

Addendum:

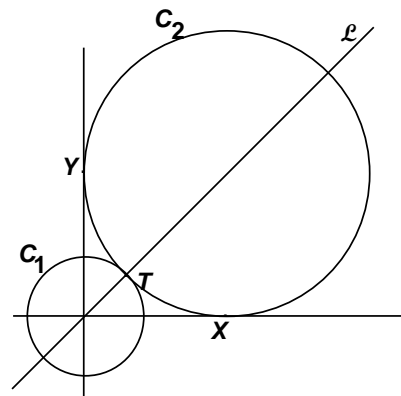
The original contest had two appeals in round 3

B) The original question was

Let circle $C_1 = \{(x, y) \mid x^2 + y^2 = 36\}$ and line $\mathcal{L} = \{(x, y) \mid y = x\}$.

Circle C_2 has its center on \mathcal{L} and is tangent to the x -axis at $X(a, 0)$, the y -axis at $Y(0, b)$ and circle C_1 at point T .

Compute the value of a .



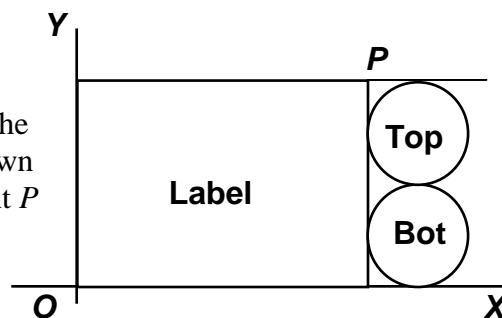
In the second line the phrase outside of C_1 was omitted and since there is a circle inside of C_1 which satisfies the verbally stated conditions of the problem, $6(\sqrt{2}-1)$ was also accepted.

C) The original question was

When removed, the label on a cylindrical can is a rectangle.

Suppose the height (H) of the can is 4 times the radius (r) of the base. The label is placed in quadrant 1 of the xy -plane as shown in the diagram at the right. The distance from point O to point P can be expressed in terms of H and r in simplest form as

$A\sqrt{B} \frac{H^2}{r}$, where A and B are positive constants and B is expressed in terms of π . Compute the ordered pair (A, B) .



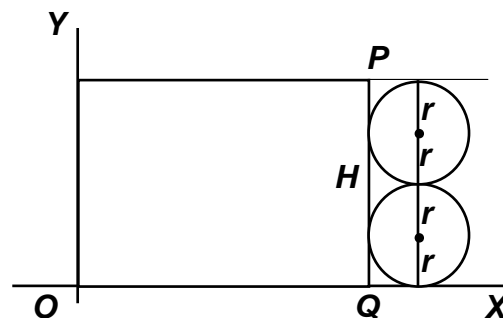
Since it was perfectly logical for a student to proceed

$$OP^2 = H^2 + OQ^2 = H^2 + (2\pi r)^2$$

Substituting for r , $H^2 + H^2 \cdot \frac{\pi^2}{4} = H^2 \left(1 + \frac{\pi^2}{4}\right)$

$$OP = H \sqrt{1 + \frac{\pi^2}{4}} \text{ and } B = 1 + \frac{\pi^2}{4}$$

$$\text{Now } \frac{AH^2}{r} = H \Rightarrow AH^2 = Hr = \frac{H^2}{4} \Rightarrow A = \frac{1}{4}$$



An alternate answer of $\left(\frac{1}{4}, \frac{\pi^2}{4} + 1\right)$ was also accepted.