

**MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 2 - NOVEMBER 2016
ROUND 7 TEAM QUESTIONS**

ANSWERS

A) _____ D) (__ , __ , __ , __ , __ , __)

B) (__ , __) $S = \{ \text{_____} \}$ E) _____

C) (_____ , _____ , _____) F) _____

A) Given: $\sum_{n=1}^{n=32} (1+i)^n = k(1-i)$ Compute k .

B) There are K possible digit-sums for the set of 2-digit primes.
Let S be the set of the most frequently occurring digit-sums and N be the number of times each of these sums occurred.

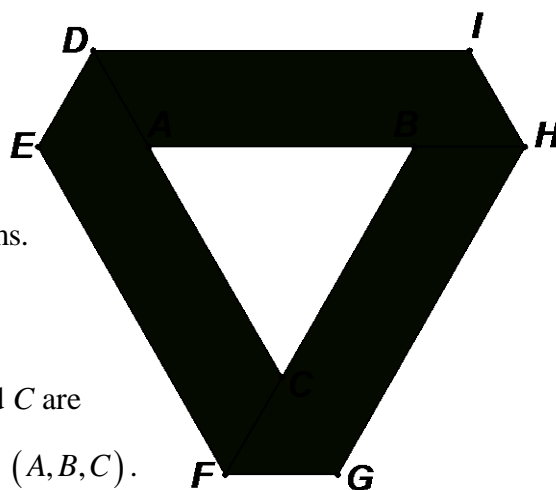
Determine the ordered pair (K, N) and the set S .

Recall: The digit-sum of a number is the sum of the digits in that number.

C) ABC is an equilateral triangle with area 1 unit².
 $DEFC$, $FGHB$ and $HIDA$ are congruent parallelograms.

If $FG = \frac{1}{2}$, the area of the shaded region can be

expressed in the form $\frac{A(\sqrt{3} + B\sqrt[4]{3})}{C}$, where A , B and C are relatively prime integers. Compute the ordered triple (A, B, C) .



D) $36x^2 - 3xy - 60y^2 + 18x + 38y - 4$ factors as the product of two trinomials, namely $Ax + By + C$ and $Dx + Ey + F$, where each constant is an integer.

If $AB < 0$, compute the ordered 6-tuple of constants (A, B, C, D, E, F) .

E) Compute $\sin 10^\circ \sin 30^\circ \sin 50^\circ \sin 70^\circ$.

F) The exterior angles (one at each vertex) of $\triangle ABC$ measure $(2(x+y)+8)^\circ$, $(5y-x)^\circ$ and $(3x+y-44)^\circ$, where x and y are integers.
 $x+y > 41$ and $2y-x > 46$

The obtuse angle formed by the bisectors of the acute interior angles of $\triangle ABC$ measures 146° .
Compute the degree-measure of the largest exterior angle of $\triangle ABC$.