

Time Series Forecasting

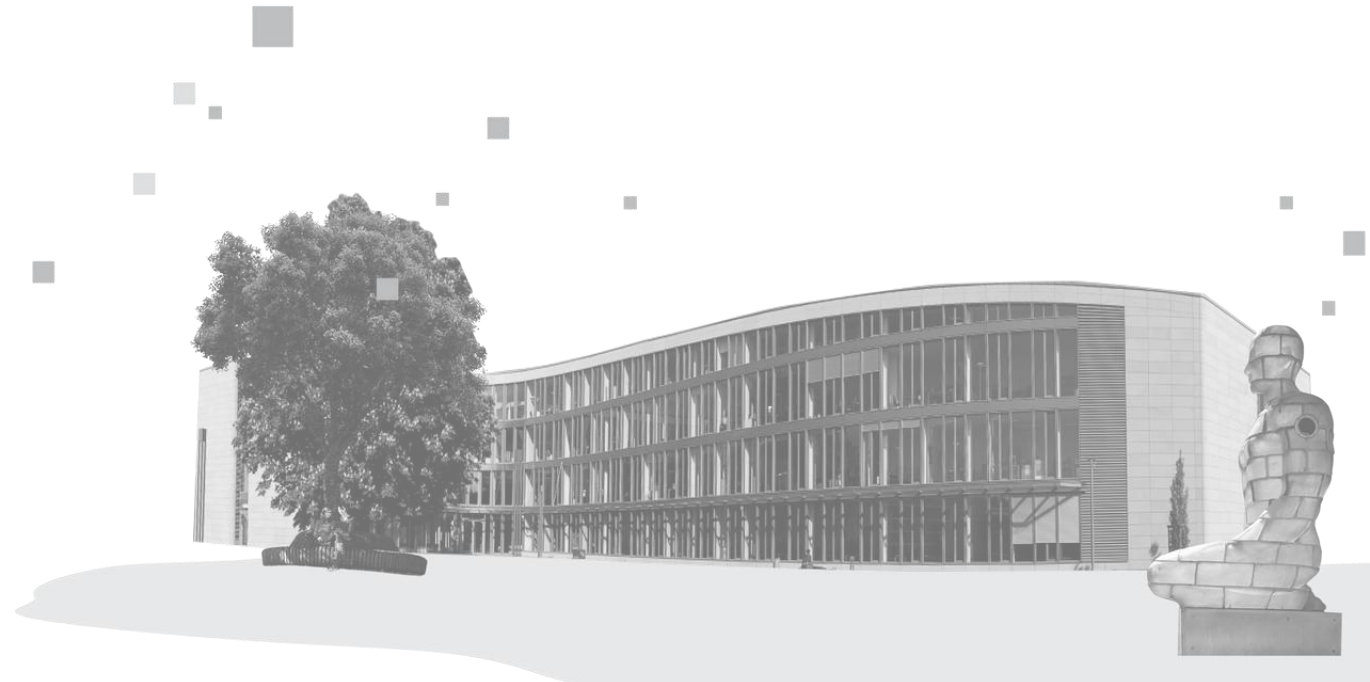
1.8 Statistical Methods II

Autoregressive models

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What we'll cover in this video



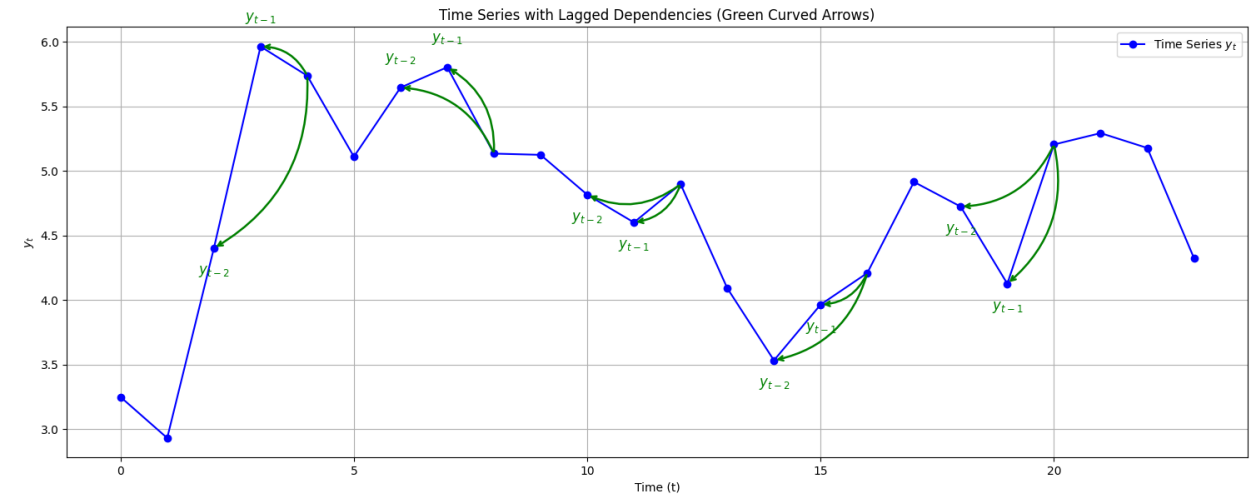
- Introduction to Autoregressive (AR) Models
- Moving Average (MA) Models
- ARMA and ARIMA Models — Handling Trends and Stationarity
- Seasonal Extensions: SARIMA, AutoARIMA, ARIMAX/SARIMAX

Autoregressive (AR) Models

- Models that predicts future values using a linear combination of past values
- Work best when the time series is stationary
- The number of past values used is called the order p
- Formula:

$$y_t = c + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \epsilon_t$$

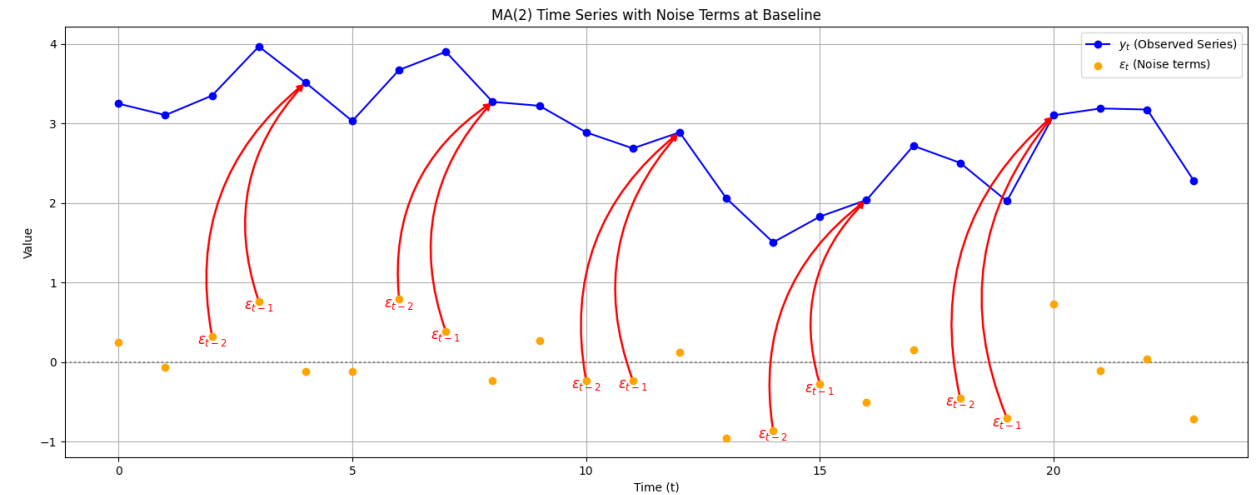
- y_t is the value at time t
- c is a constant
- ϕ_i are model coefficients
- ϵ_t is the error term (noise)



$$y_t = 3 + 0.7y_{t-1} - 0.3y_{t-2} + \epsilon_t$$

Moving Average (MA) Models

- Instead of using past values, MA models use past forecast errors to predict the current value
- The number of past errors considered is called the order q
- Formula:
- $y_t = \mu + \epsilon_t + \theta_1\epsilon_{t-1} + \theta_2\epsilon_{t-2} + \dots + \theta_q\epsilon_{t-q}$

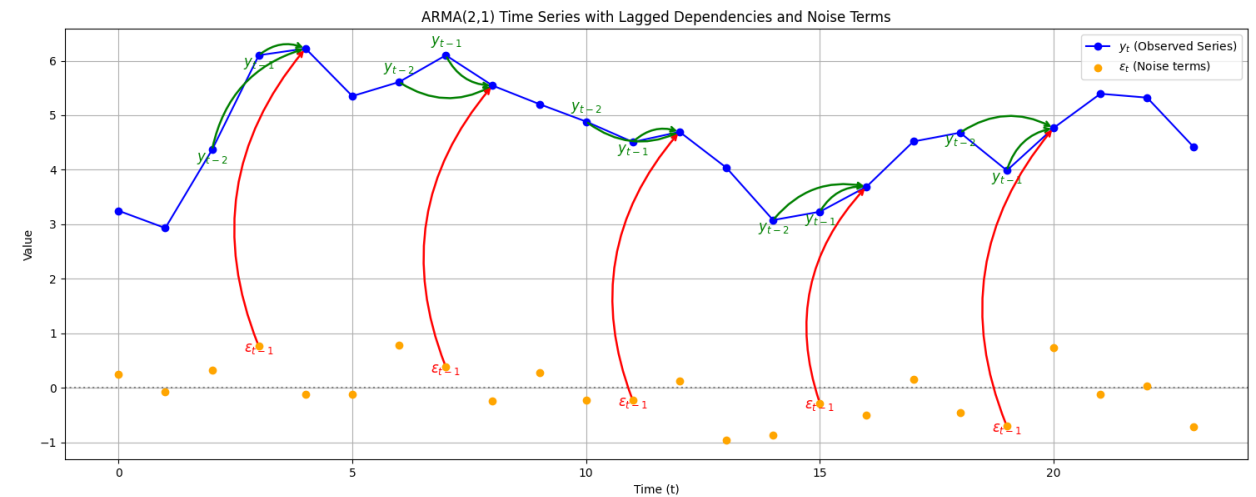


$$y_t = 3 + \epsilon_t + 0.7\epsilon_{t-1} + 0.3\epsilon_{t-2}$$

- y_t is the value at time t
- μ is the mean of the series
- ϵ_t is the current error term
- θ_i are coefficients for past errors

ARMA Models (AutoRegressive Moving Average)

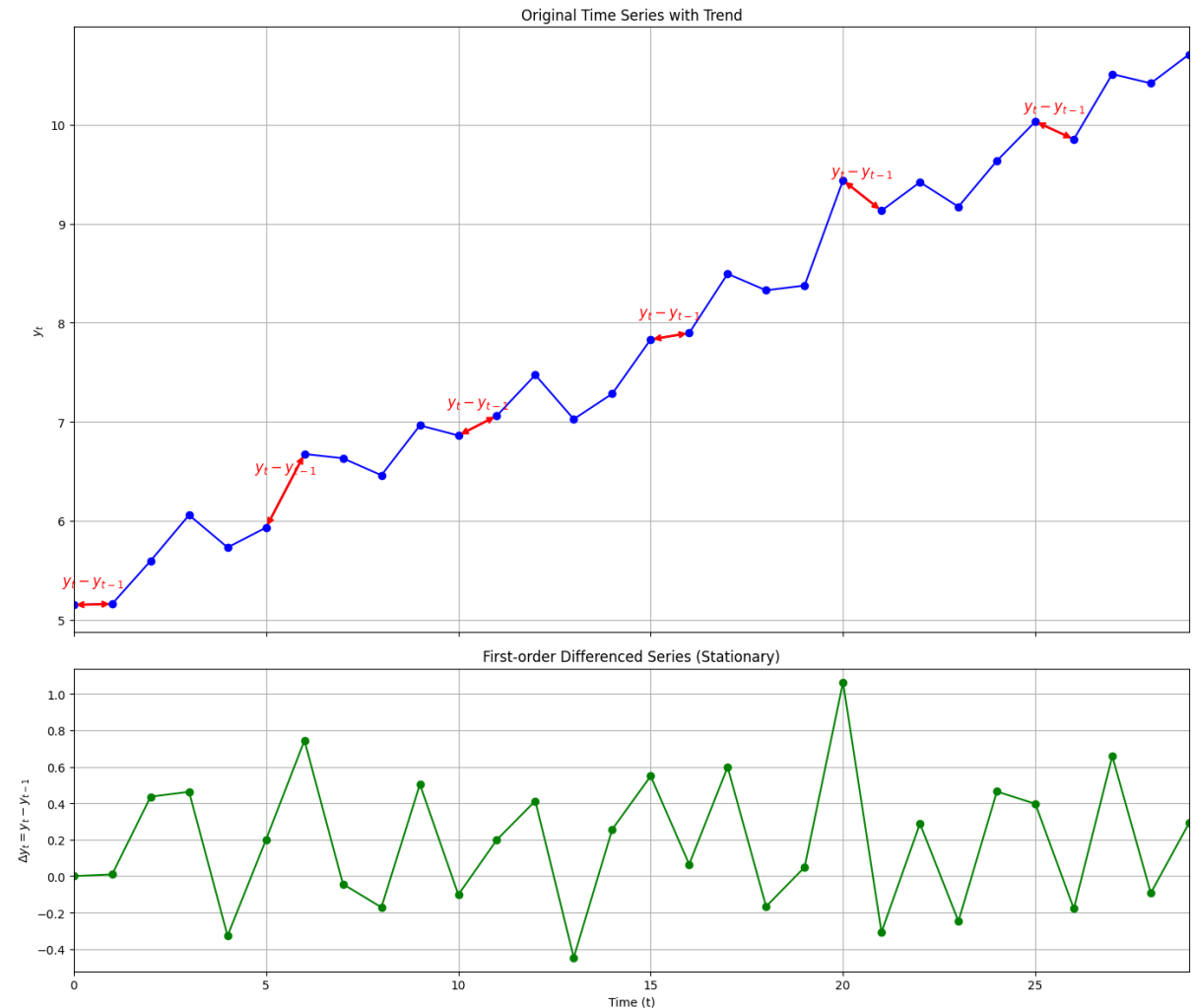
- Combines AR (AutoRegressive) and MA (Moving Average) models
- Uses both past values and past forecast errors to predict the current value
- Suitable for stationary time series
- Captures complex patterns by balancing memory of past data and adjustments for recent shocks



$$y_t = 3 + 0.7y_{t-1} - 0.3y_{t-2} + 0.5\varepsilon_{t-1} + \varepsilon_t$$

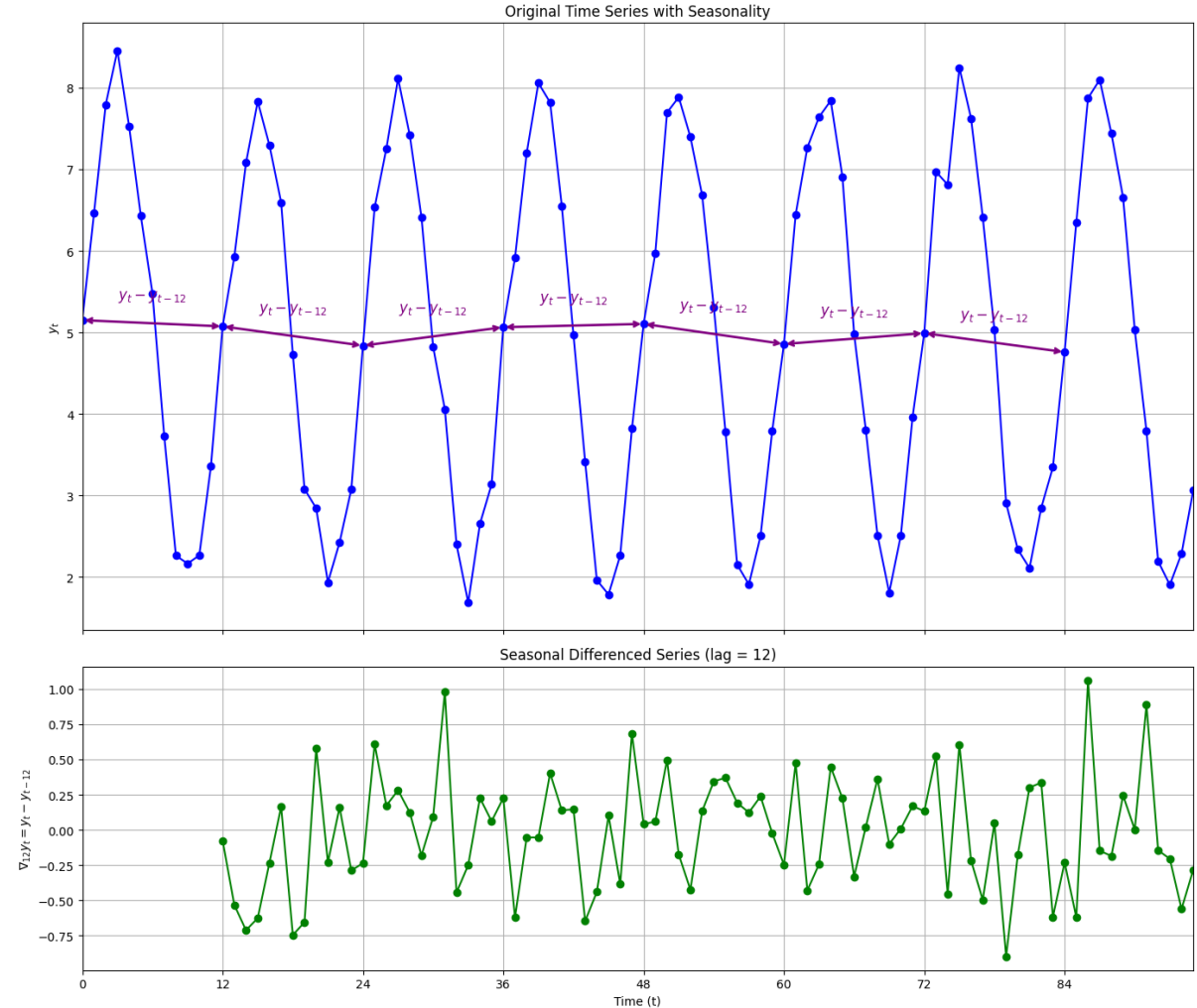
ARIMA Models (AutoRegressive Integrated Moving Average)

- Extends ARMA to handle non-stationary time series. Adds the 'Integrated' (I) part, which means applying differencing to remove trends and stabilize the series
- Differencing means looking at the changes between consecutive points instead of raw values
- Very flexible and powerful for real-world data with trends or slow changes
- Parameters:
 - p = order of AR
 - d = number of differencing steps
 - q = order of MA



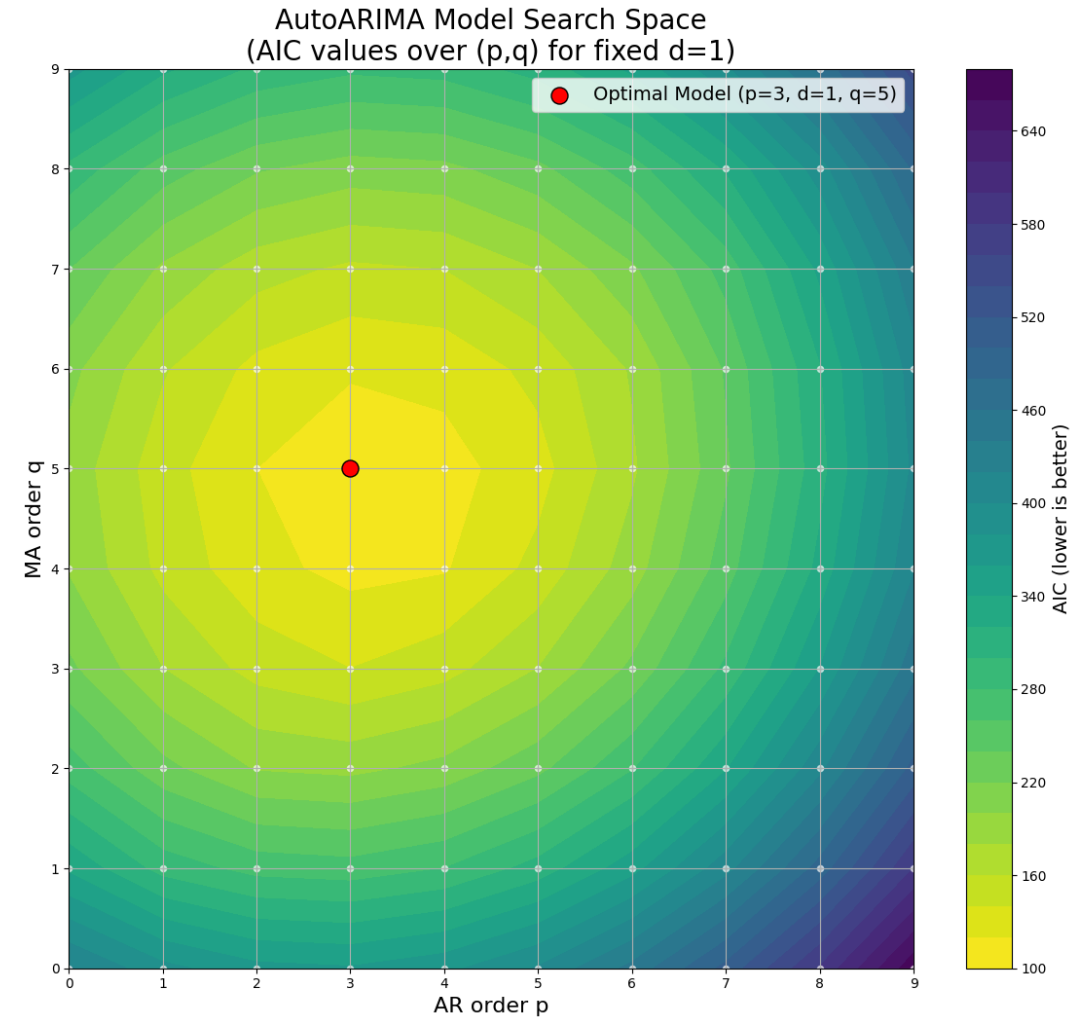
SARIMA Models (Seasonal ARIMA)

- Extends ARIMA to handle seasonality
- Adds seasonal terms to the AR, I, and MA components
- Captures repeating seasonal
- It adds new parameters
 - P = seasonal order of AR
 - D = seasonal order of I
 - Q = seasonal order of MA
 - m = length of the seasonal cycle
- Useful for complex data with both trends and seasonality



AutoARIMA

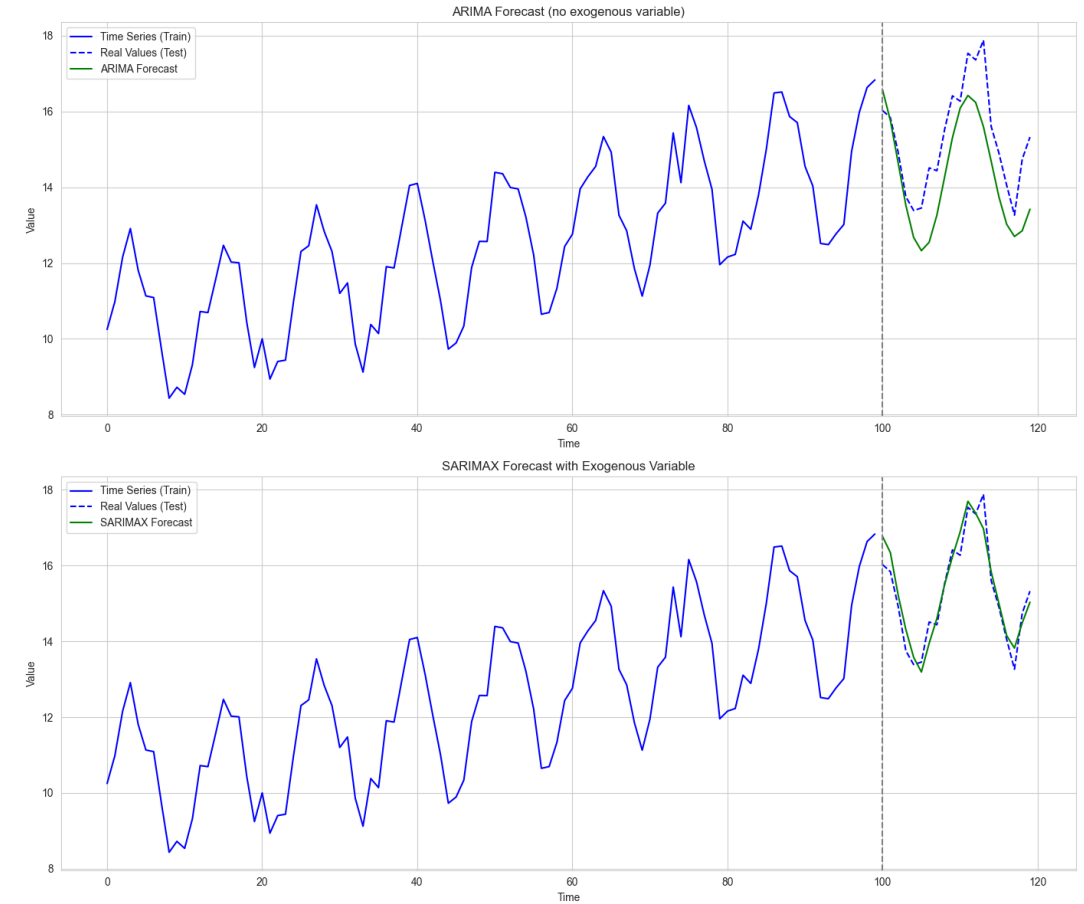
- Automated approach to select the best ARIMA or SARIMA model parameters
- Searches over combinations of p , d , q , and seasonal P , D , Q , m to find the optimal model
- Uses statistical criteria like AIC (Akaike Information Criterion) or BIC (Bayesian Information Criterion) to evaluate models
- Saves time and reduces guesswork in model selection
- Ideal for beginners and practical when working with many datasets



ARIMAX / SARIMAX Models



- Extensions of ARIMA and SARIMA that include exogenous variables
- Help improve forecasting by incorporating additional information beyond the time series itself
- Useful when other factors influence the target series, like promotions, weather, or economic indicators
- Parameters and seasonal components work like ARIMA/SARIMA but with extra inputs
- Flexible models for richer, more accurate forecasts



What we've learnt



- AR, MA, and ARMA models form the foundation for autoregressive modeling
- ARIMA adds differencing to handle trends and make data stationary
- SARIMA extends ARIMA to capture seasonal patterns
- AutoARIMA automates model selection, saving time and effort
- ARIMAX and SARIMAX incorporate external variables to improve forecasts
- Choosing the right model depends on your data's characteristics and available information