

**MASSACHUSETTS MATHEMATICS LEAGUE**  
**DECEMBER 2003**  
**ROUND 1: TRIG. TRIANGLES**

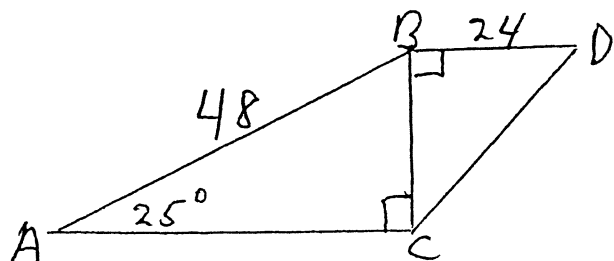
**ANSWERS**

A) 40.2°

B) 57.1

C) 585

A) Given  $\triangle ABC$ ,  $\angle A = 25^\circ$ ,  $\angle C = 90^\circ$ ,  $AB = 48$ . In  $\triangle BCD$ ,  $\angle DBC = 90^\circ$ , and  $BD = 24$ . To the nearest tenth, calculate the degree measure of  $\angle BDC$ .

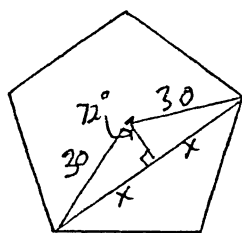


$$BC = 48 \sin 25^\circ$$

$$\tan D = \frac{48 \sin 25^\circ}{24} = 2 \sin 25^\circ$$

$$D = \tan^{-1}(2 \sin 25^\circ) = 40.2^\circ$$

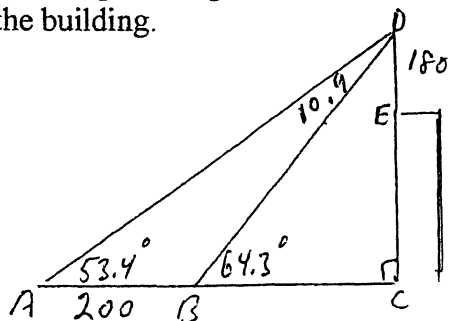
B) A regular pentagon is inscribed in a circle of radius 30 inches. Calculate to the nearest tenth of an inch the length of a diagonal of the pentagon.



$$x = 30 \sin 72^\circ$$

$$d = 2x = 60 \sin 72^\circ = 57.1$$

C) A 180 foot tall antenna is located on top of a building. Some distance from the building the angle of elevation of the top of the antenna is 64.3 degrees. From a point 200 feet farther from the building, the angle of elevation is 53.4 degrees. To the nearest integer, calculate the height of the building.



$$\frac{BD}{\sin 53.4^\circ} = \frac{200}{\sin 10.9^\circ}$$

$$CD = BD \sin 64.3^\circ = \frac{200 \sin 53.4^\circ \sin 64.3^\circ}{\sin 10.9^\circ}$$

$$= 765.1 \quad CE = 765 - 180 = 585$$