

Homework week 1

①

Name	Ph.
Lydia	1 h
Eugene	2 c
Jeff	3 c
Rick	4 h
Marty	5 c
	6 c

Is it function?

One input has several outputs \Rightarrow not a function

②

$$1) y^2 = x^2 + 1$$

for any x , there's a y .

$$y^2 = (x^2 + 1)^2$$

 $y^2 = 2^2 + 1 = 5$. then It's a function.

$$2) y^2 = x + 1$$

$$y^2 = 1 + 1$$

$$y^2 = 2$$

 $y = \pm 2 \rightarrow$ two outputs for 1 input
not a function

③ onto - each output has at least 1 input.

$$1) f: \{2\} \rightarrow \{2\} \quad f(2) = 3 \text{ n} \quad \text{not onto}$$

 n could be $\frac{1}{3}$
 $not 2 \rightarrow$ so not onto

$$2) g: \{1, 2, 3\} \rightarrow \{a, b, c\} \quad g = \begin{pmatrix} 1 & 2 & 3 \\ c & a & a \end{pmatrix}$$

 b is not in matrix, not onto

$$3) h: \{1, 2, 3\} \rightarrow \{1, 2, 3\} \Rightarrow \text{onto}$$

⑨ one-to-one - each output has at most 1 input

1) $f: \mathbb{Z} \rightarrow \mathbb{Z} : f(n) = 3n \rightarrow$ one-to-one

2) $g: \{1, 2, 3\} \rightarrow \{a, b, c\} : g^2 \begin{pmatrix} 1 & 2 & 3 \\ c & a & a \end{pmatrix}$

Both 2, 3 \rightarrow has a as input
- not one-to-one

3) $h: \{1, 2, 3\} \rightarrow \{1, 2, 3\} \rightarrow$ one-to-one

⑤ $f(x) = \frac{1}{x+2} \quad g(x) = \frac{1}{x} - 2$

$$g = f^{-1} - ?$$

$$f(x) = \frac{1}{x+2} \quad f^{-1}(x) = ?$$

$$y = \frac{1}{x+2}$$

$$x = \frac{1}{y+2}$$

$$x(y+2) = 1$$

$$y+2 = \frac{1}{x}$$

$$y = \frac{1}{x} - 2$$

$$f^{-1}(x) = \frac{1}{x} - 2 = g(x) = \text{Yes}$$

$$6) \text{ 1) } f(x) = 2 + \sqrt{x-4} \quad x \geq 4$$

$$y = 2 + \sqrt{x-4}$$

$$x = 2 + \sqrt{y-4}$$

$$(\sqrt{y-4})^2 = (x-2)^2$$

$$\cancel{y-4} = (x-2)^2$$

$$\cancel{y_1} = (x-2)^2 + 4 \quad \cancel{y_2} = (x-2)^2 + 4$$

$$y-4 = (x-2)^2$$

$$y^2 (x-2)^2 - 4$$

$$f^{-1}(x) = (x-2)^2 + 4 \quad | \quad x \in [2, \infty)$$

$$2) \frac{9}{5} \cdot C = \frac{5}{9} (F - 32) \cdot \frac{9}{5}$$

$$\frac{9}{5} C = F - 32$$

$$F = \frac{9}{5} C + 32$$

$$C = g(F) = \frac{5}{9} (F - 32)$$

$$F = g^{-1}(C) = \frac{9}{5} C + 32$$

8) $g(x) = 2\sqrt{x-4}$

$$D \Rightarrow x \in [4, \infty)$$

$$R \Rightarrow \mathbb{R} \setminus (-\infty, 4] \cup [0, \infty)$$

9) $h(x) = -2x^2 + 4x - 9$ | $D : (-\infty, \infty)$

~~Complete the square~~

$$= -(x^2 - 2x + 1) - 9 - 1$$

$$= -(x-1)^2 - 10$$

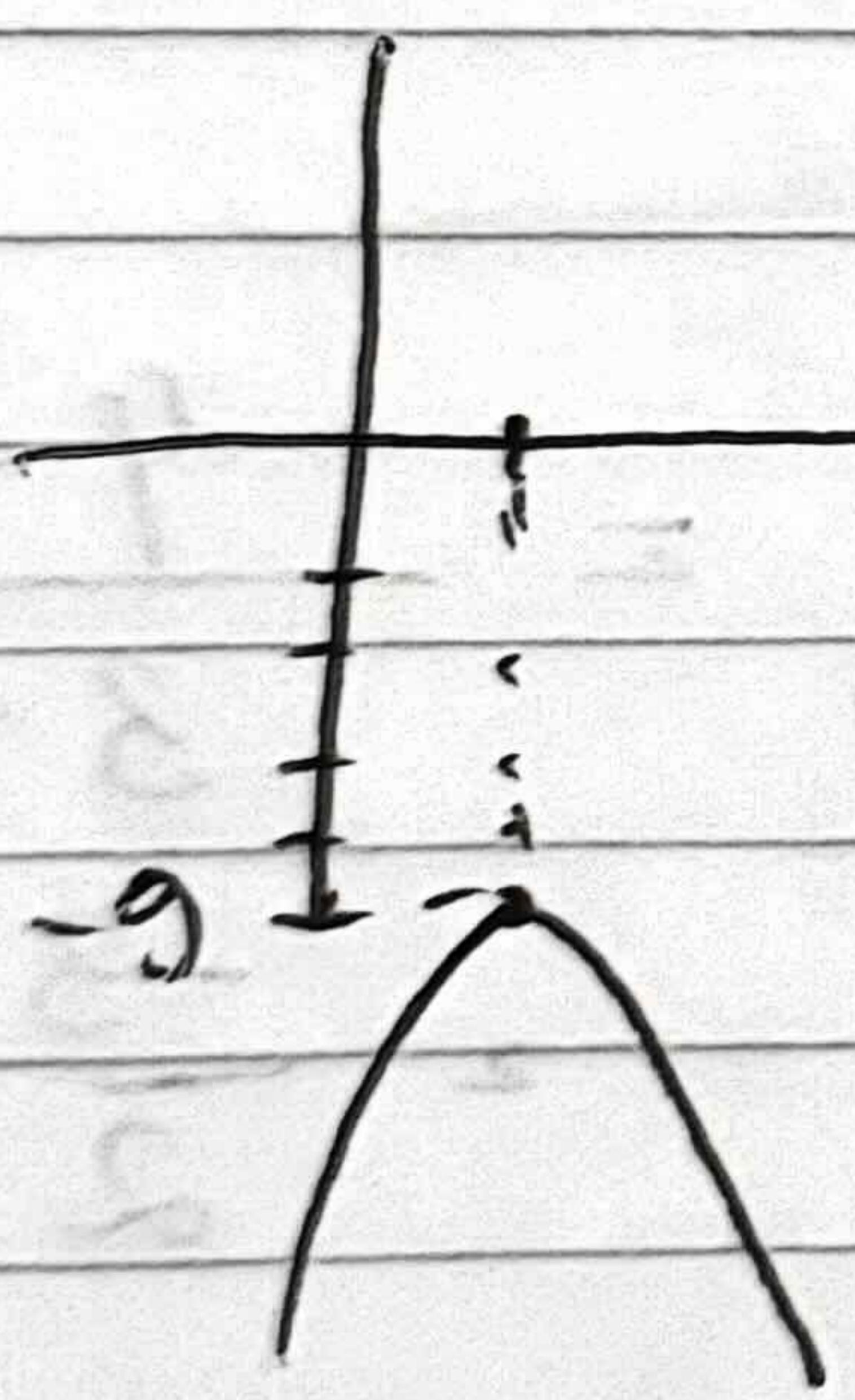
look down (-2) coeff.

$$\text{vertex: } -\frac{b}{2a} \quad a = -2, b = 4$$

$$= -\frac{4}{2 \cdot (-2)} = 1$$

$$x^2 + y^2 = -9$$

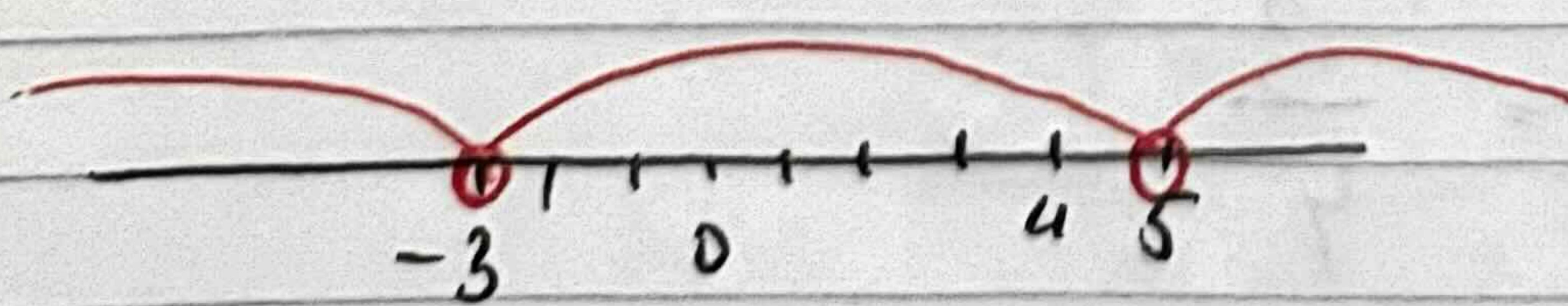
$$R : (-\infty, -9]$$



10) $f(x) = \frac{x-4}{x^2 - 2x - 15}$ | $D : ?$

$$\left(\frac{x-4}{(x-5)(x+3)} \right) > 0$$

~~Roots~~
 $x \neq 5$
 $x \neq -3$



$$D = (-\infty, -3) \cup (-3, 4) \cup (4, 5) \cup (5, \infty)$$

$$1) f(x) = \begin{cases} -2x+1 & -1 \leq x < 0 \\ x^2+2 & 0 \leq x \leq 2 \end{cases}$$

$$-2x+1 = y$$

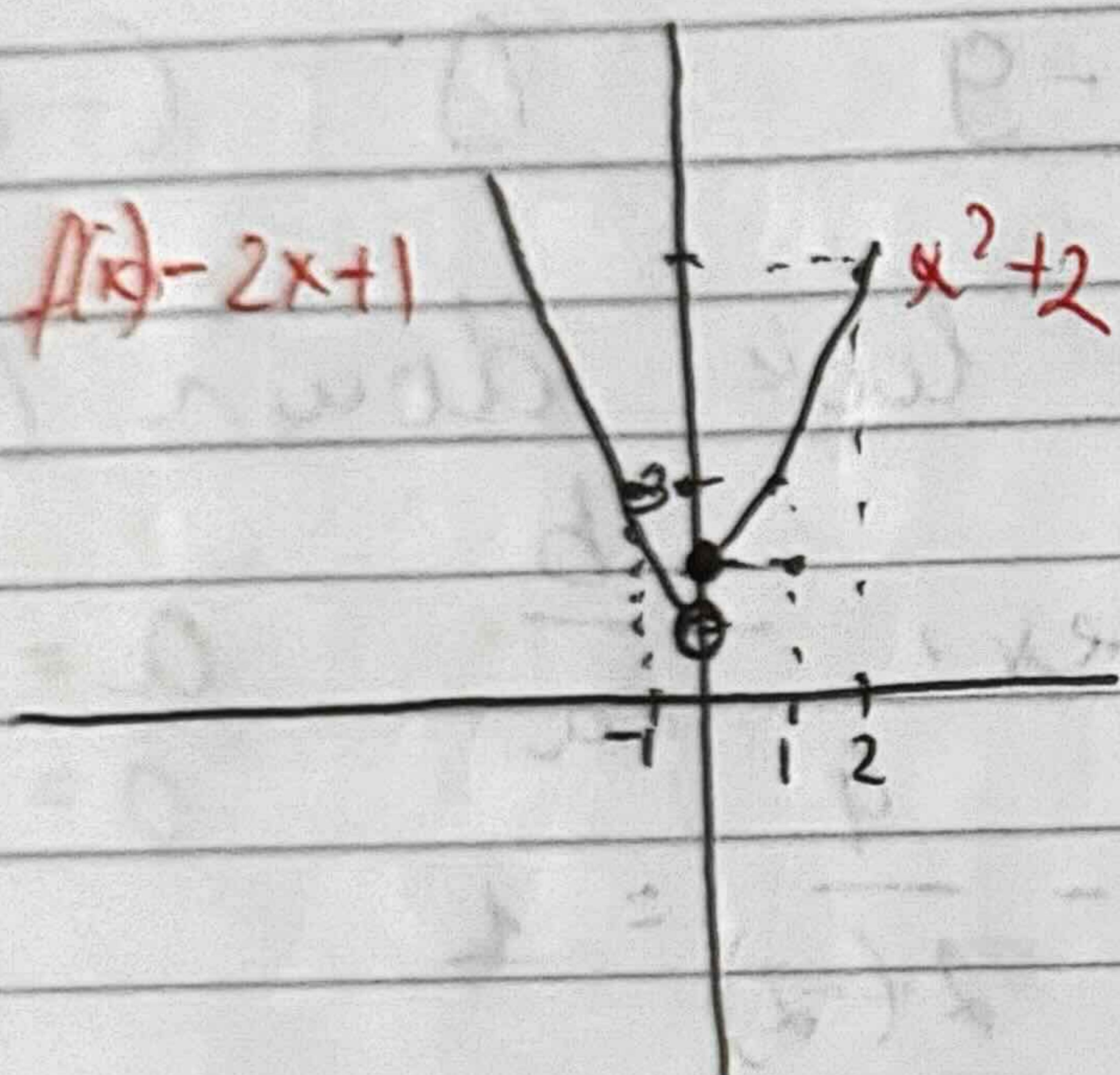
$$-2(-1)+1 = y_3 = y$$

$$x^2+2 = y$$

$$x^2 = 0 \quad y = 2$$

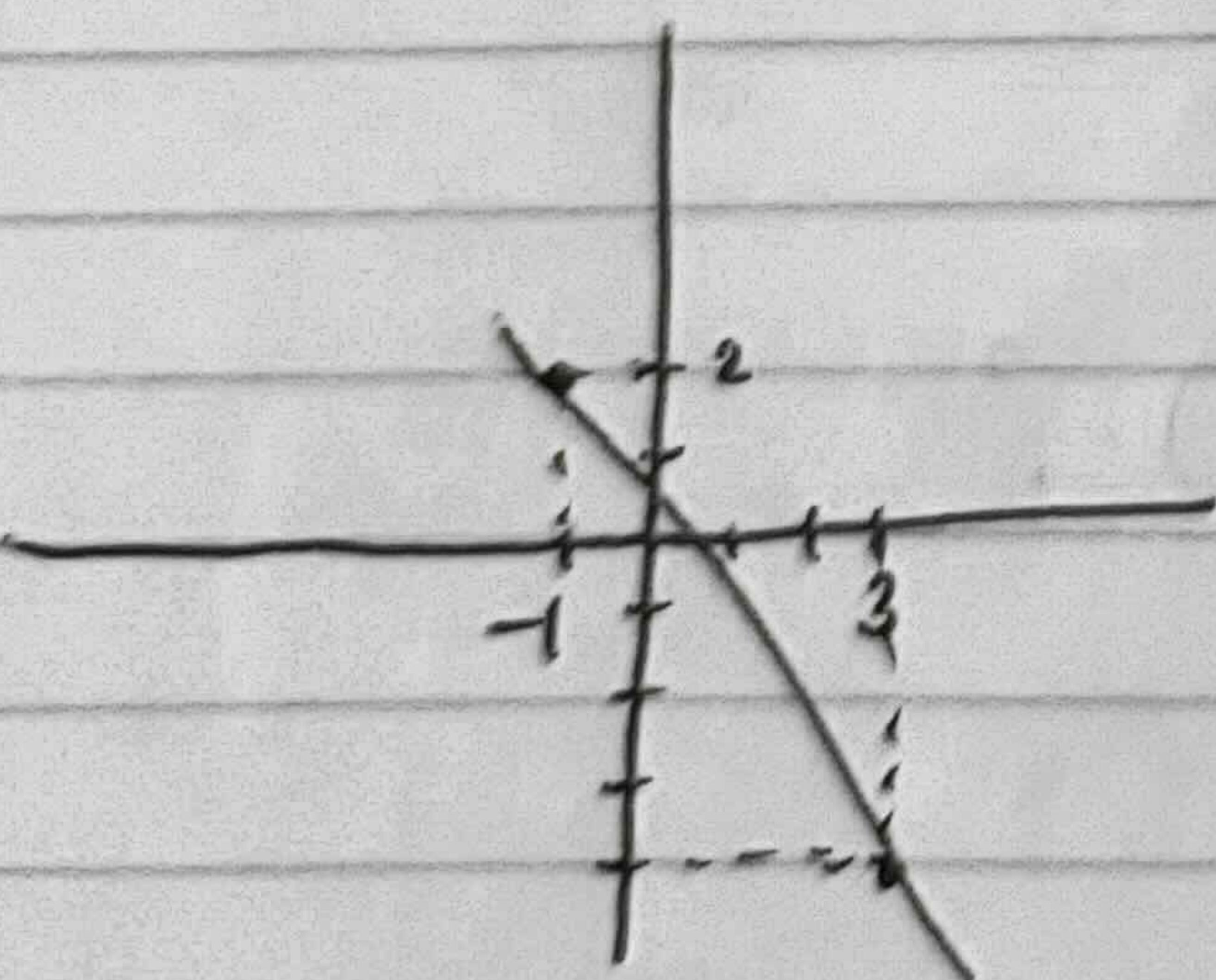
$$x^2 = 1 \quad y = 3$$

$$x^2 = 2 \quad y = 6$$



$$2) \begin{pmatrix} -1, 2 \\ x_1, y_1 \end{pmatrix} \quad \begin{pmatrix} 3, -4 \\ x_2, y_2 \end{pmatrix}$$

$$\text{slope } m = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-4 - 2}{3 - (-1)} = \frac{-6}{4} = -\frac{3}{2}$$



$$3) (1, -1)$$

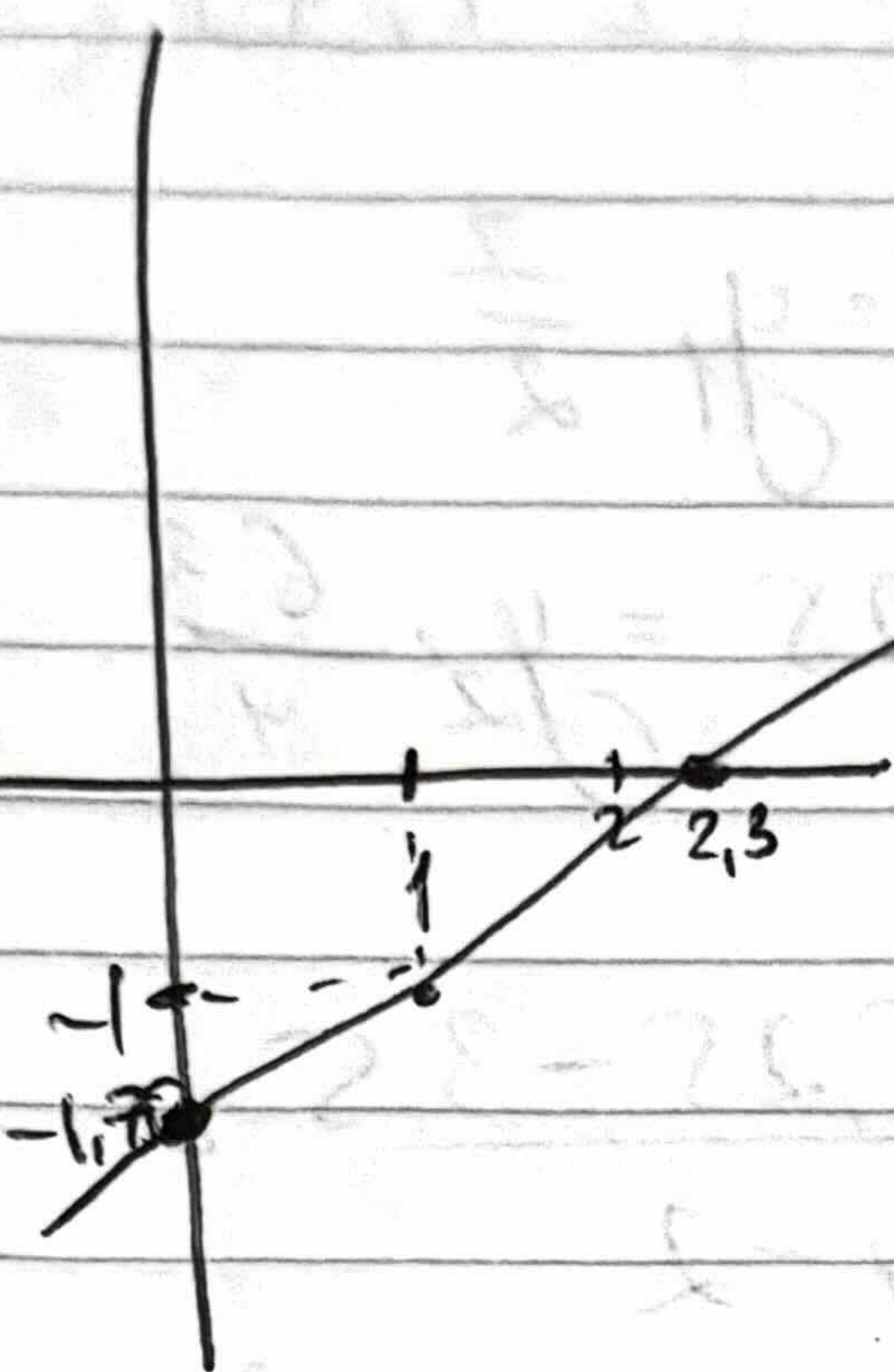
$$m = \frac{3}{4}$$

$$\frac{3}{4} = \frac{y - (-1)}{x - 1} =$$

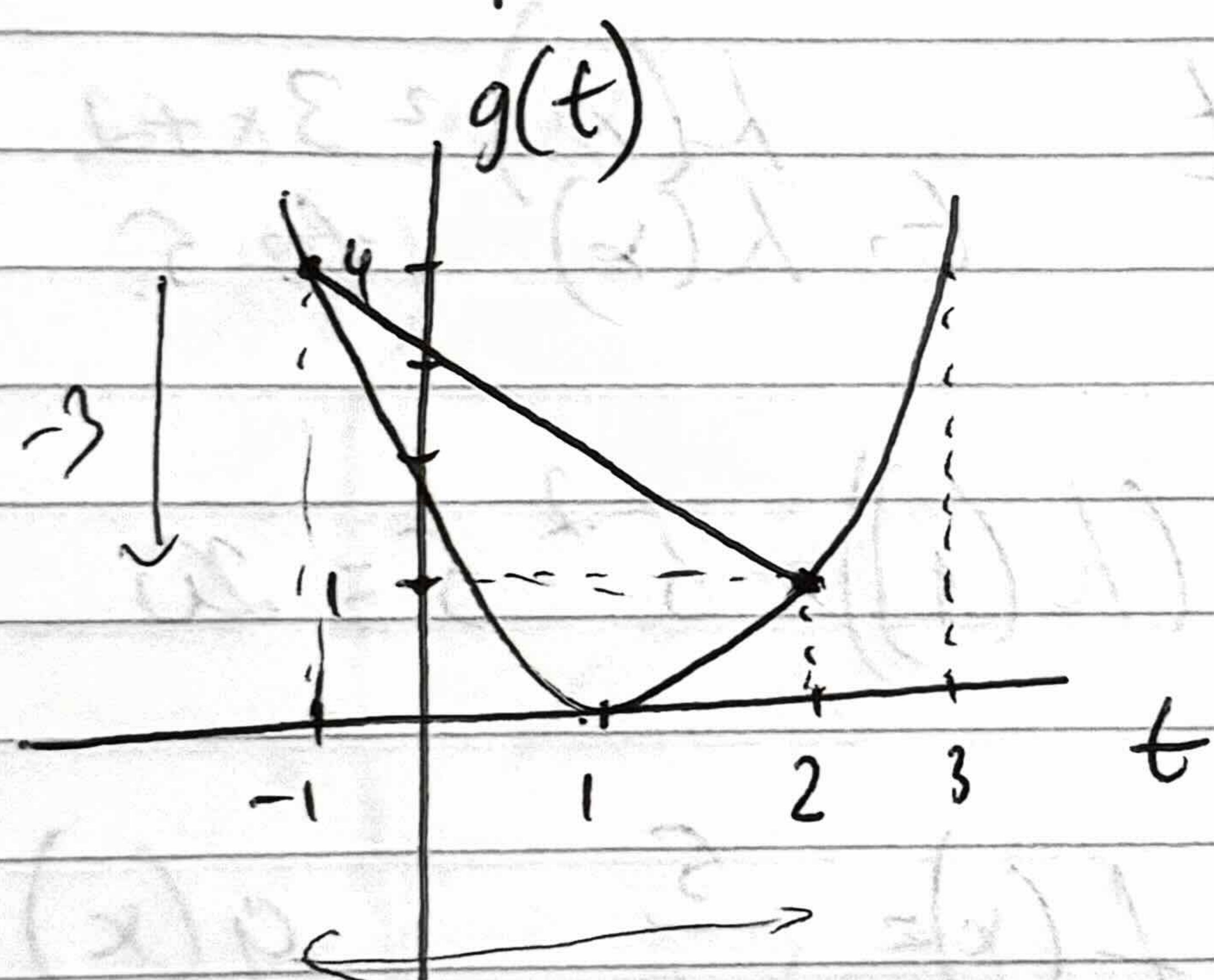
$$\frac{3x - 3}{4} = 4y + 4$$

$$y = 0 \quad x = \frac{7}{3}, 2, 3$$

$$x^2 = 0 \quad y^2 = \frac{7}{4} \quad 2, 1, 2, 3$$



(4)



$$t = -1 \quad g(-1) = 4$$

$$t = 2 \quad (g(2) = 4)$$

$$\Delta t = 3$$

$$\Delta g(t) = -3$$

$$\frac{1-4}{2-(-1)} = \frac{-3}{3} = -1$$

$$15) f(x) = x^2 - \frac{1}{x} \quad \{2, 4\}$$

$$f(x) = 2^2 - \frac{1}{2} = 3,5 = y_1 \frac{7}{2}$$

$$f(x) = 4^2 - \frac{1}{4} = 15,25 = y_2 \frac{63}{4}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{15,25 - 3,5}{4 - 2} = \frac{\frac{63 - 14}{4}}{2} = \frac{49}{8}$$

$$6) f(t) = t^2 - t \quad \begin{matrix} h(x) = 3x+2 \\ h(1) = 5 \end{matrix}$$

$$f(h(1)) =$$

~~$$f(h(1)) = 5^2 - 5 = 20$$~~

$$7) (f \circ g)(x) \quad f(x) = \frac{5}{x-1} \quad g(x) = \frac{4}{3x-2}$$

$$\frac{5}{\left(\frac{4}{3x-2}\right) - 1} \Rightarrow$$

~~$$\frac{4-3x+2}{3x-2} \neq 0$$~~

~~$$\frac{6-3x}{3x-2} \neq 0 \quad x \neq \frac{2}{3}$$~~

~~DS $x \in \mathbb{R} \setminus \left\{ \frac{2}{3} \right\}$~~

$$\frac{4}{3x-2} = 1$$

$$3x-2 = 4$$

$$\frac{3x^2 + 6}{x+2} \quad x \neq -2$$

$$x \in \left(-\infty, \frac{2}{3}\right) \cup \left(\frac{2}{3}, 2\right) \cup (2, \infty)$$

$$(8) \quad (g-f)(x) = ? \quad \left(\frac{g}{f}\right)x - ?$$

$$f(x) = x - 1$$

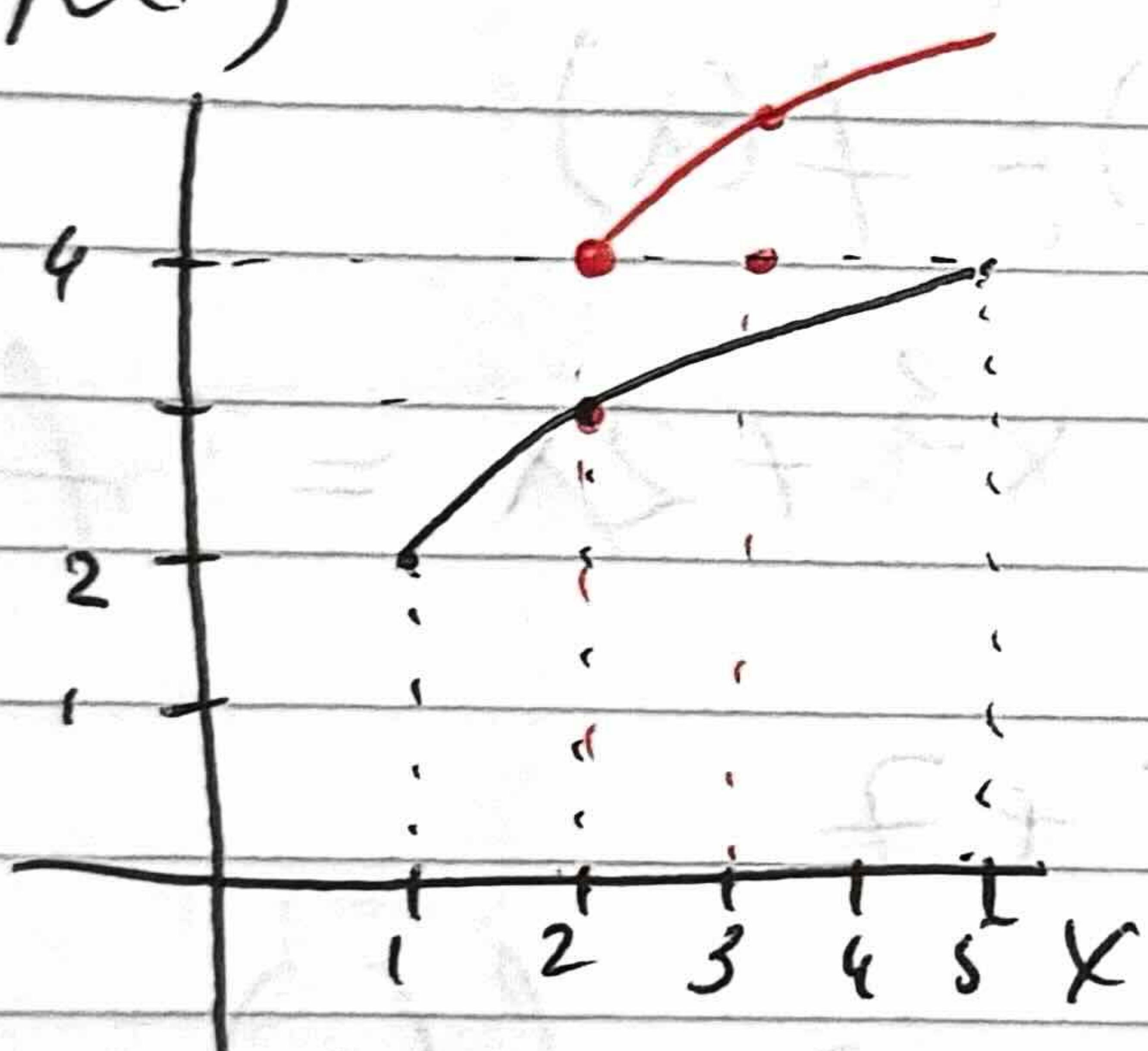
$$g(x) = x^2 - 1$$

$$x^2 - 1 - x + 1 = x^2 - x = x(x-1)$$

$$\frac{x^2 - 1}{x-1} = \frac{(x-1)(x+1)}{(x-1)} = x+1 \quad x \neq 1$$

not the same

$$(9) \quad h(x)$$



$$y = ax^2 + bx + c$$

$$\text{vertex } x = \frac{-b}{2a}$$

$$(1, 2) \quad (2, 3)$$

$$2 = a \cdot 1^2 + b \cdot 1 + c$$

$$3 = a \cdot 2^2 + b \cdot 2 + c$$

$$\boxed{y = x^2 + 2x}$$

$$3a + b = 1$$

$$b = 1 - 3a \Rightarrow -2$$

$$a = \frac{-1 + 3a}{2a}$$

$$2a^2 - 1 + 3a \\ 1 = a$$

$$h(x) = f(x-1) + 2$$

$$h(x) = \sqrt{x-1} + 2$$

$$D: x \in [1, \infty) \setminus \{2\}$$