

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 2 - NOVEMBER 2009 SOLUTION KEY**

**Round 6**

A)  $4x + 2(3x) = 180 \rightarrow x = 18 \rightarrow$  base angle:  $54^\circ \rightarrow$  exterior angle:  **$126^\circ$**

B)  $n(n-3)/2 = 740 \rightarrow n(n-3) = 1480$

Rather than trying to factor this quadratic by trial and error, guess at a value for  $n$ . If the result is too low, try a larger value of  $n$ ; if the result is too high, try a smaller value of  $n$ .

$n = 35 \rightarrow 35(32) = 1120$  (too low)

$n = 45 \rightarrow 45(42) = 1890$  (too high)

Since 1120 is closer to 1480, we'll start at 40 and step down until we find  $n$ .

$n = 40 \rightarrow 40(37) = 1480$  Bingo!

A regular polygon with 40 sides has exterior angle with  $\left(\frac{360}{40}\right) = \mathbf{9^\circ}$

C) Since  $\angle AMD$  and  $\angle MNF$  are corresponding angles of parallel lines, we have  $7x - 40 = 5x \rightarrow x = 20$

$m\angle AMD = 100 \rightarrow a + b = 80$  and  $c + d = 100$

$m\angle NMP = 3m\angle PMD \rightarrow b = 3a$

Thus,  $(a, b) = (20, 60)$

$m\angle MNP = 4m\angle PNF \rightarrow c = 4d$

Thus,  $(c, d) = (80, 20)$

Finally,  $y = 180 - (b + c) = 180 - 140 = \mathbf{40}$

