MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 2 – NOVEMBER 2014 ROUND 1 COMPLEX NUMBERS (No Trig)

ANSWERS

A) _____

B) _____

C) _____

A) Given: $(3+4i)^2 + a + bi = 3 + ki$, where a and b are real. Compute k such that a = -b.

B) Given: $\sqrt{12-5i} = x + yi$ for real numbers x and y.

Compute $\frac{x^2}{y^4}$.

C) If
$$\frac{(3\sqrt{3}-3i)^3-(3\sqrt{3}+3i)^3}{108} = x + yi$$
, compute $x^3 + y^3$.