

**MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 6 – MARCH 2007
ROUND 7 TEAM QUESTIONS**

ANSWERS

A) _____ D) _____

B) _____ E) _____

C) (_____ , _____) F) _____

******* NO CALCULATORS ON THIS ROUND *******

- A) If $a \neq b$, $\text{GCF}(a, b) = 1$ and $|b - 87| < 14$, there are exactly two ordered pairs (a, b) for which $92_a = 29_b$. Note: a and b denote the bases of two-digit numbers.

If the specific ordered pairs are (a_1, b_1) and (a_2, b_2) and $a_1 < a_2$,

then what is the value of the determinant $\begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}$?

- B) Let x = the minimum positive integer for which $(a + 1)^2 + a > 1200$.

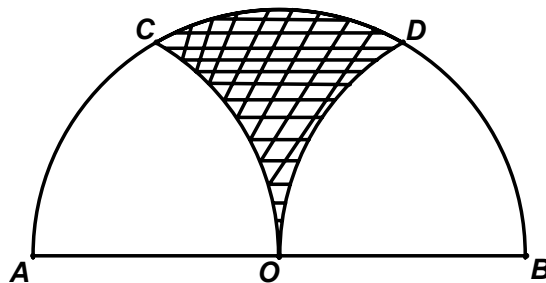
Let y = the minimum integer value of a for which $|\sqrt{a+1} - \sqrt{a}| < 0.1$

Determine the sum of the prime factors of the product $x(x + y)$.

- C) If A and B are integers and $(-1 + i)$ is a root of $p(x) = x^4 + Ax^2 + Bx - 6 = 0$, find the ordered pair (A, B) .

- D) Let A and B denote positive integers and $B \neq 1$. Find all possible ordered pairs (A, B) for which the ratio $(164 - 2A) : (3A - 6)$ is equal to the ratio $B : 1$.

- E) In semicircle O , arcs \widehat{OC} and \widehat{OD} centered at A and B are drawn passing through O . $AO = 6$
Find the exact area of the shaded region?



- F) What is the smallest integer coefficient in the expansion of $(4t + \frac{v}{2})^8$?