MASSACHUSETTS MATHEMATICS LEAGUE CONTEST 4 - JANUARY 2009 SOLUTION KEY

Round 2

A)
$$(2x-1)(x+2) = 25 \Rightarrow 2x^2 + 3x - 27 = 0 \Rightarrow (2x+9)(x-3) = 0 \Rightarrow x = \frac{9}{2}$$

B)
$$12x^5 - 36x^3 = 46x^4 \Rightarrow 2x^3(6x^2 - 23x - 18) = 0 \Rightarrow 2x^3(3x + 2)(2x - 9) \Rightarrow x = 0, -\frac{2}{3}, \frac{9}{2}$$

C)
$$72x^3 - 4x^2 + 9 - 32x^5 = 8x^3(9 - 4x^2) + (9 - 4x^2) = (8x^3 + 1)(9 - 4x^2)$$

As the sum of perfect cubes and the difference of perfect squares, this product factors to $(2x+1)(4x^2-2x+1)(3+2x)(3-2x)$