MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 3 – DECEMBER 2014 ROUND 1 TRIG: RIGHT ANGLE PROBLEMS, LAWS OF SINES AND COSINES

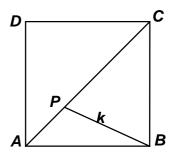
ANSWERS

| A) | | | | |
|------------|---|-------|------|-------|
| B) | (| , | |) |
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A) The hypotenuse of right triangle ABC has a length of 195 units. If all sides of $\triangle ABC$ have integer lengths, compute the perimeters of <u>all</u> possible triangles ABC.

B) Point *P* is located on the diagonal \overline{AC} (not at an endpoint) in square ABCD whose side has length 6. BP = k. For the minimum integer value of k, $\sin \angle APB = q$.

Compute the ordered pair (k,q).



C) In $\triangle ABC$, AC = 7, AB = 13 and $\angle A$ is obtuse. If \overline{BC} has integer length, what is the maximum value of $\cos A$?