

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 4 - JANUARY 2013
ROUND 7 TEAM QUESTIONS

ANSWERS

A) _____ D) (_____ , _____)

B) _____ E) _____

C) (_____ , _____ , _____ , _____ , _____) F) _____

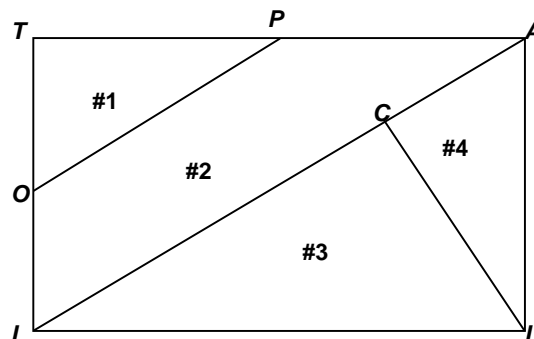
- A) The set of points in the xy -plane equidistant from $F(2, 1)$ and the line $x + y = 0$ crosses one of the axes twice. Compute the coordinates of the points of intersection with that axis.

B) Compute all values of x for which
$$\left(\frac{1}{x + \frac{1}{x + \frac{1}{2}}} \right) \div \left(\frac{1}{2 + \frac{1}{2 + \frac{1}{x}}} \right) = -1.$$

- C) The curve represented by the parametric equations $\begin{cases} x = 5 \cot(t) \\ y = 3 \csc(t) \end{cases}$ may be expressed in the form $Ax^2 + Cy^2 + Dx + Ey + F = 0$, where A, C, D, E and F are integers and $A > 0$. Determine the ordered 5-tuple (A, C, D, E, F) .

- D) For exactly two irrational values of the constant B , the equation $(2x - 3)(Bx - 1) = 5$ has exactly one real root. Compute the ordered pair (P, Q) , where $Q > 0$ and $\frac{P}{Q}$ is the reduced rational approximation of the larger value of B obtained by using the closest integer approximation for the simplified radical in the exact value of B .

- E) Given: $LATI$ is a rectangle, O and P are midpoints, $\overline{LC} \perp \overline{IA}$, $LI = 5$, $LA = 3$
 Compute the ratio of the areas of the four regions, listed from smallest to largest.
 Diagram is not necessarily drawn to scale.



- F) A fastfood restaurant has 5-piece chicken nuggets and 8-piece chicken nuggets on their value menu. A customer can not order individual chicken nuggets, so, for example, an order for 12 chicken nuggets is not possible. What is the largest number of nuggets that can not be ordered?