MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 5 – FEBRUARY 2010 ROUND 1 ALGEBRA 2: ALGEBRAIC FUNCTIONS

***** NO CALCULATORS IN THIS ROUND *****

ANSWERS

- A) _____
- B) _____
- C) (____,___,___,___)
- A) Given: $f: \{(x, f(x)) | f(x) = \frac{3}{x+2} \}$

Find the (x, y) coordinates of <u>all</u> points of intersection between f and f^{-1} .

B) In the equation $2x^4 - 7x^3 - 2x^2 + 13x + 6 = 0$, the four roots are A, B, C and D. Compute ABC + ABD + ACD + BCD.

C) Let $f(x) = Ax^3 + Bx^2 + Cx + D$. If f(-a) = -f(a), f(-3) + 2f(3) + f(5) = 3 and one zero of $Ax^3 + Bx^2 + Cx + D = 0$ is 4, determine the ordered quadruple (A, B, C, D).