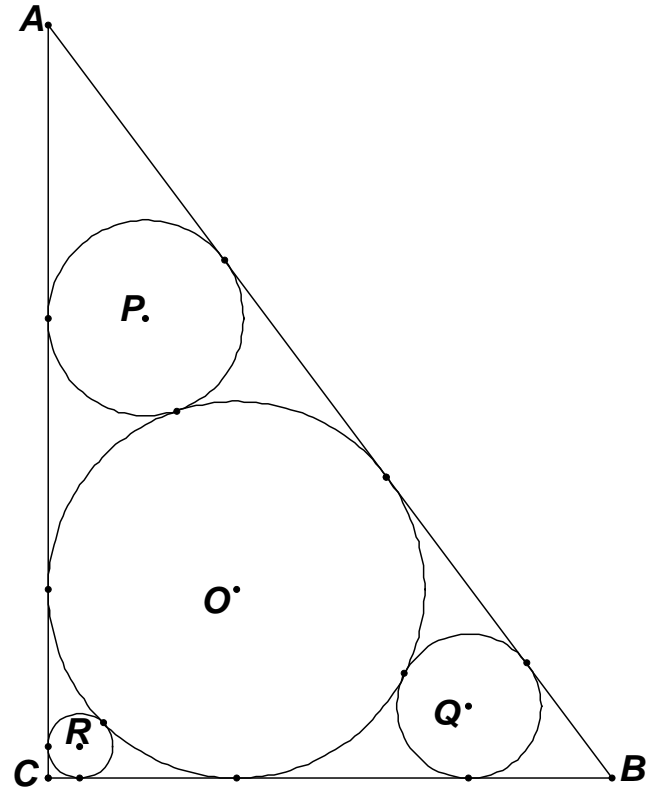


**ROUND 7 TEAM QUESTIONS - continued**

- E) Circle  $O$  is inscribed in  $\triangle ABC$ , a 3-4-5 right triangle. Three smaller circles centered at  $P$ ,  $Q$  and  $R$  are drawn inside  $\triangle ABC$ . Each is tangent to circle  $O$  and to two sides of  $\triangle ABC$ . Their radii are  $r_1$ ,  $r_2$  and  $r_3$ , where  $r_1 < r_2 < r_3$ .

Compute the ordered triple  $(r_1, r_2, r_3)$ .

The diagram is constructed to scale.



- F) A sequence, whose initial term is a positive integer  $t_1$ , is defined by the following rule:
- if a term is even, the next term is half the current term
  - if a term is odd, the next term is 1 more than the current term

For some minimum value of  $k$ , for all  $n \geq k$ ,  $t_n = 2$  and  $t_{n+1} = 1$  (or vice versa).

For example,  $t_1 = 48 \Rightarrow 48, 24, 12, 6, 3, 4, 2, 1, 2, 1, \dots \Rightarrow k = 7$

Compute all values of  $t_1$  for which  $k = 5$ .