MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 6 - MARCH 2014 SOLUTION KEY

Round 4

A) 2345_6 equals $2(6)^3 + 3(6)^2 + 4(6) + 5$ equals 569 and 1456_7 equals $1(7)^3 + 4(7)^2 + 5(7) + 6$ equals 580. Thus, the difference is 11.

B)
$$y = \frac{92 - 13x}{7} = 13 - x + \frac{1 - 6x}{7}$$

x must be picked so that $\frac{1-6x}{7}$ produces an integer.

x = -1 produces a multiple of 7 in the numerator and other possible values of x can be found by adding or subtracting 7 (or any multiple of 7).

$$x = -1 \Rightarrow y = 15$$

The slope of the line is $\frac{-13}{7}$, so as *x* increases by 7, *y* decreases by 13 or equivalently as *x* decreases by 7, *y* increases by 13.

Thus, we have ordered pairs (-1, 15), (6, 2), (13, -11). P must be (6, 2).

Other points in quadrants 2 and 4 will be further from point *P*.

Therefore,
$$y_1 + y_2 + y_4 = 2 + 15 + (-11) = \underline{6}$$
.

C) Let x and y denote the weights of the 2 contestants who initially dropped out.

$$\frac{4500 - (x + y)}{10} = 385 \Rightarrow x + y = 650 \Rightarrow \text{Ave} = \frac{x + y}{2} = 325 \text{ Then:}$$

$$L = \frac{3850 - 10W}{10} = 0.4(325) \Rightarrow L = 385 - W = 130 \Rightarrow W = 255$$