## MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 5 – FEBRUARY 2012 ROUND 1 ALGEBRA 2: ALGEBRAIC FUNCTIONS

## **ANSWERS**

| A) |    |
|----|----|
|    |    |
| B) | :: |
| C) |    |

## \*\*\*\*\* NO CALCULATORS ON THIS ROUND \*\*\*\*\*

A) Let 
$$f(x) = \begin{cases} 4x+5 & \text{for } x > 2 \\ 10 & \text{for } -2 < x \le 2 \\ 3x-4 & \text{for } -10 \le x \le -2 \end{cases}$$
 Compute:  $f(f(2)) + f(f(-2)) + f(0)$ 

B) f(x) is a function of minimum degree with integer coefficients and zeros of -1,  $\sqrt{6}$  and i. If the lead coefficient is positive and the greatest common factor of the coefficients is 1, compute the ratio 2f(-2):3f(3).

C) Given 
$$f(x) = \frac{x+1}{x-1}$$
 Express  $f(2x)$  in terms of  $f(x)$ .