

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 4 - JANUARY 2015  
ROUND 3 TRIG: EQUATIONS WITH A REASONABLE NUMBER OF SOLUTIONS**

**ANSWERS**

A) \_\_\_\_\_

B) \_\_\_\_\_

C) \_\_\_\_\_

All solutions must be expressed in radians.

Pay attention to the specified range of the solutions in each question.

A) Compute the four solutions for which  $x \in [0, 2\pi)$  and  $\frac{1}{2} + \sin^2 x = \cos^2 x$ .

B) Solve for  $x$  over  $-\pi < x < 0$ :  $8\cos^3 x - 4\cos^2 x - 2\cos x + 1 = 0$

C) Compute the two values of  $x$  over  $0 < x < \frac{\pi}{2}$ :  $\tan\left(2x - \frac{\pi}{4}\right) = \cot\left(3x + \frac{\pi}{6}\right)$