

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 3 – DECEMBER 2006
ROUND 1 TRIG: RIGHT ANGLE PROBLEMS, LAWS OF SINE AND COSINE

ANSWERS

A) _____

B) _____

C) (_____ , _____)

- A) An equilateral triangle has sides of length 6.
Points A, B, C, D, E and F are trisection points of the sides.
What is the exact length of a segment that

- connects two of these points not on the same side of the triangle and
- is not parallel to any sides of the triangle?

Express your answer as an exact value in simplified form.

- B) In $\triangle ABC$, $m\angle B = 150^\circ$, $a = BC = 10$ and $b = AC = 15$.
Determine the exact value of $\sin(B + C)$.

- C) The perimeter of a regular n -sided polygon is p . A simplified expression for the apothem of the polygon in terms of p and n may be written in the form $\frac{p \cot(\frac{X}{n})}{Yn}$, where $\frac{X}{n}$ is the degree-measure of an angle whose vertex is at the center of the regular polygon. Determine the ordered pair (X, Y) .