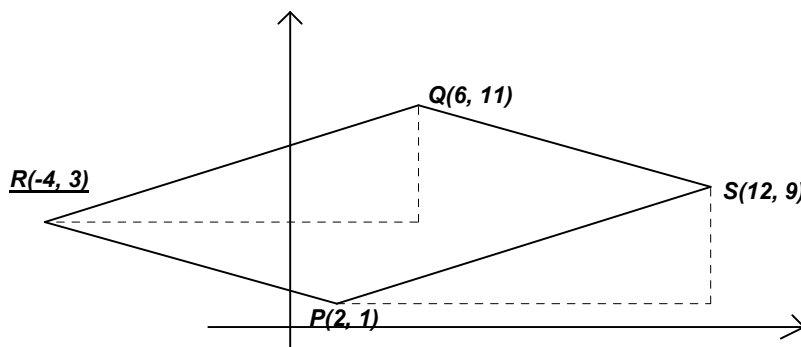
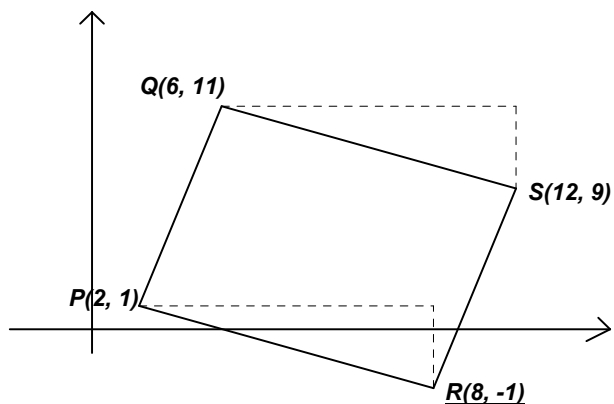


**MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 3 - DECEMBER 2009 SOLUTION KEY**

Round 1 –continued

C) - continued

Given three points $P(2, 1)$, $Q(6, 11)$ and $S(12, 9)$, there are in fact three points which could be the fourth vertex of a parallelogram. Besides $(16, 19)$ above, $(8, -1)$ and $(-4, 3)$ are possible candidates.



In the latter two cases, the quadrilaterals would be $PQSR$ and $PRQS$ respectively (or a cyclical permutation thereof).

The requested quadrilateral was $PQRS$ which implies P and R must be opposite vertices.

In these other two quadrilaterals, P and R are consecutive vertices.

Therefore, the only possible position for point R is $(16, 19)$ and the above solution is unique.