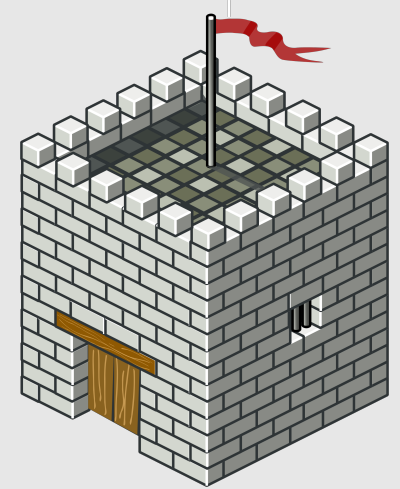


Foundations of Cybersecurity

X-Protocols



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2017



Cryptographic Protocols

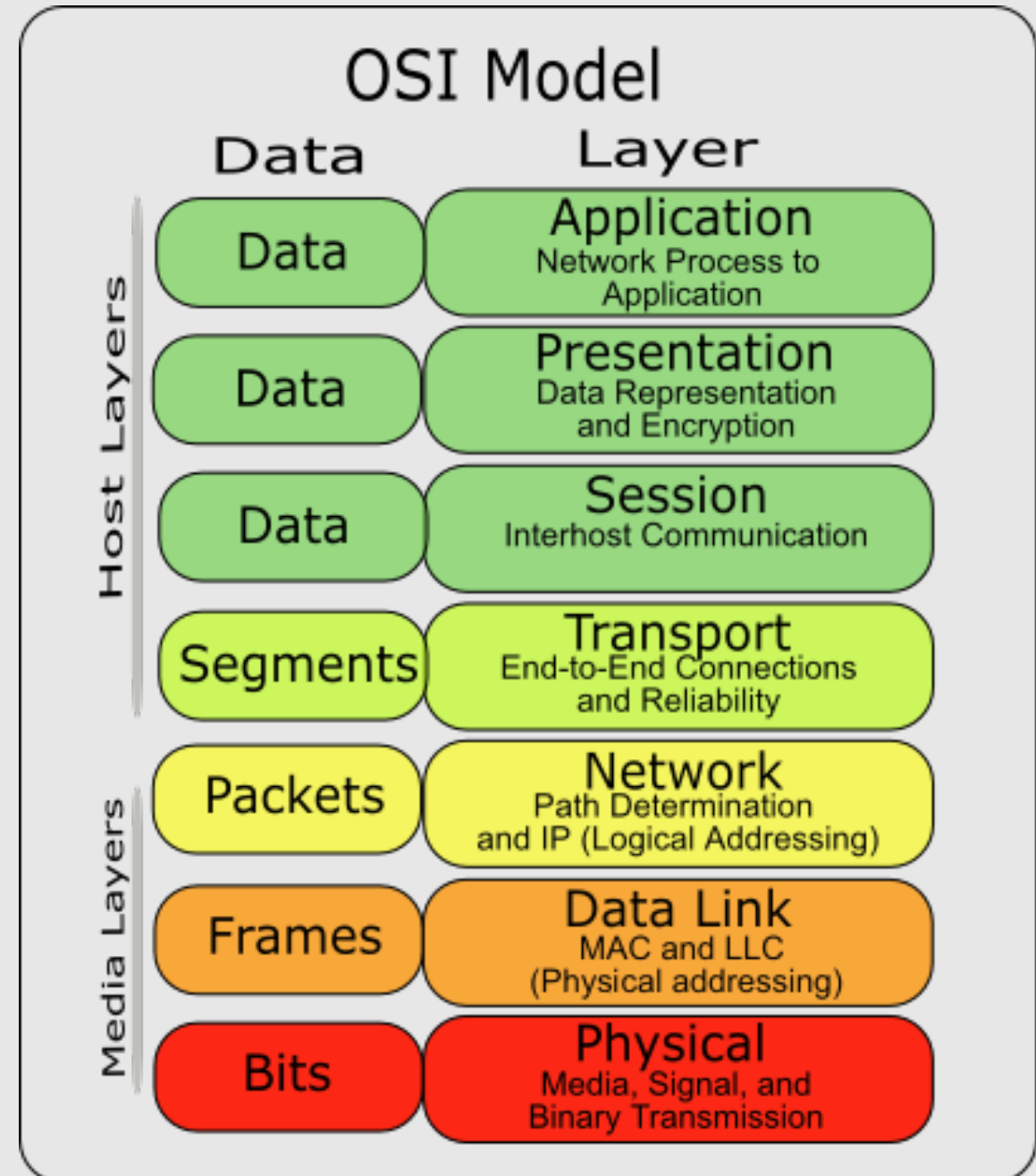
- Roles
 - Alice and Bob (client-server, customer-merchant, ...)
 - Adversary (passive, man-in-the-middle, able to steal secrets,...)
- Trust
 - Ethics, reputation, law, ...
- Incentives
 - Influence behavior, deployment, ...

Cryptographic Protocols

- Trust in cryptographic protocols
 - Cryptography tries to minimize the amount of trust required (usually, by replacing it by mathematics)
 - Number of trusted parties
 - Scope of trust
- Paranoia model
 - Alice assumes that all participants are colluding against her

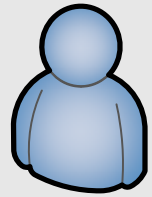
Messages and Steps

- High level of abstraction
- Transport Layer
- Protocol and Message Identity
- Message Encoding and Parsing
- Protocol State Machine
- Errors
- Replay and Retries



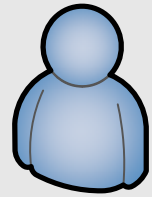
Key Negotiation

Recap: Basic DH



Alice

Random secret a



Bob

Random secret b

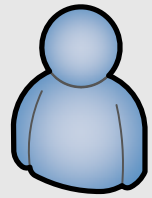
$$g^a \bmod p$$

$$g^b \bmod p$$

$$K = (g^b)^a \bmod p$$

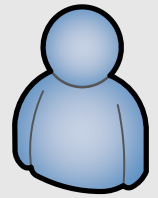
$$K = (g^a)^b \bmod p$$

Authenticated DHv1



Alice

known (g, p, q)
 $a = \text{random}(1, q-1)$
 $A = g^a \text{ mod } p$



Bob

known (g, p, q)

$b = \text{random}(1, q-1)$
 $B = g^b \text{ mod } p$

A

B

$K = (B)^a \text{ mod } p$

$AUTH_{Alice}(K)$

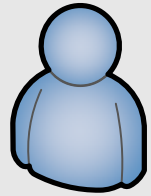
$K = (A)^b \text{ mod } p$

check $AUTH_{Alice}(K)$

$AUTH_{Bob}(K)$

check $AUTH_{Bob}(K)$

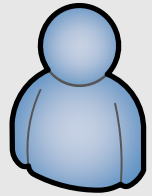
Authenticated DHv2



Alice

choose (g, p, q)
 $a = \text{random}(1, q-1)$
 $A = g^a \text{ mod } p$

$(g, p, q), A, AUTH_{Alice}$



Bob

check (g, p, q)
check $A, AUTH_{Alice}$
 $b = \text{random}(1, q-1)$
 $B = g^b \text{ mod } p$

$B, AUTH_{Bob}$

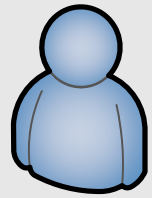
check $B, AUTH_{Bob}$
 $K = (B)^a \text{ mod } p$

$K = (A)^b \text{ mod } p$

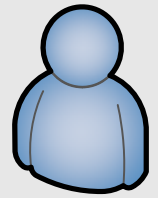
Choosing (g, p, q) :

1. $p = 2q + 1$
2. p, q are prime
3. $a = \text{random}(2, p-2)$
4. $g = a^2 \text{ mod } p \wedge g \neq 1 \wedge g \neq p-1$

Authenticated DHv3



Alice



Bob

$s = \text{min } p \text{ size}$

$N = \text{random}(0, 2^{256}-1)$

s, N

choose (g, p, q)

$b = \text{random}(1, q-1)$

$B = g^b \text{ mod } p$

$(g, p, q), B, AUTH_{Bob}$

check (g, p, q)

check $B, AUTH_{Bob}$

$a = \text{random}(1, q-1)$

$A = g^a \text{ mod } p$

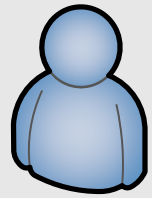
$A, AUTH_{Alice}$

check $A, AUTH_{Alice}$

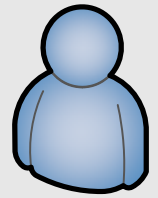
$K = (B)^a \text{ mod } p$

$K = (A)^b \text{ mod } p$

Authenticated DH (final, short)



Alice



Bob

$s = \min p \text{ size}$

$N = \text{random}(0, 2^{256}-1)$

s, N

choose (g, p, q)

$b = \text{random}(1, q-1)$

$B = g^b \text{ mod } p$

$(g, p, q), B, AUTH_{Bob}$

check (g, p, q)

check $B, AUTH_{Bob}$

$a = \text{random}(1, q-1)$

$A = g^a \text{ mod } p$

$A, AUTH_{Alice}$

check $A, AUTH_{Alice}$

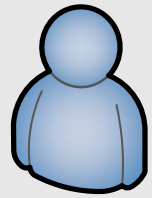
$K' = (B)^a \text{ mod } p$

$K = \text{SHA-256}(K')$

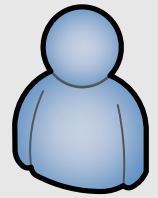
$K' = (A)^b \text{ mod } p$

$K = \text{SHA-256}(K')$

Authenticated DH (final, long)



Alice



Bob

$s_a = \min p \text{ size}$
 $N = \text{random}(0, 2^{256}-1)$

s_a, N

$s_b = \min p \text{ size}$
 $s = \max(s_a, s_b)$
assert $s \leq 2 \cdot s_b$
choose (g, p, q) : $\log_2 p \geq s-1$
 $b = \text{random}(1, q-1)$
 $B = g^b \text{ mod } p$

$(g, p, q), B, AUTH_{Bob}$

check $AUTH_{Bob}$
assert $s_a-1 \leq \log_2 p \leq 2 \cdot s_a$
assert $255 \leq \log_2 q \leq 256$
check (p, q) both prime
assert $q \mid (p-1) \wedge g \neq 1 \wedge g^q = 1$
assert $B \neq 1 \wedge B^q = 1$
 $a = \text{random}(1, q-1)$
 $A = g^a \text{ mod } p$

$A, AUTH_{Alice}$

check $A, AUTH_{Alice}$
assert $A \neq 1$ and $A^q = 1$
 $K' = (A)^b \text{ mod } p$
 $K = \text{SHA-256}(K')$

$K' = (B)^a \text{ mod } p$
 $K = \text{SHA-256}(K')$

The Clock

Uses

- Expiration
 - Limit validity period of a document or credential
- Unique Value
 - Timestamp + make sure it is unique
 - It is predictable
- Monotonicity
 - Replay protection
 - Auditing and logging
- Real-Time Operations
 - Payments

Security

- Manipulating the Clock
 - Setting back, stopping, setting forward
- Reliable Clock
 - No simple solution (CPU, network time, atomic clock, GPS, ...)
- The Same-State Problem
 - Embedded devices
- Time Standard
 - UTC (issues the leap seconds)

Key Servers

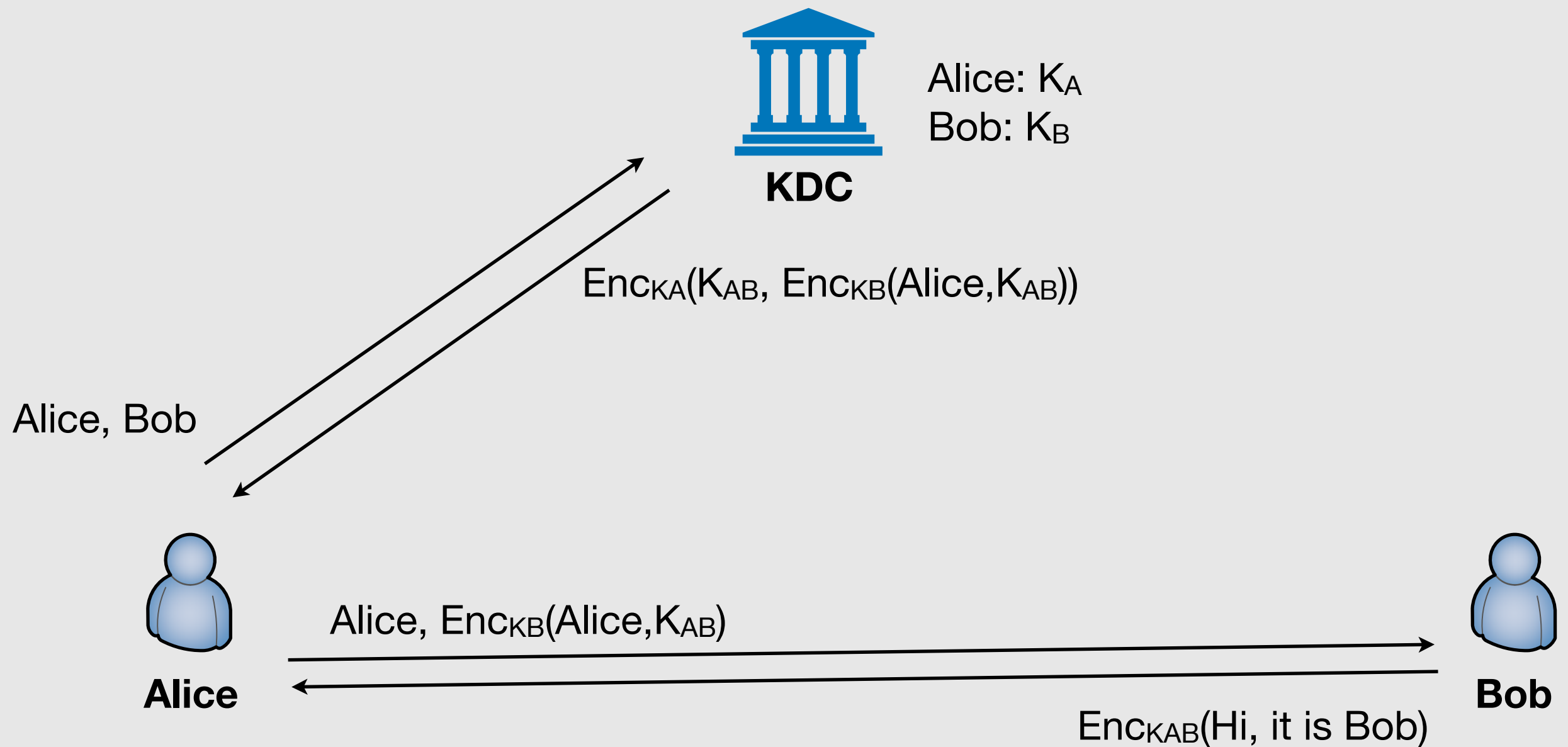
Key Management

- How Alice and Bob recognize each other?
- Challenging as people are involved
 - Hard to understand and predict
- Key server
 - A trusted entity that holds keys of all participants

Key Server

- Everybody sets up a shared key with the key server
 - The server knows K_A shared with Alice, and K_B shared with Bob
- Alice wants to talk to Bob
 - She has no key shared with Bob
 - ... but she can communicate securely with the server, which in turn can communicate securely with Bob
 - The server could ask as a proxy, but due to scalability issue it is much better when the server establish a key for Alice and Bob

Kerberos (simplified)



Kerberos

- Complicated
 - What is authenticated?
 - What is encrypted?
 - What is timestamped/nonced?
- Replay attacks
 - Needham–Schroeder protocols
- Key-Distribution Center (KDC)
 - Trusted
 - It is a single point of failure
 - Significant overheads

Alternatives

- Alice can simply establish a secure channel with KDC
 - The secure channel provides authenticated, confidentiality, replay protection, ...
 - K_A can be used to derive a new key(s), used for the secure channel establishment
 - encrypted K_{AB} can be sent by the server within the channel
- Now a protocol to pass K_{AB} to Bob is only needed
 - That task seems to be simpler

Discussion&Classwork