

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 4 - JANUARY 2017
ROUND 4 ALG 2: QUADRATIC EQUATIONS

ANSWERS

A) (_____ , _____ , _____)

B) _____

C) (_____ , _____ , _____)

A) One solution of the quadratic equation $Ax^2 + Bx + C = 0$ is $\frac{5+i\sqrt{3}}{2}$.

If A , B and C are integers, $A > 0$, and the greatest common factor of A , B and C is 1, compute the ordered triple (A, B, C) .

B) J and K are positive integers.

The ordered pair $(x, y) = (J, K)$, where $J + K < 100$, satisfies the equation $x + 2 = y^2 - 7$.

Compute the sum of the largest and smallest possible values of J .

C) The quadratic equation $Ax^2 + Bx + C = 0$, where A , B and C are relatively prime integers and

$A > 0$, has roots $r_1 = \sqrt{\frac{40}{9} + \frac{41}{4}}$ and $r_2 = B + 2$.

Compute the ordered triple (A, B, C) .