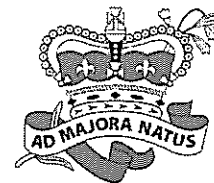


St Aloysius' College
Year 9 5.3 Term I Mathematics Assessment
18th March 2016



Time allowed: 40 minutes

Total Marks: 44

NAME: SOLUTIONS.
TEACHER: GON KAU FDE MLM

Instructions:

- Approved calculators may be used.
- All necessary working is to be shown for Part C.
- Marks may be deducted for careless or poorly arranged work.

PART A: Multiple Choice Questions:

5 marks

For questions 1 – 5, circle the correct answer, A, B, C or D.

1. Which of these decimals could be rounded to 34.71?

(A) 34.715 (B) 34.707 (C) 34.7 (D) 34.7039

2. Expand and simplify $3(5 - 2p) - 2(4p - 3)$

(A) $21 - 14p$ (B) $9 - 14p$ (C) $14p - 21$ (D) $12 - 10p$

3. Tobias invests \$4,500 in an account paying 5.2% p.a. simple interest over a period of 3 years.

What amount would Richard be able to withdraw from his account at the end of the 3 years?

(A) \$156 (B) \$702 (C) \$4,656 (D) \$5,202

4. Luke earns \$3,998.40 per month. How much is this per week?

(A) \$888.53 (B) \$919.52 (C) \$922.70 (D) \$999.60

5. Solve $3 - 2x \leq 11$

(A) $x \leq -7$ (B) $x \geq -7$ (C) $x \leq -4$ (D) $x \geq -4$

PART B:**Short Answer Questions:** 10 questions. All questions are worth one mark.**10 marks**

Give your answer only in the right-hand column.

Working out may be shown in the left-hand column.

	Answer
1. Round off 0.025376 to 3 significant figures.	0.0254
2. Solve for m : $4m - 17 = 45$ $4m = 62$	15.5
3. A digital camera was purchased for \$423.50, after a GST of 10% was added to the original price. How much was the GST paid? $110\% = \$423.50$ $1\% = \$3.85$	\$38.50
4. James bought an item for \$680, and later sold it for \$986. What was his percentage profit? $\frac{306}{680} \times 100$	45%
5. Simplify: $\frac{32a^7b^4}{40a^2b^6} =$	$\frac{4a^5}{5b^2}$
6. If 5 bottles of soft drink cost \$C, write an algebraic expression for the cost of m bottles of soft drink.	$\frac{\$Cm}{5}$
7. The population of a country town is decreasing at an annual rate of 6%. If its current population is 36 000, what will its population be in 10 years time? Give answer to the nearest whole number. $A = 36000(1 - 0.06^{10})$	\$19,390

8. Using the tax table below, determine the tax payable on a taxable income of \$93,000.

Taxable Income	Tax Payable
\$0 – \$18,200	NIL
\$18,201 – \$37,000	19 cents for each \$1 over \$18,200
\$37,001 – \$80,000	\$3,572 plus 32 cents for each \$1 over \$37,000
\$80,001 – \$180,000	\$17,547 plus 37 cents for each \$1 over \$80,000
\$180,001 and over	\$54,547 plus 45 cents for each \$1 over \$180,000

$$\text{Tax payable} = \{(93,000 - 80,000) \times 0.37\} + 17,547$$

\$22,357

9. The time taken for one complete swing of a pendulum is given by $T = \frac{1}{5}\sqrt{L}$ where L is the length of the pendulum, in cm, and T is the time in seconds. If the time of the swing is 2 seconds, find the length of the pendulum, L in cm.

$$2 = \frac{1}{5}\sqrt{L}$$

$$10 = \sqrt{L}$$

$$L = 100$$

100 cm

10. Dominic, a car salesman works on a commission basis. He is given a retainer of \$400 per week, plus 2% of the selling price of a car. If in one week he sells a car for \$48 000, what is his gross wage for that week?

$$\text{Wage} = 400 + (0.02 \times 48,000)$$

\$1,360

PART C:

NAME: SOLUTIONS
TEACHER: GON KAU FDE MLM



Free Response Questions:

All necessary working is to be shown for Part C.

29 marks

1. Connor's gross income last year was \$72,000. He had allowable tax deductions of \$5,000. Connor paid 1.5% of his taxable income for the Medicare Levy.

How much was Connor's Medicare Levy?

$$ML = \frac{1.5}{100} \times 67000$$
$$= \$1005$$

$$TI = 72,000 - 5000$$
$$= 67,000$$

1

2. Solve for p : $18 - \frac{4p}{5} = .32$

$$-\frac{4p}{5} = 14$$

$$-4p = 70$$

$$p = -\frac{70}{4} \text{ or } -17.5$$

2

3. Josh earned \$1440 in a week.
He worked 28 hours during normal working hours, Monday to Friday.
He also worked 6 hours on Saturday at time-and-a-half, plus 4 hours on Sunday at double-time. Calculate his hourly rate of pay.

$$\text{Time worked} = 28 + (6 \times 1.5) + (4 \times 2)$$
$$= 45 \text{ h}$$

$$\text{Rate pay} = \frac{1440}{45} = \$32/\text{h}$$

2

4. Tomas invests \$24 000 and earns \$9 000 simple interest in 6 years.
Calculate the simple interest rate, giving answer to two decimal places.

$$I = PRN$$

$$9000 = 24000 \times R \times 6$$

$$R = 6.25\%$$

2

5. Solve: $15 - 4(2x - 7) = 19 - 5x$

$$15 - 8x + 28 = 19 - 5x$$

$$43 - 8x = 19 - 5x$$

$$24 = 3x$$

$$x = 8$$

2

6. Josh invests \$38 000 for 6 years, at 9% p.a. interest, the amount compounded monthly.
What is the balance in the account at the end of 6 years?

$$A = 38000 \times 1.0075^{6 \times 12}$$

$$n = 6 \times 12 = 72$$

$$r = \frac{0.09}{12} = 0.0075$$

$$= \$65077$$

2

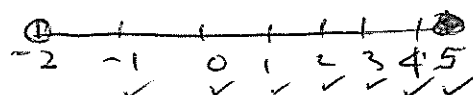
7. How many *integers* satisfy BOTH of the given inequations?

$$11 - 3x \geq -4 \quad \text{and} \quad 4x - 15 > -23$$

$$-3x \geq -15 \quad 4x > -8$$

$$x \leq 5 \quad x > -2$$

3



$\therefore 7$

8. When Nicholas used the tax table shown below, to calculate his income tax payable.

Taxable Income	Tax Payable
\$0 – \$6 000	NIL
\$6 001 – \$30 000	NIL plus 15 cents for each \$1 over \$6 000
\$30 001 – \$75 000	\$3 600 plus 30 cents for each \$1 over \$30 000
\$75 001 – \$150 000	A plus 40 cents for each \$1 over \$75 000
\$150 001 and over	\$47 100 plus 45 cents for each \$1 over \$150 000

- (i) After Nicholas did all his calculations, he calculated his tax payable to be \$12 225. What was his taxable income?

$$12225 = \{(x - 30,000) \times 0.30\} + 3600$$

$$8625 = 0.3x - 9000$$

$$17625 = 0.3x$$

$$x = \$58750$$

$$\therefore TI = \$58750$$

- (ii) From the Tax Scale table above, calculate the value of A.

$$\begin{aligned}
 A &= \{(75,000 - 30,000) \times 0.3\} + 3600 \\
 &= \$13500 + 3600 \\
 &= \$17,100
 \end{aligned}$$

9. A formula is given by $p = \frac{m-n}{mn-1}$. Make m the subject.

$$p(mn-1) = m-n$$

$$pmn - p = m - n$$

$$pmn - m = p - n$$

$$m(pn-1) = p-n$$

$$m = \frac{p-n}{pn-1}$$

10. A certain amount of money is invested at 9% p.a. interest, with the interest compounded yearly. How many years will it take for the original amount to grow to three times its original amount? Give answer to the nearest whole year.

$$3P = P(1.09)^n$$

$$3 = 1.09^n$$

$$1.09^{12} = 2.81$$

$$1.09^{13} = 3.06$$

\therefore 13 years

11. Using the elimination method, solve the two equations below simultaneously, obtaining the values of x and y .

$$\begin{array}{rcl} 5x - 2y = 8 & \text{---} & \textcircled{1} \\ 7x - 8y = -20 & \text{---} & \textcircled{2} \end{array}$$

$$\textcircled{1} \times 4$$

$$\begin{array}{rcl} 20x - 8y = 32 & \text{---} & \textcircled{3} \\ 7x - 8y = -20 & \text{---} & \textcircled{2} \\ \hline \textcircled{3} - \textcircled{2} & & \end{array}$$

$$13x = 52$$

$$x = 4$$

\therefore Sub $x = 4$ in $\textcircled{1}$

$$5(4) - 2y = 8$$

$$20 - 2y = 8$$

$$-2y = -12$$

$$y = 6$$

12. The sum of three consecutive odd numbers is 23 more than the sum of the even numbers that lie between them.

(i) By using the pronumeral x , form an equation showing the above relationship.

$$2x + 1 + 2x + 3 + 2x + 5 = 2x + 2 + 2x + 4 + 23$$

(ii) Solve the equation from part (i), to find the three consecutive numbers.

$$2x = 20$$

$$x = 10$$

2

\therefore Numbers are 21, 23 and 25.

-
13. At a local fruit shop, apples are sold at 24c each, and pears are sold at 28c each. Christopher bought 8 more pears than apples, and paid the fruiterer \$3.80. How many apples and pears did Christopher purchase?

$$a = 0.24$$

$$p = 0.28$$

Let

$x = \text{no of apples.}$

$$a + p = 3.80$$

$$0.24x + 8 + x(0.28) = 3.80$$

3

$$0.24x + 2.24 + 0.28x = 3.80$$

$$0.52x = 1.56$$

$$x = 3$$

\therefore 3 apples, 11 pears.

End of Assessment