

Optimizing Molecular Dynamics

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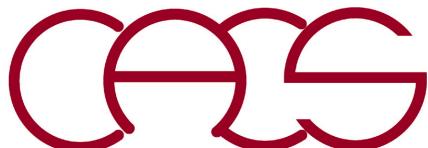
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- Intranode optimization: CPU & memory access
- Internode optimization: Communication

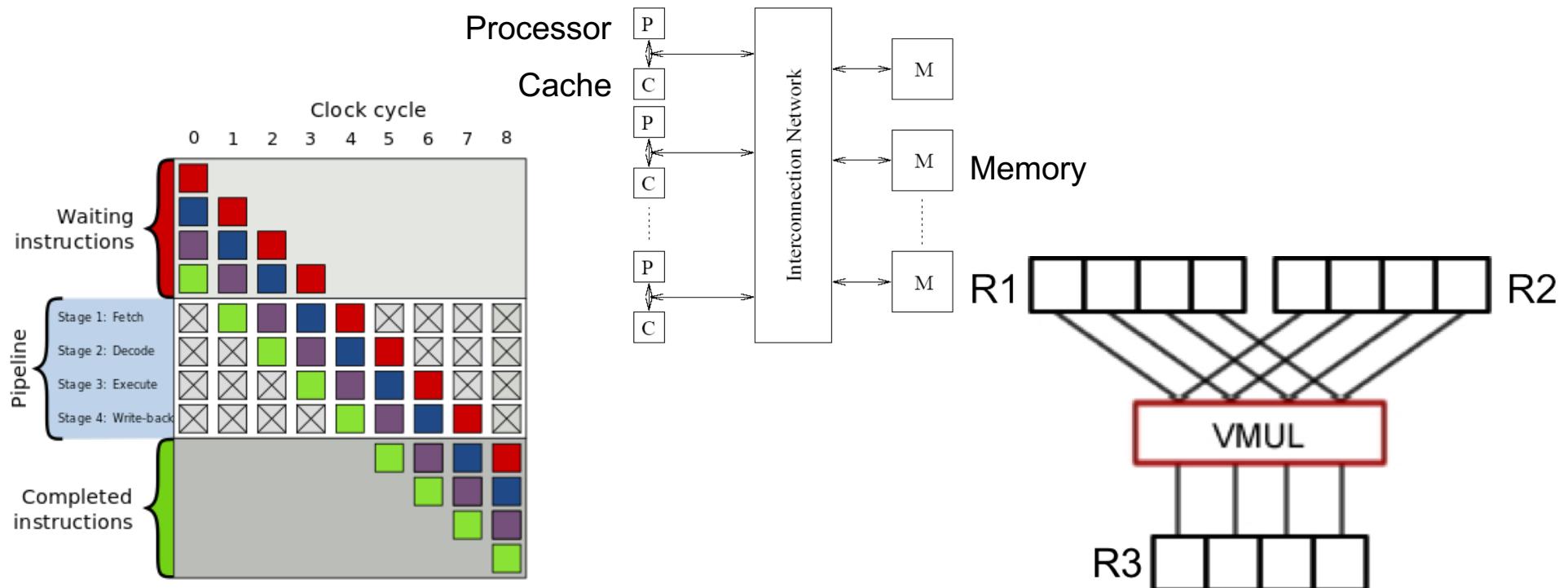


Data/computation locality!



Key Hardware Features

- **Pipelining:** Multiple stages of computation are executed concurrently for multiple data elements
- **Cache:** Fast memory that holds a subset of main memory
- **Vectorization:** Single-instruction multiple-data (SIMD) parallelism on vector registers each holding multiple data elements simultaneously hold



Roofline Model of Performance

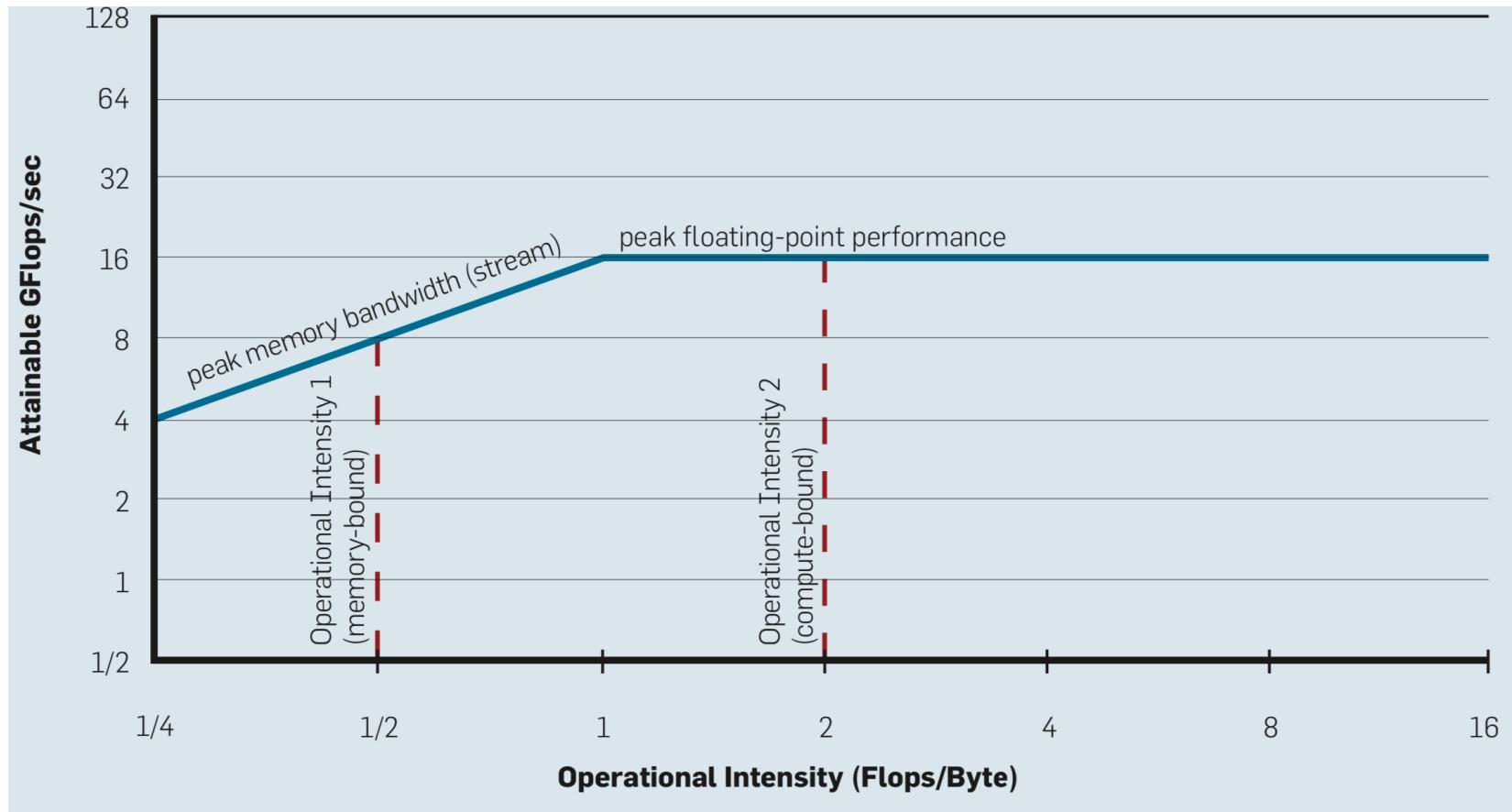
- Off-chip memory bandwidth (from DRAM) is critical for performance (to feed enough data to be operated)
- *Operational intensity*: Operations per byte of DRAM traffic
- *Roofline model*: Predicts the floating-point (fp) performance from operation intensity, theoretical peak fp performance & peak memory bandwidth

$$\text{Attainable fp performance} \left[\frac{\text{Gflop}}{\text{sec}} \right] = \min \left(\text{Peak fp performance} \left[\frac{\text{Gflop}}{\text{sec}} \right], \text{Peak memory bandwidth} \left[\frac{\text{GByte}}{\text{sec}} \right] \times \text{Operational intensity} \left[\frac{\text{flop}}{\text{Byte}} \right] \right)$$

S. Williams *et al.*, *Commun. ACM* **52(4)**, 65 ('09)
V. Elango *et al.*, *ACM. T. Arch. Code Opt.* **11**, 67 ('15)

Roofline Model of Performance

$$\text{Attainable fp} \left[\frac{\text{Gflop}}{\text{sec}} \right] = \min \left(\text{Peak fp} \left[\frac{\text{Gflop}}{\text{sec}} \right], \text{Memory bandwidth} \left[\frac{\text{GByte}}{\text{sec}} \right] \times \text{Operational intensity} \left[\frac{\text{flop}}{\text{Byte}} \right] \right)$$

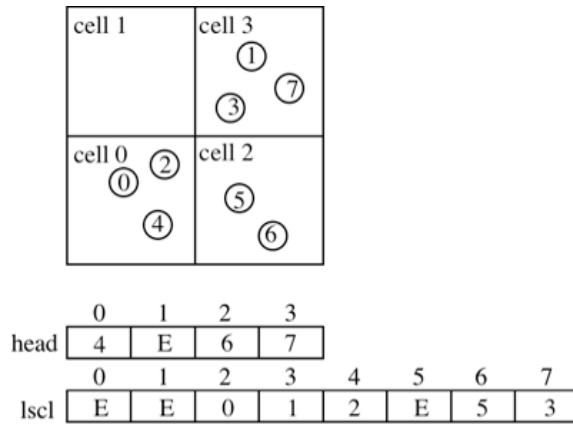


Key: Data/computation locality:

see Berkeley CS267 lecture on “memory hierarchies & matrix multiplication”

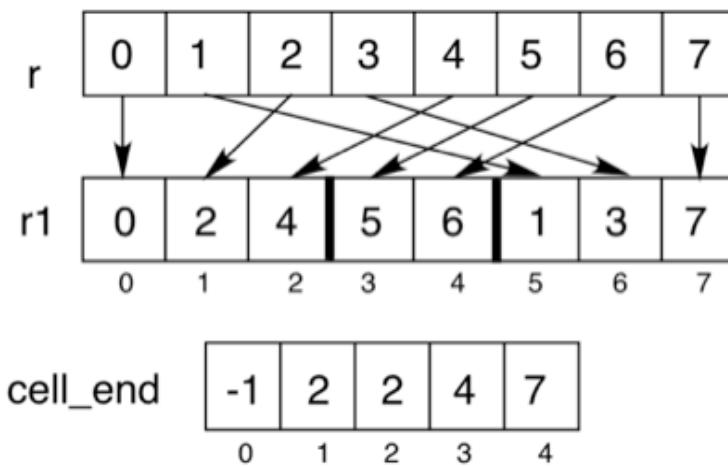
Intranode: Memory Access

- Linked-list cells—irregular memory access pattern



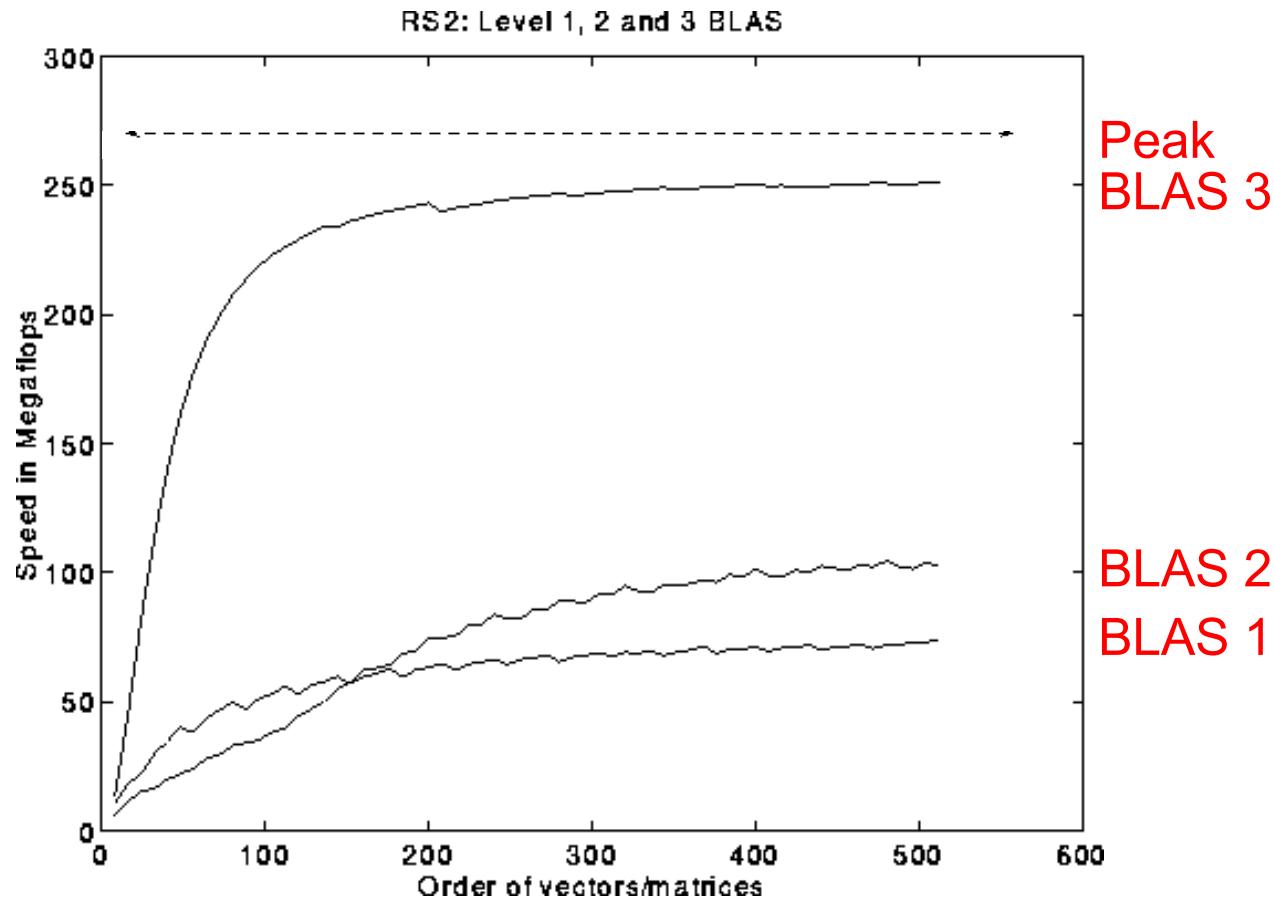
- Data locality: Regular data layout

```
for i = cell_end[c]+1 to cell_end[c+1]
    access r1[i]
endfor
```



BLAS3-Performance Molecular Dynamics?

- BLAS3: $q = \text{flop}/\text{memory access} = (\text{block size})^{1/2}$



- Molecular dynamics: $q = O(n^2)/O(n) = O(n)$: block size
 - > Use of SIMD (single instruction multiple data) instructions on multicore (SSE)?

cf. BLASification in Quantum Mechanics

- Transform from band-by-band to all-band computations to utilize a matrix-matrix subroutine (DGEMM) in the level 3 basic linear algebra subprograms (BLAS3) library
- Algebraic transformation of computations

Example: Nonlocal pseudopotential operation

D. Vanderbilt, *Phys. Rev. B* **41**, 7892 ('90)

$$\hat{v}_{\text{nl}}|\psi_n^\alpha\rangle = \sum_I^{N_{\text{atom}}} \sum_{ij}^{L_{\max}} |\beta_{i,I}\rangle D_{ij,I} \langle \beta_{j,I}| \psi_n^\alpha \rangle \quad (n = 1, \dots, N_{\text{band}})$$



$$\Psi = [|\psi_1^\alpha\rangle, \dots, |\psi_{N_{\text{band}}}^\alpha\rangle] \quad \tilde{\mathbf{B}}(i) = [|\beta_{i,1}\rangle, \dots, |\beta_{i,N_{\text{atom}}}\rangle] \quad [\tilde{\mathbf{D}}(i,j)]_{I,J} = D_{ij,I} \delta_{IJ}$$

$$\hat{v}_{\text{nl}}\Psi = \sum_{i,j}^L \tilde{\mathbf{B}}(i) \tilde{\mathbf{D}}(i,j) \tilde{\mathbf{B}}(j)^T$$

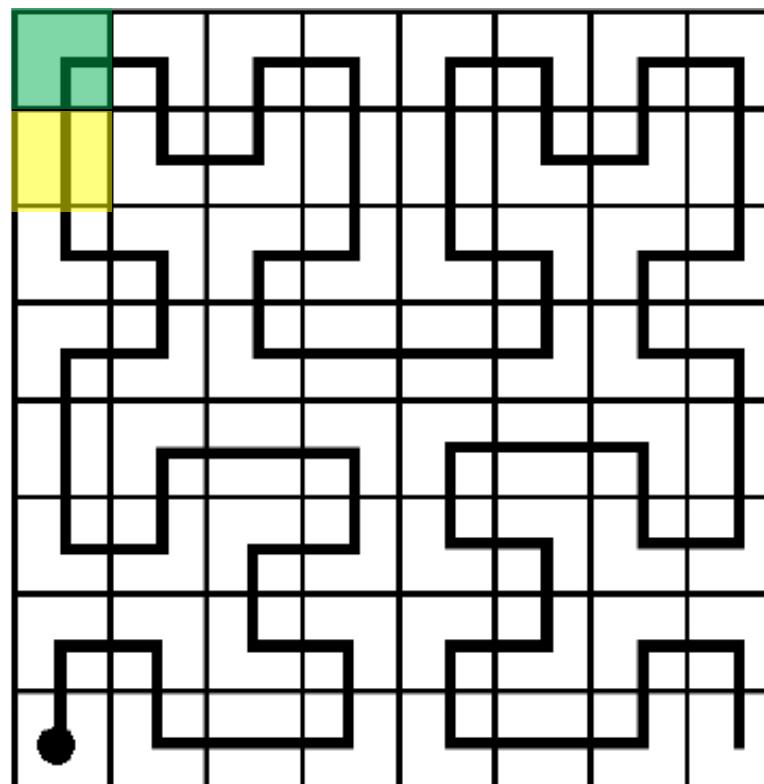
- **50.5% of the theoretical peak FLOP/s performance on 786,432 Blue Gene/Q cores (entire Mira at the Argonne Leadership Computing Facility)**
- **55% of the theoretical peak FLOP/s on Intel Xeon E5-2665**

K. Nomura *et al.*, *IEEE/ACM Supercomputing, SC14* ('14)

Computation Locality

Data-to-computaion locality: How to traverse the linked-list cells?

- **Pair-interaction computation:** Preserve nearest-neighbor cells' proximity in memory
- **Spacefilling curve:** Mapping from the d -dimensional space to one-dimensional list to preserve spatial proximity of consecutive list elements



Hilbert-Peano Curve

- Gray code: a sequence of numbers such that successive numbers have Hamming distance 1

Algorithm: Recursive generation of k-bit Gray code $G(k)$

(1) $G(1)$ is a sequence: 0 1.

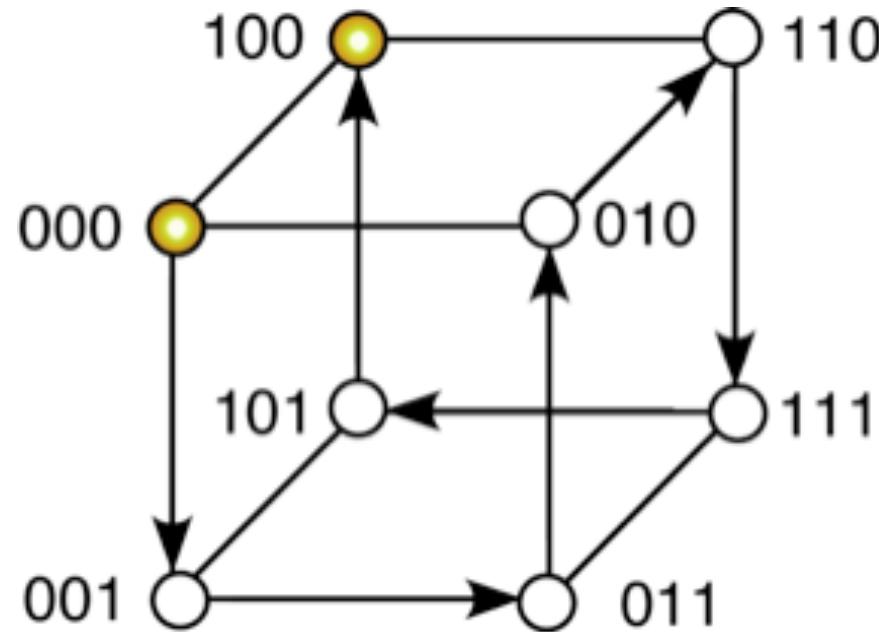
(2) $G(k+1)$ is constructed from $G(k)$ as follows:

- Construct a new sequence by appending a 0 to the left of all members of $G(k)$.
- Construct a new sequence by reversing $G(k)$ & then appending a 1 to the left of all members of the sequence.
- $G(k+1)$ is the concatenation of the sequences defined in steps a & b.

- $G(3)$: 000 001 011 010 110 111 101 100



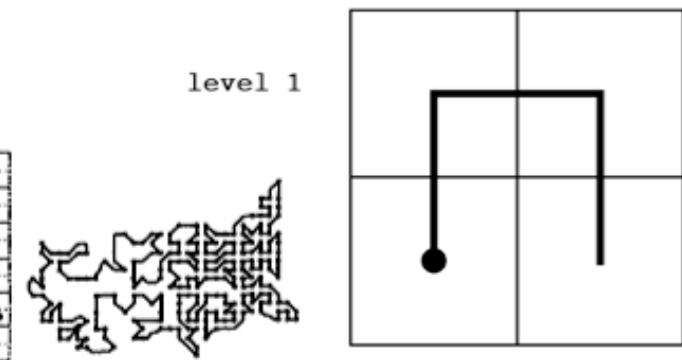
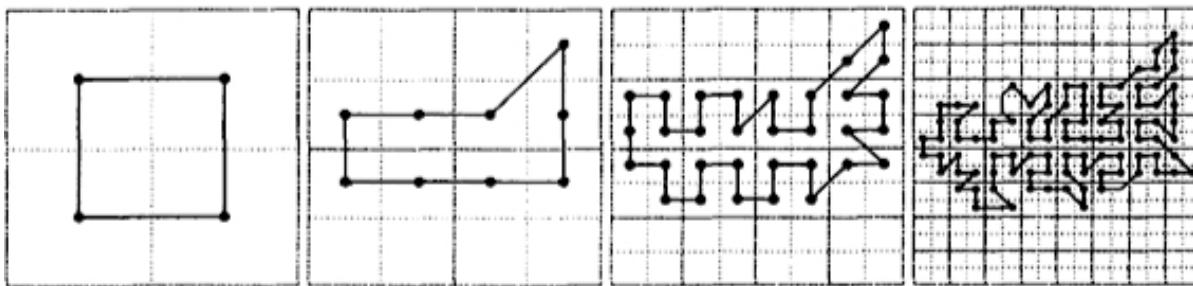
David Hilbert (1862–1943)



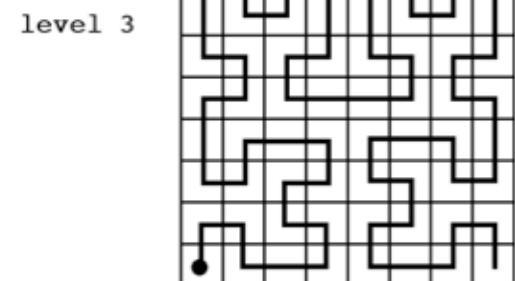
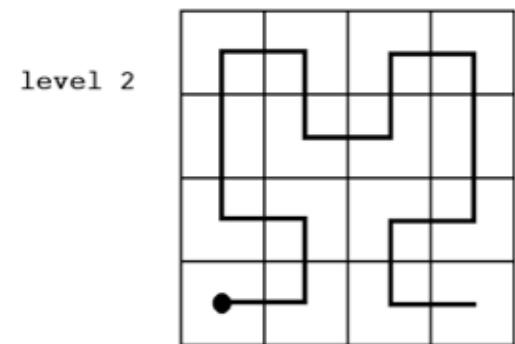
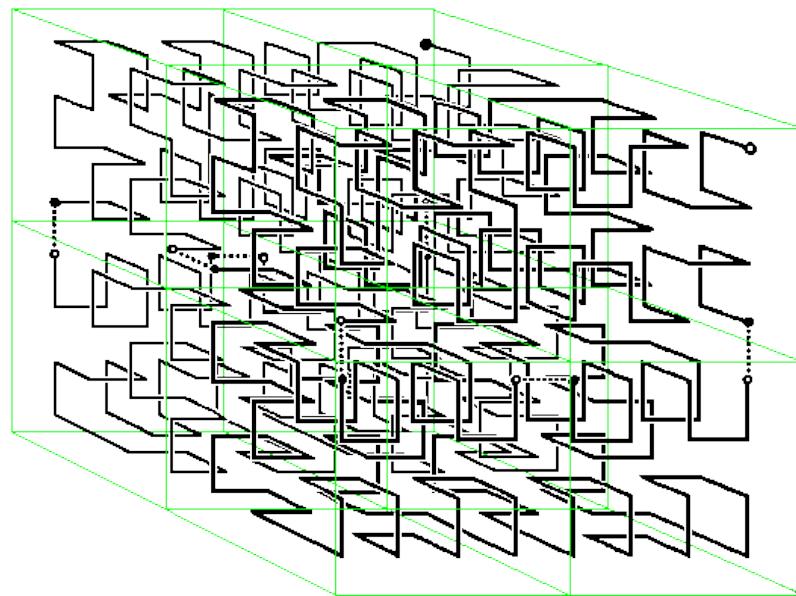
Giuseppe Peano (1858–1932)

Hilbert-Peano Curve

- Hilbert curve: recursive application of the d -dimensional Gray codes
- 2-dimensional Hilbert curve



- 3-dimensional Hilbert curve

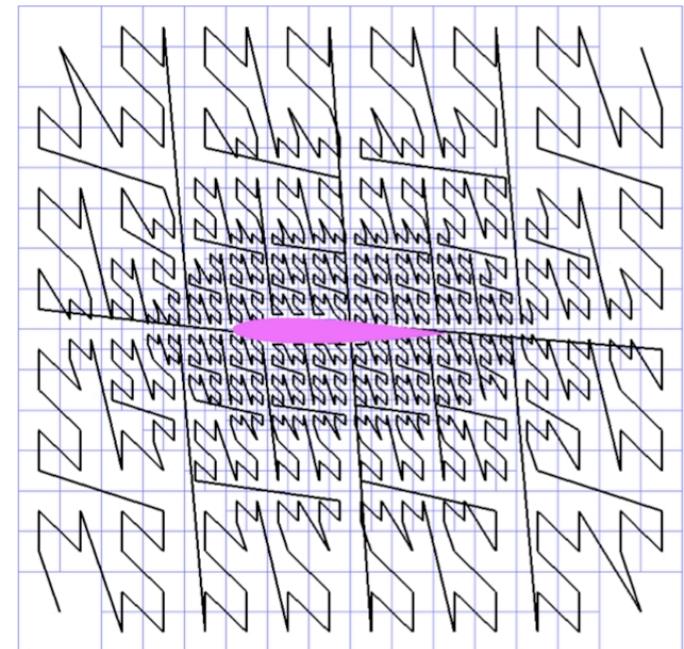
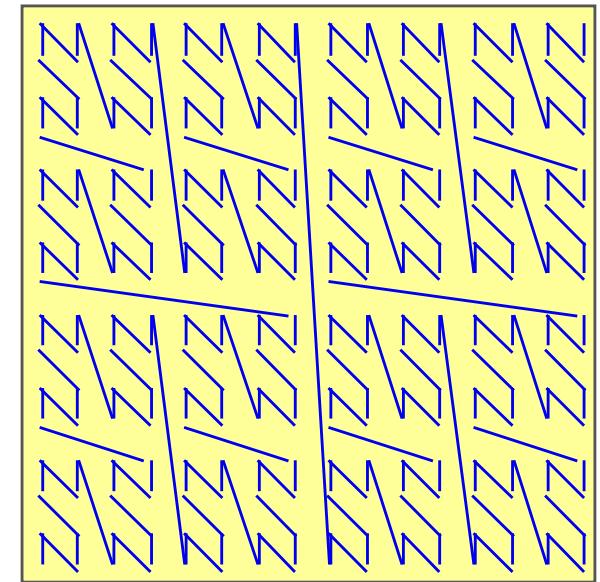
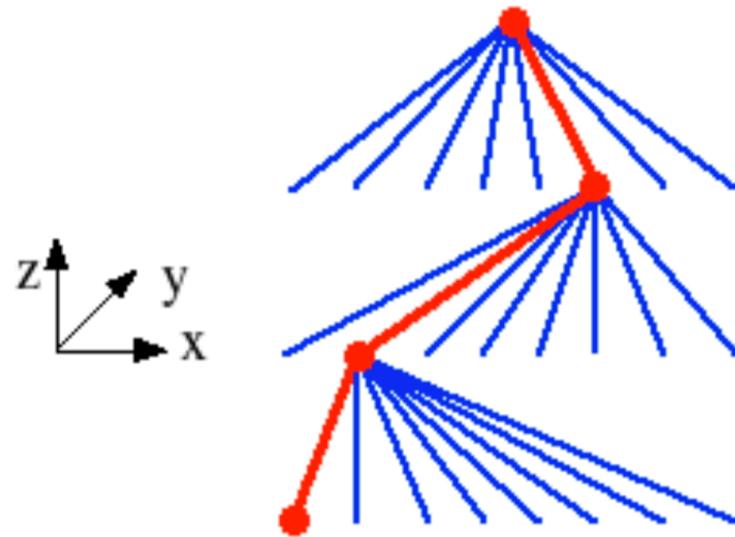
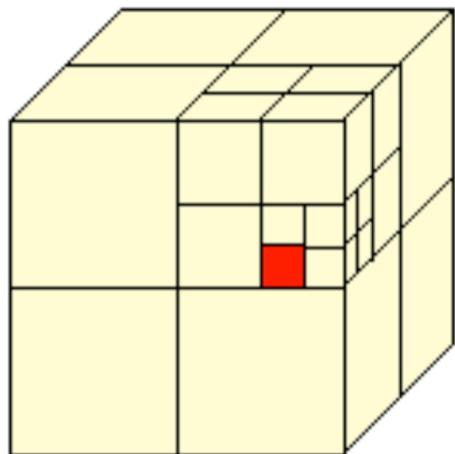


Morton (Z) Curve

- Spacefilling curve based on octree index

$$\begin{array}{r} \mathbf{x} = \quad 1 \quad 1 \quad 0 \\ \mathbf{y} = \quad 0 \quad 0 \quad 0 \\ \mathbf{z} = \underline{1 \quad 0 \quad 0} \\ \mathbf{R} = \underline{\mathbf{101} \quad \mathbf{001} \quad \mathbf{000}} \end{array}$$

- 3D \rightarrow list map preserves spatial proximity
- Multiresolution analysis made easy



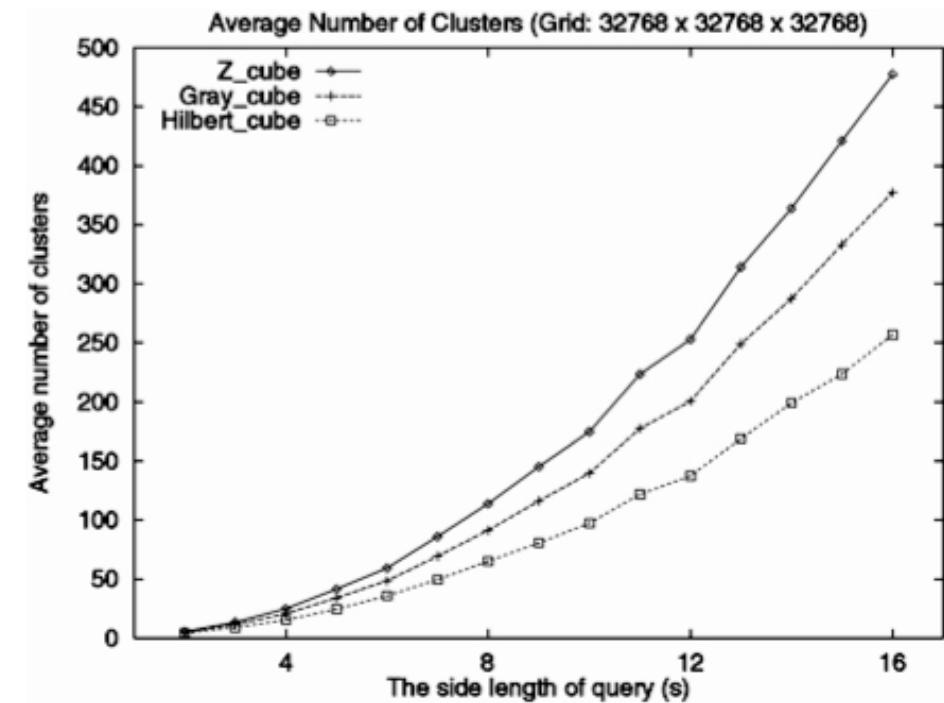
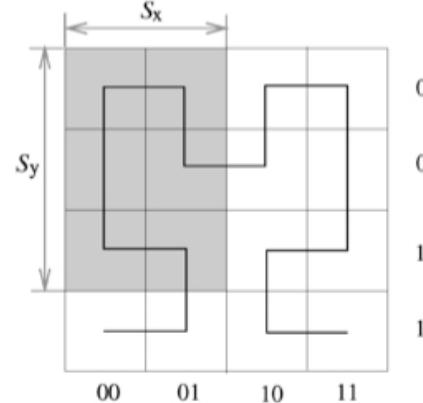
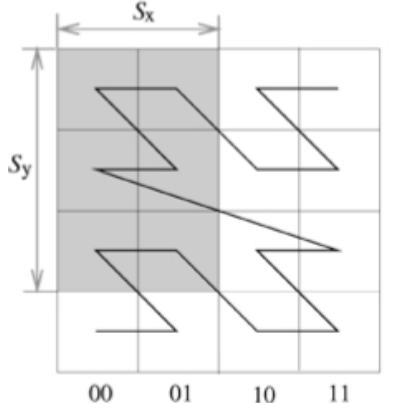
Analysis of Data Locality

124

IEEE TRANSACTIONS ON KNOWLEDGE AND DATA ENGINEERING, VOL. 13, NO. 1, JANUARY/FEBRUARY 2001

Analysis of the Clustering Properties of the Hilbert Space-Filling Curve

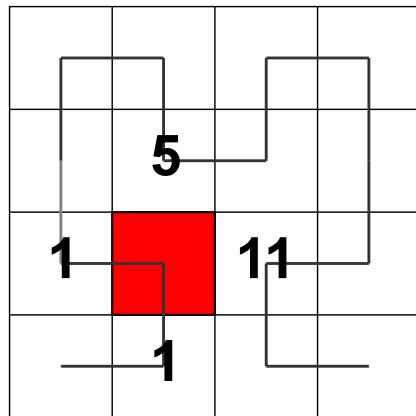
Bongki Moon, H.V. Jagadish, Christos Faloutsos, *Member, IEEE*, and
Joel H. Saltz, *Member, IEEE*



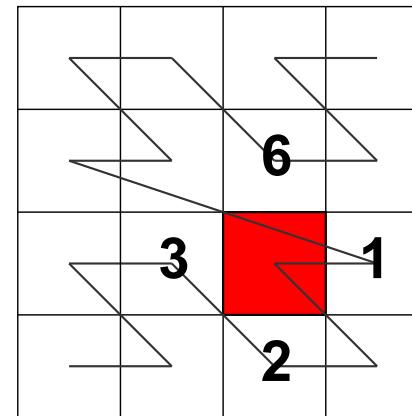
- How many cache lines are involved in a range query?
- Common wisdom: Hilbert is better than Morton

Alternative Locality Measure for MD

- Doubly nested loops of cell access
- Evaluate curves based on along-curve distances to neighbors
- Compare number below and above threshold cutoff k_c (like cache)



- 4x4 Hilbert:
 - 30 1s
 - 10 3s
 - 4 5s
 - 2 11s
 - 2 13s
- Lower median, higher variance
- Better for $k_c=1$

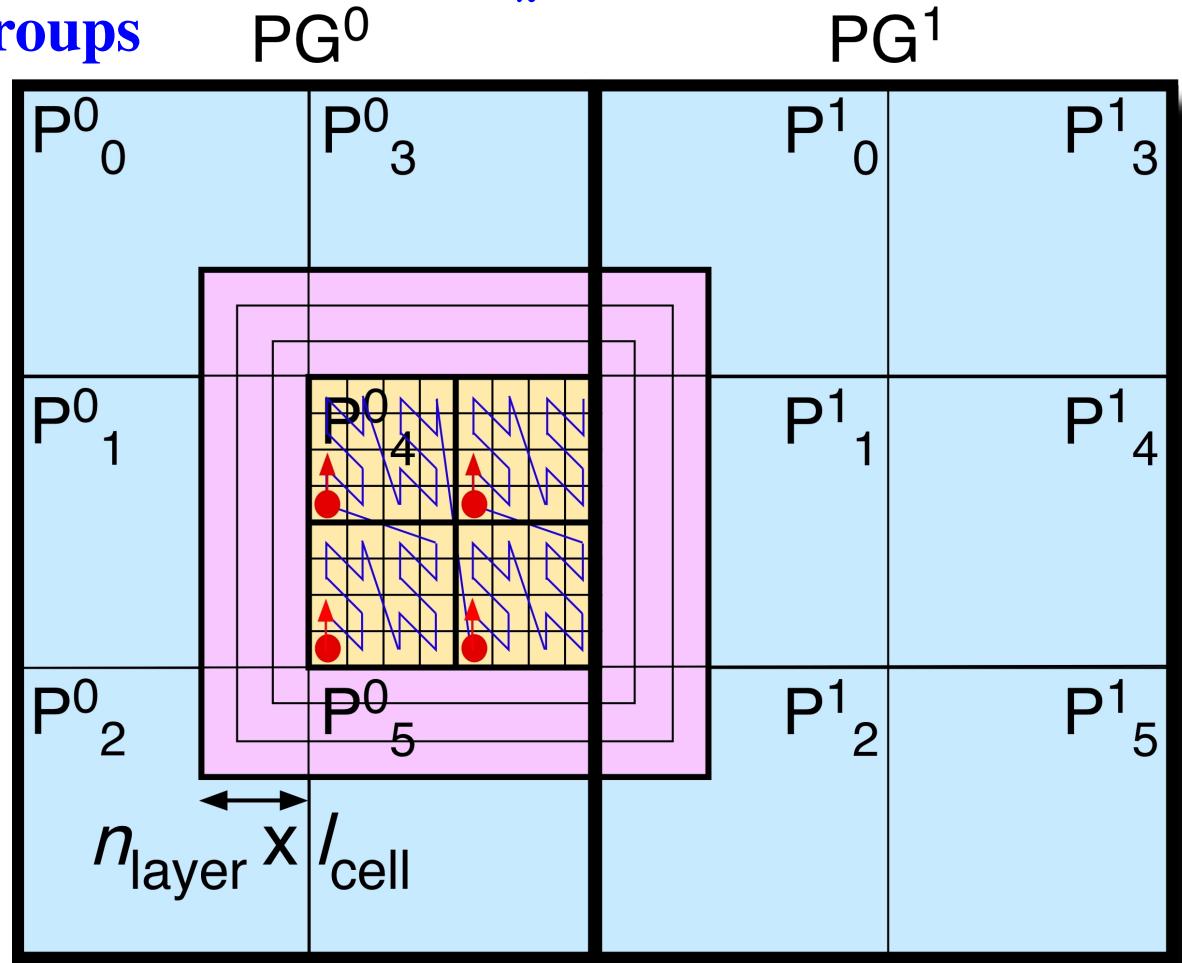


- 4x4 Z-curve:
 - 16 1s
 - 16 2s
 - 8 3s
 - 8 6s
- Higher median, lower variance
- Better for $2 < k_c < 13$

Tunable Hierarchical Cellular Decomposition

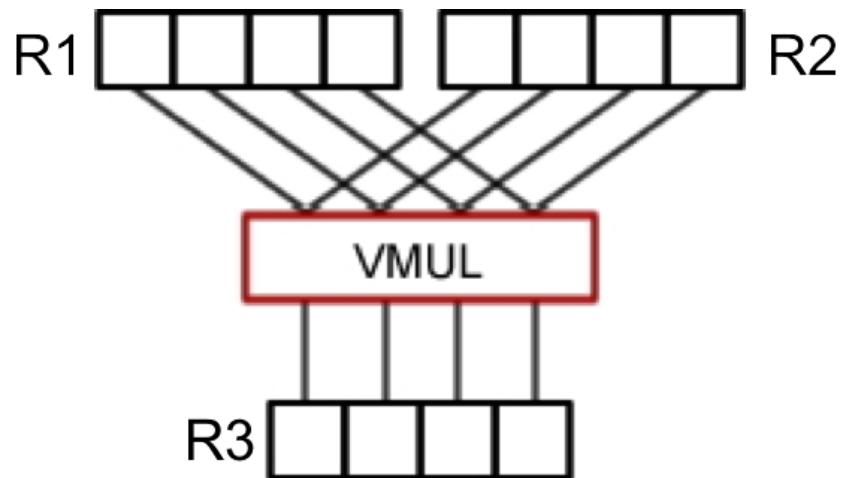
Mapping $O(N)$ D&C algorithms onto deep memory hierarchies

- Spatial decomposition with atom “caching” & “migration”
- Computational cells (linked-list cells in MD or domains in DC-DFT) < cell blocks (threads) < processes (P^{γ}_{π} , spatial decomposition subsystems) < process groups (P^{γ} , Grid nodes)
- Multilayer cellular decomposition (MCD) for n -tuples ($n = 2\text{--}6$) in F-ReaxFF
- Tunable cell data & computation structures: Data/computation re-ordering & granularity parameterized at each decomposition level
- Tunable hybrid MPI + OpenMP + SIMD implementation



SIMD/Vector Operation

- Single-instruction multiple-data (SIMD) parallelism: An arithmetic operation is operated on multiple operand-pairs stored in vector registers, each of which can hold multiple double-precision numbers.

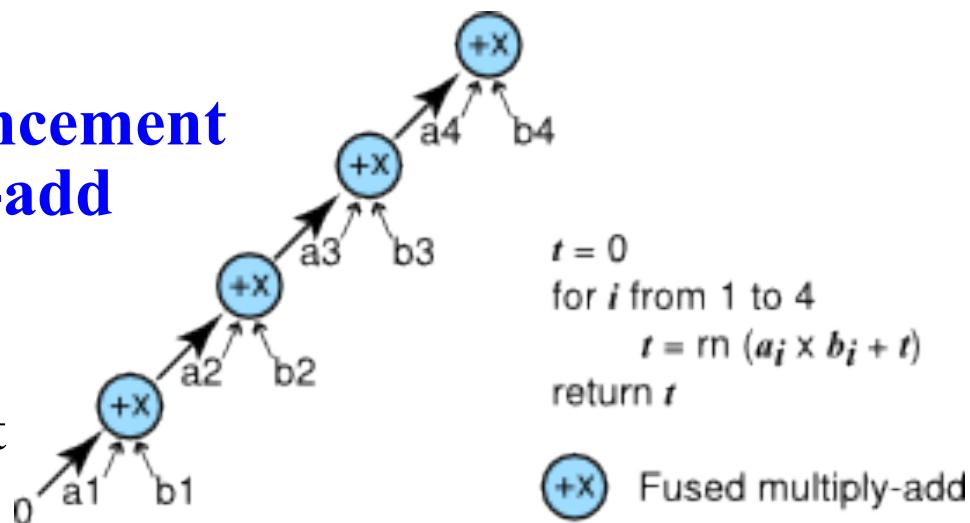


Example: Vector multiplier (VMUL) loads data from two vector registers, R1 and R2, each holding 4 double-precision numbers, concurrently performs 4 multiplications, and stores the results on vector register R3.

- Peak performance enhancement on top of fused multiply-add (FMA) unit.

$$a \leftarrow a + b \times c$$

with 1-cycle throughput



Vector Processing at HPC

Node information

<http://hpcc.usc.edu/support/infrastructure/node-allocation>

Partition Names	Node Range	# of Nodes	Mem Size	Cores per Node	CPU Speed GHz	CPU Type	GPUs per Node	GPU Model	avx	Model	/tmp Size	Network
large main quick	hpc0965 – hpc0972	8	24 GB	12	3.0	xeon	–	–	–	sl160	110 GB	myri
large main quick	hpc4331 – hpc4388	58	128 GB	20	2.4	xeon	2	p100	avx avx2	xl190r	1.79 TB	IB

Intel & AMD advanced vector extension (AVX):

- AVX2 operates on 4 double-precision floating-point numbers
- AVX512

SIMD Vectorization: MD

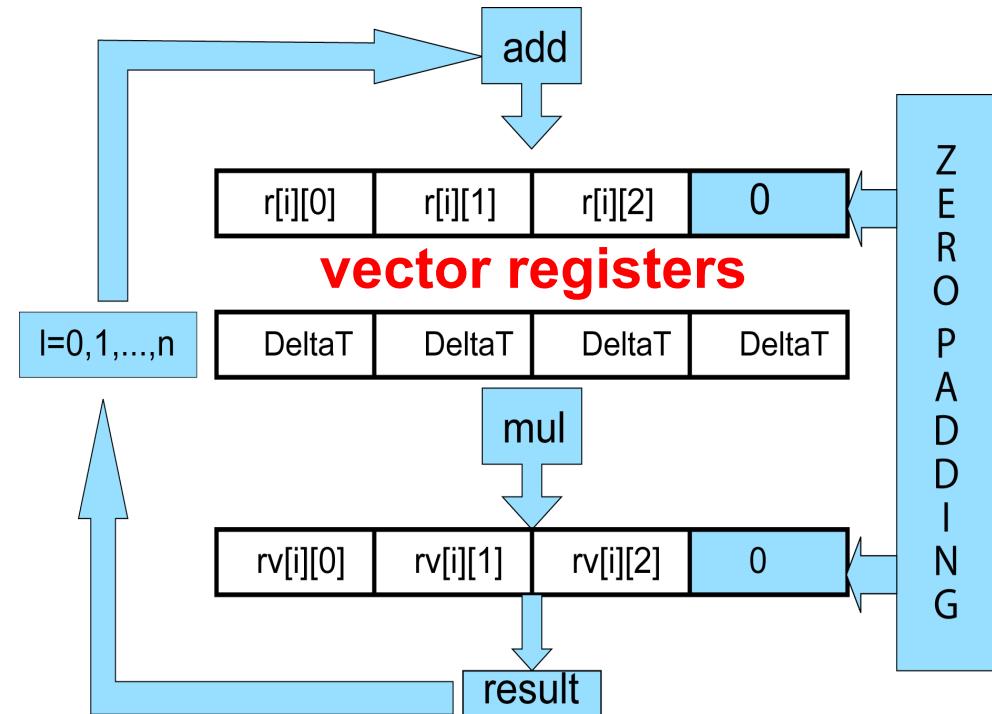
- Single-instruction multiple-data (SIMD) parallelism using vector registers

(Example) Zero padding to align complex data in molecular dynamics

Original solution

```
for (i=0; i<N; i++)
    for (a=0; a<3; a++)
        r[i][a] =
        r[i][a] +
        DeltaT*rv[i][a];
```

SIMD solution

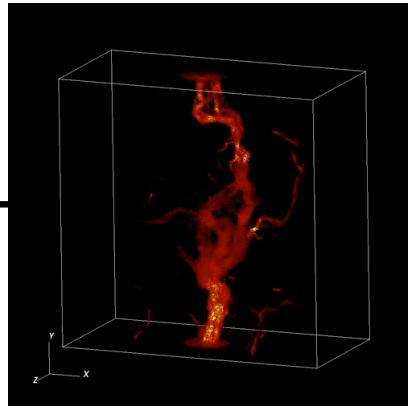


SIMD Vectorization: LBM

- Translocated statement fusion in lattice-Boltzmann flow simulation

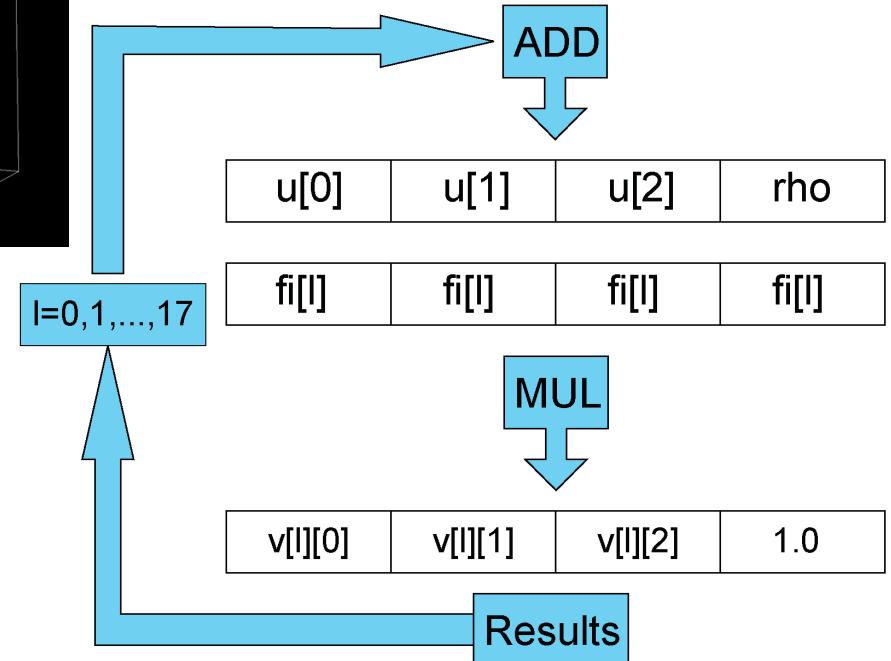
Original solution

```
for(i=0;i<3;i++){  
    u[i]=0.0; rho=0.0;  
    for(l=0;l<18;l++){  
        fi[l] = f[18*cnz+1];  
        u[i] += fi[l]*v[l][i];  
        rho += fi[l];  
    }  
}
```



$3 \times 18 \times 5 = 270$ computation

SIMD solution



SIMDizable mathematical formulations:

Special relativity, quaternion, etc.

$18 \times 4 = 72$ computation

Ideal Speedup 3.5

$$J^\alpha = (c\rho, j^1, j^2, j^3)$$

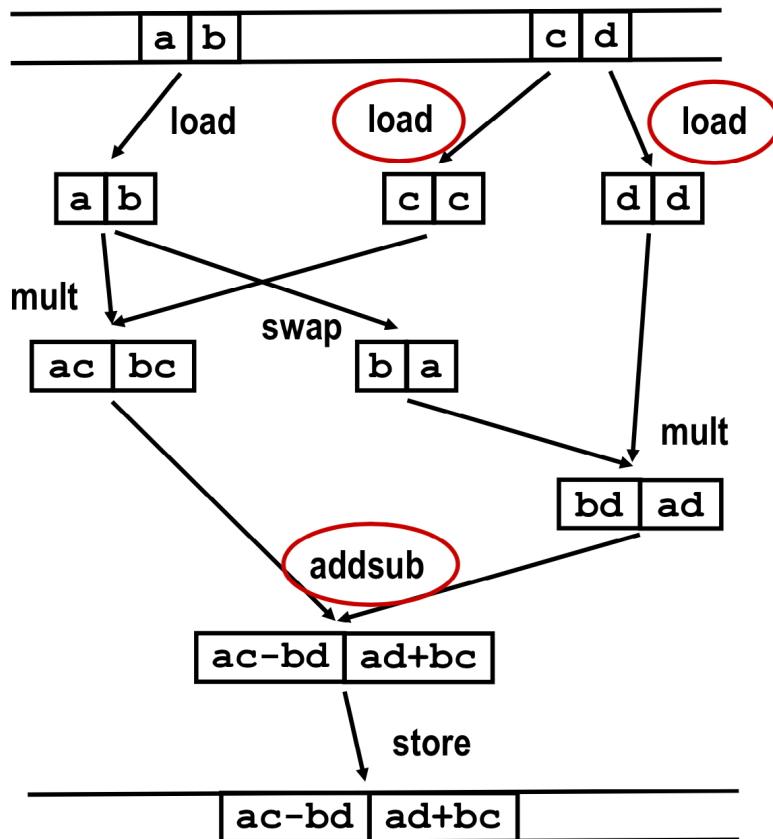
$$A^\alpha = (\phi/c, A^1, A^2, A^3)$$

$$\square A^\alpha = \left(\frac{1}{c^2} \frac{\partial^2}{\partial t^2} - \nabla^2 \right) A^\alpha = \frac{4\pi}{c} J^\alpha$$

SIMDized Complex Multiplication

- SSE (streaming SIMD extension) instruction set
- For quantum dynamics?

$$(a + ib)(c + id) = (ac - bd) + i(ad + bc)$$



Memory

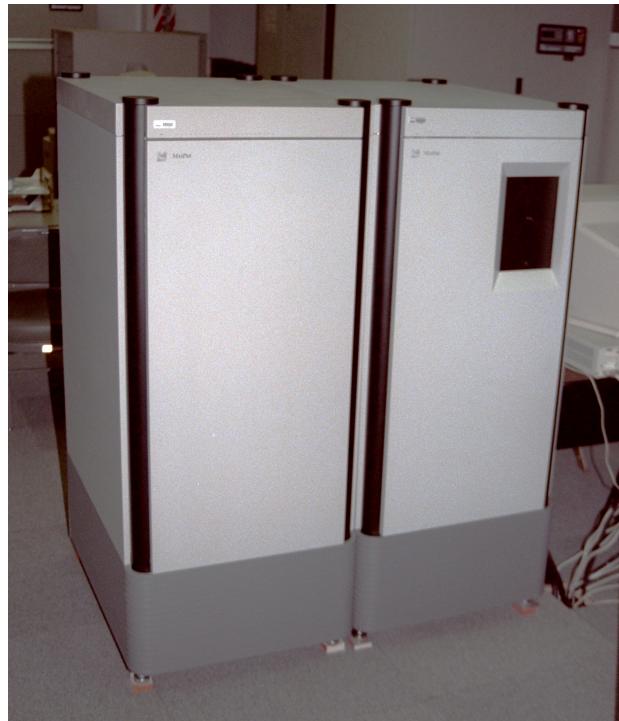
Result:

4 load/stores
3 arithm. ops.
1 reorder op

Not available
in SSE2

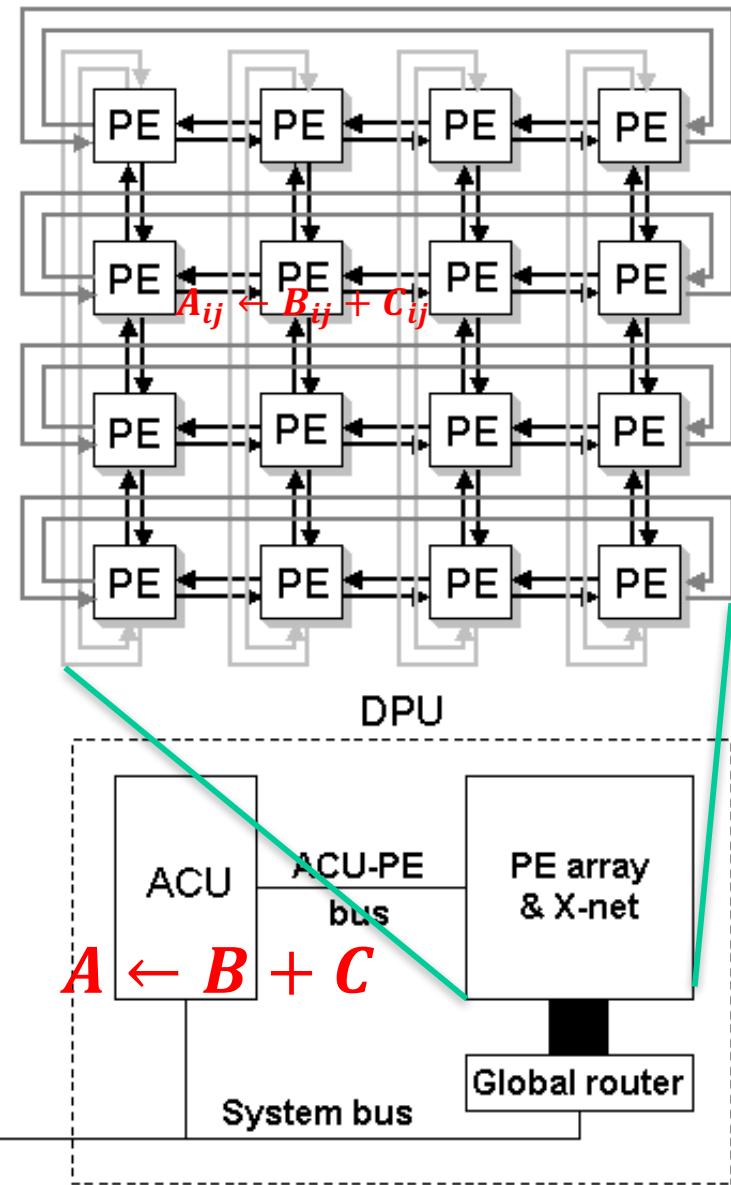
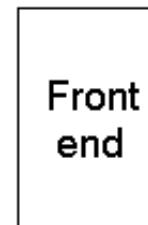
Memory

Massive SIMD Data Parallelism



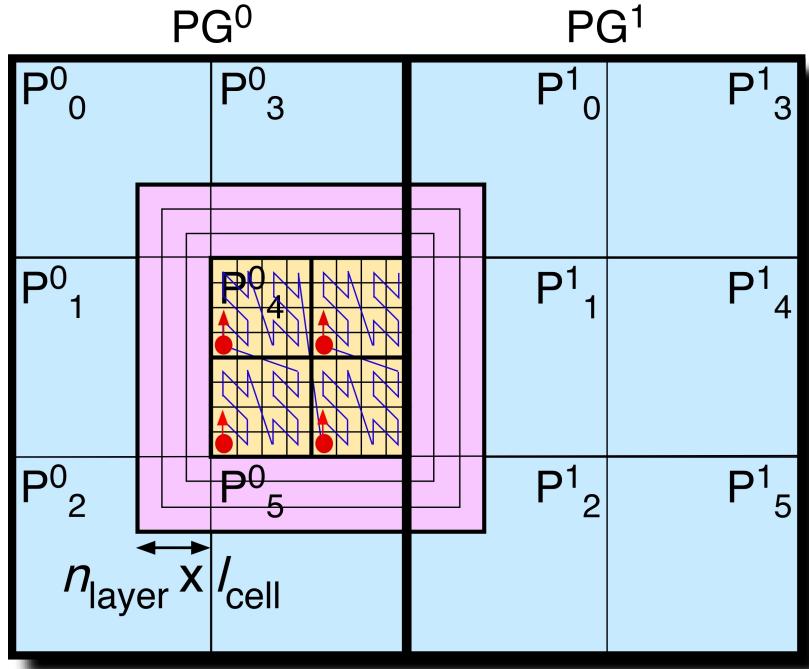
Quantum dynamics on 8,192-processor
 (128×64) MasPar 1208B

Nakano,
Comput. Phys. Commun.
83, 181 ('94)



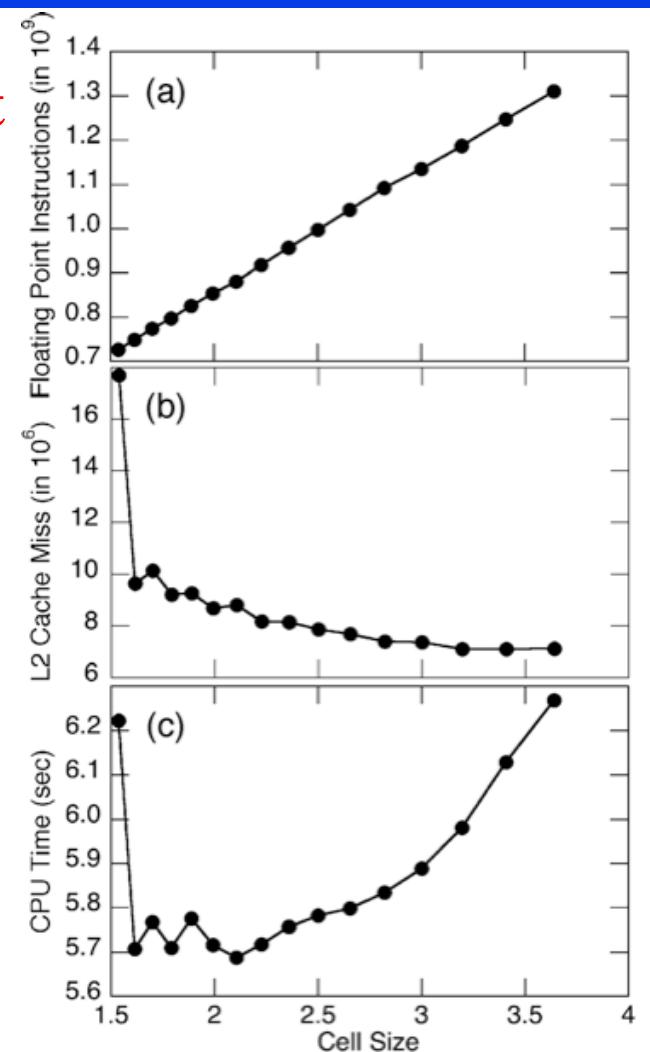
See lecture on "[pre-Beowulf parallel computing](#)"

Performance Tunability



MPI/OpenMP parallelism trade-off:
8,232,000-atom silica MRMD & 290,304-atom RDX F-ReaxFF on 8-way 1.5 GHz Power4

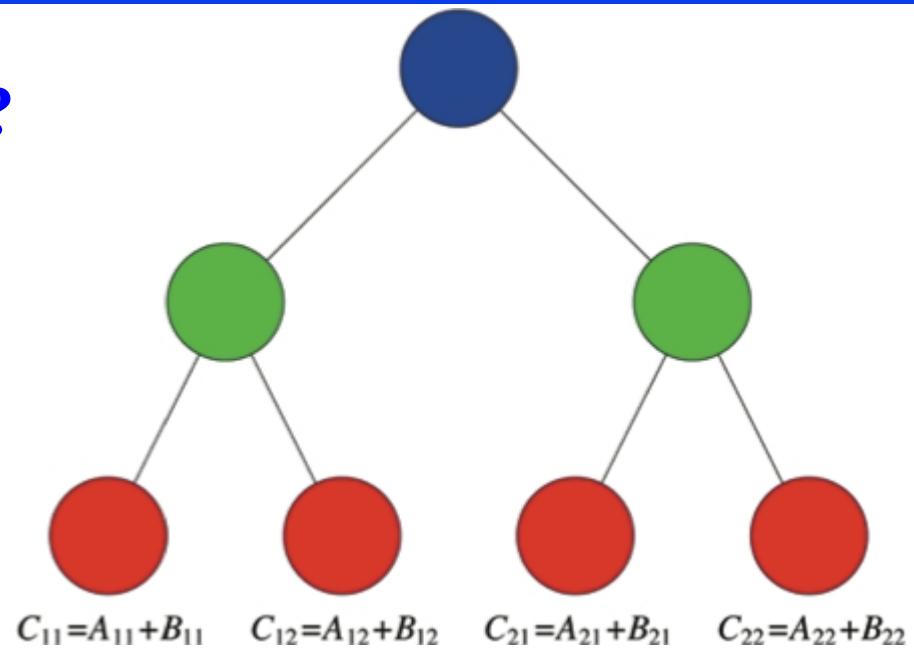
**Floating-point operation/L2 cache miss trade-off:
 331,776-atom silica MRMD on 1.4GHz Pentium III**



Number of OpenMP threads, n_{td}	Number of MPI processes, n_p	MRMD	Execution time/MD time step (sec)	
			P-ReaxFF	MRMD
1	8	4.19	62.5	
2	4	5.75	58.9	
4	2	8.60	54.9	
8	1	12.5	120	

Cache-Oblivious Linked-List Cell MD?

- Recursive blocking for cells?



Cache-Oblivious Algorithms

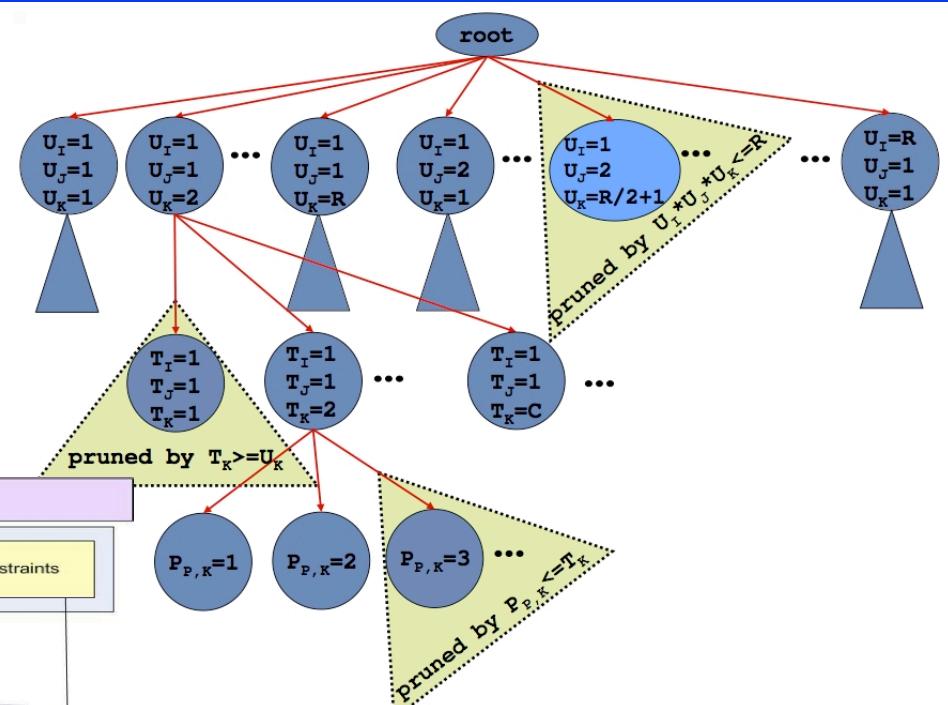
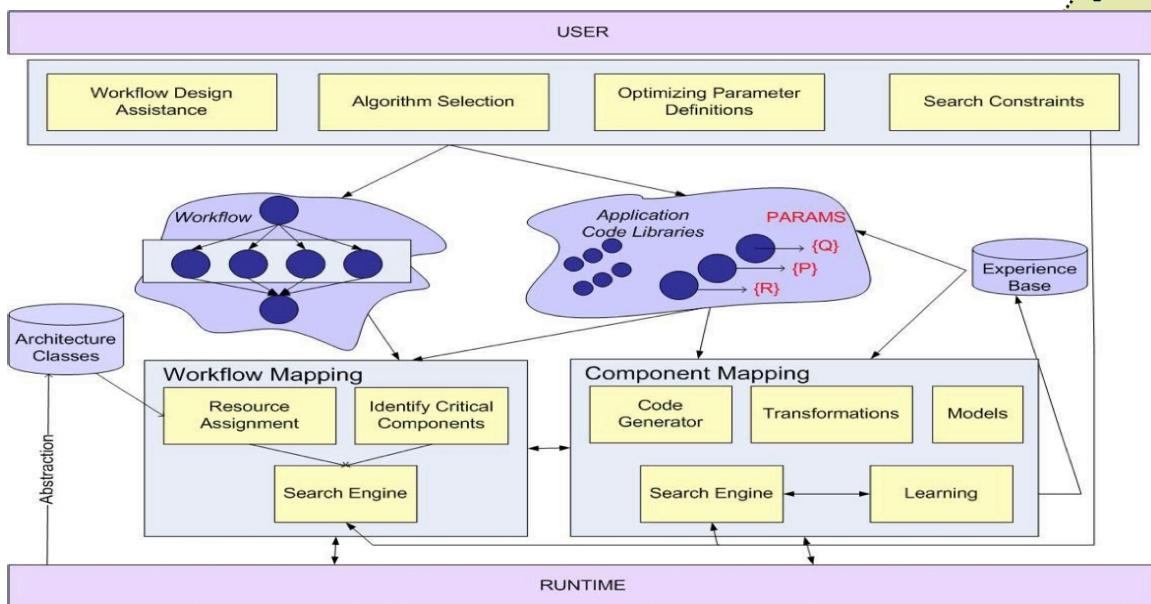
EXTENDED ABSTRACT SUBMITTED FOR PUBLICATION.

Matteo Frigo Charles E. Leiserson Harald Prokop Sridhar Ramachandran
MIT Laboratory for Computer Science, 545 Technology Square, Cambridge, MA 02139
`{athena, cel, prokop, sridhar}@supertech.lcs.mit.edu`

We introduce an “ideal-cache” model to analyze our algorithms, and we prove that an optimal cache-oblivious algorithm designed for two levels of memory is also optimal for multiple levels.

Intelligent Performance Optimization

- Knowledge representation to express concurrency/data locality & machine learning to optimally map them to hardware



Pruned decision tree
C. Chen, Ph.D.
Thesis (Computer
Science, USC, '07)

"Intelligent optimization of parallel & distributed applications," B. Bansal, U. Catalyurek, J. Chame, C. Chen, E. Deelman, Y. Gil, M. Hall, V. Kumar, T. Kurc, K. Lerman, A. Nakano, Y. L. Nelson, J. Saltz, A. Sharma, and P. Vashishta, in *Proc. of Next Generation Software Workshop, Int'l Parallel & Distributed Processing Symposium (IPDPS 07)*

Key Internode Feature

Simple communication cost model

$$t_{\text{comm}} = t_l + m/b$$

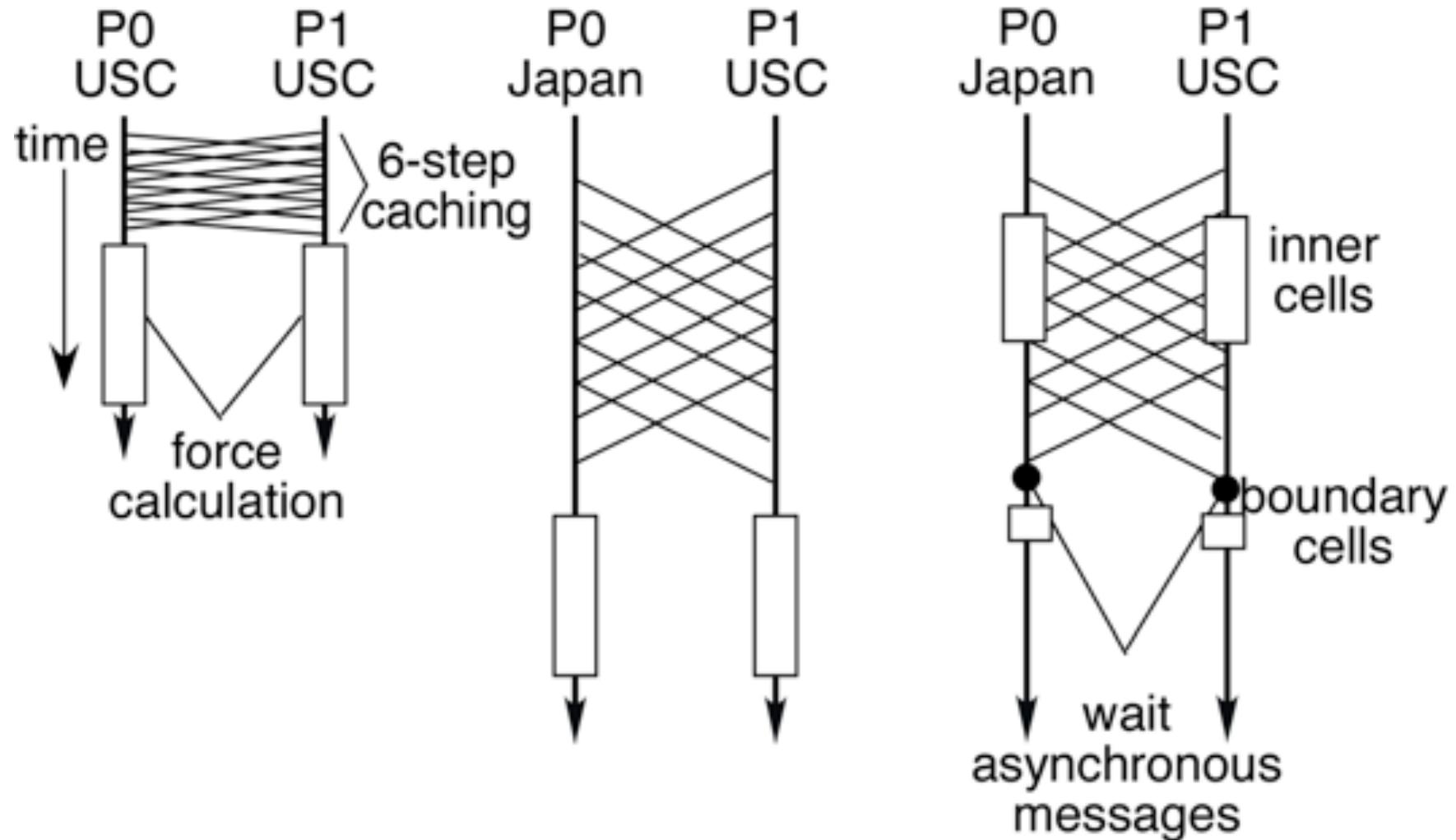
t_{comm} : Total communication time for m Bytes

t_l : Latency = time delay for the head of a message to travel between the source & destination nodes

b : Bandwidth = number of Bytes per second that can be transmitted through the communication link

Internode Optimization

- Communication bottleneck in metacomputing on a Grid

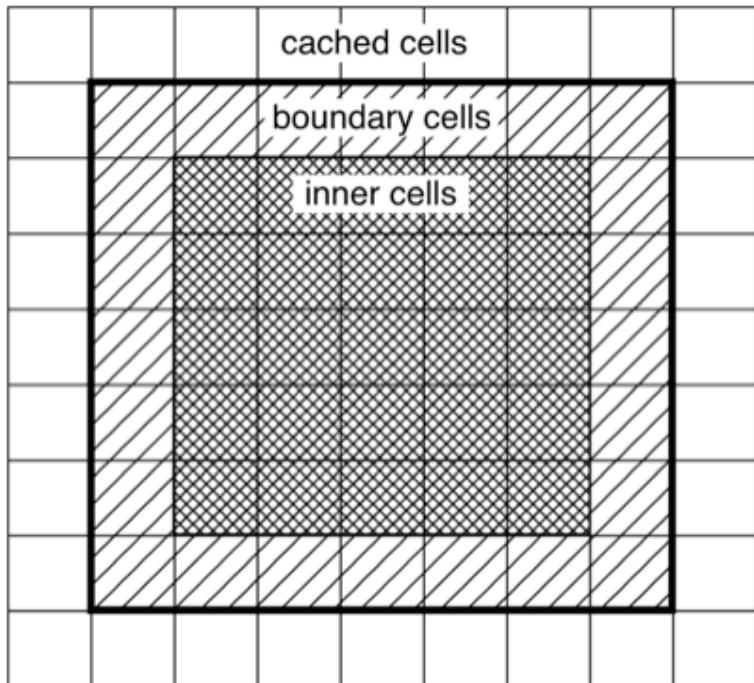


- Overlap computation & communication to hide the latency

Grid-Enabled MD Algorithm

Grid MD algorithm:

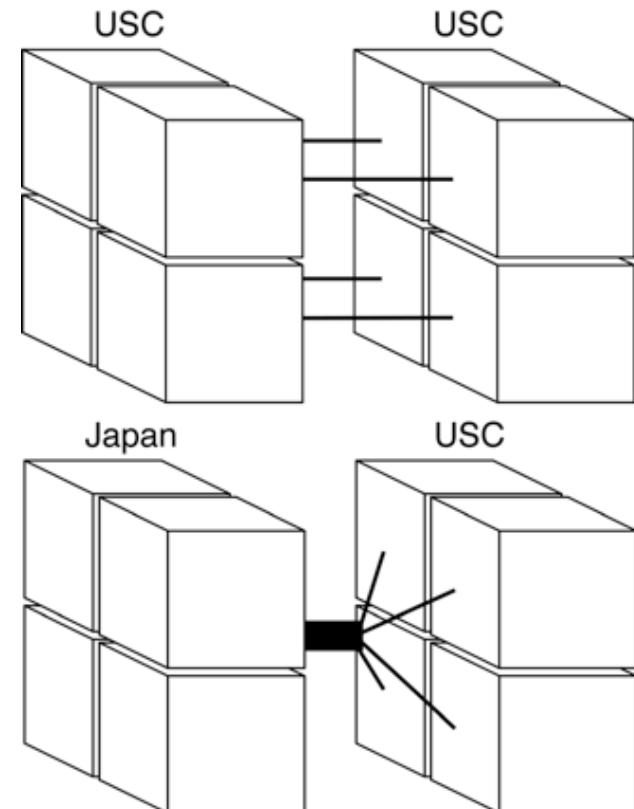
1. asynchronous receive of cells to be cached
2. send atomic coordinates in the boundary cells
3. compute forces for atoms in the inner cells
4. wait for the completion of the asynchronous receive
5. compute forces for atoms in the boundary cells



Kikuchi *et al.*, in Proc. SC02

Renormalized Messages:

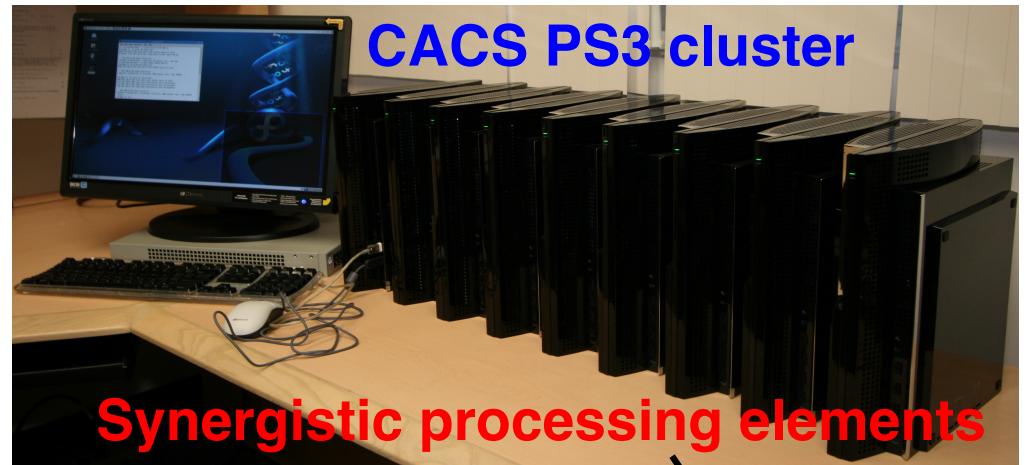
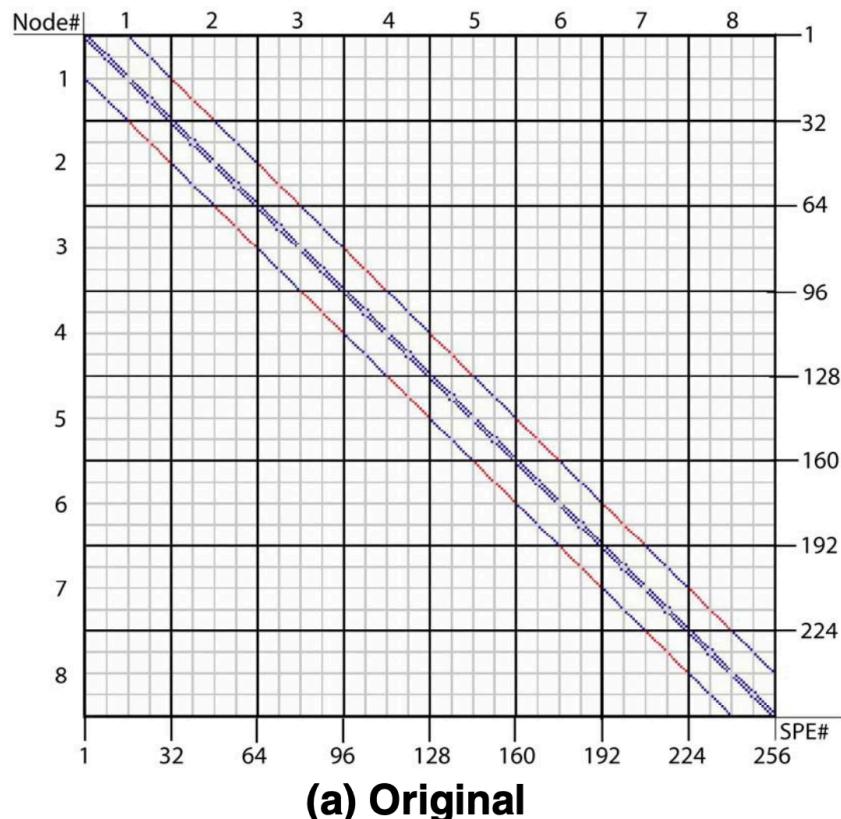
Latency can be reduced by composing a large cross-site message instead of sending all processor-to-processor messages



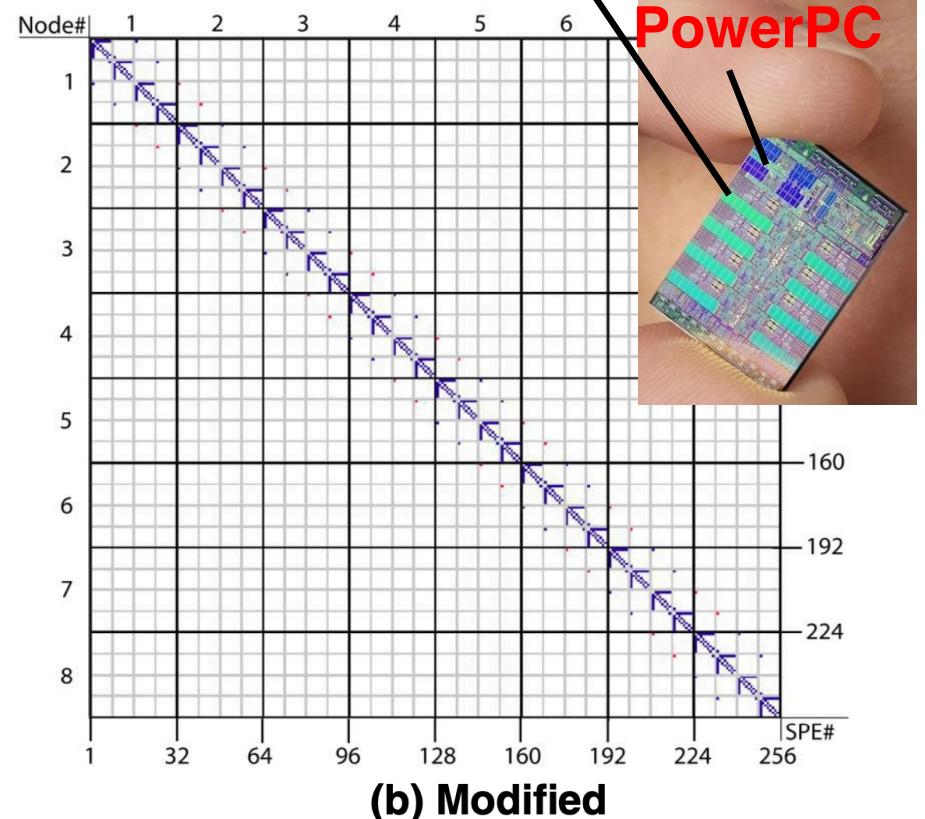
Renormalized Message Passing

- Mapping a 3D-lattice problem onto 8 computing nodes each with 4 Cell processors (or 32 cores)
- Renormalized message passing reduce the number of internode communications

H. Dursun et al., *Par. Proc. Lett.* **19**, 535 ('09)



Synergistic processing elements

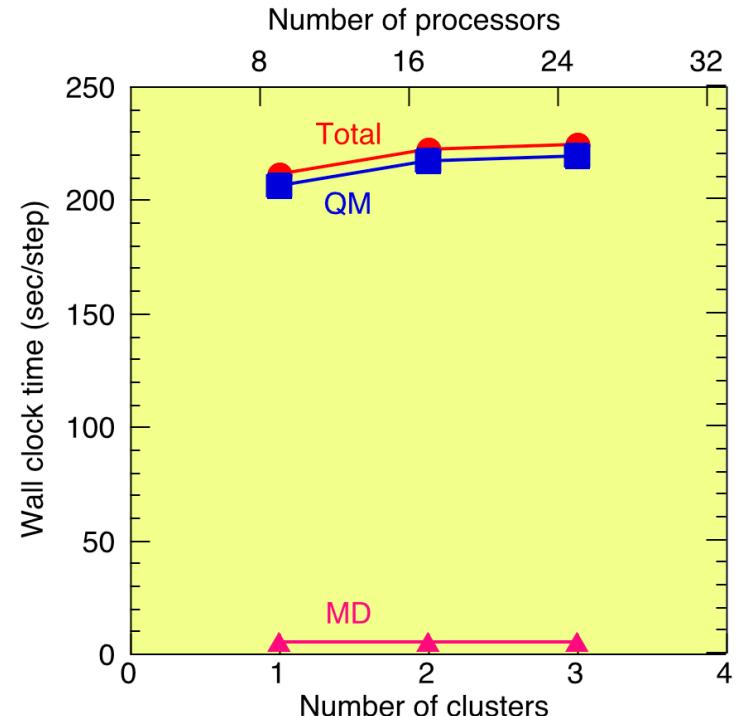
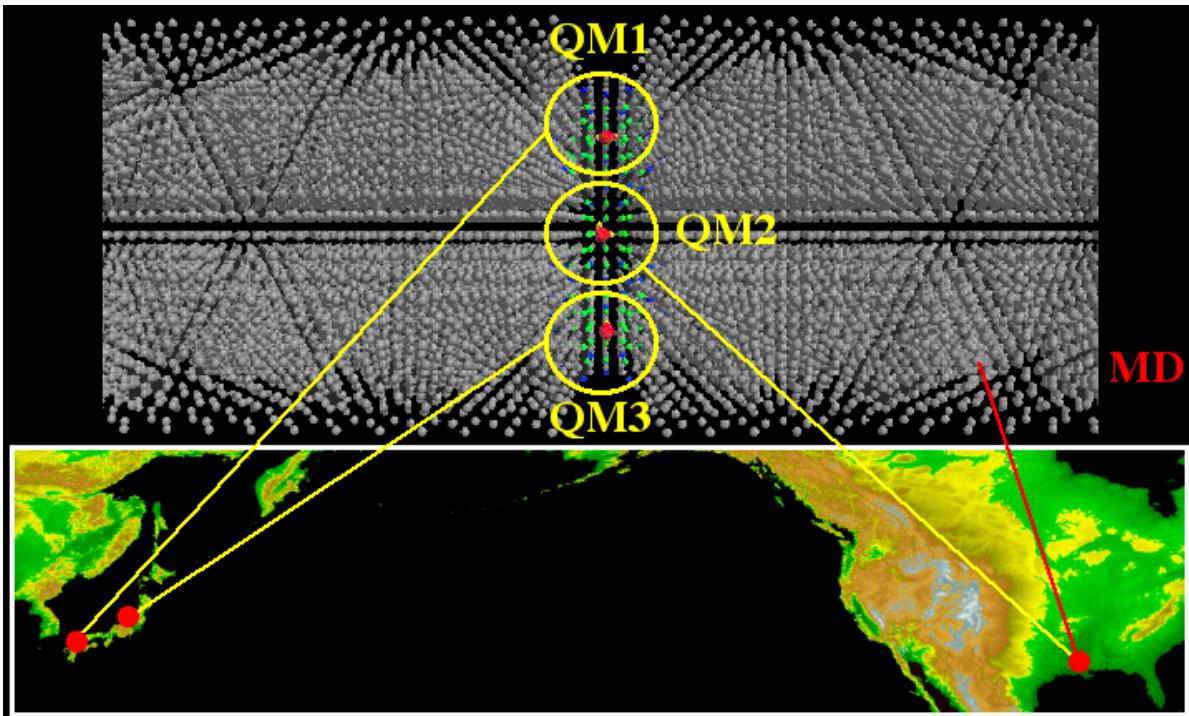


PowerPC

Global Collaborative Simulation

Multiscale divide-&-conquer MD/QM simulation on
a Grid of distributed PC clusters in the US & Japan

- Task decomposition (MPI Communicator) + spatial decomposition
- MPICH-G2 (www.niu.edu/mpi)/Globus (www.globus.org)



Japan: Yamaguchi—65 P4 2.0GHz

Hiroshima, Okayama, Niigata—3×24 P4 1.8GHz

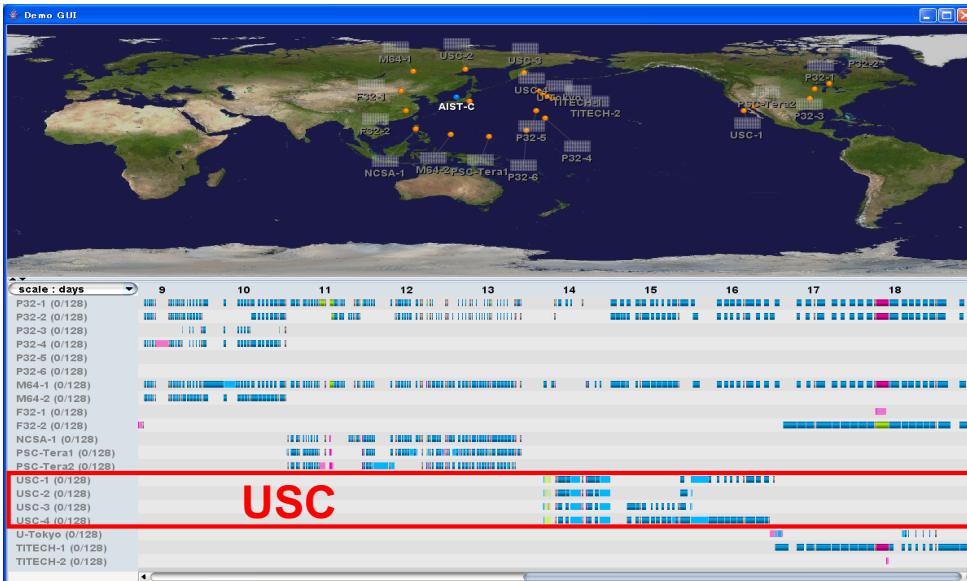
US: Louisiana—17 Athlon XP 1900+

MD — 91,256 atoms

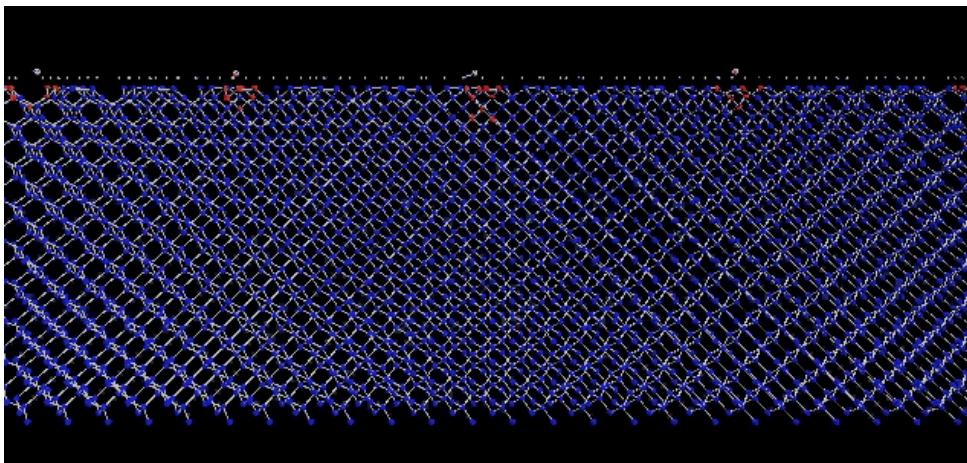
QM (DFT) — 76n atoms on n clusters

- Scaled speedup, $P = 1$ (for MD) + $8n$ (for QM)
- Efficiency = 94.0% on 25 processors over 3 PC clusters

Global Grid QM/MD

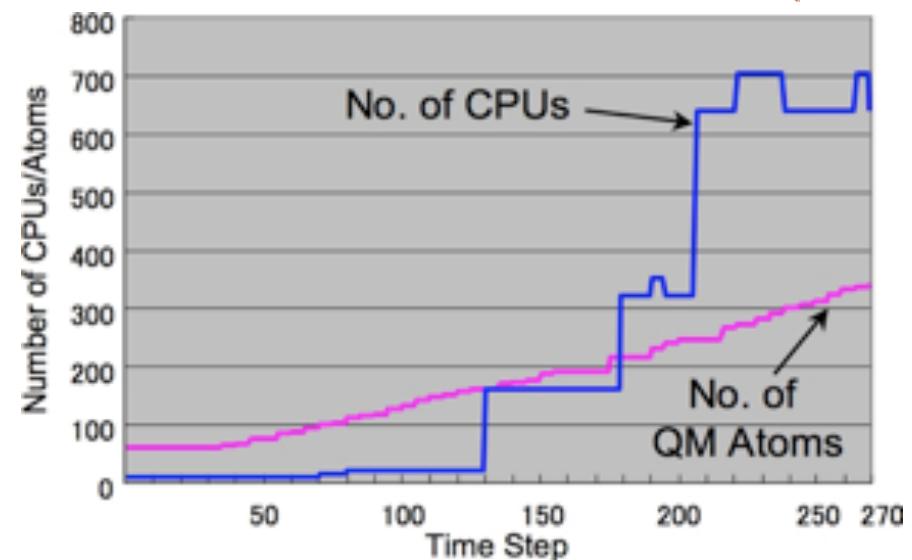
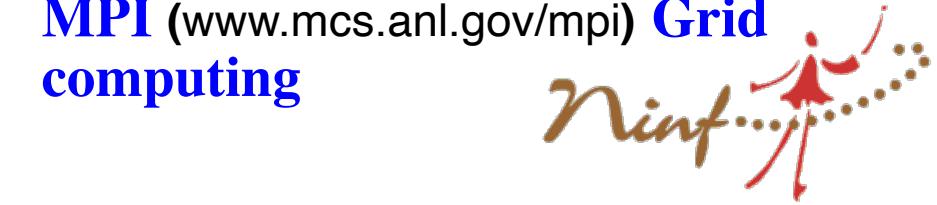


High-energy beam oxidation of Si



H. Takemiya et al., Proc. IEEE/ACM SC06

- Sustained (153,600 cpu-hrs) Grid supercomputing at 6 centers in the US (USC, NCSA, PSC) & Japan (AIST, U Tokyo, TITech)
- Dynamic allocation of computing resources on demand & automated migration due to reservation schedule & faults
- Hybrid GridRPC (ninf.apgrid.org) + MPI (www.mcs.anl.gov/mpi) Grid computing



Fast TCP

BBC NEWS WORLD EDITION

Last Updated: Thursday, 5 June, 2003, 10:48 GMT 11:48 UK

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Promise of ultra-fast downloads

Soon you could be downloading an entire movie off the net far faster than you do now.

US researchers are working on ways to improve the way that net protocols decide how quickly data travels around the net.

Early tests of the new system show that it can triple data transmission speeds.

By linking lots of the faster systems together the researchers have produced data transfer speeds many times higher than is possible today.



Fast net tech could soon take off

Packet tracking promises ultrafast internet

10:54 05 June 03

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Imagine an internet connection so fast it will let you download a whole movie in just five seconds, or access TV-quality video servers in real time. That is the promise from a team at the California Institute of Technology in Pasadena, who have developed a system called Fast TCP.

HOW TO SPEED UP THE NET

Standard internet

Data packets sent across internet



If a packet is lost, the transmission speed is halved



With Fast TCP higher speed connection paths can be ganged together to boost speed to more than 6000 times the capacity of today's broadband links

Data transmitted in same way as on standard internet



When return message says delays are low, packet transmission rate is boosted to highest rate connection can support



Fast TCP: Achieved 8.6 Gb/s between Sunnyvale, CA & CERN, Switzerland

Steven Low (Caltech)

<http://netlab.caltech.edu/FAST>