

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 1 - OCTOBER 2014 SOLUTION KEY**

**Round 3**

- A) The cost per pound of the beans is \$1.60, while the corn costs \$.90 per pound.

Let  $x$  denote the # pounds of beans needed. Then:

$$1.60x + 0.90(30) = 1.10(30 + x) \Rightarrow 160x + 2700 = 3300 + 110x \Rightarrow 50x = 600 \Rightarrow x = \underline{12}$$

- B) For  $x = k$ ,  $y = 3k + 2$

$$\text{For } x = k + 3, y = 3(k + 3) + 2 = 3k + 11$$

$$\text{Thus, } 3k + 11 = 2(3k + 2) + 1 \Rightarrow 3k = 6 \Rightarrow k = \underline{2}$$

Check: For  $x = 2$ ,  $y = 8$ . For  $x = 5$ ,  $y = 17$ . ( $17 = 2 \cdot 8 + 1$ )

- C)  $3X + 7Y = 92 \Rightarrow X = \frac{92 - 7Y}{3} = 30 - 2Y + \frac{2 - Y}{3}$  Clearly, our choices for  $Y$  are restricted to 2,

5, 8, 11 ..., so that the last term is an integer. Thus, we have ordered pairs  $(X, Y) = (26, 2)$ ,  $(19, 5)$ ,  $(12, 8)$ ,  $(5, 11)$ .

Note that since the slope of the line  $3X + 7Y = 92$  is  $\frac{-3}{7}$  or  $\frac{3}{-7}$ , as  $X$  decreases by 7,  $Y$  increases by 3.

Therefore, we look no further. (The next ordered pair would be  $(-2, 14)$ .)

Since  $X + Y < 25$ , the possible ordered pairs are (19, 5), (12, 8) and (5, 11).