

Performance Measures: Precision, Recall, and F1

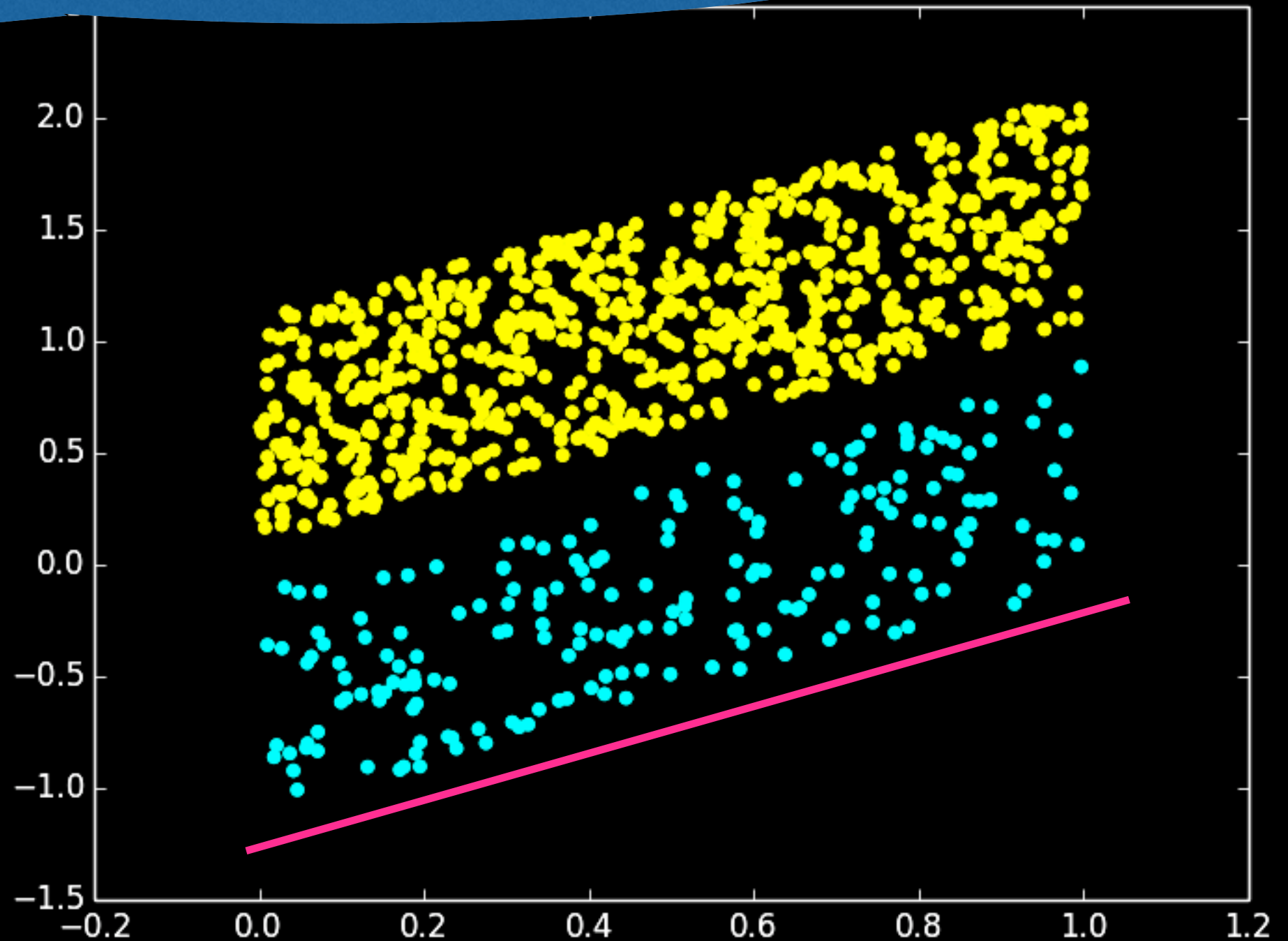
Dirk Hovy

Center for Language Technology
University of Copenhagen

Performance Problems

I have a classifier that's 70% accurate!

x	y	\hat{y}
frog	1	1
deer	1	1
wolf	1	1
dog	1	1
bear	1	1
fish	1	1
bird	1	0
cat	1	0
stone	0	1
tree	0	0



	predicted		
g o i d		1	0
	1	TP	FN
	0	FP	TN

True and False

TARGET = LABEL 1

x	y	\hat{y}	
frog	1	1	true positive
deer	1	1	
wolf	1	1	
dog	1	1	
bear	1	1	
fish	1	1	false negative
bird	1	0	
cat	1	0	
stone	0	1	false positive
tree	0	0	true negative

$$\text{accuracy} = (TP + TN) / (P + N)$$

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F1 = 2 (\text{prec} \times \text{rec}) / (\text{prec} + \text{rec})$$

$$\text{accuracy} = 7/10 = 0.7$$

$$\text{precision} = 6/7 = 0.86$$

$$\text{recall} = 6/8 = 0.75$$

$$F1 = 0.81$$



g o i d	predicted		
		1	0
	1	TP	FN
	0	FP	TN

Changing Target

TARGET = LABEL 0

x	y	\hat{y}	
frog	0	0	
deer	0	0	
wolf	0	0	
dog	0	0	true negative
bear	0	0	
fish	0	0	
bird	0	1	
cat	0	1	false positive
stone	1	0	false negative
tree	1	1	true positive

$$\text{accuracy} = (TP + TN) / (P + N)$$

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F1 = 2 (\text{prec} \times \text{rec}) / (\text{prec} + \text{rec})$$

$$\text{accuracy} = 7/10 = 0.7$$

$$\text{precision} = 1/3 = 0.33$$

$$\text{recall} = 1/2 = 0.5$$

$$F1 = 0.4$$



	predicted		
actual	1	0	
	TP	FN	
0	FP	TN	

MICRO Averaging

WEIGH BY CLASS SIZE

TARGET=1 TARGET=0

x	y	ŷ	x	y	ŷ
frog	1	1	frog	0	0
deer	1	1	deer	0	0
wolf	1	1	wolf	0	0
dog	1	1	dog	0	0
bear	1	1	bear	0	0
fish	1	1	fish	0	0
bird	1	1	bird	0	0
cat	1	0	cat	0	1
stone	0	1	stone	1	0
tree	0	0	tree	1	1

$$\text{accuracy} = (TP + TN) / (P + N)$$

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F1 = 2 (\text{prec} \times \text{rec}) / (\text{prec} + \text{rec})$$

$$\text{acc} = 7/10 + 7/10 = 14/20 = 0.7$$

$$\text{prec} = 6/7 + 1/3 = 7/10 = 0.7$$

$$\text{rec} = 6/8 + 1/2 = 7/10 = 0.7$$

$$F1 = 0.7$$



	predicted		
actual	1	0	
	TP	FN	
0	FP	TN	

MACRO Averaging

WEIGH ALL CLASSES EQUALLY

TARGET=1 TARGET=0

x	y	\hat{y}	x	y	\hat{y}
frog	1	1	frog	0	0
deer	1	1	deer	0	0
wolf	1	1	wolf	0	0
dog	1	1	dog	0	0
bear	1	1	bear	0	0
fish	1	1	fish	0	0
bird	1	1	bird	0	0
cat	1	0	cat	0	1
stone	0	1	stone	1	0
tree	0	0	tree	1	1

$$\text{accuracy} = (TP + TN) / (P + N)$$

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F1 = 2 (\text{prec} \times \text{rec}) / (\text{prec} + \text{rec})$$

$$\text{acc} = (0.7 + 0.7) / 2 = 0.7$$

$$\text{prec} = (0.86 + 0.33) / 2 = 0.6$$

$$\text{rec} = (0.5 + 0.75) / 2 = 0.63$$

$$F1 = 0.61$$



g o i d	predicted		
	0	1	0
	1	TP	FN
0	FP	TN	

PREDICT MAJORITY CLASS FOR ALL

Cheating": Total Recall

TARGET = LABEL 1

x	y	ŷ	
frog	1	1	
deer	1	1	
wolf	1	1	
dog	1	1	true positive
bear	1	1	
fish	1	1	
bird	1	1	
cat	1	1	
stone	0	1	false positive
tree	0	1	

$$\text{accuracy} = (TP + TN) / (P + N)$$

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F1 = 2 (\text{prec} \times \text{rec}) / (\text{prec} + \text{rec})$$

$$\text{accuracy} = 8/10 = 0.8$$

$$\text{precision} = 8/10 = 0.8$$

$$\text{recall} = 8/8 = 1.0$$

$$F1 = 0.9$$



Take-home points

- **accuracy** can be too general
- **precision** and **recall** are per-class measures
- **precision** = how many of instances labeled as target class are actually *in* target class?
- **recall** = how many of *all* target class instances in data identified correctly?
- **F1** = symmetric mean of precision and recall

Thanks!

Questions?