

NATIONAL UNIVERSITY OF SINGAPORE

SCHOOL OF COMPUTING  
FINAL ASSESSMENT FOR  
Semester 2 AY2017/2018

CS2030 Programming Methodology II

May 2018

Time Allowed 2 Hours

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INSTRUCTIONS TO CANDIDATES

1. This assessment paper contains 17 questions and comprises 16 printed pages, including this page.
2. Write all your answers in the answer sheet provided.
3. The total marks for this assessment is 70. Answer **ALL** questions.
4. This is an **OPEN BOOK** assessment.
5. All questions in this assessment paper use Java 9 unless specified otherwise.
6. State any additional assumption that you make.
7. Please write your student number only. Do not write your name.

## Part I

## Multiple Choice Questions (36 points)

- For each of the questions below, **write your answer in the corresponding answer box on the answer sheet**. Each question is worth 3 points.

Questions 1 and 2 are based on the following scenario. Consider an object-oriented program written for the game of chess. A game consists of a chess board and multiple chess pieces moving on the chess board. There are six types of chess pieces: king, queen, bishop, rook, knight, and pawn. Each type of chess piece is drawn differently on the screen and each moves on the chess board in a different way. The chess board consists of multiple cells and each cell either contains a chess piece or is empty. There are two players for each game, and each chess piece belongs to either one of the players.

You created the following classes: ChessBoard, ChessPiece, King, Queen, Bishop, Knight, Rook, Pawn, Cell, and Player to model the corresponding nouns in the above description.

1. (3 points) Which of the following decision to model the chess game is the LEAST appropriate?
- A. Subclasses of ChessPiece override the draw method in ChessPiece.
  - B. Subclasses of ChessPiece override the move method in ChessPiece.
  - C. Cell contains a field of type Optional<ChessPiece>.
  - ☒ D. ChessPiece inherits from Player.
  - E. ChessPiece is an abstract class.

Write X in the answer box if all of the choices above are equally appropriate.

2. (3 points) We model King, Queen, Bishop, Knight, Rook, and Pawn as subclasses of ChessPiece. Let's say that we want to keep the pieces belong to one player in a List<...> called pieces. We want to be able to write code like the follows:

```
pieces.add(new Queen());  
ChessPiece p = pieces.remove();
```

What should the type of the variable pieces be?

- A. List<>
- B. List<?>
- ☒ C. List<ChessPiece>
- D. List<? super ChessPiece>
- E. List<? extends ChessPiece>
- F. List<King, Queen, Bishop, Knight, Rook, Pawn>

Write X in the answer box if none of the choices above is correct.

3. (3 points) Consider the code below:

```
class A {  
    static int x;  
  
    static int foo() {  
        return 0;  
    }  
  
    int bar() {  
        return 1;  
    }  
  
    static class B {  
    }  
  
    public static void main(String[] args) {  
        :  
    }  
}
```

Which of the following line of code, when called from main, would result in a compilation ERROR?

- A. x = 1; ✓
- B. A a = new A(); ✓
- C. B b = new B(); ✓
- D. new A().foo(); ✓
- E. new A().bar(); ✓

Write X in the answer box if none of the choices above would lead to a compilation error. X

4. (3 points) Which of the following process happens ONLY during compilation time in Java?

- (i) type inference – inferring the type of a variable whose type is not specified.
- (ii) type erasure – replacing a type parameter of generics with either Object or its bound.
- (iii) type checking – checking if the value matches the type of the variable it is assigned to.

- A. Only (i)
- B. Only (i) and (ii)
- C. Only (i) and (iii)
- D. Only (ii) and (iii)
- E. (i), (ii), and (iii)

Write X in the answer box if none of the combinations is correct.

5. (3 points) Which of the following process happens ONLY during runtime in Java?

- (i) late binding – determine which instance method to call depending on the type of a reference object.
- (ii) type casting – converting the type of one variable to another.
- (iii) accessibility checking – checking if a class has an access to a field in another class.

- A. Only (i)
- B. Only (ii)
- C. Only (i) and (iii)
- D. Only (ii) and (iii)
- E. (i), (ii), and (iii)

Write X in the answer box if none of the combinations is correct.

6. (3 points) Suppose we have two classes Shape and Circle. Circle is a subclass of Shape. Recall that Double is a subclass of Number.

We declare the following variables:

```
Function<Shape, Double> s2d;  
Function<Circle, Number> c2n;  
Function<Object, Object> o2o;
```

Which of the following assignment would result in a compilation error?

- (i) s2d = c2n; ■
- (ii) o2o = c2n;
- (iii) c2n = o2o; ■

- A. Only (i)
- B. Only (ii)
- C. Only (i) and (iii)
- D. Only (ii) and (iii)
- E. (i), (ii), and (iii)**

Write X in the answer box if none of the combinations is correct.

7. (3 points) Suppose we have a class A that implements the following methods:

```
class A {
    int x;
    boolean isPositive;

    static A of(int x) {
        A a = new A();
        a.x = x;
        a.isPositive = (x >= 0);
        return a;
    }

    A foo(Function<Integer, A> map) {
        return map.apply(this.x);
    }

    A bar(Function<Integer, A> map) {
        if (this.isPositive) {
            return map.apply(this.x);
        } else {
            return A.of(this.x);
        }
    }
}
```

Which of the following conditions hold for A for all values of x. f and g are both variables of type Function<Integer, A>; a is an object of type A.

- (i) A.of(x).foo(f) always returns f.apply(x) ✓
- (ii) a.foo(f).bar(g) equals to a.foo(x -> f.apply(x)).bar(g) ✓
- (iii) a.bar(f).bar(g) equals to a.bar(x -> f.apply(x)).bar(g) ✓

- A. Only (i)
- B. Only (ii)
- C. Only (i) and (iii)
- D. Only (ii) and (iii)
- ☒ E. (i), (ii), and (iii)

Write X in the answer box if none of the combinations is correct.



8. (3 points) Consider the following two statements:

```
Stream.of(20, 40, 60, 80, 100, 120, 140)
    .reduce(100, (x, y) -> Math.max(x, y)); // Statement X
```

```
Stream.of(20, 40, 60, 80, 100, 120, 140)
    .parallel()
    .reduce(100, (x, y) -> Math.max(x, y)); // Statement Y
```

Which of the following about Statement X and Statement Y above is CORRECT:

- A. Statement X may produce a different answer than Statement Y.
- ☒ B. Statement Y always returns the same value every time it is executed.
- C. Statement X returns 100.
- D. Statement X returns 20.
- E. Statement Y always runs faster than Statement X because the reduce operation is executed in parallel.

Write X in the answer box if none of the choices is correct.

9. (3 points) Wei Tsang tried to demonstrate to the class that parallelizing code with side effects will lead to an undeterministic result. He wrote the following method:

```
void foo() {
    int sum = 0;
    Stream.of(1, 2, 3, 4, 5)
        .parallel()
        .forEach(i -> {
            sum = sum + i;    // Line 6
        });
    System.out.println(sum); // Line 8
}
```

This is not a good demonstration, because:

- A. foo always prints 15 since forEach will be executed sequentially.
- B. foo always prints 15 since the lambda expression passed to forEach has no side effect.
- ☒ C. foo will not compile because Java expects sum to be either final or effectively final.
- D. foo always prints 0 since, due to variable capture, there are two copies of sum now, and the captured version of sum is being incremented in Line 6.
- E. foo may print different results every time foo is invoked, but not due to side effects. The reason is that System.out.println on Line 8 is invoked in parallel with the code on Line 6. The code should call join() to wait for all the elements in the stream to be added to sum before printing.

Write X in the answer box if none of the choices is correct.

10. (3 points) Consider the following RecursiveTask called BinSearch for finding an item within a sorted array using binary search.

```
class BinSearch extends RecursiveTask<Boolean> {  
    int low;  
    int high;  
    int toFind;  
    int[] array;  
  
    BinSearch(int low, int high, int toFind, int[] array) {  
        this.low = low;  
        this.high = high;  
        this.toFind = toFind;  
        this.array = array;  
    }  
  
    protected Boolean compute() {  
        if (high - low <= 1) {  
            return array[low] == toFind;  
        }  
  
        int middle = (low + high)/2;  
        if (array[middle] > toFind) {  
            BinSearch left = new BinSearch(low, middle, toFind, array);  
            left.fork(); return left.join(); // Line X  
        } else {  
            BinSearch right = new BinSearch(middle, high, toFind, array);  
            return right.compute();  
        }  
    }  
}
```

For example,

```
int[] array = {1, 2, 3, 4, 6};  
new BinSearch(0, array.length, 3, array).compute(); // return true  
new BinSearch(0, array.length, 5, array).compute(); // return false
```

Assuming that we have a large number of parallel processors in the system and we never run into stack overflow, which of the following statement(s) about how BinSearch works is CORRECT?

- (i) If we replace  
`left.fork(); return left.join();`  
on Line X with  
`return left.compute();`  
the search will likely run faster.
  - (ii) If we swap the order of `fork()` and `join()`, i.e., replace  
`left.fork(); return left.join();`  
with  
`left.join(); return left.fork();`  
the search will likely run faster.
  - (iii) Searching for the largest element in the input array will likely be faster than searching for the smallest element in the input array.
- A. Only (i)
  - B. Only (ii)
  - C. Only (i) and (iii)
  - D. Only (ii) and (iii)
  - E. (i), (ii), and (iii)

Write X in the answer box if none of the combinations is correct.



Questions 11 and 12 are based on the following asynchronous code:

```
CompletableFuture<A> cf1;  
CompletableFuture<B> cf2;  
  
cf1 = CompletableFuture.supplyAsync(() -> foo());  
cf2 = cf1.thenApplyAsync(x -> bar(x));  
  
B b = cf2.thenCombineAsync(  
    cf1.thenApplyAsync(x -> thud(x)),  
    (x, y) -> grunt(x, y))  
    .join();
```

None of the methods in this question has wildcard / bounded wildcard as the type of the arguments. Every method invoked in the lambda expressions above is a pure function. The code compiles without any errors.

The relevant `CompletableFuture<T>` methods are (we removed the bounded wildcards for clarity):

**static <U> CompletableFuture<U> supplyAsync(Supplier<U> supplier)**

Returns a new `CompletableFuture` that is asynchronously completed with the value obtained by calling the given `Supplier`.

**<U> CompletableFuture<U> thenApplyAsync(Function<T, U> fn)**

When the calling `CompletableFuture` completes normally, apply the given function `fn` to the result of the calling `CompletableFuture` asynchronously. It returns a new `CompletableFuture<U>` that encapsulates the result of `fn`.

**<U,V> CompletableFuture<V> thenCombineAsync(CompletableFuture<U> other, BiFunction<T, U, V> fn)**

When the calling `CompletableFuture` and `other` both complete normally, apply the given `BiFunction` to the results of these two `CompletableFuture` asynchronously. It returns a new `CompletableFuture<V>` that encapsulates the result of `fn`.

11. (3 points) Which of the following statements is CORRECT about the value of `b` after executing the above sequence?

- ☒ A. The value of `b` is equivalent to the value obtained by invoking  
`b = grunt(bar(foo()), thud(foo()))`  
synchronously.
- B. The value of `b` is equivalent to the value obtained by invoking  
`b = grunt(thud(foo()), bar(foo()))`  
synchronously.
- C. The value of `b` is equivalent to the value obtained by invoking  
`b = grunt(thud(bar(foo()), foo()))`  
synchronously.
- D. The value of `b` is undeterministic because the order of executing `bar` and `thud` is undeterministic.
- E. The variable `b` is uninitialized since `CompletableFutures cf1` and `cf2` are not joined.

Write X in the answer box if none of the choices is correct.

12. (3 points) Which of the following statement about the code above is INCORRECT?

- A. `bar` must return a value of type `B`. ■
- B. `grunt` must return a value of type `B`. ■
- ☒ C. The argument `x` to `thud` must have the type `B`.
- D. The first argument `x` to `grunt` must have the type `B`. ■
- E. The return type of `thud` is the same as the type of the second argument `y` to `grunt`. ■

Write X in the answer box if none of the choices is correct.

## Part II

## Short Questions (34 points)

Answer all questions in the space provided on the answer sheet. Be succinct and write neatly.

13. (6 points) **Curry.**

The interface `TriFunction<S, T, U, R>` is a functional interface for a function that takes in three arguments, of types `S`, `T`, and `U` respectively, and returns a result of type `R`.

```
interface TriFunction<S, T, U, R> {
    R apply(S s, T t, U u);
}
```

Suppose we want to write a method `curry` that takes in a `TriFunction` and returns a curried version of the method.

```
.. curry(TriFunction<S, T, U, R> lambda) {
    // missing line
}
```

For instance, calling `curry` on

```
(x, y, z) -> x + y * z
```

returns

```
x -> y -> z -> x + y * z.
```

(a) (3 points) What should the return type of `curry` be? `Function<S, Function<T, Function<U, R>>>`

(b) (3 points) Write the body of the method `curry`. `return x -> y -> z -> lamda.apply(x, y, z);`

14. (3 points) **Compose.**

Write a method `compose` that returns a composition of a `Predicate<R>` with `Function<T, R>`. The returned function is a `Predicate<T>` that tests if the result of applying the given `Function<T, R>` matches the condition of the given `Predicate<R>`.

```
Predicate<T> compose(Function<T, R> f, Predicate<R> p) {
    // missing line    return x -> p.test(f.apply(x));
}
```

For example:

```
Predicate<String> predicate = compose(str -> str.length(), x -> x < 4);
```

```
Stream.of("I", "don't", "like", "green", "eggs", "and", "ham")
    .filter(predicate)
    .toArray();
```

returns the array with `["I", "and", "ham"]`.

Fill in the body of the method `compose`.

Recall that to evaluate a `Predicate p` on an input `x`, we call `p.test(x)`.

15. (6 points) **Substream.**

We say that a Stream *s* is a *substream* of another Stream *t*, if every element in *s* is contained in *t*. For example, a stream created with `Stream.of(0, 0, 1, 2)` is a substream of the infinite stream created with `Stream.iterate(0, i -> i + 1)`.

The method `isSubstream` below returns `true` if *s* is a substream of *t* and `false` otherwise.

```
static <T> boolean isSubstream(Stream<T> s, Stream<T> t) {
    // missing line return s.allMatch(sElement -> t.anyMatch(tElement -> sElement.equals(tElement)));
}                                     // this is a wrong answer, t can only be scanned once -> cause IllegalStateException
```

(a) (3 points) Complete the body of the method `isSubstream`.

The following methods of `Stream<T>` are helpful (you may not need to use all):

**boolean allMatch(Predicate<? super T> predicate)**

Returns whether all elements of this stream match the provided predicate.

**boolean anyMatch(Predicate<? super T> predicate)**

Returns whether any elements of this stream match the provided predicate.

**boolean noneMatch(Predicate<? super T> predicate)**

Returns whether no elements of this stream match the provided predicate.

**Stream<T> filter(Predicate<? super T> predicate)**

Returns a stream consisting of the elements of this stream that match the given predicate.

**long count()**

Returns the count of elements in this stream.

(b) (3 points) The method `isSubstream` above requires that both arguments must be streams containing the same type *T*. Suppose that we want to relax this constraint so that the type *s* is a subtype of the type of *t*. Rewrite the method signature for `isSubstream` to make it so.

```
static <T> boolean isSubstream(Stream<? extends T> s, Stream<T> t)
```

16. (13 points) **Undoable**.

In this question, we are going to implement a class `Undoable`<sup>1</sup> that encapsulates a value that can be transformed with `flatMap` and can be restored to its previous state with the method `undo`.

Internally, an `Undoable<T>` object maintains a value of type `T` and a `LinkedList<Object>` storing a history of past values. When we apply a given function to the value, we also append the current value to the end of the history list. When we undo, we remove the last value from the history list, and replace the current value with this last value.

`Undoable<T>` is a monad – we can chain together different operations on an `Undoable` object using `flatMap`, and create a new `Undoable` object with an empty history using `of`.

For example, the following expression finds the length of the string "hello" and half its value:

```
Undoable<Double> d = Undoable.of("hello")
    .flatMap(s -> length(s))
    .flatMap(i -> half(i));
```

The `Undoable<Double>` object `d` now holds the value 2.5 and has a history list containing objects "hello" and 5, in that order.

Calling

```
Undoable<Integer> i = d.undo();
```

yields a new `Undoable<Integer>` object which holds the value 5 and has a history list containing object "hello". Calling

```
Undoable<String> s = i.undo();
```

gives a new `Undoable<String>` object which holds the value "hello" and has an empty history. Calling `s.undo()` would lead to an unchecked exception `CannotUndoException` being thrown.

Part of the class `Undoable` has been provided for you. We omit the `import` statements for brevity. The following methods provided by `LinkedList<E>` could be useful:

**LinkedList()**

Constructs an empty list.

**LinkedList(Collection<? extends E> c)**

Constructs a list containing the elements of the specified collection, in the order they are returned by the collection's iterator.

**boolean add(E e)**

Appends the specified element to the end of this list.

**boolean addAll(Collection<? extends E> c)**

Appends all of the elements in the specified collection to the end of this list, in the order that they are returned by the specified collection's iterator.

**E removeLast()**

Removes and returns the last element from this list. Throws `NoSuchElementException` if this list is empty.

---

<sup>1</sup>UNDO-able, not UN-doable.



```

class CannotUndoException extends RuntimeException {
}

class Undoable<T> {
    T value;
    Deque<Object> history;

    Undoable(T t, Deque<Object> history) {
        this.value = t;
        this.history = history;
    }

    static <T> Undoable<T> of(T t) {
        return new Undoable<T>(t, new LinkedList<Object>());
    }

    public <R> Undoable<R> flatMap(Function<T, Undoable<R>> mapper) {
        // fill in the blank
        Dequeue<Object> newHistory = new LinkedList<Object>(this.history);
        Undoable<R> newUndoable = mapper.apply(value);
        newHistory.addAll(newUndoable.history);
        return new Undoable(newUndoable.value, newHistory);
    }

    public <R> Undoable<R> undo() {
        Deque<Object> newHistory = new LinkedList<>(this.history);
        R r;
        try {
            r = (R)newHistory.removeLast(); // Line A
        } catch (NoSuchElementException e) {
            // Missing line B
            throw new CannotUndoException();
        }
        return new Undoable<R>(r, newHistory);
    }
}

```

- (a) (3 points) Fill in the body of the method `length` below. This method takes in a `String str` and returns an `Undoable<Integer>` containing the length of the string `str`.

```

Undoable<Integer> length(String str) {
    : Dequeue<Object> history = new LinkedList<>();
    history.add(str);
    return new Undoable<Integer>(str.length(), str);
}

```

- (b) (3 points) Complete the body for method `flatMap`.
- (c) (3 points) Explain why Line A would lead to a compiler warning of unchecked cast.
- (d) (3 points) Let's say that we leave Line A as it is and ignore the compilation warning. What would happen if we do the following? Explain.

```

Undoable<Integer> i = Undoable.of("hello").flatMap(s -> length(s));
Undoable<Double> d = i.undo();

```

- (e) (1 point) The missing Line B should throw a `CannotUndoException`. Fill in this missing line.



17. (6 points) **LazyList**.

The class `LazyList` defines a possibly infinite list using lazy evaluation. It is a simpler version of `InfiniteList` you see in class – it does not cache the computed head / tail and supports only `iterate`, `empty`, `isEmpty`, `map`, `concat`, and `forEach` operation. The definition of `empty` and `isEmpty` methods are omitted for brevity. The `iterate` method is slightly different, as it supports a condition to stop iterating.

```
class LazyList<T> {
    private Supplier<T> head;
    private Supplier<LazyList<T>> tail;

    public LazyList(Supplier<T> head, Supplier<LazyList<T>> tail) {
        this.head = head;
        this.tail = tail;
    }

    public static <T> LazyList<T> iterate(T init, Predicate<T> cond,
        UnaryOperator<T> op) {
        if (!cond.test(init)) {
            return LazyList.empty();
        } else {
            return new LazyList<T>(
                () -> init,
                () -> iterate(op.apply(init), cond, op));
        }
    }

    public <R> LazyList<R> map(Function<T, R> mapper) {
        return new LazyList<R>(
            () -> mapper.apply(head.get()),
            () -> tail.get().map(mapper));
    }

    public T forEach(Consumer<T> consumer) {
        LazyList<T> list = this;
        while (!list.isEmpty()) {
            consumer.accept(list.head.get());
            list = list.tail.get();
        }
    }

    :
}
```

- (a) (3 points) Suppose we call `fgce fgce`  
`InfiniteList.iterate(0, i -> i < 2, i -> i + 1).map(f).map(g).forEach(c)`  
 where `f` and `g` are lambda expressions of type `Function` and `c` is a lambda expression of type `Consumer`. Let `e` be the lambda expression `i -> i + 1` passed to `iterate`.  
 Write down the sequence of which the lambda expressions `e`, `f`, `g`, and `c` are evaluated.

- (b) (3 points) The method `concat` takes in two `LazyList` objects, `l1` and `l2`, and creates a new `LazyList` whose elements are all the elements of the first list `l1` followed by all the elements of the second list `l2`. The elements in newly concatenated list must be lazily evaluated as well.  
 For example, in

```
LazyList<Integer> l1 = LazyList.iterate(0, i -> i < 2, i -> i + 1);
LazyList<Integer> l2 = LazyList.iterate(5, i -> i < 8, i -> i + 2);
LazyList<Integer> l3 = LazyList.concat(l1, l2);
l3.forEach(x -> System.out.print(x));
```

Note that, being a lazily evaluated list, nothing is evaluated when `l3` is created. Thus, `concat` should not result in an infinite loop if the list `l1` is infinitely long. The elements are only evaluated when terminal operator `forEach` is called. In the example above, 0157 will be printed.  
 Complete the body of the method `concat`.

```
static <T> LazyList<T> concat(LazyList<T> l1, LazyList<T> l2) {
    if (l1.isEmpty()) {
        return l2;
    } else {
        return new LazyList<>() {
            head = l1.head;
            tail = () -> LazyList.concat(l1.tail.get(), l2);
        };
    }
}
```

END OF PAPER