

Bonus Assignment Week 5

This week we are using numpy and matplotlib

In [1]:

```
# Start by loading the relevant libraries
import numpy as np
```

Numpy: Magic Square

A [magic square](#) is a matrix in which the sum of all rows, columns and diagonals are the same. You can verify this fact for the matrix below by:

- calculating an array containing the sums of all rows
- calculate the minimum and maximum of this array
- calculating an array containing the sum of all columns
- calculate the minimum and maximum of this array
- calculating the sum of both diagonals
- check that both minimums and maximums and diagonals are the same value.

```
msquare = np.array([
    [17, 24, 1, 8, 15],
    [23, 5, 7, 14, 16],
    [4, 6, 13, 20, 22],
    [10, 12, 19, 21, 3],
    [11, 18, 25, 2, 9]])
```

Assignment 5.1

Write a function `is_magic_square()` that takes a matrix as input and returns **True** if the matrix is a magic square and **False** otherwise. Use the matrix above to test your function.

Hint: Use `np.diag` and `np.fliplr` to get the diagonals of a matrix.

In [2]:

```
msquare = np.array([
    [17, 24, 1, 8, 15],
    [23, 5, 7, 14, 16],
    [4, 6, 13, 20, 22],
    [10, 12, 19, 21, 3],
    [11, 18, 25, 2, 9]])

def is_magic_square(X):

    a1=min(X.sum(axis = 0))
    a2=max(X.sum(axis = 0))
    a3=min(X.sum(axis = 1))
    a4=max(X.sum(axis = 1))
    a5=np.diag(X).sum()
    a6=np.diag(np.fliplr(X)).sum()

    if a1==a2==a3==a4==a5==a6:
        return True
```

```
        else:
            return False

is_magic_square(msquare)
```

Out[2]:

True

In []:

Generating Magic Squares

The above function can be used in a (crude) method to generate magic squares

Assignment 5.2

Write a function `generateMagicSquare()` that generates a 3x3 magic square (containing numbers 1...9).

Use the following algorithm:

- Use the function `is_magic_square()` from the previous question to check if a matrix is a valid magic square or not.
- Generate random 3x3 squares filled with the exact numbers 1..9 in some order and check if that matrix is a magic square. If so, print the magic square.
- You may need to generate 100,000 matrices to find one that is a magic square (by chance).

Hint: Use `np.random.permutation` to generate a random permutation of an array.

In [3]:

```
def generateMagicSquare():
    for i in range(100000):
        a = np.random.permutation(np.arange(1,10)).reshape((3,3))
        if is_magic_square(a):
            print(a)
            break

generateMagicSquare()
```

```
[[8 3 4]
 [1 5 9]
 [6 7 2]]
```

More grading

This question continues from the exercise made in class (see file 'Week5_class_part1_numpy.ipynb'). We quickly recreate the dataset here, see the aforementioned files for details.

In [4]:

```
# create students and grades arrays, using random grades
students = np.array(['Anne', 'Bob', 'Mary', 'John', 'Julia', 'Mike', 'Susan',
                     'Zach'])
grades = np.random.rand( 8,20 ) * 6 + 4

# create an array with the average grades per student
```

```

avg_grades = grades.mean(axis=1)

# create a masked array where we mask away all grades below 5.8
masked_grades = np.ma.masked_array( grades, grades < 5.8 )

# calculate the averages per student
avg_grades = masked_grades.mean( axis = 1 )

# print the array to see what we have
print(avg_grades)

```

```

[7.78052274196028  7.626971690696596  7.6804664619422365  7.967539048838483
 7.666909333248285  8.011163106702446  7.983003442897682  8.303631617277786]

```

Assignment 5.3

Using the above data, do the following:

1. Plot the average grade per student in a bar chart, set the axis and labels accordingly.
2. Plot the average grades for each of the 20 assignments.
3. Try to fit a line to this line and try to predict the average grades for the next assignment. Plot the result.

Hint Use `np.polyfit()` to find a fitting function. Use `np.polyval()` to evaluate a polynomial. How does the degree of the polynomial effect the fitting?

In [8]:

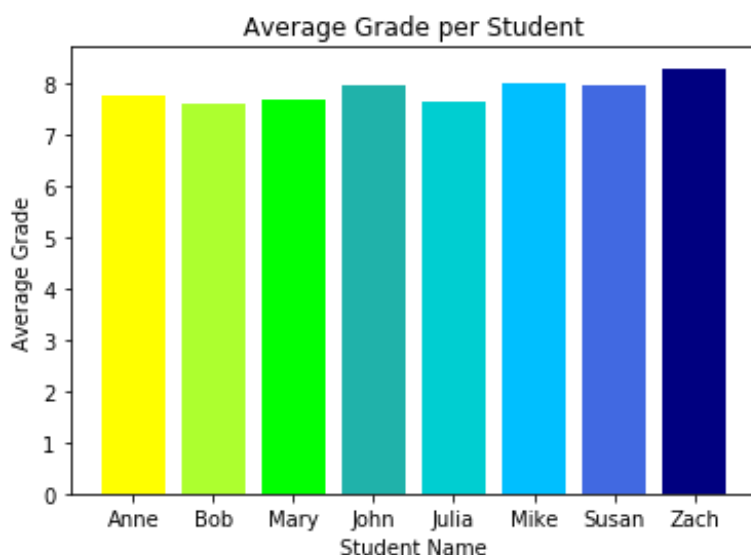
```

import matplotlib.pyplot as plt

colors=['YELLOW','GREENYELLOW','LIME', 'LIGHTSEAGREEN',
'DARKTURQUOISE','DEEPSKYBLUE','ROYALBLUE','NAVY']
x_pos = [i for i, p in enumerate(students)]
plt.bar(x_pos, avg_grades, color=colors)
plt.xlabel("Student Name")
plt.ylabel("Average Grade")
plt.title("Average Grade per Student")
plt.xticks(x_pos, students)

plt.show()

```



In [6]:

```

avg_assignment_grades = masked_grades.mean( axis = 0 )

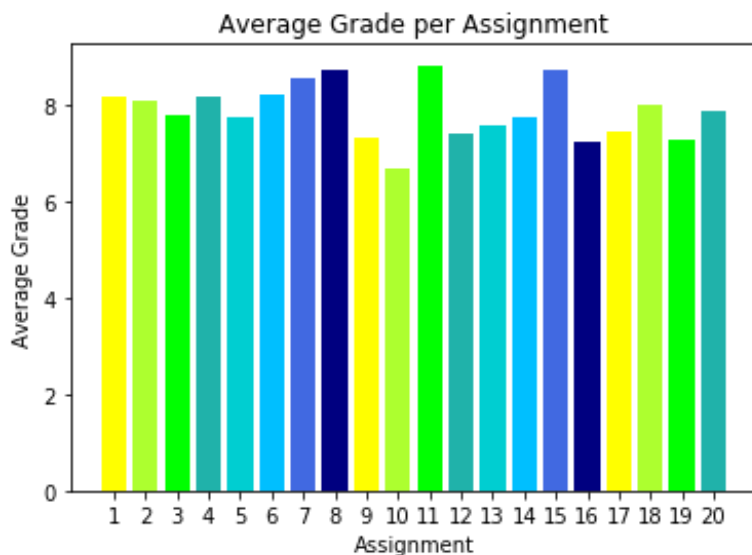
```

```

colors=['YELLOW','GREENYELLOW','LIME', 'LIGHTSEAGREEN',
'DARKTURQUOISE','DEEPSKYBLUE','ROYALBLUE','NAVY']
x_pos = [i+1 for i, p in enumerate(avg_assignment_grades)]
plt.bar(x_pos, avg_assignment_grades,color=colors)
plt.xlabel("Assignment")
plt.ylabel("Average Grade")
plt.title("Average Grade per Assignment")
plt.xticks(x_pos)

plt.show()

```



In [7]:

```

z = np.polyfit(x_pos, avg_assignment_grades, 1)
#The higher the degree of polynomial, the better fit the line
p = np.polyld(z)

xp = np.linspace(1, 20, 20)

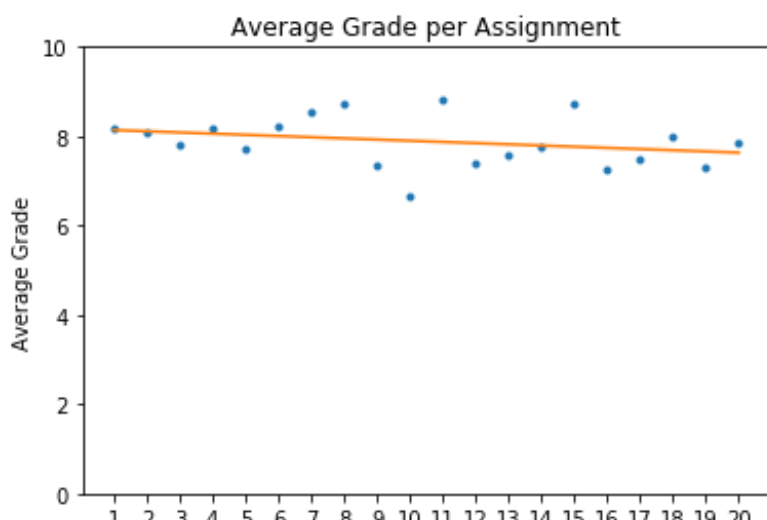
plt.plot(x_pos, avg_assignment_grades, '.', xp, p(xp), '-')

plt.xlabel("Assignment")
plt.ylabel("Average Grade")
plt.title("Average Grade per Assignment")
plt.xticks(x_pos)
plt.ylim(0,10)

plt.show()

print("Predicted average grade of assignment #21 is:", np.polyval(z,21))

```



1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
Assignment

Predicted average grade of assignment #21 is: 7.606610841717395