

**MASSACHUSETTS MATHEMATICS LEAGUE**  
**CONTEST 3 - DECEMBER 2010**  
**ROUND 7 TEAM QUESTIONS**  
**ANSWERS**

- A) \_\_\_\_\_ D) \_\_\_\_\_
- B) \_\_\_\_\_ E) ( \_\_\_\_\_ , \_\_\_\_\_ , \_\_\_\_\_ )
- C) \_\_\_\_\_ F) ( \_\_\_\_\_ , \_\_\_\_\_ )

**\*\*\*\* NO CALCULATORS ON THIS ROUND \*\*\*\***

- A) In  $\triangle ABC$ ,  $AB = 10$ ,  $AC = 12$  and  $m\angle B = 2m\angle A$ .  
 If  $A$  is the smallest angle in  $\triangle ABC$ , compute  $BC$ .

- B) Using the letters, arrange the following in order from largest to smallest.

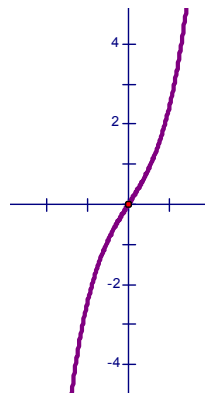
$$A = (16,874,535)^{5000} g(16,874,537)^{5000}$$

$$B = (16,874,533)^{5000} g(16,874,539)^{5000}$$

$$C = (16,874,536)^{5000} g(16,874,536)^{5000}$$

$$D = (16,874,534)^{5000} g(16,874,538)^{5000}$$

- C) Three vertices of rectangle  $PQRS$  are  $P(-8, -1)$ ,  $Q(k, k)$  and  $R(14, 2)$ .  
 Determine all possible coordinates  $(x, y)$  of vertex  $S$ .



- D) The graph of  $y = \frac{5^x - 5^{-x}}{2}$  is shown at the right.

Solve for  $x$  in terms of  $y$ .

- E) My son, his daughter (my granddaughter) and I have the same birthday! I was 21 when my son was born. On our next birthday, our combined ages will total 100 years, and when my granddaughter turns 25, the ratio of my age to my son's age will be 3 : 2.  
 Compute the ordered triple  $(g, s, f)$ , where  $g, s$  and  $f$  denote the ages of granddaughter, son and father respectively on our next birthday.

- F) Eight points lie on a circle and form the vertices of an octagon. Let  $M$  and  $m$  denote the maximum and minimum number of interior points of intersection of the diagonals respectively, i.e. excluding the vertices of the octagon. Determine the ordered pair  $(M, m)$ .  
 The diagram at the right shows a regular octagon  $ABCDEFGH$  with all its diagonals.

