MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 1 - OCTOBER 2014 ROUND 6 ALG 1: EVALUATIONS

ANSWERS



A) Given:
$$\begin{cases} w = 5 - x \\ x = 6y + 1 \\ y = -\frac{2}{3}z \end{cases}$$

Find a simplified expression for z in terms of w.

B) Definition:

 $f(x, y) = x + \frac{1}{y}$, that is, the sum of the first argument and the reciprocal of the second argument.

For example,
$$f(4,2) = 4.5$$
, $f(2,4) = 2.25$.

If
$$\frac{f(x, y)}{f(y, x)} = \frac{2}{3}$$
 and $x - y = 4$, find the ordered pair (x, y) .

C) Given:
$$x = 5x - 2$$
, $x = \frac{x + a}{b}$

If a and b are positive integers, where a < 10 and b < 10, determine the <u>largest</u> possible value

of
$$a+b$$
 if x = x .