MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 4 - JANUARY 2010 ROUND 4 ALG 2: QUADRATIC EQUATIONS / THEORY OF QUADRATICS

ANSWERS

A)

***** NO CALCULATORS IN THIS ROUND *****

A) Consider the following quadratic equation: $x^2 + 3x + 2M = 0$

If M = a, the constant term is 3 greater than the coefficient of x^2 .

If M = b, the equation has equal roots.

If M = c, the product of the roots is 10.

Compute the product *abc*.

B) Find all values of the constant k for which the roots of the quadratic equation

$$y^2 + k^2 y = 5ky + 6y + 7$$

are numerically equal, but opposite in sign.

C) The line 2x - y + 7 = 0 intersects $y = Ax^2 + Bx + C$ at x = -2 and x = 7. The low point V has coordinates (1, -3) Compute the value of C.

