## MASSACHUSETTS MATHEMATICS LEAGUE JANUARY 2004 ROUND 7: TEAM QUESTIONS

ANSWER	₹S	•
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A)	D)
B)	<b>E</b> )
C)	F)

A) A parabola which has vertex V at the focus of the parabola  $x^2 = 8y$ , and focus at the origin O, intersects  $x^2 = 8y$  at points A and B. Calculate the area of quadrilateral AVBO.

**B)** A two foot by three foot poster is framed with a border of uniform width. If the area of the border is the same as the area of the poster, calculate in <u>inches</u> the width of the border.

C) Solve for  $0^{\circ} \le \theta < 360^{\circ}$ ,  $\cos 3\theta + \cos \theta = \sqrt{2} \cos 2\theta$ 

**D)** In the equation  $ax^2 + bx + c = 0$ , a, b, and c are relatively prime integers. If the product of its roots is  $-\frac{8}{3}$ , and the difference of its roots is  $\frac{10}{3}$ , calculate two possible values for b.

E) In  $\triangle ABC$ , AB = CB,  $\angle B = 108^{\circ}$ , D is on  $\overline{AC}$  so that  $\angle CBD$  is twice  $\angle ABD$ . If DA = 2, calculate CB in simplified radical form.

F) Mary's speed on her bike was 6 mph on the level, 4 mph downhill, and 12 mph uphill. One day she rode to Greg's house and returned by the same route in one hour. How far in miles is it to Greg's house?