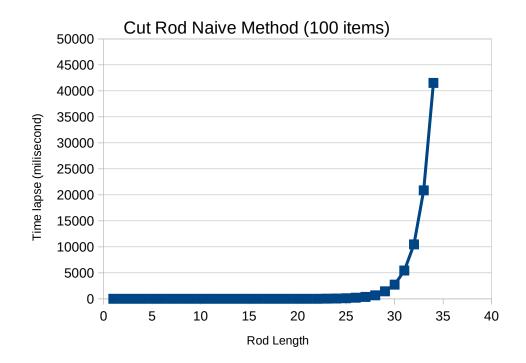
HW4 Aida Sharif Rohani

Array:

[4, 14, 20, 15, 6, 2, 11, 6, 11, 9, 17, 16, 13, 11, 1, 17, 20, 18, 11, 14, 8, 14, 18, 13, 9, 13, 10, 9, 4, 20, 12, 3, 10, 9, 1, 13, 9, 19, 11, 5, 1, 7, 16, 13, 20, 17, 8, 11, 5, 3, 14, 16, 8, 10, 3, 4, 3, 8, 15, 13, 9, 9, 18, 3, 19, 18, 6, 16, 4, 15, 15, 4, 3, 9, 4, 17, 8, 5, 2, 10, 4, 12, 11, 10, 10, 5, 11, 12, 18, 20, 19, 14, 14, 9, 20, 2, 8, 1, 16, 9]

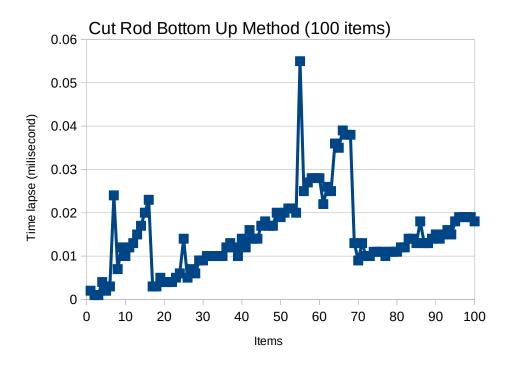
Result:

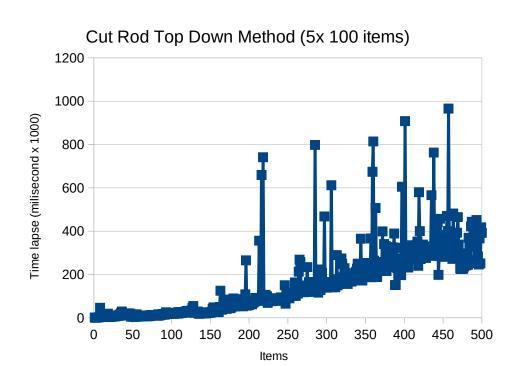
1- The maximum length calculated was 34. As the length increases the number of calculations exponentially increases. The shape of the graph is exponential, it means we can't calculate large array of elements with this method and it's very expensive and lengthy time wise.

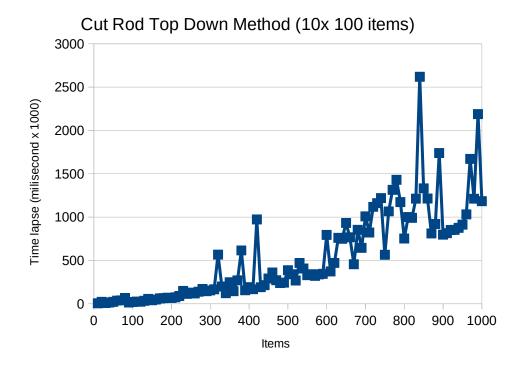


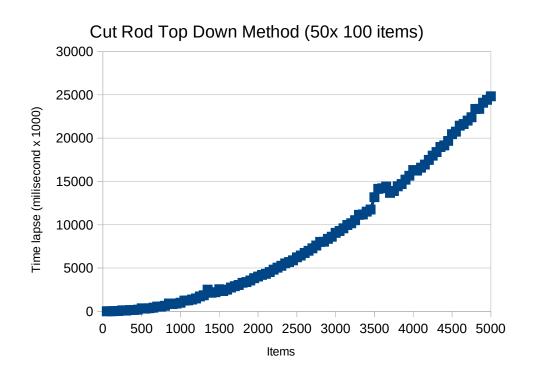
2- In top down in contrast to naive method all the numbers are calculated in less than 0.06 milliseconds. It shows that memoization makes it much faster to do the calculations as each number is only calculated once and after that it's saved in an array. The plot is not very smooth but the higher than average points are just noises and it's normal in order of milliseconds.

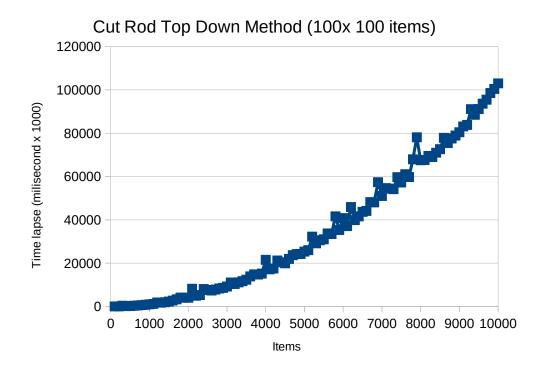
The higher elements makes the graph smoother and the time is increasing in n^2. For example when doing for 100x times the time increases by 10000 times. Which implies we can calculate much larger arrays compared to naive method.











3-In bottom up method we get the same results as bottom up; again all the numbers are calculated in less than 60 milliseconds. It shows that bottom up methods makes it much faster to do the calculations as each number is only calculated once and after that it's saved in an array. The plot is not very smooth but the higher than average points are just noises and it's normal in order of milliseconds.

The higher elements makes the graph smoother and the time is increasing in n^2. For example when doing for 100x times the time increases by 10000 times. Which implies we can calculate much larger arrays compared to naive method.

