

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 5 – FEBRUARY 2007
ROUND 3 TRIG: IDENTITIES AND/OR INVERSE FUNCTIONS

ANSWERS

A) _____

B) _____

C) _____

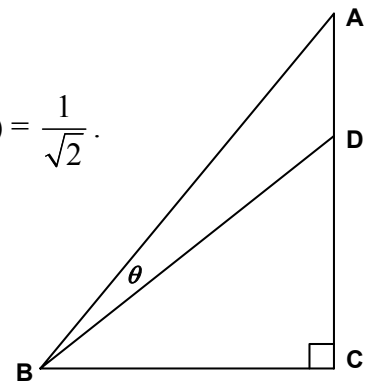
A) Given $A = \sin^{-1}\left(\frac{35}{37}\right)$, $B = \cos^{-1}\left(-\frac{15}{17}\right)$

Find $\sin(A + B)$ as a simplified fraction.

B) In right $\triangle ABC$, $m\angle C = 90^\circ$, $m\angle DBC = 45^\circ$, $AB = 1 + \sqrt{2}$ and $\tan(\theta) = \frac{1}{\sqrt{2}}$.

Determine BC in simplified radical form.

Hint: $BC = AB\cos(\angle ABC)$



C) Let $\theta = \arccos\left(\frac{1}{2x+1}\right)$, where $x > 0$. Express the fraction $\frac{x^2 + x}{2x + 1}$ as a single simplified fraction in terms of $\cos(\theta)$.