MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 3 - DECEMBER 2007 SOLUTION KEY

Team Round - continued

E)
$$\frac{85+W}{132+W+L} \ge 0.700$$
 (rounded to 3 dec. pl.)

$$850 + 10W \ge 924 + 7W + 7L \rightarrow L \le \frac{3W - 74}{7}$$

The minimum value of W is determined by letting L = 0.

$$\frac{85 + W}{132 + W} \ge 0.700 \implies 3W > 74 \implies W \ge 25$$

There are a maximum of 30 games remaining in the schedule.

The ordered pair (25, 0) works (0.701), as well as (W, 0) for $26 \le W \le 30 \rightarrow 6$ pairs

(26,1) fails (0.698)

(27,1) passes (0.700), as do (28, 1) and (29, 1)

(27, 2) fails (0.696)

(28, 2) fails (0.6975)

Thus, there are **9** pairs.

F)
$$DC = 60, EC = 36$$

$$\triangle DEC$$
 is a right triangle \rightarrow (36, ?, 60) = 12(3, x, 5)

$$\Rightarrow x = 4 \Rightarrow DE = 48$$

$$Area(\Delta DEC) = \frac{1}{2} \cdot 36 \cdot 48 = \frac{1}{2} \cdot 60 \cdot NE \Rightarrow NE = \frac{144}{5}$$

In right
$$\triangle NEC$$
, $(EN, NC, EC) = \left(\frac{144}{5}, ?, 36\right)$

$$=\frac{1}{5}(144,?,180)=\frac{36}{5}(4,x,5)$$

$$x = 3 \rightarrow NC = \frac{108}{5}$$

Since *MENC* is a kite, its perimeter is
$$2\left(\frac{144+108}{5}\right) = \frac{504}{5}$$
 or 100.8