MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 6 - MARCH 2008 ROUND 2 ALG1: EXPONENTS AND RADICALS

ANSWERS

A)

A) Given:
$$N = 2x^{-2/3}$$

If $x = 64$, find y, where $N = 4^y$.

B) Simply $\sqrt{4 + \left(x - \frac{1}{x}\right)^2} \cdot \left(\frac{x}{3} + \frac{1}{3x}\right)^{-1}$ so that your answer is free of radicals and/or negative exponents.

C) Determine the ordered pair of positive integers (A, B) for which the quotient $\frac{\sqrt{49-8\sqrt{3}}}{\sqrt{21+12\sqrt{3}}}$ may be expressed as $\frac{A-B\sqrt{3}}{3}$.