

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 6 – MARCH 2009
ROUND 1 ALG 2: SIMULTANEOUS EQUATIONS AND DETERMINANTS

ANSWERS

A) _____

B) _____

C) _____

A) Solve for x .

$$\begin{vmatrix} 1 & -3 & 5 \\ 0 & 2 & 1 \\ x & 2 & 8 \end{vmatrix} = 38 - 5x$$

B) For what value(s) of a does the system $\begin{cases} (1) & x + 2y - 3z = 5 \\ (2) & 2x + y + 2z = 7 \\ (3) & 7x + 8y - 5z = a \end{cases}$ have an infinite number of solutions?

C) It has been stated that we count in base ten because we have ten fingers.
A race of humanoids (called Cylons) have only one hand with many fingers.
Suppose a Cylon solves the quadratic equation $x^2 + 21x + 99 = 0$ and claims that the difference between its roots is 12. How many fingers does a Cylon have?
It is understood that all numerical values have been expressed in the Cylon base b , which is equal to the total number of fingers that a Cylon has.