

Cut a Strip



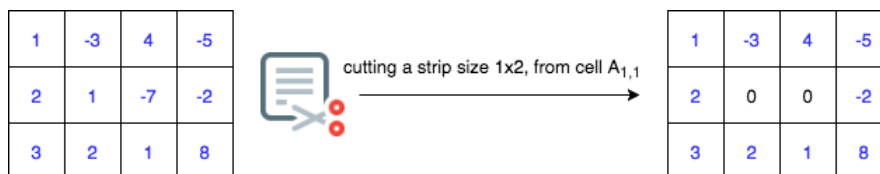
You are given a 2-d integer array.

Apart from this, you are also given an integer. Your task is to cut valid rectangular strips of length lesser than or equal to the given integer, from the array and return the maximum sum over all subarrays of the resultant 2-d array.

What is a valid strip?

- A strip is any one dimensional rectangular subarray, cut vertically or horizontally, keeping in mind that the length of the strip is less than or equal to the given integer.
- The process of cutting a strip is the process of assigning 0's to all array elements covered by the strip.

For example, from the array shown below, we decide to cut a strip of size 1×2 starting from the cell $A_{1,1}$, then after the cut, the array looks like:



A strip of size 2×1 can also be cut from the above array. Keep in mind that once the strip is cut, you need to obtain the maximum sum over subarrays and hence, cut accordingly.

The goal is to return a maximum sum over subarrays of the given 2-d array after a valid strip is cut from the original array. Complete the function `cutAStrip` that takes a 2-D array input and return an integer denoting the maximum sum over subarrays after a valid strip is cut.

Input Format

In the first line, there are 3 space-separated integers n, m and k .

n - Number of rows in the array.

m - Number of columns in the array.

k - Integer based on which the size of the strip is decided. i.e, a strip can be cut, of size $1 \times x$ or $x \times 1$ for $1 \leq x \leq k$.

After that, n lines follow. The i -th of these lines contains m space-separated integers

$A_{i,0}, A_{i,1}, \dots, A_{i,m-1}$.

Constraints

$$1 \leq n, m, k \leq 380$$

$$-5000 \leq A_{i,j} \leq 5000$$

Output Format

In a single line, print a single integer denoting the maximum sum over subarrays of A after a valid strip is cut from the original array.

Sample Input 0

```
2 4 2
1 -3 4 -5
2 1 -7 -2
```

Sample Output 0

5

Explanation 0

In this case, one solution is to cut out the whole second column (a vertical strip of size 2x1) resulting in a grid:

```
1 0 4 -5
2 0 -7 -2
```

and then take the sum of the subarray `[1 0 4]` as the result. It's not possible to get a sum larger than 5.

Sample Input 1

```
3 4 3
-10 1 1 1
-10 1 -1 1
-10 1 1 1
```

Sample Output 1

8

Explanation 1

In this case, the best we can do is to cut out a single cell containing -1. After the cut, the array looks like this:

```
-10 1 1 1
-10 1 0 1
-10 1 1 1
```

then, there exists a subarray with sum 8 (it contains all elements besides the first column). There is no way to produce a larger sum than 8.

Sample Input 2

```
3 2 1
1 2
3 4
5 6
```

Sample Output 2

20

Explanation 2

The best that can be done is to cut a single cell (a strip of size 1x1) containing value 1. This results in the following grid:

```
0 2
3 4
5 6
```

and the best sum that we can get from this grid is 20 when we take the sum of the whole grid.