

#1: When using the last element of the array for the partition value the worst possible case for quick sort arises when the partition makes no swaps
#aka the array is sorted in ascending or descending order
#when this is the case, quick sort requires $n-1$ total runs with $n-1$ -runs comparisons, which ends up being the same as bubble sorts average case with $\frac{n(n-1)}{2}$

#2: a vector with 16 elements that could represent this case simply counts from 0 to 15, [0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15] though for demonstration purposes it is easier

#to choose a reverse sorted list [15,14,13,12,11,10,9,8,7,6,5,4,3,2,1,0]

#after first partition the list will be [0,15,14,13,12,11,10,9,8,7,6,5,4,3,2,1]

#followed by recalls with sub sections of the list as follows [0]

[14,13,12,11,10,9,8,7,6,5,4,3,2,1]

#following this trend all the way through we get

#[1,15,14,13,12,11,10,9,8,7,6,5,4,3,2]

#[1] [15,14,13,12,11,10,9,8,7,6,5,4,3,2]

#[2,15,14,13,12,11,10,9,8,7,6,5,4,3]

#[2] [15,14,13,12,11,10,9,8,7,6,5,4,3]

#[3,15,14,13,12,11,10,9,8,7,6,5,4]

#[3][15,14,13,12,11,10,9,8,7,6,5,4]

#[4,15,14,13,12,11,10,9,8,7,6,5]

#[4][15,14,13,12,11,10,9,8,7,6,5]

#[5,15,14,13,12,11,10,9,8,7,6]

#[5][15,14,13,12,11,10,9,8,7,6]

#[6,15,14,13,12,11,10,9,8,7]

#[6][15,14,13,12,11,10,9,8,7]

#[7,15,14,13,12,11,10,9,8]

#[7][15,14,13,12,11,10,9,8]

#[8,15,14,13,12,11,10,9]

#[8][15,14,13,12,11,10,9]

#[9,15,14,13,12,11,10]

#[9][15,14,13,12,11,10]

#[10,15,14,13,12,11]

#[10][15,14,13,12,11]

#[11,15,14,13,12]

#[11][15,14,13,12]

#[12,15,14,13]

#[12][15,14,13]

#[13,15,14]

#[13][15,14]

#[14,15]

#[14][15]

#resulting in the final list[0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15]

#4: The results match our complexity analysis with a quadratic curve modeling the results of comparisons against number of elements in the worst case, similar to that of the average case of bubble sort