

**MASSACHUSETTS MATHEMATICS LEAGUE**  
**CONTEST 2 - NOVEMBER 2012**  
**ROUND 5 TRIG: FUNCTIONS OF SPECIAL ANGLES**

**ANSWERS**

A) \_\_\_\_\_

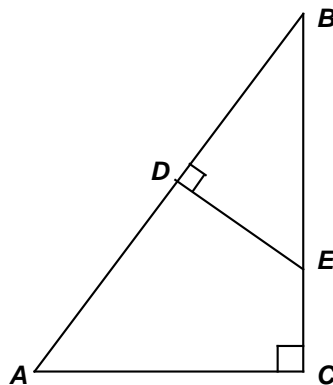
B) \_\_\_\_\_

C) \_\_\_\_\_

A) In  $\triangle ABC$ , the measures of the angles are  $x^\circ$ ,  $\frac{x}{5}^\circ$  and  $\frac{3x}{10}^\circ$ . Compute  $2\cos^2(x^\circ) - 1$ .

B) Given:  $\cos(\angle BED) = \frac{3}{5}$

Compute  $\cot^2 A + \cos(\angle DEC)$ .



C) Suppose  $A = 60^\circ$ . There are many ordered pairs  $(k, B)$  of relatively prime positive integers that are solutions of  $k \tan\left(\frac{A}{2}\right) = \sin 2A + B \sin A$ . Of those pairs compute the smallest prime value of the sum  $k + B$ .