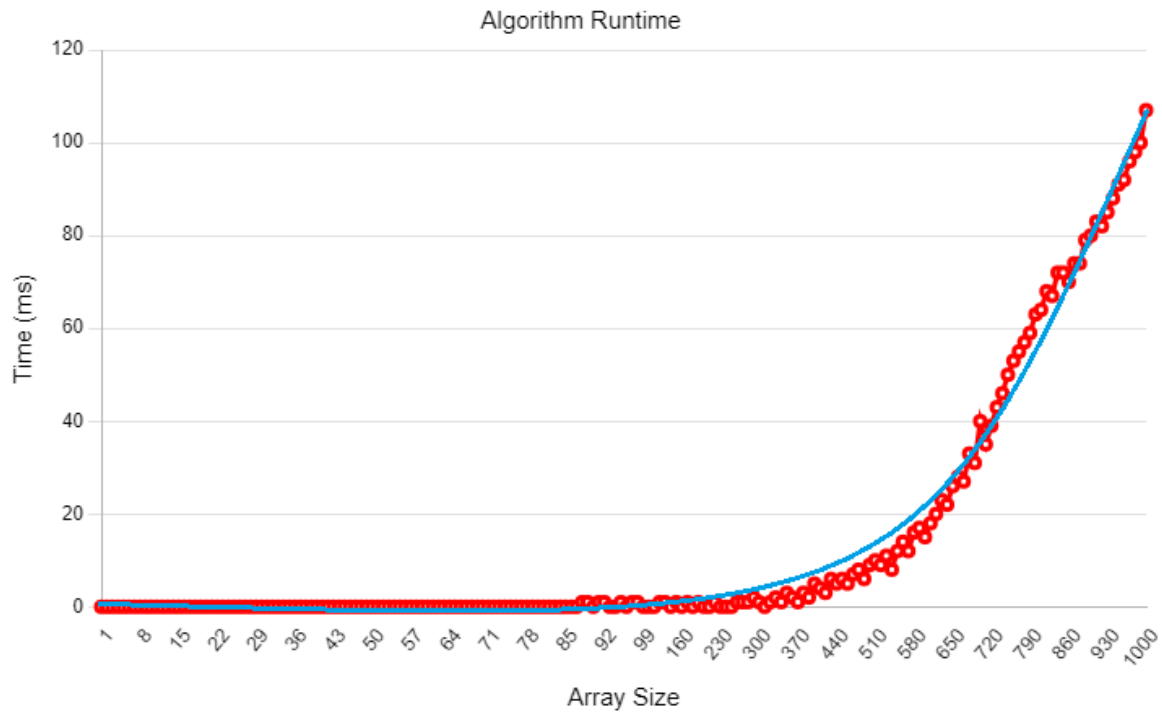


$$1. \quad T(n) = \sum_{i=1}^n \sum_{j=1}^n (1) = \sum_{i=1}^n (n) = n * \sum_{i=1}^n (1) = n * n = n^2$$

2.

**Red** = Data Points

**Blue** = Fitted Curve



3.

Since the fitted curve is a polynomial, we will assume that  $T(n) = an^2 + bn + c$ .

Upper Bound:  $an^2 + bn + c$

Lower Bound:  $n^2$

Big O Notation -  $O(n^2)$

Big  $\Omega$  Notation -  $\Omega(n^2)$

Big  $\Theta$  Notation -  $\Theta(n^2)$

4. Yes, the runtime will increase. The  $y = 1$  outside the loops will make no difference, but the added statement  $y = i + j$  will approximately double the runtime, as in practice, this doubles the runtime from about  $n^2$  to about  $2n^2$ .
5. No. Despite the fact that the runtime has increased in practice, we ignore all constants in theory, so our runtime is still  $O(n^2)$ .