

1 Scoping Review Protocol: Statistical Models for Longitudinal Data

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3 2022-08-18

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23 **1 Background**

24 Longitudinal studies are frequently used in the health sciences (biomedical research, epidemiology, public
25 health, among others) as they allow to examine how the temporal effect of a treatment or an intervention,
26 in contrast to a cross-sectional study, which only allows to examine the effect of the intervention at a single
27 time point. When compared their cross-sectional counterparts, longitudinal studies allow for increased
28 statistical power and more cost efficient strategies^{1,2}. However, the statistical analysis of longitudinal data
29 requires to take into consideration factors such as data missingness, correlation, and non-linear trends,
30 which do not occur on cross-sectional data^{3,4}. In other words, there is an “analytic cost” associated with
31 the increased complexity of longitudinal data².

32 This additional layer of complexity has led to a problem of model misspecification in the statistical analysis
33 of the data (i.e., the use of a statistical model that is not coherent with the data), which has been reported to
34 occur in many fields, including the health sciences⁵. For example, in a landmark study Liu et al. showed that
35 in a subset of papers in the biomedical sciences, the most popular model used to analyze longitudinal data
36 was the analysis of variance (ANOVA, an approach that fails to take into account the correlation between
37 measures over time), and that only 18% of the studies analyzed used models intended for longitudinal
38 analysis while checking that the assumptions of the model were satisfied by the data⁶.

39 Historically, the repeated measures ANOVA (rm-ANOVA, a statistical model for longitudinal data) has
40 been the preferred method in the health sciences to analyze longitudinal data, despite the fact that the
41 multiple assumptions required by this model are frequently not satisfied by the data collected in longitudinal
42 studies⁴. On the other hand, the last 30 years have seen incredible progress in the field of Statistics with the
43 development of statistical models for longitudinal data that relax the assumptions of rm-ANOVA. Linear
44 mixed models, generalized additive models, Bayesian models, and generalized estimating equations are
45 among these modern statistical models developed for longitudinal data^{7–11}. From these statistical methods,

linear mixed models and generalized estimating equations are the two classes of models that have been frequently applied to analyze longitudinal data in the health sciences during the last decade^{12–14}.

However, modern statistical methods that are suited to analyze longitudinal data have been the exception rather than the norm in the health sciences. In 2001, a study reported that only 30% of the clinical trials analyzed used linear mixed models to analyze their results, and that the preferred method of analysis continued to be rm-ANOVA¹⁵ (in comparison, McCullagh and Nelder’s seminal book on the generalized linear model (GLM) was published in 1989¹⁶, and there was ongoing work on the extension of the GLM framework to the mixed model case by 1993¹⁷). Apart from the aforementioned study, there are not recent papers that examine the use of modern statistical methods for longitudinal data in the health sciences. Such information is critical to understand if the use of these methods has increased or decreased in the field over the last 20 years, and the reasons behind such changes.

Additionally, the reproducibility crisis is an ongoing issue in the health sciences^{18,19}, a major component of it being the misuse and lack of reproducibility of statistical analyses^{20,21}. Despite the fact that the landscape of statistical software has vastly increased in the last decade with many statistical computational tools (software, packages) now available to researchers, reproducibility standards vary between each computational tool²². Furthermore, there is still high variability in the amount of statistical reporting across journals²³. Understanding what statistical computational tools are used nowadays by researchers in the health sciences can provide an assessment of the advances in the field towards research reproducibility, while identifying limitations that might still be in place.

In this study, we surveyed the statistical methods used in papers dealing with longitudinal data in the health sciences in order to: 1) identify statistical methods used in order to assess the trends in adoption of modern statistical methods, 2) determine what are the computational tools used by researchers to perform statistical analyses, and 3) use the previous points to provide context to the current status of the advances in research reproducibility in the field.

2 Objective

This study aims to summarize the different statistical models for longitudinal data that are used in the health sciences to identify the current extent in the adoption of modern statistical methods, determine what are the computational tools used in each case and how this in turn affects the reproducibility, and provide an updated list on methods recently developed for longitudinal data in order to determine if they can be

75 broadly applied to longitudinal data in the health sciences.

76 **3 Review Question**

77 Summarize the statistical methods used to analyze longitudinal data in the health sciences to identify
78 which methods are most commonly used, the applicability of such methods in the context of each study,
79 and gaps that might exist that prevent the adoption of modern statistical methods that can be better suited
80 to analyze the data. Additionally, identify if studies check for model assumptions, and how this in turn
81 impacts the reported results.

82 **4 Databases**

- 83 • PubMed
- 84 • Web of Science

85 **5 Search Terms**

86 **5.1 For the Application of Modern Models on Longitudinal Biomedical/Health** 87 **Data**

88 **5.1.1 PubMed**

89 **5.1.1.1 Query 1:**

90 (biomedical OR health) AND ((repeated measures) OR (longitudinal study) OR (ANOVA) OR (mixed
91 effects) OR (growth curve) OR (generalized additive model) OR (generalized estimating equation)) NOT
92 ((review) OR (meta analysis))

93 Hits: 393,188

94 Comments: query picks too many papers, and is not specific

95 **5.1.1.2 Query 2:**

(biomedical OR health) AND ((repeated measures) OR (longitudinal study)) AND ((statistical analyses)
OR (statistical analysis)) NOT ((review) OR (meta analysis))

Hits: 12,617

Comments: [This is the best query so far.](#)

Papers from this query appear to be good. The query catches many papers from psychology and psychiatry,
but the ones I checked did said used linear mixed models or regression in their analyses.

5.1.2 Web of Science

5.1.2.1 Query 1:

WC=(biom* OR health OR allergy OR cell biology OR cardio* OR hematology OR immunology OR life
sciences biomedicine other topics OR medical informatics OR neuro* OR oncology OR pharmacology OR
radiology, nuclear medicine & medical imaging OR research & experimental medicine OR substance abuse
OR optics) AND AK=(longitudinal study OR repeated measures study) NOT ALL=(review OR meta
analysis) NOT AK=(model* AND study design) NOT KP=(model)

Hits: 4,716

Comments: [This query seems to be good.](#)

Web of Science allows to specify more fields that result in a more targeted search. The last two parts of the
query (AK and KP) removed studies method or tutorial papers from journals such as *Statistics in Medicine*.

5.2 For Methods on Longitudinal Data

5.2.1 Web of Science

5.2.1.1 Query 1:

AK=((longitudinal OR repeated measures OR longitudinal data) AND (model OR design)) NOT
ALL=(review OR meta analysis) NOT ALL=(survival analysis)

Hits: 3,071

Comments: [This query seems to be good.](#)

This query returns papers that deal with methods for longitudinal analysis. Two additional options can be
selected: 1) include only articles (which reduces the number of hits to 2,936 as book chapters and editorials

are omitted) and 2) select from the 01/01/2000 until today (which could be reasonable as the increment of models has occurred during the last two decades. This option reduces the number to papers to 2,849).

6 Criteria

6.1 Inclusion Criteria

- methods paper see new methods developed
- application

6.2 Exclusion Criteria

7 Additional Resources

8 Comparison (?)

9 Data Extraction

10 Data Synthesis Strategy

11 References

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