## MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 3 – DECEMBER 2009

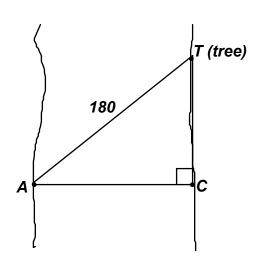
## ROUND 1 TRIG: RIGHT ANGLE PROBLEMS, LAWS OF SINES AND COSINES

\*\*\*\*\* NO CALCULATORS IN THIS ROUND \*\*\*\*\*

## **ANSWERS**

- A) \_\_\_\_\_
- B) \_\_\_\_\_
- C) \_\_\_\_\_
- A) From point *A* on a river bank, the distance to a tree on the opposite bank is 180 meters.

If  $\tan(\angle TAC) = \frac{\sqrt{5}}{2}$ , compute AC, the width of the river.



- B) In <u>acute</u>  $\triangle ABC$ ,  $m \angle C = 30^{\circ}$ , AB = 4 and AC = n, where n is an integer. Determine how many values of n are possible?
- C) In  $\triangle ABC$ , m $\angle A = 30^{\circ}$ , a = 10, b = 15 and  $\angle B$  is as large as possible. Determine the <u>exact</u> value of sin *C*.