

Assignment NO: 2

Name: - Bhavesh Santosh Ainkar

Roll No: - 01

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Sem - VII

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D.P.P	D.O.C.	Marks	Sign.
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Q.1] Solve the following with forward chaining
or backward chaining or resolution
(any one) use predicate logic as language
of knowledge representation clearly
Specify the facts & inference rule used.

a.1] Example:-

- 1) Every child sees some witch. no witch has both a black cat & a pointed hat.
- 2) Every witch is good or bad.
- 3) Every child who sees any good witch gets candy
- 4) Every witch that is bad has a black cat
- 5) Every witch that is seen by any child has a pointed hat.

6) prove: every child gets candy

→ A) Facts into FOL

- 1) $\exists x \forall y (\text{child}(x), \text{witch}(y) \rightarrow \text{sees}(x, y))$
 $\neg \exists y (\text{witch}(y) \rightarrow \text{has}(y, \text{black cat}) \wedge \text{has}(y, \text{pointed hat}))$
- 2) $\forall y (\text{witch}(y) \rightarrow \text{good}(y) \vee \text{bad}(y))$
- 3) $\exists x (\text{sees}(x, y) \rightarrow (\text{witch}(y) \rightarrow \text{good}(y)) \rightarrow \text{get}(x, \text{candy}))$

4] $\exists y ((\text{witch}(y) \rightarrow \text{bad}(y)) \rightarrow \text{has}(y, \text{black hat}))$

5] $\exists y (\text{sees}(x, y) \rightarrow \text{has}(y, \text{pointed hat}))$

6] Fol into CNF

1] $\exists x \forall y (\text{child}(x), \text{witch}(y) \rightarrow \text{sees}(x, y))$

$\rightarrow \neg \exists y, (\text{witch}(y) \rightarrow \text{has}(y, \text{black hat}))$

$\rightarrow \neg \exists y (\text{witch}(y) \rightarrow \text{has}(y, \text{pointed hat}))$

2] $\exists y (\text{witch}(y) \rightarrow \text{good}(y) \vee \text{bad}(y))$

3] $\exists x (\text{sees}(x, y) \rightarrow (\text{witch}(y) \rightarrow \text{good}(y))) \Rightarrow$
 $\text{get}(x, \text{candy})$

4] $\exists y (\text{witch}(y) \rightarrow \text{bad}(y)) \rightarrow \text{has}(y, \text{black hat})$

5] $\exists y (\text{sees}(x, y) \rightarrow \text{has}(y, \text{pointed hat}))$

B) Fol into CNF

1] $\exists x \forall y (\text{child}(x), \text{witch}(y) \rightarrow \text{see}(x, y))$

$\rightarrow \neg \exists y, (\text{witch}(y) \rightarrow \text{has}(y, \text{black hat}))$

$\rightarrow \neg \exists y (\text{witch}(y) \rightarrow \text{has}(y, \text{pointed hat}))$

2] $\forall y (\text{witch}(y) \rightarrow \text{good}(y))$

$\forall y (\text{witch}(y) \rightarrow \text{bad}(y))$

3] $\exists x [\text{sees}(x, y) \rightarrow (\text{witch}(y) \rightarrow \text{good}(y)) \rightarrow \text{get}(x, \text{candy})]$

$\rightarrow \exists x [\text{sees}(x, \text{good}(y)) \rightarrow \text{get}(x, \text{candy})]$

4) $\exists y [bad(y) \rightarrow \text{has}(y, \text{black hat})]$

5) $\exists y [\text{seen}(x, y) \rightarrow \text{has}(y, \text{pointed hat})]$

$\rightarrow \sim \forall y [\text{seen}(x, y) \rightarrow \text{has}(y, \text{black hat})]$

6) $\begin{array}{l} \rightarrow \\ \text{Sees}(x, y) \end{array}$ $\begin{array}{l} \text{witch}(y) \vee \text{sees}(x, y) \\ \{\text{good} \vee \text{bad}\} \end{array}$

$\sim \text{sees}(x, \text{good}) \wedge \text{sees}(x, \text{bad}) \quad \text{has}(y, 2)$
 $\qquad\qquad\qquad \{y/\text{good} \vee \text{bad}\}$
 $\qquad\qquad\qquad \{2/\text{black hat} \vee \text{pointed hat}\}$

$\text{seen}(x, \text{good}) \vee \text{seen}(x, \text{bad})$

$\begin{array}{l} | \\ \text{has}(\text{good}, \text{pointed} \\ \text{hat}) \vee \text{get}(x, \text{candy}) \end{array}$

$\begin{array}{l} \text{seen}(x, \text{good}) \vee \text{has}(\text{good}, \\ \text{pointed hat}) \vee \text{get}(x, \text{candy}) \end{array}$

$\begin{array}{l} \text{seen}(x, \text{good}) \vee \\ \text{get}(x, \text{candy}) \end{array}$

$\text{get}(x, \text{candy})$

$\text{get}(x, \text{candy})$

2) Example 2:

- 1) Every boy or girl is a child
- 2) Every child gets a doll or a train or a lump of coal
- 3) No boy gets any doll
- 4) Every child who is bad gets any lump of coal
- 5) No child gets a brain
- 6) Ram gets lump of coal
- 7) Prove Ram is bad.

- 1) $\forall x (\text{boy}(x) \text{ or } \text{girl}(x)) \rightarrow \text{child}(x)$
- 2) $\forall y (\text{child}(y)) \rightarrow \text{gets}(y, \text{doll}) \text{ or } \text{gets}(y, \text{train})$
 $\text{or } \text{gets}(y, \text{coal})$
- 3) $\forall w (\text{boy}(w)) \rightarrow \text{gets}(w, \text{doll})$
- 4) for all $z (\text{child}(z) \text{ and } \text{bad}(z)) \rightarrow$
 $\text{gets}(z, \text{coal})$) $\forall y \text{ child}(y) \rightarrow \text{gets}(y, \text{train})$
- 5) $\text{child}(\text{ram}) - \text{gets}(\text{ram}, \text{coal})$
To prove $(\text{child}(\text{ram}) \rightarrow \text{bad}(\text{ram}))$

CNF clauses.

1) $\text{boy}(x) \text{ or } \text{child}(x)$
 $\text{girl}(x) \text{ or } \text{child}(x)$

2) $\text{child}(y) \text{ or } \text{gets}(y, \text{doll}) \text{ or }$
 $\text{gets}(y, \text{brain}) \text{ or } \text{gets}(y, \text{coal})$

3) $\text{boy}(w) \text{ or } \text{gets}(w, \text{doll})$

- 4) $\neg \text{child}(2) \text{ or } \neg \text{bad}(2) \text{ or gets}(2, \text{coa})$
 5) $\neg \text{child}(\text{ram}) \rightarrow \text{gets}(\text{ram}, \text{coa})$
 6) $\neg \text{bad}(\text{ram})$

Resolution

- 4) $\neg \text{child}(2) \text{ or } \neg \text{bad}(2) \text{ or get}(2, \text{coa})$
 6) $\neg \text{bad}(\text{ram})$
 2) $\neg \text{child}(\text{ram}) \text{ or gets}(\text{ram}, \text{coa})$
 substituting 2 by ram
~~1)~~ (a) $\neg \text{boy}(x) \text{ or } \text{child}(x)$
 boy(ram)
 2) $\text{child} \& \text{ram}$ (substituting X by ram)
 7) $\neg \text{child}(\text{ram}) \text{ or gets}(\text{ram}, \text{coa})$
 8) $\text{child}(\text{ram})$
 9) $\text{gets}(\text{ram}, \text{coa})$
 2) $\neg \text{child}(4) (\text{or gets}(4, \text{doll}) \text{ or gets}(4, \text{train}))$ or
 $\text{gets}(\text{ram}, \text{train}) \text{ or gets}(4, \text{coa})$
 2) $\text{child}(\text{ram})$
 10) $\text{gets}(\text{ram}, \text{doll}) \text{ or gets}(\text{ram}, \text{train}) \text{ or}$
 $\text{gets}(\text{ram}, \text{coa})$
 (substituting 4 by ram)
 9) $\text{gets}(\text{ram}, \text{coa})$
 10) $\text{gets}(\text{ram}, \text{doll}) \text{ or gets}(\text{ram}, \text{train}) \text{ or}$
 $\text{gets}(\text{ram}, \text{coa})$
 11) $\text{gets}(\text{ram}, \text{doll}) \text{ or gets}(\text{ram}, \text{coa})$

3) !boy (w) or !gets (w, doll)

5) boy (ram)

12) !get(ram, doll) (substituting w by ram)

11) gets (ram, doll) or gets (ram, ~~ram~~)

12) !gets (ram, doll)

13) gets (ram, coal)

6) <9> get (ram, coal)

13) gets (ram, coal)

Hence, bad (ram) is proved.

a.2] Differentiate between STRIPS and ADL

STRIPS language

Only allow positive literals in the states
for e.g.: A valid sentence.
is ~~strike~~ STRIPS is expressed as
→ Intelligent \wedge Beautiful

ADL

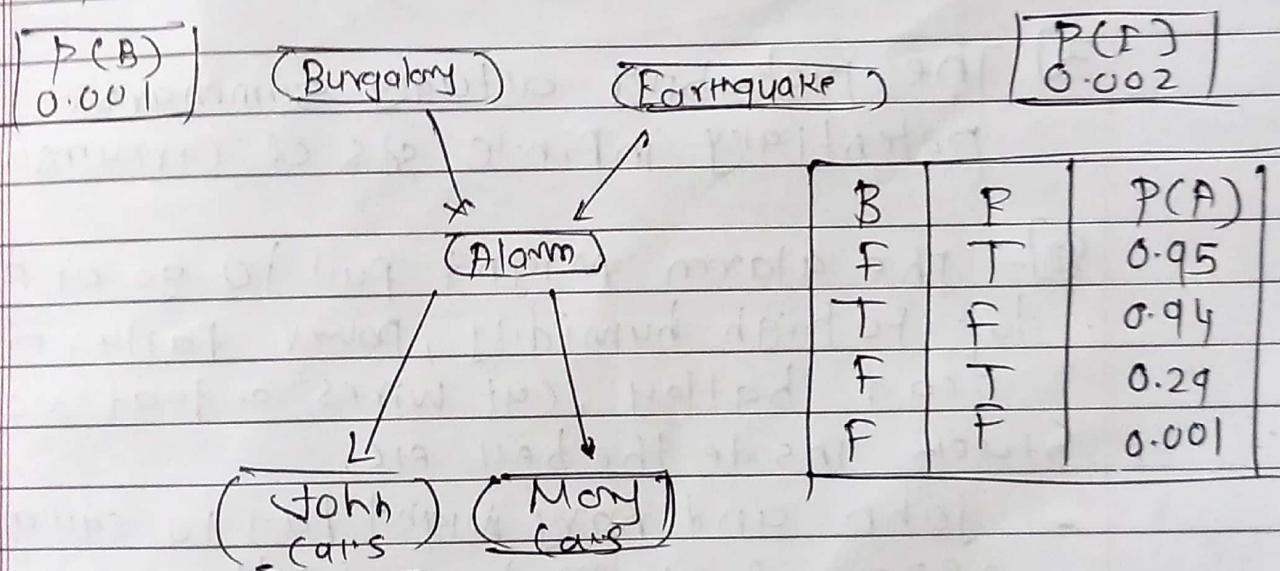
Can support both positive & negative literals.
for e.g.: Same sentence is expressed as
Stupid \wedge ugly

2) STRIPS stand for standard Research Institute problem Solver

2) stand for Action Description language

- | | |
|--|---|
| 3) Makes use of closed world assumption (i.e.) unmentioned literals are false. | 3) Makes use of open world assumption (i.e.) unmentioned literals are unknown. |
| 4) We can only find ground literals in goals for e.g.: Intelligent A beautiful. | 4) We can find qualified variables in goals for e.g.: $\exists x A \wedge [P_1(x) \wedge A \wedge (P_2, x)]$ is the goal of having P_1 & P_2 in the same place in the example of blocks |
| 5) Goals are conjunctions for e.g.: ($\text{Intelligent} \wedge \text{Beautiful}$) | 5) Goals may involve conjunctions & disjunctions. for e.g.: ($\text{Intelligent} \wedge (\text{Beautiful} \vee \text{Rich})$) |
| 6) Effects are conjunctions | 6) Conditional effects are allowed: when $P \leq P$ means F is an effect only if P is satisfied. |
| 7) Does not support equality | 7) Equality predicate ($x = y$) is built-in |
| 8) Does not have support for types. | 8) Support for types for e.g.: The variable P : person. |

(Q.4) You have two neighbours J and M, who have promised to call you at work when they hear the alarm. J always calls when he hears the alarm but sometimes confuses telephone ringing with alarms & calls them too. M likes loud music and sometimes misses the alarm together. Given the evidence of who has or has not called we would like to estimate the probability of burglary. Draw a Bayesian network for this domain with suitable probability table.



A	P(T)
T	0.09
F	0.05

A	P(M)
T	0.70
F	0.01

- I] The topology of the network indicates that
 - Burglary and earthquake affect the probabilities of the alarm going off.

→ Whether John and Mary call depends on alarm

They do not perceive any burglaries directly they do not notice minor earthquakes and they do not compare before calling.

2) Mary listening to loud music & John confusing phone ringing to sound of alarm can be read from network only implicitly as uncertainty associated to calling at work.

3] The probability actually summarizes potentially infinite sets of circumstances

① - The alarm might fail to go off due to high humidity, power failure, dead battery, cut wires or dead mouse stuck inside the bell etc.

- John and Mary might fail to call and report the alarm because they are out to lunch on vacation, temporarily deaf, passing helicopter, etc.

4] The condition probability tables in NW gives probability for values of random variables depending on combination of values for the parent nodes.

- 5] Each row must sum to 1 because entries represent exhaustive set of cases for variable
- 6] All variables are Boolean
- 7] In general, a table for a Boolean variable with K parents contains 2^K independently specific probabilities.
- 8] A Variable with no parents has only one row representing prior probabilities of each possible value of the variable.
- 9] Every entry in full joint probability distribution can be calculated from information in Bayesian network
- 10] A generic entry in joint distribution is probability of a conjunction of particular assignment to each variable $P(X_1 = x_1 \wedge \dots \wedge x_n = x_n)$ abbreviated as $P(x_1, \dots, x_n)$
- 11] The value of this entry is $P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(x_i))$, where $\text{parents}(x_i)$ denotes the specific values of the variables parents(x_i)
 $- P(j \wedge m \wedge a \wedge b \wedge n \wedge m)$

$$\begin{aligned} &= P(j|q) P(m|q) P(a \text{ in base}) \\ &\quad P(\neg b) e(m) \end{aligned}$$

$$\begin{aligned} &= 0.09 \times 0.07 \times 0.001 \times 0.999 \times 0.998 \\ &\approx 0.000628 \end{aligned}$$

12] Bayesian Network.

