MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 2 - NOVEMBER 2006 ROUND 3 PLANE GEOMETRY: AREAS OF RECTILINEAR FIGURES

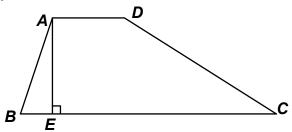
ANSWERS

A) Find the exact area of trapezoid *ABCD*, with bases \overline{AD} and \overline{BC} , given:

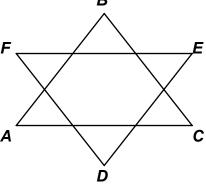
$$AB = 25$$
, $BC = DC = 40$, $AE = 24$

$$AD \le BC$$
 and E is between B and C

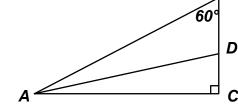
The diagram is not necessarily drawn to scale.



B) A six-pointed star is formed by taking equilateral $\triangle ABC$, flipping it over a horizontal line to form $\triangle DEF$, and placing it on top of the $\triangle ABC$ so that all of its sides are trisected by the intersection points. Express (in simplest form) the ratio of the area of the entire star to the area of the original $\triangle ABC$.



C) The area of $\triangle ABC$ is 6 units². The 30° angle is bisected by \overline{AD} . Determine the exact area of $\triangle ADC$.



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