

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 2 - NOVEMBER 2011  
ROUND 2 ALGEBRA 1: ANYTHING**

**ANSWERS**

A) \_\_\_\_\_ inches

B) \_\_\_\_\_

C) \_\_\_\_\_

**\*\*\* NO CALCULATORS IN THIS ROUND \*\*\***

- A) A rectangular piece of cardboard is 4" by 6".  
Squares of equal size are cut from each of the 4 corners.  
If the total area of the cutouts is 37.5% of the area of the original piece of cardboard,  
compute the length (in inches) of the side of the squares cut from each corner.

- B) When a two-digit number is divided by the sum of its digits, the quotient is 7  
and the remainder is 0. When the same number is multiplied by the sum of its digits,  
the product is 567. Find this number.

~~—Joe Ford—2009~~

~~When a two-digit number is divided by the sum of its digits, the quotient is 7.~~  
~~When the same number is multiplied by the sum of its digits, the product is 567.~~  
~~Find this number.~~

~~Ans: 63~~

$$\begin{cases} (1) & 10t + u = 7(t + u) \\ (2) & (10t + u)(t + u) = 567 \end{cases}$$

~~(1)  $\rightarrow t = 2u$~~

~~Substituting for  $10t + u$  in (2),  $7(t + u)^2 = 567 \rightarrow (t + u)^2 = 81 \rightarrow t + u = 3u = 9$~~

~~$\rightarrow u = 3, t = 6 \rightarrow \underline{63}$~~