## MASSACHUSETTS MATHEMATICS LEAGUE **CONTEST 2 – NOVEMBER 2008 SOLUTION KEY**

## Round 2

A) Subtracting 2009 from both sides and squaring,  $x - 2009 = (x - 2009)^2$ Since this equation is of the form  $k = k^2$ , which has solutions k = 0, 1, we have x = 2009, 2010.

B) 
$$x - \frac{6}{x} = \frac{5}{2} \Rightarrow 2x^2 - 12 = 5x \Rightarrow 2x^2 - 5x - 12 = 0 \Rightarrow (2x + 3)(x - 4) = 0 \Rightarrow x = \underline{-3/2, 4}$$

C) 
$$\begin{cases} F = \frac{5}{9}C - 32 \\ F = C \end{cases} \Rightarrow 5C - 288 = 9C \Rightarrow 4C = -288 \Rightarrow C = F = -72$$

C)  $\begin{cases} F = \frac{5}{9}C - 32 \\ F = C \end{cases} \Rightarrow 5C - 288 = 9C \Rightarrow 4C = -288 \Rightarrow C = F = -72$  Either from recall or solving the system  $\begin{cases} F = \frac{9}{5}C + 32 \\ F = C \end{cases}, C = F = -40$ 

Thus, 
$$-40 - (-72) = 32$$