MASSACHUSETTS MATHEMATICS LEAGUE **CONTEST 3 - DECEMBER 2013 ANSWERS**

Round 1 Trig: Right Triangles, Laws of Sine and Cosine

A)
$$4\sqrt{3}$$

B)
$$\frac{63}{65}$$

Round 2 Arithmetic/Elementary Number Theory

Round 3 Coordinate Geometry of Lines and Circles

A)
$$\left(-\frac{8}{15},4\right)$$

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 B) $A\left(-\frac{1}{2}, -\frac{5}{2},\right) B\left(\frac{7}{2}, -\frac{5}{2},\right)$ C) $(x-3)^2 + (y+2)^2 = 20$

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Round 4 Alg 2: Log and Exponential Functions

B)
$$x = b^{\frac{60}{13}}$$

C)
$$2 + \sqrt{17} - \sqrt{5}$$

Round 5 Alg 1: Ratio, Proportion or Variation

B)
$$\left(-\frac{4}{3},4\right)$$

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 C) $\frac{3R}{5}$ (or $\frac{3}{5}R$ or $0.6R$)

(The zero is not required.)

Round 6 Plane Geometry: Polygons (no areas)

B)
$$36 \le 36 \le 108$$

C)
$$\frac{23+4\sqrt{3}}{4}$$

(or equivalent)

(Accept A) and B) with or without the degree symbol.)

Team Round

D)
$$\frac{1}{10,000}$$

E)
$$\frac{4}{3}, \frac{5}{3}$$

C)
$$\frac{133}{8}$$
 (or 16.625)