

MASSACHUSETTS MATHEMATICS LEAGUE
OCTOBER 2003
ROUND 3: LINEAR EQUATIONS

ANSWERS

A) $-\frac{5}{2}$

B) 40

C) 39

A) Solve for x leaving the result as a reduced fraction

$$4(x-3) + 3(x+7) - \frac{6}{5}(5x+10) = \frac{2}{3}(x-5) - \frac{1}{3}(x-4)$$

$$4/x - 12 + 3x + 21 - 6x - 12 = \frac{2}{3}x - \frac{10}{3} - \frac{1}{3}x - \frac{4}{3}$$

$$x - 3 = \frac{1}{3}x - \frac{14}{3}$$

$$\frac{2}{3}x = 3 - \frac{14}{3} = -\frac{5}{3}$$

$$x = -\frac{5}{2}$$

B) The coins from Jeremy's tips total \$3.16. He has two more dimes than quarters, one less than twice as many nickels as dimes, and three more pennies than dimes. How many coins does he have?

$$D = \# \text{ dimes} \quad 25(D-2) + 10D + 5(2D-1) + (D+3) = 316$$

$$Q = D-2 \quad 25D - 50 + 10D + 10D - 5 + D + 3 = 316$$

$$N = 2D-1 \quad 46D - 52 = 316 \quad Q = 6$$

$$P = D+3$$

$$46D = 368$$

$$D = 8$$

$$N = 15$$

$$P = 11$$

ANS 40

C) Karin's exercise route is 4 miles long. She alternates running one-quarter mile at ten mph, and then walking one-half mile at five mph. How many minutes does it take her to complete her route?

$$\begin{array}{cccccccccccc} R & W & R & W & R & W & W & R & W & R & W & R \\ \frac{1}{4} & \frac{1}{2} & \frac{1}{4} & \frac{1}{2} & \frac{1}{4} & \frac{1}{4} & \frac{1}{4} & \frac{1}{4} & \frac{1}{2} & \frac{1}{4} & \frac{1}{2} & \frac{1}{4} \end{array}$$

$$\frac{1}{4} \cdot 6 = \frac{3}{2} \text{ mi. running}$$

$$\frac{1}{2} \cdot 5 = \frac{5}{2} \text{ mi. walking}$$

$$\frac{3}{2} \cdot \frac{1}{10} \cdot 60 + \frac{5}{2} \cdot \frac{1}{5} \cdot 60 = \text{Time in min}$$

$$9 + 30 = \underline{39}$$