MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 4 – JANUARY 2015 ROUND 1 ANALYTIC GEOMETRY: ANYTHING

ANSWERS

A)	(.)
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B)
$$(x - \Box)^2 + (y - \Box)^2 = \Box$$

A) An ellipse has a focus at (4, -7) and vertices at $(4, \pm 13)$.

Its equation is written in the form $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$.

Determine the ordered quadruple (h, k, a^2, b^2) .

B) Find the equation of the circle containing the points P(-5, 2), Q(-3, 4) and R(1, 2). Give your answer in $(x-h)^2 + (y-k)^2 = r^2$ form.

C) The equations of the asymptotes of the conic defined by $9x^2 - 6y^2 + 18x + 18 = 0$ are written in the form $y = \pm m(x - h) + k$. Compute the ordered triple (m, h, k), where m > 0.