MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 5 - FEBRUARY 2010 ROUND 3 TRIG: IDENTITIES AND/OR INVERSE FUNCTIONS

***** NO CALCULATORS IN THIS ROUND *****

ANSWERS

A)
$$Cos^{-1}\left(-\frac{1}{2}\right) - Sin^{-1}\left(-\frac{1}{2}\right) = k^{\circ}$$
. Compute k .

Do <u>not</u> include the degree symbol in your answer.

B) Compute the two smallest positive values of x (in <u>radians</u>) that satisfy $\frac{1-2\sin^2 x}{\sin x \cos x} = 2\sqrt{3}$.

C) Given:
$$\begin{cases} y = \sin^3 t \\ x = \cos^3 t \end{cases}$$
, where $0 \le t \le 2\pi$.

Compute all real values of y for which $x = \frac{64}{125}$.