

# Improving an Exact Solution to the $(l,d)$ Planted Motif Problem

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## Introduction

The  $(l,d)$  planted motif problem  
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## EMS-GT

The EMS-GT algorithm  
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- ▶ DNA motif finding: search for motifs over a set of DNA sequences, allowing for mismatches due to mutation
- ▶ known as a difficult problem in computational biology and CS (proven NP-complete)

# The $(l,d)$ planted motif problem

*Find a motif of length  $l=8$  across 5 DNA sequences, each containing the motif with at most  $d=2$  mismatches.*

```
atcactcgttctcctctaattgtgtaaagacgtactaccgacctta
acgccgaccgggtcgcgaccttgtatagctcctaacgggcatcagc
tcctgactgcacgcgatctcggtagtttctgttcacatcatttt
ggccttcagcatcgtgctcctgctaacacattcccatgcagctt
tgaaaagaatttacggtaaaggatccacatccaatcgtgtgaaag
```

*Motif:* ccacggtt

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acgccgaccggtcgatccttgtatagctcctaacgggcatcagc
tcttgactgcacgcgatctcggtagtttctgttcatcatttt
ggcctcagcatcgtgctcctgctaacacattcccatgcagctt
tgaaaagaatttacggtaaaggatccacatccaatcgtgtgaaag
```

*Motif:* ccatacgtt

Given a set  $\mathcal{S} = \{S_1, \dots, S_n\}$  of  $n$  DNA sequences of length  $L$ , find  $M$ , the set of sub-sequences (motifs) of length  $l < L$  which occur with at most  $d$  mismatches in each sequence in  $\mathcal{S}$ .



# Definitions of key concepts

- ▶  $l$ -mer
- ▶ Hamming distance  $dH(x_1, x_2)$
- ▶  $d$ -neighborhood  $N(x, d)$  of  $l$ -mer  $x$
- ▶  $d$ -neighborhood  $\mathcal{N}(S, d)$  of sequence  $S$

## Definitions of key concepts

- ▶  $l$ -mer

- sequence of length  $l$

For  $l = 7$ ,

$S = \text{acgccgattacatccgatccttgatatagctcctaacgggcatcac}$

↪ **gattaca** is the 6<sup>th</sup>  $l$ -mer in  $S$ .

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- ▶ Hamming distance  $dH(x_1, x_2)$ 
  - number of mismatches between  $l$ -mers  $x_1$  and  $x_2$

$x_1 = \text{gattaca}$

$x_2 = \text{cgttaga}$

$\hookrightarrow x_1$  and  $x_2$  differ in their first, second and sixth characters.

Thus,  $dH(x_1, x_2) = 3$ .

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  - set of all  $l$ -mers having at most  $d$  mismatches with  $x$

$N(\text{gattaca}, 2) = \{$  gattaca,  
aattaca, cattaca, tattaca,  
gcttaca, ggttaca, gtttaca,  
...,  
acttaca, agttaca, atttaca, ..., tcttaca, tggttaca, ttttaca,  
aaattaca, aacttaca, aagttaca, ..., taattaca, tacttaca, tagttaca,  
aataatca, aatcaca, aatgaca, ..., tataatca, tatcaca, tatgaca,  
...,  
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- ▶  $d$ -neighborhood  $\mathcal{N}(S, d)$  of sequence  $S$ 
  - union of  $d$ -neighborhoods of all  $l$ -mers in  $S$

$S = \text{acgccgattacatccgatccttgatatagctcctaacgggcatcac}$

$$\mathcal{N}(S, 2) = N(\text{acgccga}, 2) \cup N(\text{cgccgat}, 2) \cup \dots \cup N(\text{gcatcac}, 2)$$

$\hookrightarrow d$ -neighborhood of first  $l$ -mer in  $S$

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2. *Test candidates*

For every candidate  $c$  in  $C$ , check whether a  $d$ -neighbor of  $c$  appears in each of the remaining sequences  $S_{n'+1}, S_{n'+2}, \dots, S_n$ . If this is the case, accept  $c$  as a motif.

# EMS-GT efficiency strategies

- ▶  $l$ -mer enumeration
- ▶ Bit-based set representation
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1. To develop a speedup technique for EMS-GT that takes advantage of distance-related patterns in the search space;
2. To evaluate the speedup technique with regard to improvement in runtime; and
3. To evaluate the improved version of EMS-GT against state-of-the-art motif search algorithms.

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Performance is benchmarked on “challenging”  $(l,d)$  instances:  $(9,2)$ ,  $(11,3)$ ,  $(13,4)$ ,  $(15,5)$  and  $(17,6)$ .

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- ▶ *Synthetic datasets*

- sets of 20 randomly-generated DNA sequences of length 600, with the same  $(l,d)$  motif planted once in each sequence.

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# Pattern-based speedup technique

# Performance improvement with speedup

# Performance vs PMS8, qPMS9

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Thank you!