

The Rado Graph and Maps from the lattice to the interval.

12/7 (1)

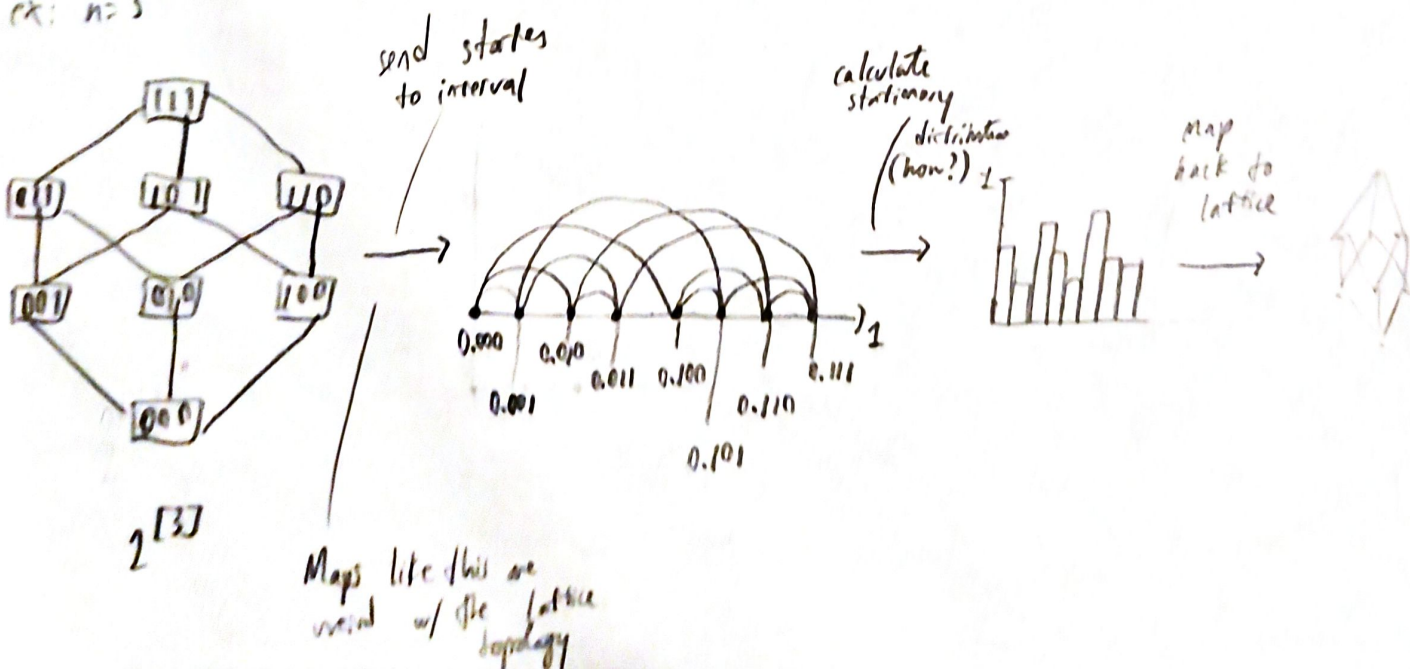
This is not the same problem as the one I've been considering, but I want it written out so I can come back to it the next time I have a desire to.

Let  $G$  be the Rado graph (which I believe is represented by graphon  $A \equiv 1/2$ ? (can check this)), and let  $G_n$  be the induced subgraph of  $G$  on  $[n]$ . Let  $A_n$  be the adjacency matrix. Let  $L$  be an integer corresponding to an  $l\%$  load on  $[n]$ , and let  $B = B_L$ . Also, let  $2^{[n]} = [1]_0^n$ , and finally, let  $\text{BrAn}(A, B, \epsilon)$  be the ergodified breacher-annihilator process, with  $0 < \epsilon < 1$ .

~~$\text{BrAn}$  imposes a directed graph on  $2^{[n]}$~~

$\text{BrAn}$  is an ergodic Markov chain on  $2^{[n]}$ , but the statespace is so large that analyzing the stationary distribution is very difficult. What I've been wanting to try is a map such as the following:

ex:  $n=3$



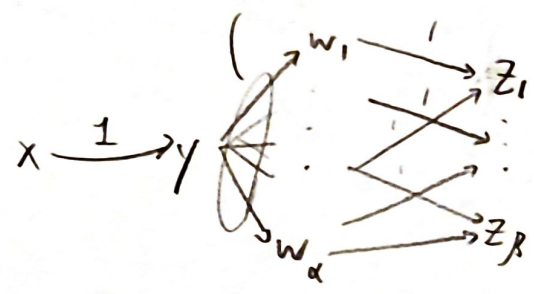
$$2^{[n]} \xrightarrow{A} [n]_0^n \xrightarrow{+b} [n+1]_0^n \xrightarrow{f(\cdot)} 2^{[n]}$$

## Appendix 1

Basically, ~~we~~ only ~~have~~ have brute force to calculate the transition probabilities:

we've seen before that

stored in  $w\_dict$



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For all  $x \in 2^{[n]}$ :
     $y = Ax$ ;  $w\_avbl = \{\}$ ,
    for all  $b$  in  $B$ :
         $w = y + b$ 
         $w\_avbl \cup= \{w\}$ 
     $w\_dict = \{w: [] \text{ for } w \text{ in } w\_avbl\}$ 
    for all  $b$  in  $B$ :
         $w = y + b$ 
         $w\_dict[w].append(IP(b_t = b | x_t = x))$ 
    for  $w$  in  $w\_dict.keys()$ :
         $w\_dict[w] = \text{sum}(w\_dict[w])$ 
     $z\_dict = \{z: \{\} \text{ for } z \text{ in } 2^{[n]}\}$ 
    for  $w$  in  $w\_dict.keys()$ :
         $z = f(w)$ 
         $z\_dict[z] \cup= \{w\}$ 
    for  $z$  in  $2^{[n]}$ 
         $T(x, z) = \text{sum}([w\_dict[w] \text{ for } w \text{ in } z\_dict[z]])$ 
    
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• Check in the future and perhaps translate into math notation or pseudocode.

Appendix 2 is proof that  $IP(\tau > n)$  is a fraction of  $\pi$