

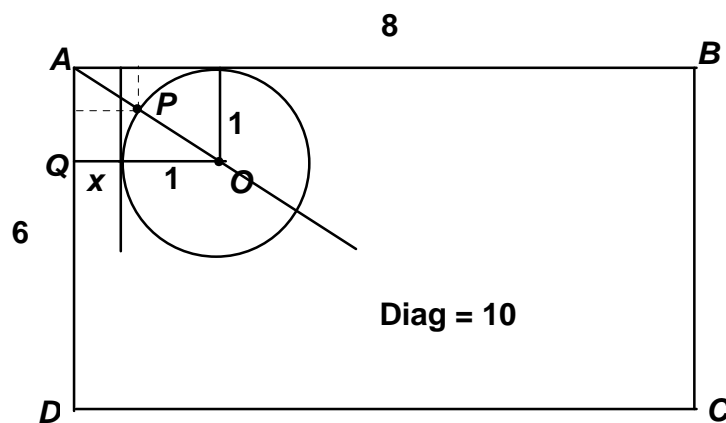
Appeal from Hamilton Wenham in Round 5 Question B

The original wording of the question was as follows:

A bead with a 2 inch diameter slides along a metal rod which connects opposite corners of a rectangular 6 inch by 8 inch wooden frame. When the bead touches the side of the frame it reverses direction. Let P and Q be the points along the wire where the bead comes closest to the opposite corners of the frame. Compute PQ .

Assuming P was not the center of the bead.

Zoom in on the upper left corner of the frame when the bead touches the top edge of the frame.



$$\triangle AOQ \sim \triangle ACD \Rightarrow \frac{AQ}{OQ} = \frac{AD}{CD} \Leftrightarrow \frac{1}{x+1} = \frac{6}{8} = \frac{3}{4} \Rightarrow 3x+3=4 \Rightarrow x = \frac{1}{3}$$

Using the Pythagorean Theorem on $\triangle AQO$,

$$\left(\frac{4}{3}\right)^2 + 1^2 = AO^2 \Rightarrow AO^2 = \frac{25}{9} \Rightarrow AO = \frac{5}{3} \Rightarrow AP = \frac{5}{3} - 1 = \frac{2}{3}$$

$$\text{Therefore, } PQ = 10 - 2\left(\frac{2}{3}\right) = \underline{\underline{\frac{26}{3}}}$$

Alternate interpretation was accepted.