

**MASSACHUSETTS MATHEMATICS LEAGUE  
CONTEST 2 - NOVEMBER 2016 SOLUTION KEY**

**Team Round**

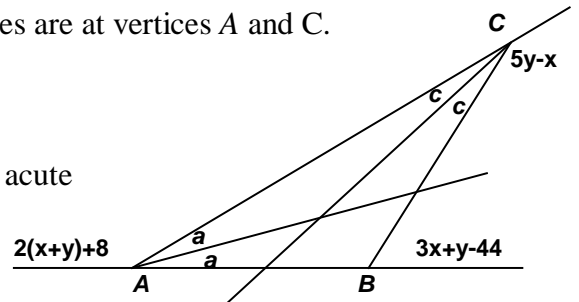
- F) From the diagram it *appears* that the acute interior angles are at vertices A and C.

But is this the case?

$$x + y > 41 \Rightarrow 2(x + y) + 8 > 90 \Rightarrow \angle CAB \text{ is acute}$$

$$\begin{cases} x + y > 41 \\ 2(2y - x > 46) \end{cases} \Rightarrow 5y - x > 92 + 41 = 133 \Rightarrow \angle BCA \text{ is acute}$$

Thus, the interior angles at A and C are in fact acute!



$$a + c + 146 = 180 \Rightarrow a + c = 34$$

$$\Rightarrow 2a + 2c = 68 \Rightarrow 2(x + y) + 8 + (5y - x) = 360 - 68 \Rightarrow x + 7y = 284$$

The exterior angles (one at each vertex) must total  $360^\circ$ .

$$\text{Therefore, } (2(x + y) + 8) + (5y - x) + (3x + y - 44) = 360 \Rightarrow x + 2y = 99$$

$$\text{Subtracting, } 5y = 185 \Rightarrow y = 37, x = 25.$$

The exterior angles are 132, 68 and **160**.