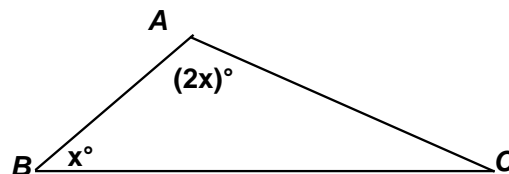


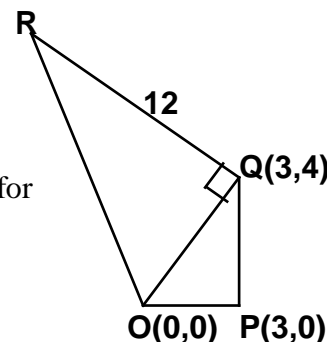
**MASSACHUSETTS MATHEMATICS LEAGUE**  
**CONTEST 3 - DECEMBER 2015**  
**ROUND 7 TEAM QUESTIONS**  
**ANSWERS**

- A) \_\_\_\_\_ D) \_\_\_\_\_
- B) \_\_\_\_\_ E) ( \_\_\_\_\_ , \_\_\_\_\_ )
- C) ( \_\_\_\_\_ , \_\_\_\_\_ ) F) \_\_\_\_\_

- A) In  $\triangle ABC$ , with angles as indicated,  
 $D$  lies on  $\overline{BC}$  such that  $\overline{AD}$  bisects  $\angle A$ .  
 $\frac{DC}{DA} = 2$  and  $BC = 6$ .  
 Compute the perimeter of  $\triangle ABC$ .



- B) Consider the following statements about the integer  $x$ .  
 $x$  and  $x + 2$  are prime.  
 $x - 1$  is a multiple of 5.  $x + 3$  is a multiple of 7.  
 The minimum positive integer value of  $x$  for which all of these statements are true is  $x = 11$ . Determine the next largest value of  $x$  for which all of these statements are true.



- C) Compute the coordinates of point  $R$ .

- D) Given:  $a, b, m, n > 0$ ,  $a^{b+c} = m$  and  $b^{c+a} = n$ .  
 If  $\log(a^b b^a) = 2$ , express  $(ab)^c$  as a simplified expression in terms of  $m$  and  $n$ .

- E) List the integers from 1 to 100 inclusive in 10 rows as indicated at the right.  
 Let  $n$  be the smallest prime in the list.

Repeat the following pair of statements until  $n^2 > 100$ .

Cross out every  $n^{\text{th}}$  number in the list which is larger than  $n$ .

Now let  $n$  be the smallest integer in the list not crossed out.

1	2	3	...	10
11	12	13	...	20
21	22	23		30
...				
81	82	83	...	90
91	92	93	...	100

Let  $(a, b)$  be consecutive un-crossed-out integers, where  $b > a$ .

The simplified ratio of the number of ordered pairs for which  $b - a = 2$  to the number of ordered pairs for which  $b - a = 6$  is  $k : j$ .

Determine the ordered pair of integers  $(k, j)$ .

- F) A polygon with  $n$  sides has more than 1,000,000 diagonals. What is the minimum number of sides this polygon could have?