## MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 6 - MARCH 2016 ROUND 7 TEAM QUESTIONS ANSWERS

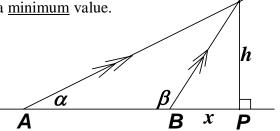


A) Given: 
$$\begin{cases} x + y + z = n \\ 2x - y - z = n + 1 \\ x + 2y - 2z = n + 2 \end{cases}$$
, where  $x, y, z$  and  $n$  are positive integers.

If x + y > 100, compute (x, y, n) for which x + y + n has a minimum value.

B) Given: 
$$\begin{cases} x = t + t^{-1} \\ y = t - t^{-1} \end{cases}$$

Compute all possible real values of y, if  $x = \frac{1}{2}\sqrt{17}$ .



- C) A missile fired from point A is intercepted at point I by a missile fired from point B. If AB = 500,  $\beta = 2\alpha$ ,  $\tan \alpha = \frac{2\sqrt{3}}{3}$  and  $\beta$  is obtuse, compute the ordered pair (x,h).
- D) The Lady Bird Johnson Souvenir Sheet contains 6 stamps. The dimensions of the sheet are L mm by (L+12) mm, where L is an integer. Consider each stamp a rectangle whose dimensions (in mm) are integers in an 8:5 ratio. The area of the 6 stamps (in mm²) equals 25% the area of the sheet plus  $260 \text{ mm}^2$ . Compute the  $\underline{\text{minimum}}$  area of the sheet for which this is true.
- E) Given: Right  $\triangle ABC$  with hypotenuse AB = 3An arc is drawn with radius AC and center A intersecting  $\overline{AB}$  at point E. An arc is drawn with radius BC and center B intersecting  $\overline{AB}$  at point D. If DE = 1.2, compute the area of  $\triangle ABC$ .

