

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 4 - JANUARY 2016
ROUND 4 ALG 2: QUADRATIC EQUATIONS

ANSWERS

A) _____

B) _____

C) _____

- A) It is not uncommon for an equation, like $x^2 = 38x - N$, to have two real solutions.
For example, when $N = 280$, $x = 10$ or 28 . Determine the unique value of the constant N
for which the quadratic equation has exactly one solution.

- B) Compute the product of the cubes of the rational roots of $\left(x + \frac{4}{x}\right)^4 - 17\left(x + \frac{4}{x}\right)^2 + 16 = 0$.

- C) The equation $x^2 - kx + 2k = 2x$ has one root which is 3 greater than the other root.
If the roots are R_1 and R_2 , find all ordered triples (R_1, R_2, k) , where $R_1 > R_2$.