

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 3 - DECEMBER 2016
ROUND 6 PLANE GEOMETRY: POLYGONS (no areas)

ANSWERS

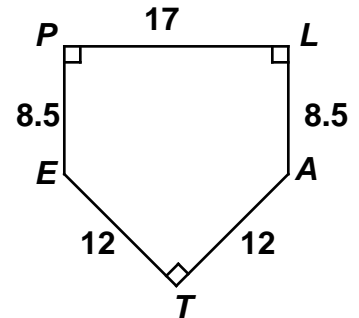
A) _____

B) _____ A _____ O _____ R _____

C) (_____ , _____)

- A) In a polygon with n sides, the ratio of the sum of the measures of the exterior angles (one at each vertex) to the sum of the measure of the interior angles is $\frac{1}{8}$. How many diagonals does this polygon have, *originating from any single vertex*?

- B) In baseball, home plate according to the MLB rulebook, has 3 right angles and dimensions shown at the right. Rules may be rules, but, as students of mathematics, we realize that *this shape cannot exist*. $m\angle ETA$ may be close to 90° , but $\angle ETA$ is **not** a right angle. Is interior $\angle ETA$ Acute, Obtuse or Reflexive? Circle the correct letter in the answer blank above.



- C) The diagonals of quadrilateral $ABCD$ (segments \overline{AD} and \overline{BC}) do not intersect. This is always the case for a concave quadrilateral. Note: Points A, B, C, D , and E all lie in the same plane. Assume E lies on \overline{BC} .

If $\overline{ADE} \perp \overline{BC}$, $AB = BC = 25$, $AC = 30$, $BD = BE + 3$, $AE = 3(BE + 1)$, compute the ordered pair (DC, d) , where d denotes the absolute value of the difference between the lengths of the diagonals.

