

MASSACHUSETTS MATHEMATICS LEAGUE
CONTEST 2 – NOVEMBER 2009
ROUND 1 COMPLEX NUMBERS (No Trig)

***** NO CALCULATORS IN THIS ROUND *****

ANSWERS

A) _____

B) _____

C) _____

Note: $i = \sqrt{-1}$

A) Simplify completely: $\frac{1 + 2i + 3i^2 + 4i^3}{1 - 2i + 3i^2 - 4i^3}$

B) Given: $(3 + 3i)^{40} = r^n$, where r and n are both integers
Determine the smallest possible value of the sum $r + n$.

C) If $\sqrt{-40 - 9i} = A + Bi$, compute $\left(\frac{A}{B}\right)^2$.