

Master Thesis

Estimation of Underactuated Degrees of
Freedom(DOF's) in Humanoid Robots

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INTRODUCTION

1.1 Motivation

The field of *Robotics* have seen a tremendous development since the introduction of the term by *Isaac Asimov* in 1940s. The fundamental components of robotic systems are mechanical structure, actuators, sensors and controller. Robotic system ranges from simple *Cartesian manipulator* to the complex *Humanoids*. *Industrial robots* are robots that are used in applications such as palletizing, material loading and unloading, part sorting, packaging etc. These robots usually operate in the structured environment whose geometrical or physical characteristics are known in priori. They are pre programmed to execute the set of tasks. These robots have largely aided the automation of manufacturing processes in the industries. *Mobile robots* that are used in the environments where human beings can hardly survive or be exposed to unsustainable risks are called *Field robots*. *Field robots* normally operate in the unstructured environments, where the geometry or physical characteristics are not know in priori. Mars rover *Curiosity* is one such example. Locomotion in these robots are achieved either by wheels or by mechanical legs. Operating in the unknown environments and dynamic balancing of mechanical structure demands advanced control schemes for *Field robots*.

Abbildung

Figure 1.1: Eine Beispiel-Abbildung.

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GRUNDLAGEN

3

KALMAN FILTERING

Kalman filter is a state estimation principle that is used for determining the internal states of the system from the series of measurements observed over time. For linear systems Kalman filter is proved to be the optimal state estimator.

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STATE ESTIMATION

State estimation is the principle of estimating the internal state of the system from the measurement of inputs and outputs of the system. In general knowledge of the internal state of the system will make the system easy to control. Figure 4.1 shows the usage of state estimator in state feedback control loop.

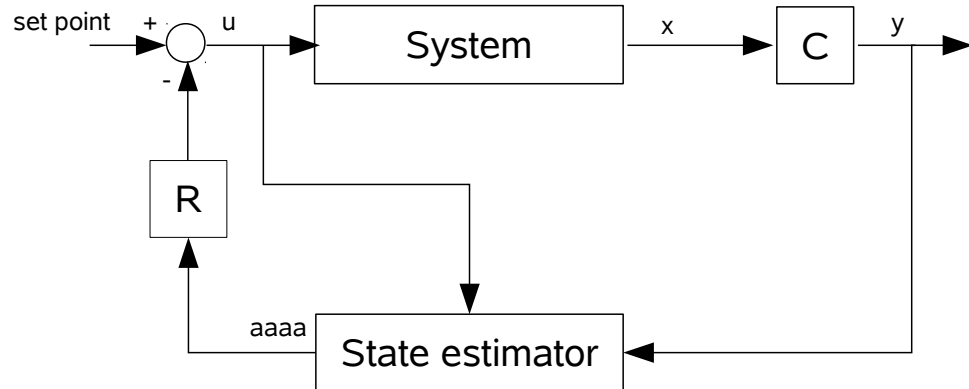


Figure 4.1: Structure of state feedback controller with state estimator

A general nonlinear system in state space form,

$$\begin{aligned}\dot{x}(t) &= f(x(t), u(t)), x(t=0) = x_0 \\ y(t) &= g(x(t), u(t))\end{aligned}\tag{4.1}$$

In Equation 4.1, $x(t)$ represents the vector of internal states, $u(t)$ represents the vector of inputs and $y(t)$ represents the vector of outputs of the system. x_0 is the initial state of

4 State Estimation

the system which is usually unknown. The state estimator is described by the system equation with additional correction term

$$\begin{aligned}\dot{\hat{x}}(t) &= f(\hat{x}(t), u(t)) + K(y(t) - \hat{y}(t)), \hat{x}(t=0) = \hat{x}_0 \\ \hat{y}(t) &= g(\hat{x}(t), u(t))\end{aligned}\tag{4.2}$$

$\hat{x}(t)$ is the state vector of estimator and K is the gain matrix. A state estimator should satisfy the following properties

- **Simulation property:** For the same initial condition $x(t_0) = \hat{x}_0$ of the estimator and the system to be observed, then it holds that $x(t) = \hat{x}(t) \forall t > 0$.
- **Convergence property:** If $x(t_0) \neq \hat{x}_0$, then $x(t) - \hat{x}(t)$ tends to zero as $t \rightarrow \infty$

The different approaches for state estimator design differs in the calculation of gain matrix K in Equation 4.2.

4.1 Kalman Filter

Kalman filter is a statistical state estimation algorithm which gives the optimal estimate of states from the noisy measurements.

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Hiermit bestätige ich, die vorliegende Diplomarbeit selbständig und nur unter Zuhilfenahme der angegebenen Literatur verfasst zu haben.

Ich bin damit einverstanden, dass Exemplare dieser Arbeit in den Bibliotheken der Universität Dortmund ausgestellt werden.

Dortmund, den July 19, 2013

Name