

Chapter 11: Computations in a functor context III. Monad transformers

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2019-01-05

Computations within a functor context: Combining monads

- Programs need to combine monadic effects
- “Effect” \equiv what else happens in $A \Rightarrow M^B$ besides computing B from A
- Examples of effects for some standard monads:
 - ▶ **Option** – computation will have no result or a single result
 - ▶ **List** – computation will have zero, one, or multiple results
 - ▶ **Either** – computation may fail to obtain its result
 - ▶ **Reader** – computation needs to read an external context value
 - ▶ **Writer** – some value will be appended to a (monoidal) log
 - ▶ **Future** – computation will be scheduled to run later
- How to combine several effects in the same functor block (**for**/**yield**)?

<pre>// This is not valid Scala! val result = for { i ← 1 to n j ← Future { q(i) } k ← maybeError(j) } yield f(k) // What should be the type of result??</pre>	<pre>// This is not valid Scala! (1 to n).flatMap { i ⇒ Future(q(i)).flatMap { j ⇒ maybeError(j).map { k ⇒ f(k) } } }</pre>
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- Need to compute the type of functor that contains all given effects

How to combine monadic effects

There are several ways of combining two monads into a new monad

- If M_1^A and M_2^A are monads then $M_1^A \times M_2^A$ is also a monad
 - ▶ But $M_1^A \times M_2^A$ describes two separate values with two separate effects
- If M_1^A and M_2^A are monads then $M_1^A + M_2^A$ is usually not a monad
 - ▶ If it worked, it would be a choice between two different values / effects
- If M_1^A and M_2^A are monads then one of $M_1^{M_2^A}$ or $M_2^{M_1^A}$ is often a monad
- Examples and counterexamples:
 - ▶ Combine `Future[A]` and `Option[A]` as `Future[Option[A]]`
 - ▶ Combine $Z \Rightarrow A$ and List^A as $Z \Rightarrow \text{List}^A$
 - ▶ But `Either[Z, Future[A]]` and `Option[Z \Rightarrow A]` are not monads
 - ▶ Neither `Future[State[A]]` nor `State[Future[A]]` are monads
- The order of effects matters when composition works both ways:
 - ▶ Combine `Either` ($M_1^A = Z + A$) and `Writer` ($M_2^A = W \times A$)
 - ★ as $Z + W \times A$ – either compute result and write a message, or all fails
 - ★ as $(Z + A) \times W$ – message is always written, but computation may fail
- Find a general way of defining a new monad for combined effects
- Derive properties required for the combined monad

- 1 For a given