MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 5 – FEBRUARY 2007 ROUND 1 ALG 2: ALGEBRAIC FUNCTIONS

ANSWERS

A) Determine the domain of the function
$$f(x) = \frac{1}{\sqrt{4x - 3x^2}}$$
.

B) Given:
$$f(0) = 0$$
 and $f(x) = x - f(x - 1)$ for $x > 0$
Find $f(2007)$.

C) Find the largest 3-digit integer (in base 10) that can be formed from the distinct digits *A*, *m* and *b*, given:

$$f(x) = Ax^2$$
 and $g(x) = mx + b$, where $A \neq 0$ and $m \neq 0$

$$f(g(x)) \equiv g(f(x))$$
 (i.e. an identity valid for all real values of x)