MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 5 – FEBRUARY 2008 ROUND 2 ARITHMETIC / NUMBER THEORY

ANSWERS

A) What is the <u>units</u> digit of the product $7^{218}(3^{507})$?

B) Let $x^2 - y^2 = 31$, where x and y are positive integers. If N = xy, how many positive factors does N have?

C) Using only the prime digits 2, 3, 5 and 7 <u>without repetition</u>, form all possible positive integers in base 10 with at most 4 digits (i.e. less than 10,000), that will be divisible by 15. What is the sum of all these positive integers?