

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 4 – JANUARY 2008  
ROUND 7 TEAM QUESTIONS**

**ANSWERS**

A) \_\_\_\_\_ D) \_\_\_\_\_

B) \_\_\_\_\_ E) \_\_\_\_\_

C) \_\_\_\_\_ F) \_\_\_\_\_

A) In a plane, the locus of a curve is defined by the parametric equations

$$x = 9\sec(t) \text{ and } y = 7\tan(t), \text{ where } 90^\circ < t < 180^\circ$$

Express  $x$  directly as a simplified function of  $y$ .

B) Determine all ordered pairs  $(x, y)$  of positive integers, where

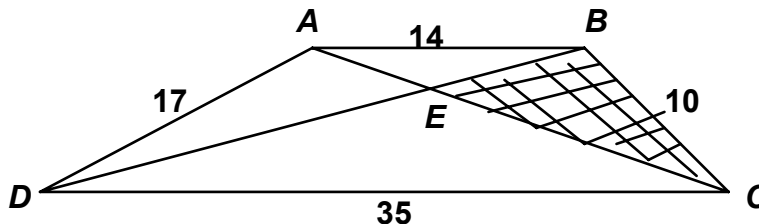
$$x > y \text{ and } x^3 - x^2y - xy^2 + y^3 = 1024.$$

C) Determine the sum of all values of  $x$  over  $[0, 360^\circ)$  for which

$$\cot^2(270^\circ - 2x) - \csc(90^\circ + 2x) - 1 = 0$$

D) Determine all ordered pairs of integers  $(n, x)$  for which  $n > 3$  and  $\sum_{k=3}^{k=n} (xk + 3) = 45$ .

E) In trapezoid  $ABCD$  (with bases  $\overline{AB}$  and  $\overline{CD}$ ),  $AB = 14$ ,  $BC = 10$ ,  $CD = 35$  and  $AD = 17$ .  
Compute the area of  $\triangle BEC$ .



F) Let  $a$ ,  $b$  and  $c$  be positive integers and  $a$  and  $b$  be consecutive.  
If  $a + b + c = 21$ , determine the sum of all distinct products  $abc$ .