Chapter 11: Computations in a functor context III. Monad transformers

Sergei Winitzki

Academy by the Bay

2019-01-05

Computations within a functor context: Combining monads

- Programs need to combine monadic effects
- "Effect" \equiv what else happens in $A \Rightarrow M^B$ besides computing B from A
- Examples of effects for some standard monads:
 - ▶ Option computation will have no result or a single result
 - ▶ List computation will have zero, one, or multiple results
 - ▶ Either computation may fail to obtain its result
 - ▶ Reader computation needs to read an external context value
 - ▶ Writer some value will be appended to a (monoidal) log
 - ▶ Future computation will be scheduled to run later
- How to combine several effects in the same functor block (for/yield)?

• map replaces the last left arrow, flatMap replaces other left arrows

How flatMap works with lists

- consider List(x1, x2, x3).flatMap(x \Rightarrow f(x))
- assume that

```
f: X \Rightarrow List[Y]
f(x1) = List(y0, y1)
f(x2) = List(y2)
f(x3) = List(y3, y4, y5, y6)
```

• then the result is List(y0, y1, y2, y3, y4, y5, y6)

Exercises I

- For a given Set[Int], compute all subsets (w, x, y, z) of size 4 such that w < x < y < z and w + z = x + y
- ② Given 3 sequences xs, ys, zs of type Seq[Int], compute all (x, y, z)such that $x \in xs$, $y \in ys$, $z \in zs$ and x < y < z and x + y + z < 10
- Solve the *n*-queens problem on an $3 \times 3 \times 3$ cube
- Write a tiny library for arithmetic using Future's; use it to compute 1+2+...+100 via for/yield and verify the result. E.g. implement:

```
const: Int ⇒ Future[Int]
add(x: Int): Int \Rightarrow Future[Int]
isEqual(x: Int): Int ⇒ Future[Boolean]
```

- Read a file into a string and write it to another file using Java Files and Paths API. Use Try and for/yield to make this safe.
- **6** Given a semigroup W, make a semimonad out of $F^A \equiv E \Rightarrow A \times W$
- Implement a semimonad instance for the (recursive) type constructor $F^A = A + A \times A + F^A + F^A \times F^A$
- Find the largest prime number below 1000 via a simple Sieve of Eratosthenes; use the State[S, Int] monad with S = Array[Boolean]