MATH435 Latex Exercise

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This is the SEIR model:

$$\frac{dS}{dt} = -\beta SI,\tag{1}$$

$$\frac{dE}{dt} = \beta SI - \eta E,\tag{2}$$

$$\frac{dI}{dt} = \eta E - \gamma I,\tag{3}$$

$$\frac{dR}{dt} = \gamma I \tag{4}$$

with initial conditions

$$S(0) = S_0, E(0) = E_0, I(0) = I_0, R(0) = R_0.$$

Note that (2) is not in the usual SIR model.

We can prove that

- 1. The total population N = S + E + I + R is constant.
- 2. $\lim_{t\to\infty} S(t) = S_{\infty} > 0$, that is, not every body gets the disease.