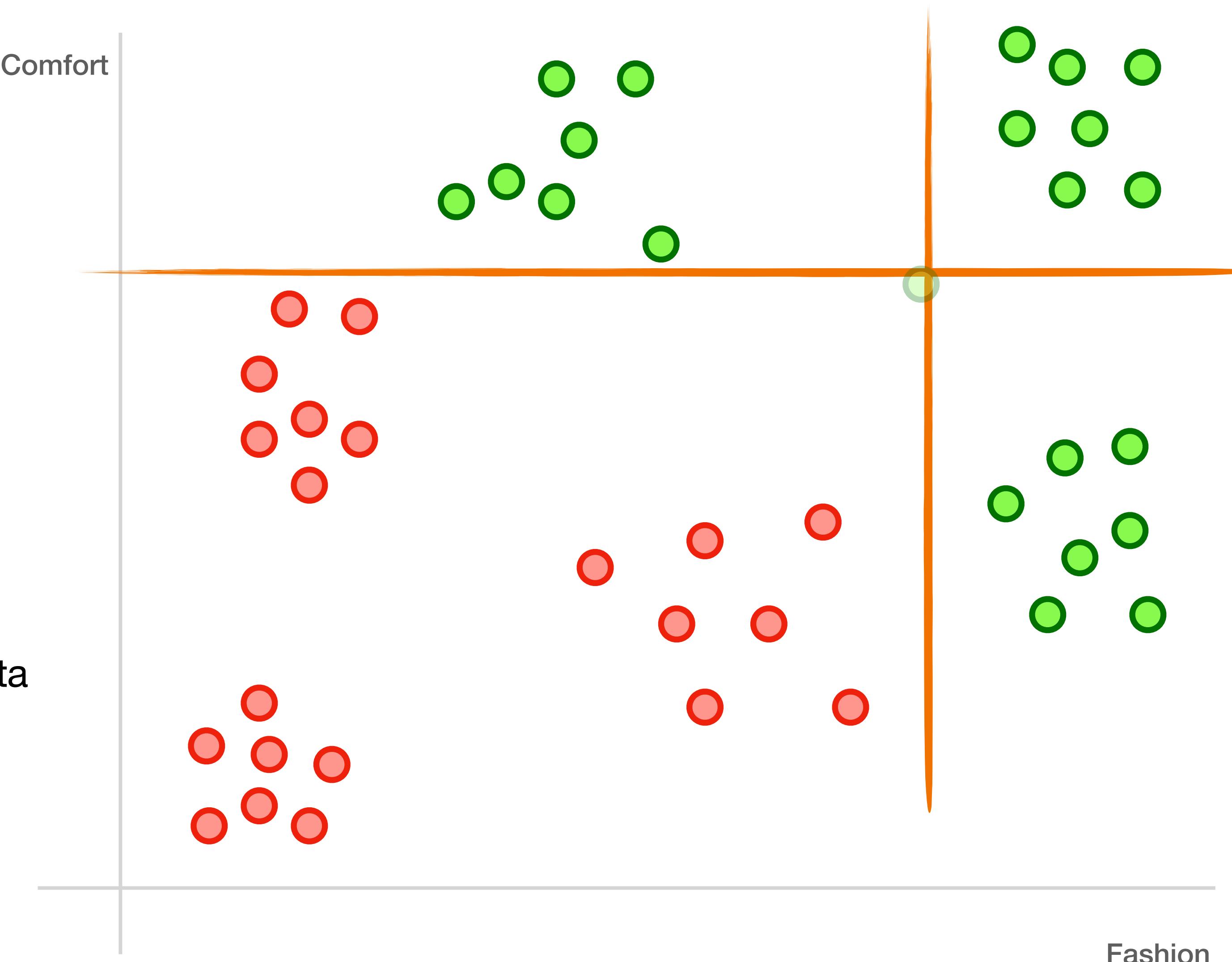
“split”

this is fine,
but...



“split”

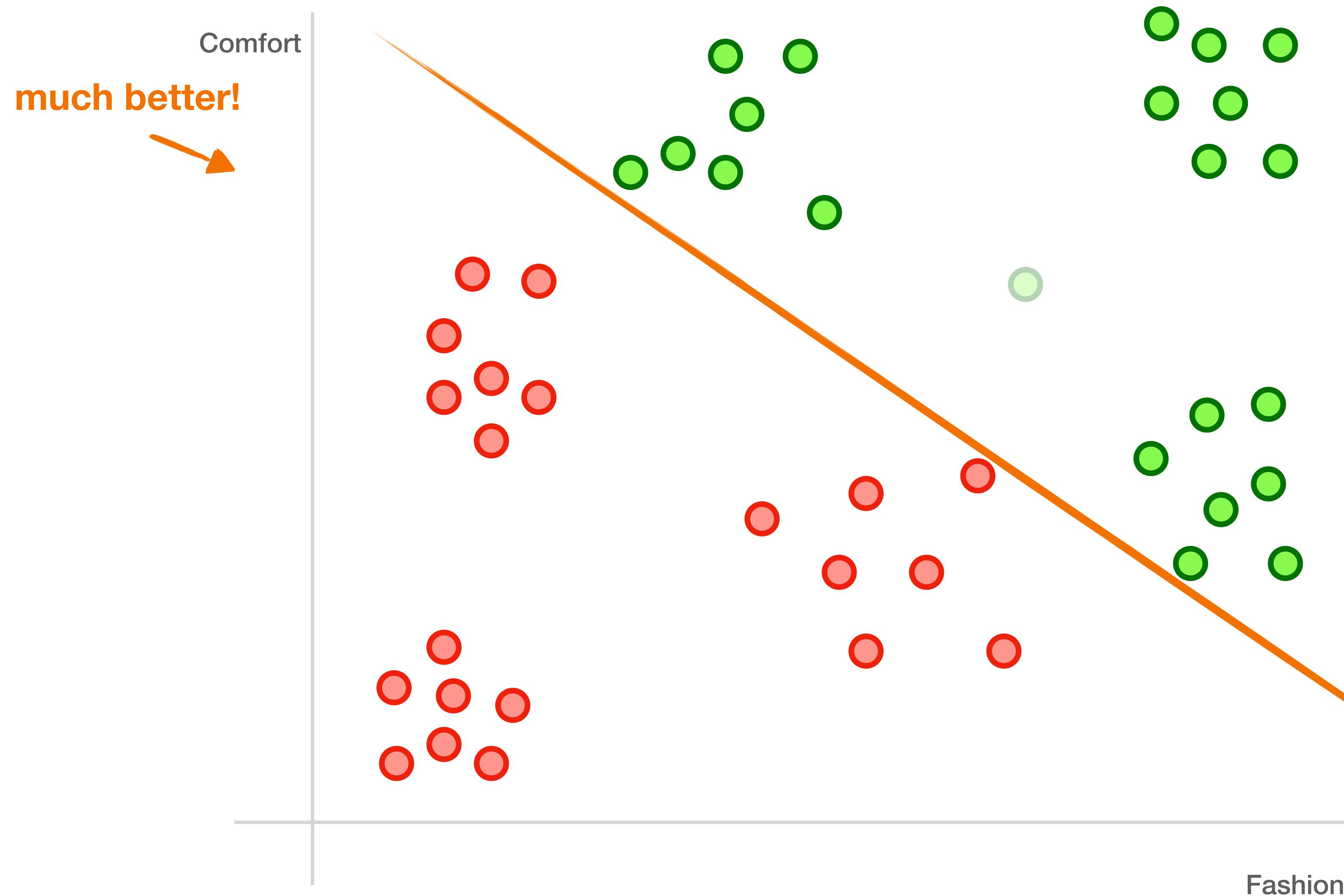
- the **binary splits** in decision trees often don't do well in complex, multivariate data



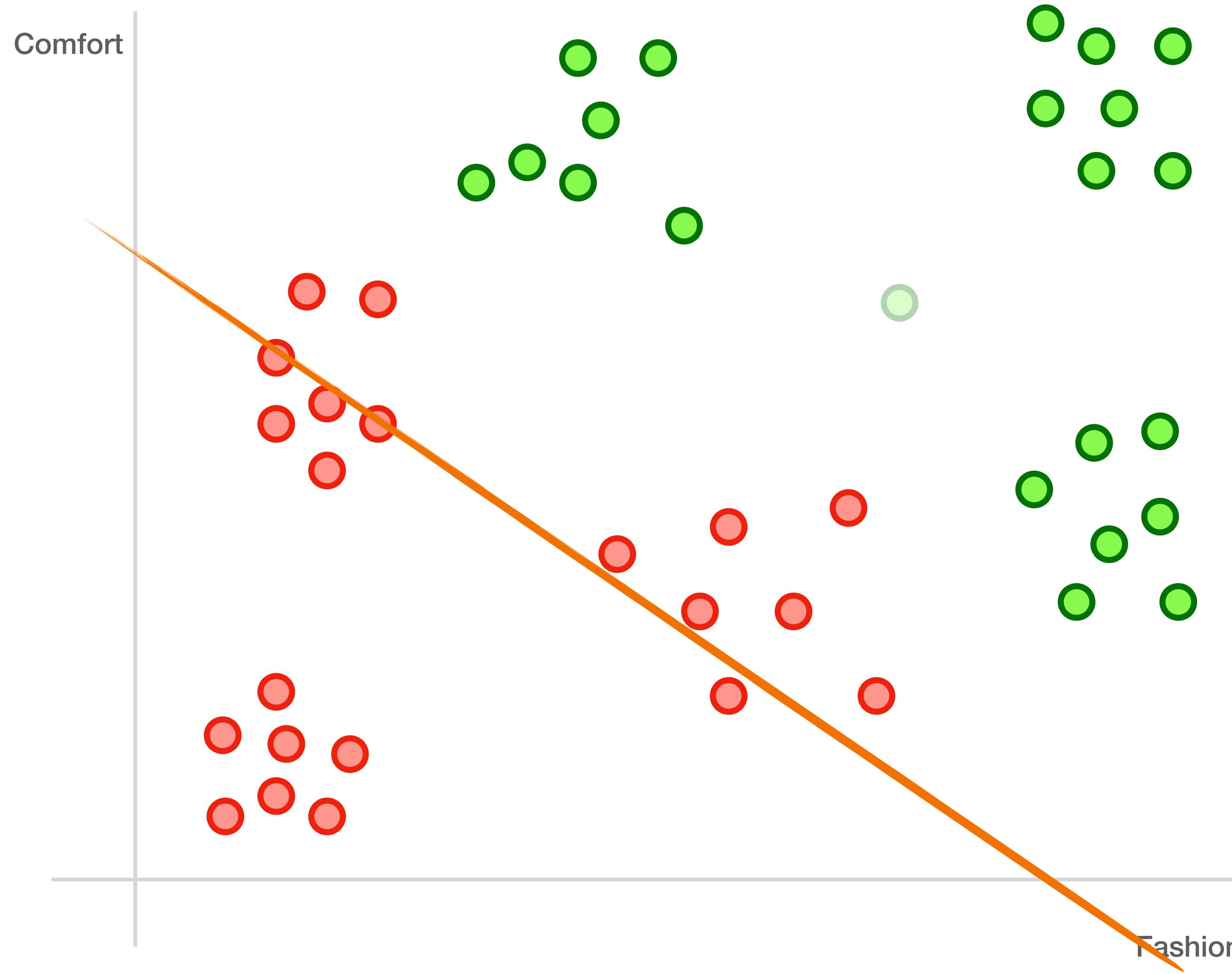
we need a more complex model

Support vector machines!

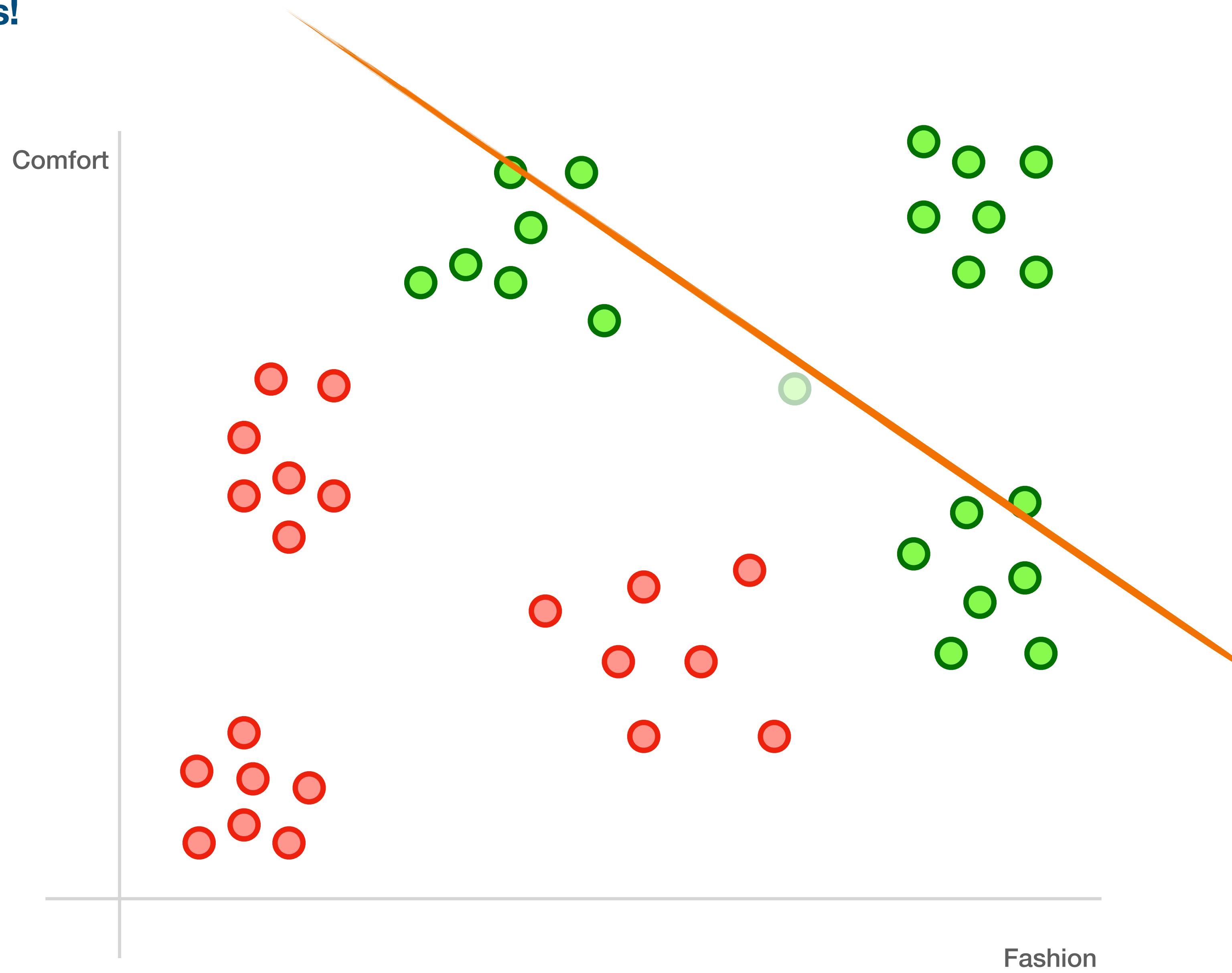
Support vector machines!



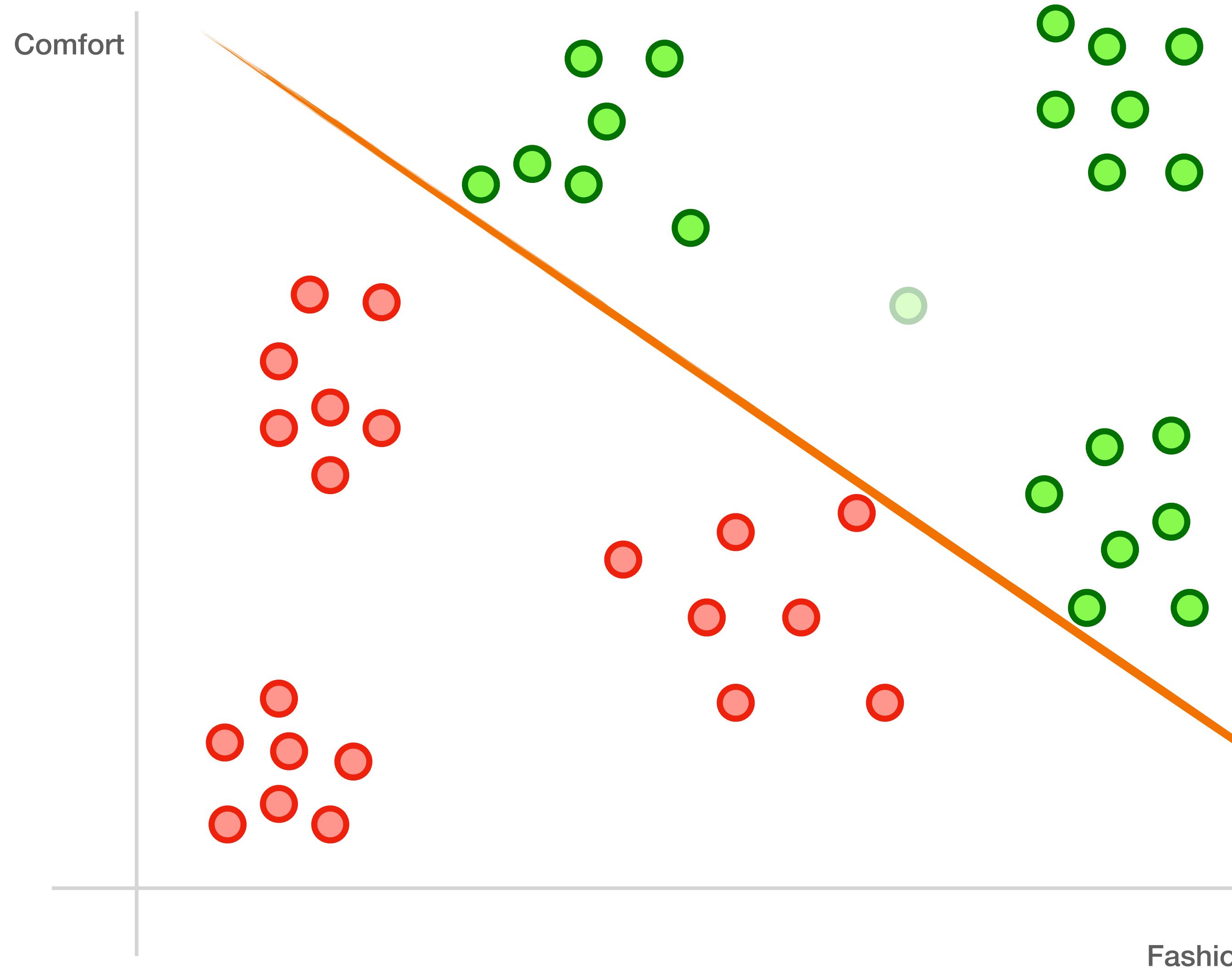
Support vector machines!



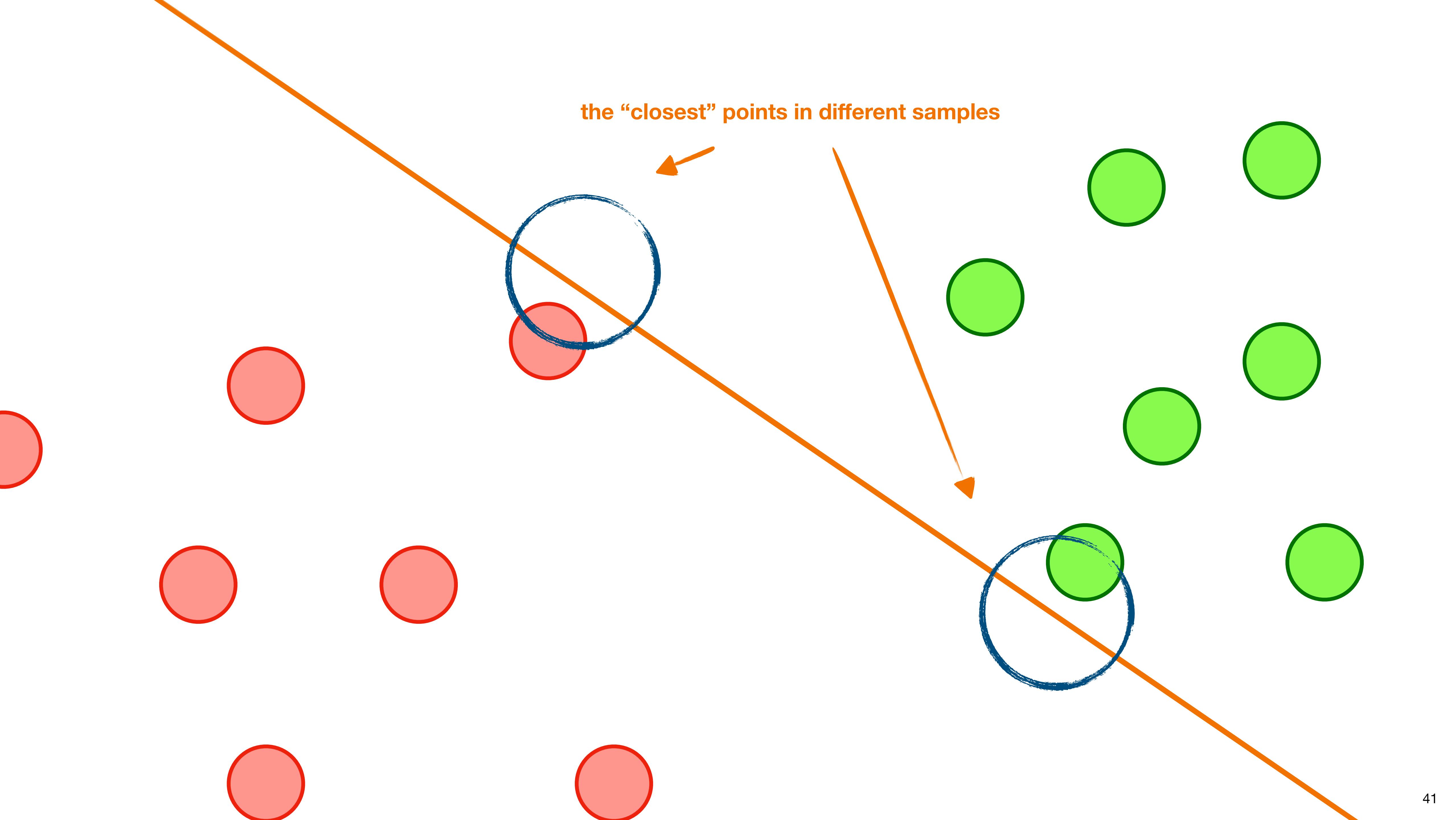
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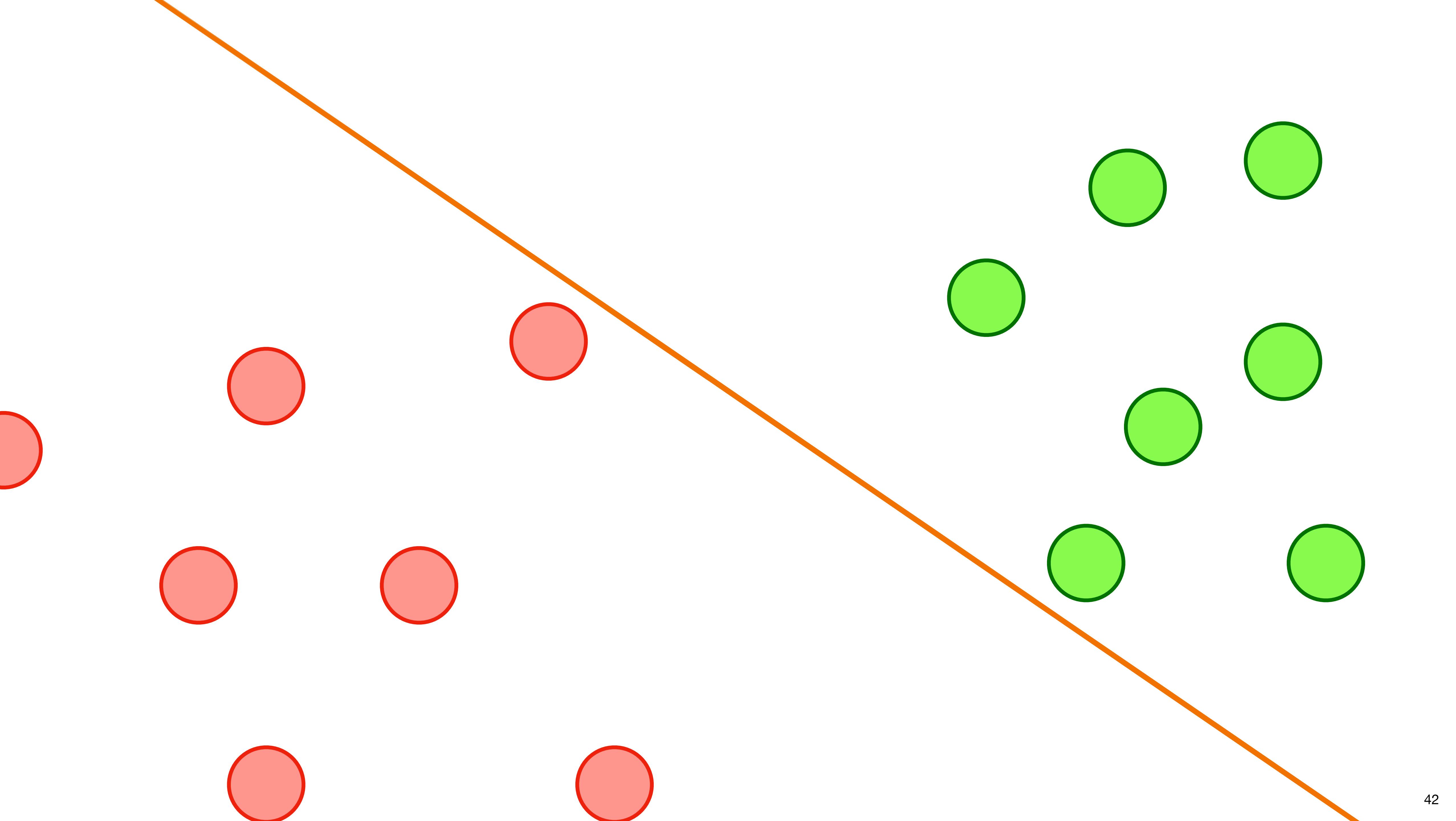


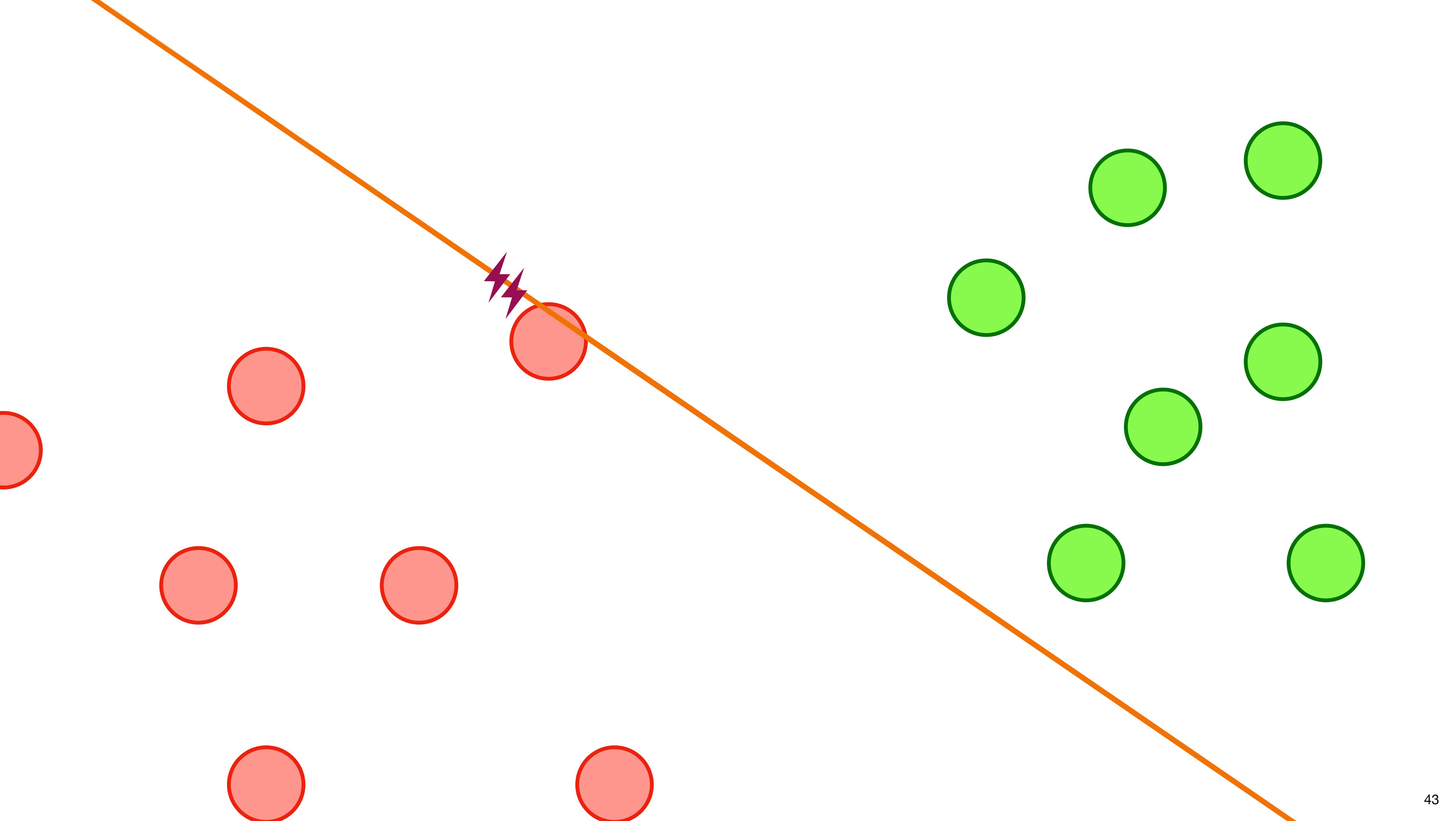
Support vector machines!

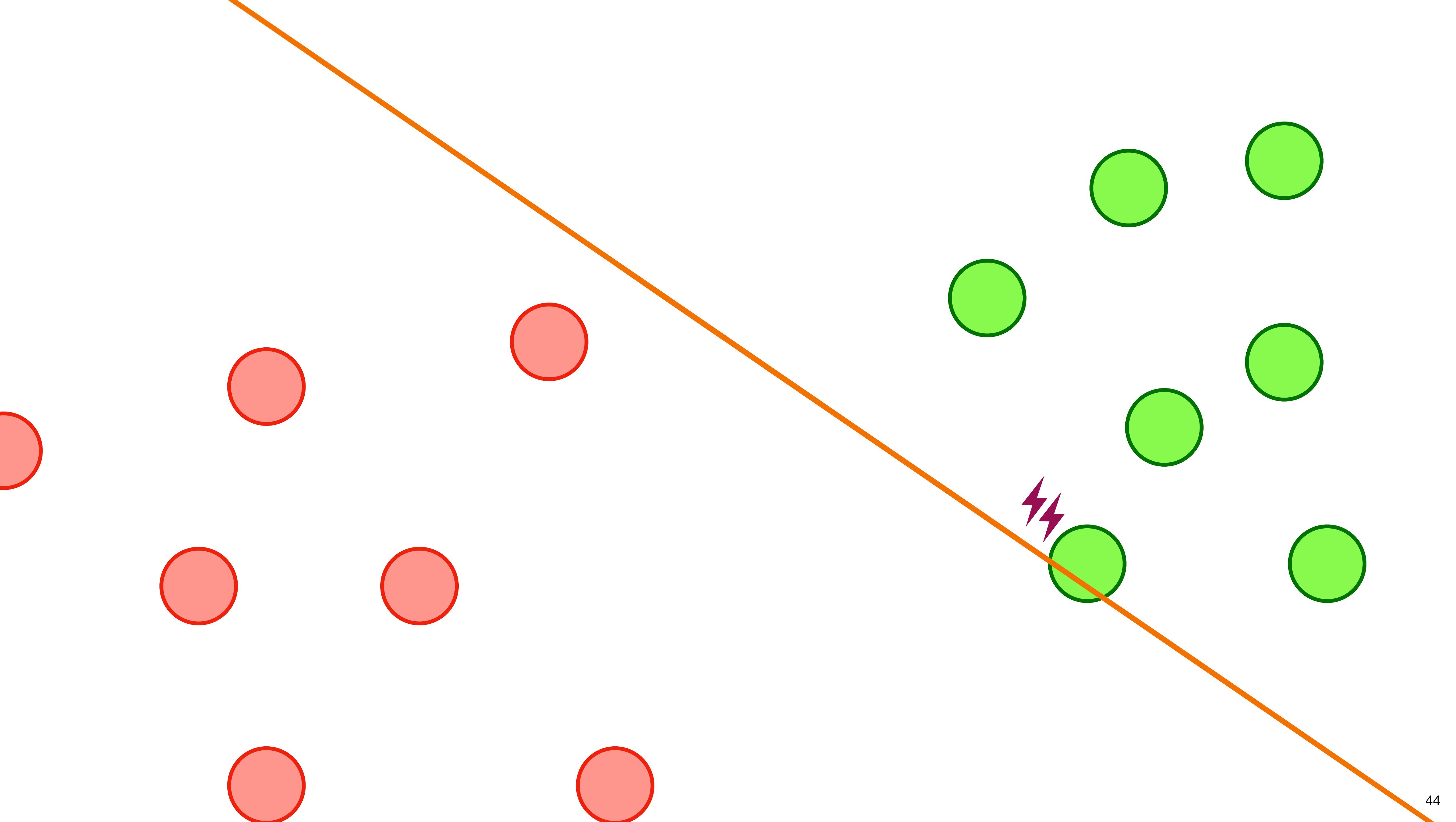


the “closest” points in different samples

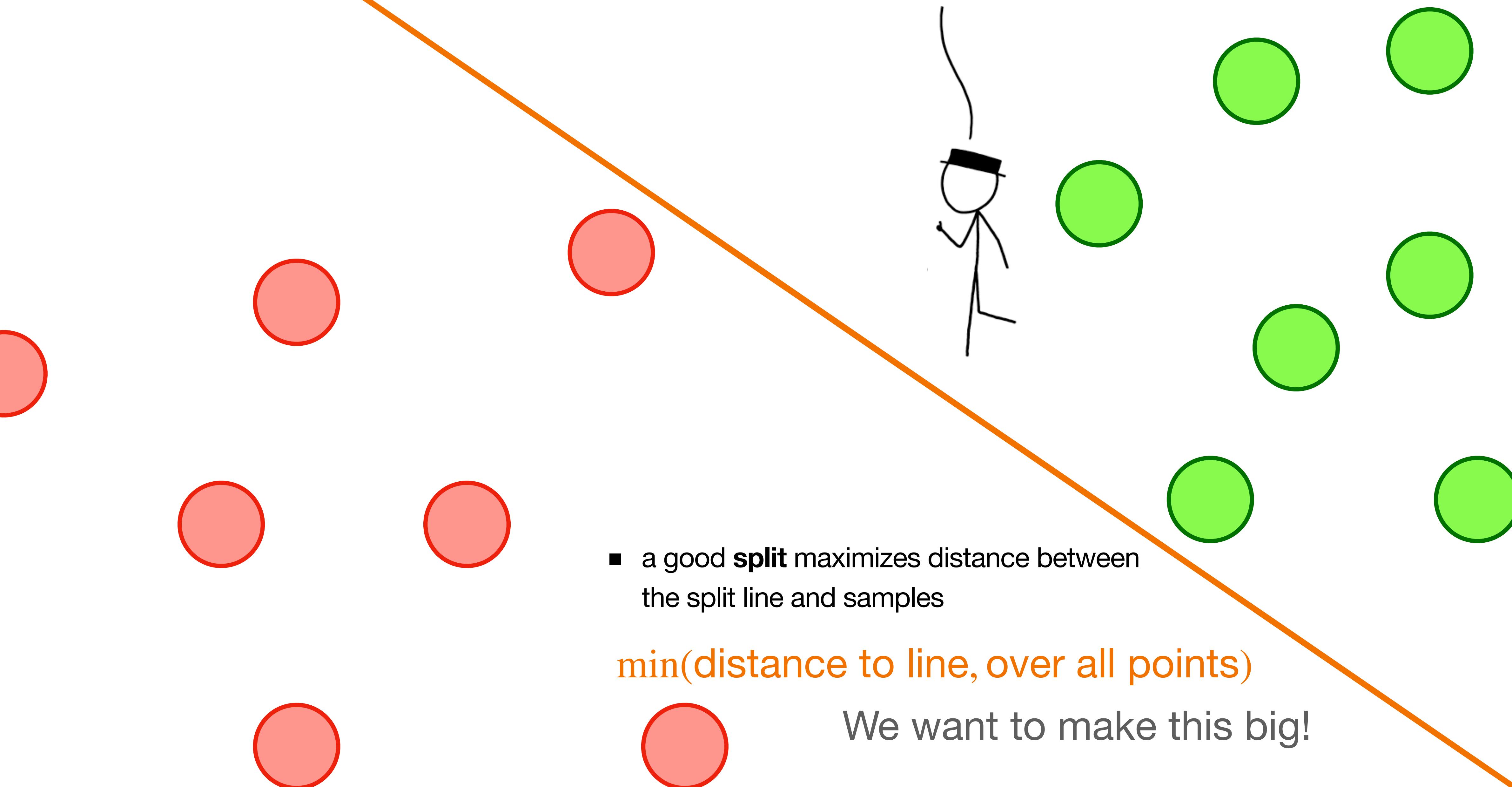






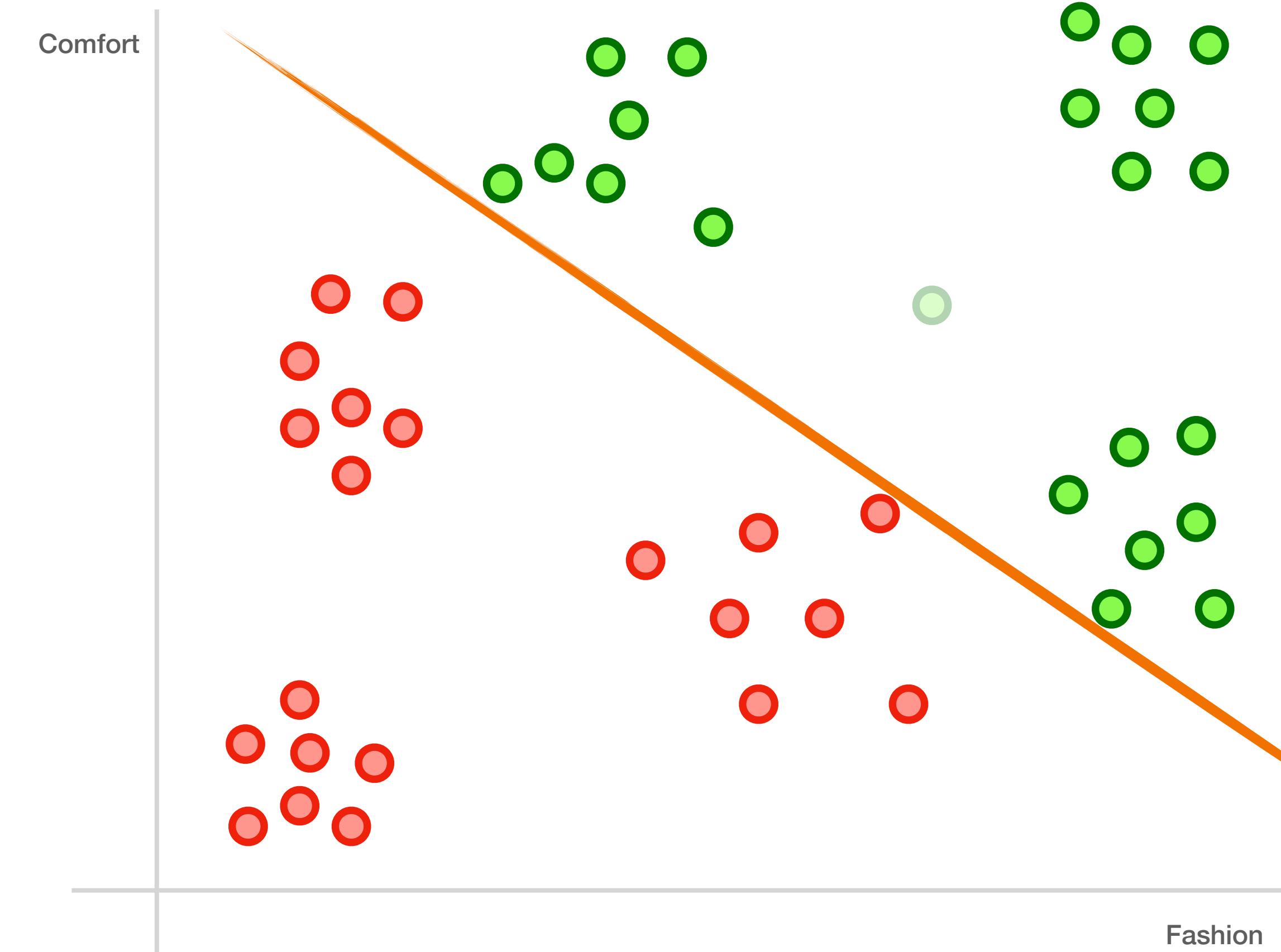


We gotta do better
than this!

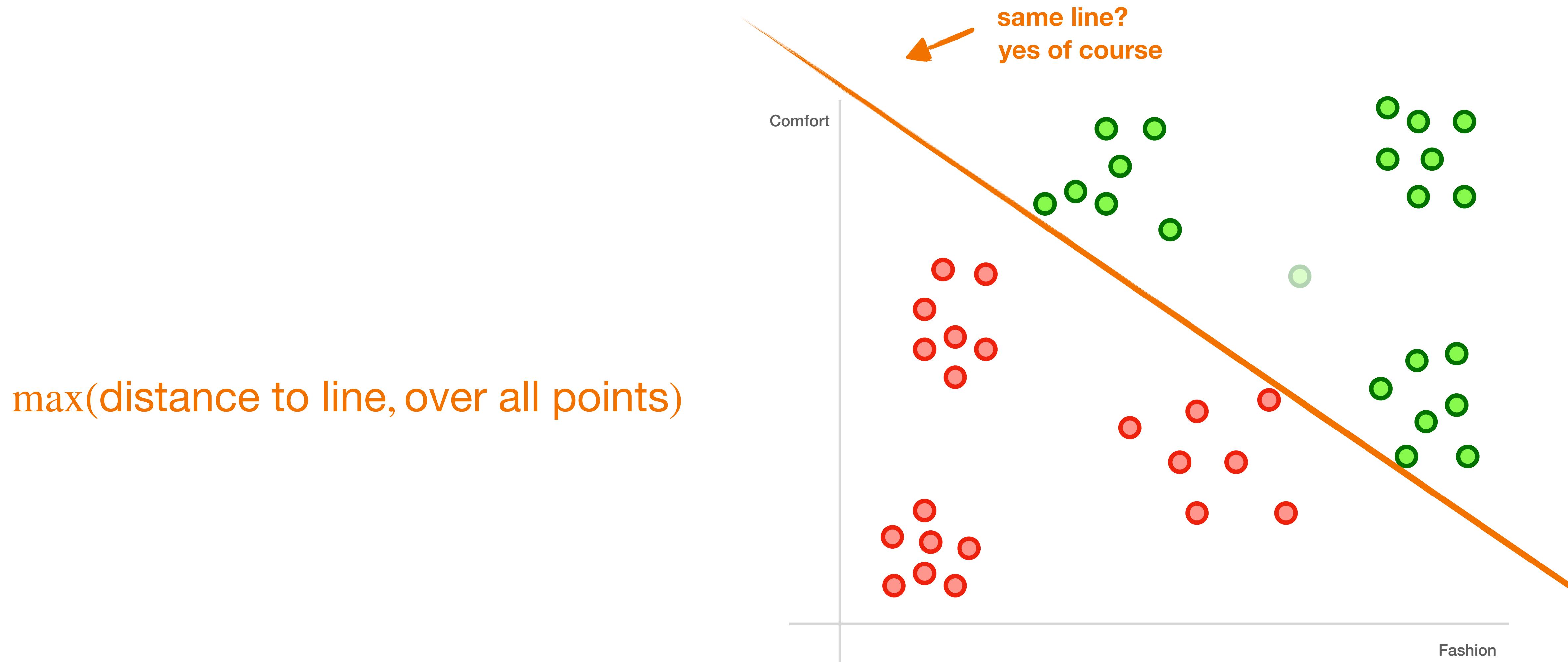


Support vector machines!

$\max(\text{distance to line, over all points})$

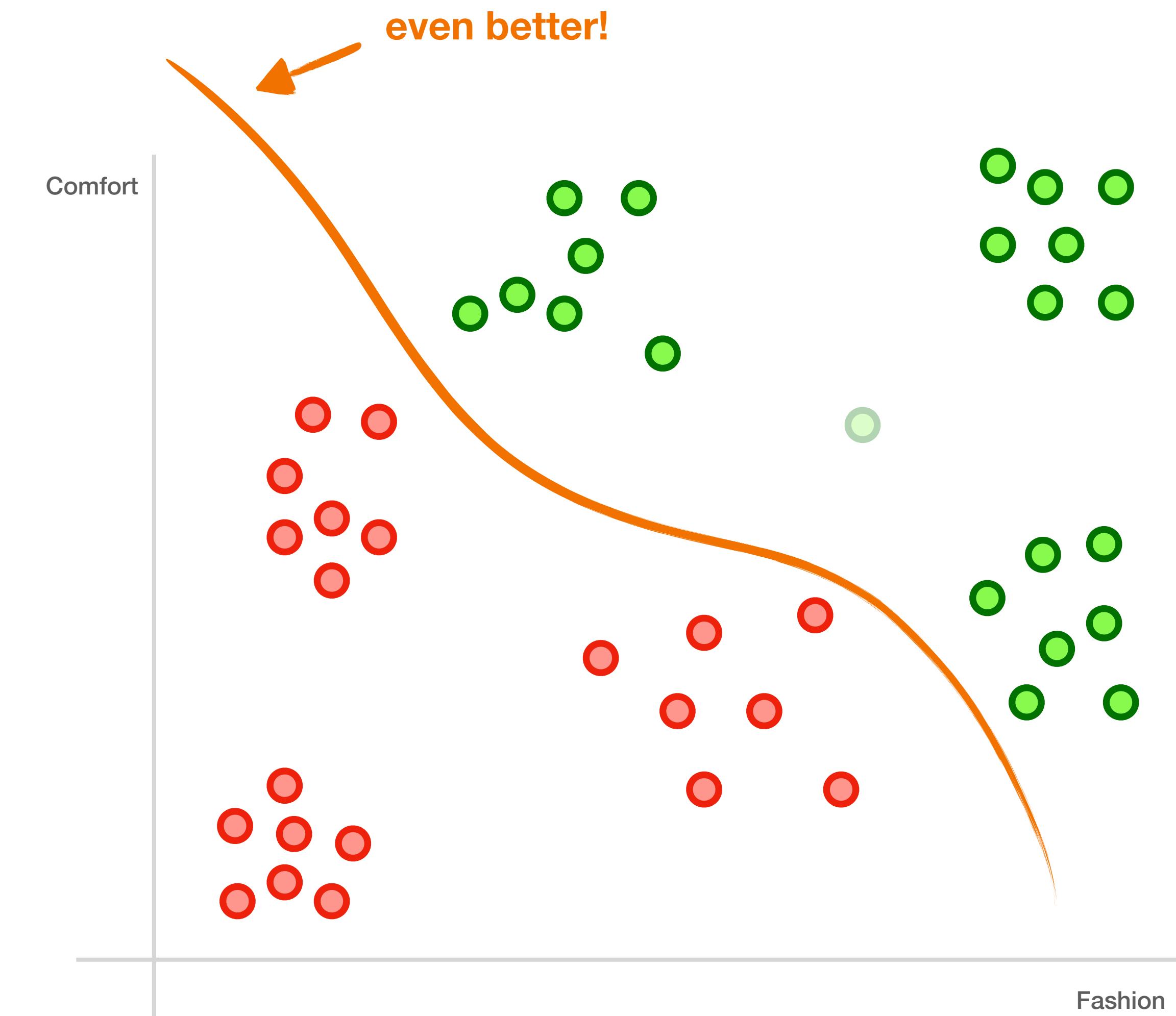


Support vector machines!



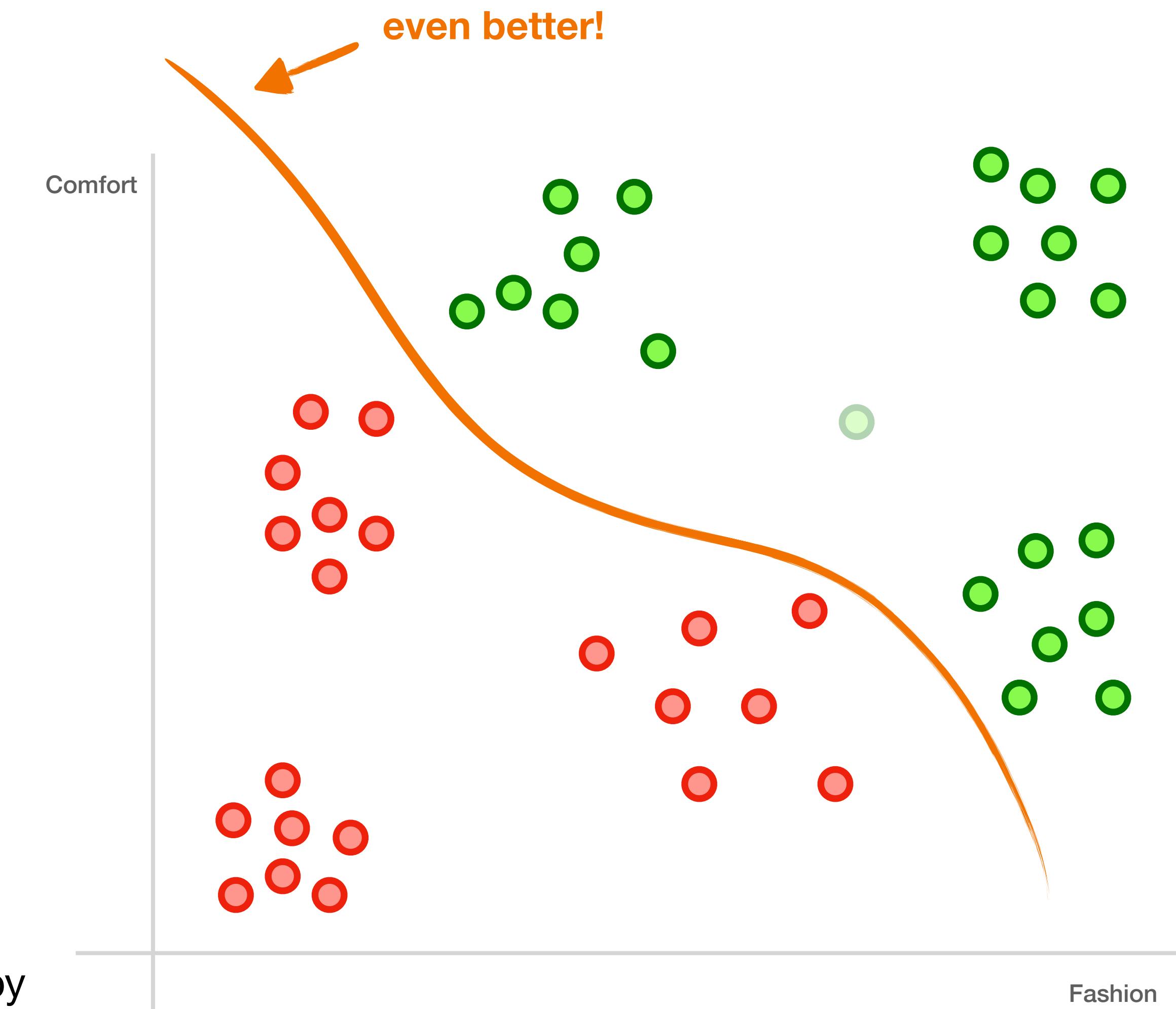
Support vector machines!

max(distance to line, over all points)



Support vector machines!

max(distance to line, over all points)



- **support-vector machines** are classifiers that divide data by class, aiming to create a **margin** that's as wide as possible.
- They use non-linear functions

**BACK ←
TO THE PROBABILITY**

PROBABILITY

Internal Memo:

**146 Hagley Road, Birmingham
Birmingham B3 3PJ**

**From the Desk of
Mr. Jerry Smith
Date: 13/01/14**

Attn: Sir/Madam,

I seize this opportunity to extend my unalloyed compliments of the new season to you and your family hoping that this year will bring more joy, happiness and prosperity into your house hold.

I am certain that by the time you read this letter I might have already gone back to my country **United Kingdom**. I visited South Africa during the New Year period and during my stay, I used the opportunity to send you this letter believing that it will reach you in good state.

PROBABILITY

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- “unalloyed complements” → Spam
- “\$100,000 dollars” → Spam
- “relative dying of cancer” → Spam

PROBABILITY

IF we have this	THEN we have this
“unalloyed complements”	Spam
“\$100,000 dollars”	Spam
“relative dying of cancer”	Spam

PROBABILITY

IF we have this THEN we have this

PROBABILITY

IF we have this THEN we have this

$$A \mid B$$

IF we have this THEN we have this

$$A \mid B$$

- Is Spam
- “Nigerian Prince”

PROBABILITY

IF we have this THEN we have this

spam | nigerian prince

IF we have this THEN we have this

$$P(\text{spam} \mid \text{nigerian prince})$$

high?	Nigerian prince	→	spam likely
low?	Nigerian prince	→	not spam

- **conditional probabilities** can be used as a classifier!

PROBABILITY

$$P(\text{spam} \mid \text{nigerian prince}) = \frac{P(\text{spam})P(\text{nigerian prince} \mid \text{spam})}{P(\text{nigerian prince})}$$

PROBABILITY

$$P(\text{spam} | \text{nigerian prince}) = \frac{P(\text{spam})P(\text{nigerian prince} | \text{spam})}{P(\text{nigerian prince})}$$

Diagram illustrating the components of the Bayes' theorem formula:

- % of spam in dataset (orange arrow pointing to the first term)
- % of Nigerian prince in dataset (orange arrow pointing to the denominator)
- % of spam in dataset that relates to Nigerian prince (orange arrow pointing to the second term)

Naïve Bayes Classifier

$$P(\text{spam} \mid \text{nigerian prince}, \text{offer}) = \frac{P(\text{spam})P(\text{nigerian prince} \mid \text{spam})}{P(\text{nigerian prince})} \cdot \frac{P(\text{offer} \mid \text{spam})}{P(\text{offer})}$$



- **conditional probabilities** can be used as a classifier!
- a classifier made this way, however, is “**naïve**” when extended to multiple features

multiplication for AND assumes independence!
“naïve”

Three classifiers! That's a lot.
Let's get to the *long lab!*