



Sino Bright School Chongqing

## Monthly Exam, 2024-2025 T2

Subject: Further Math

Date: May 2025

Time: 60 Minutes

Teacher Responsible: Shi Feng

### **IMPORTANT: Read together before beginning the exam.**

Students must complete the assessments to the best of their ability. Any students found cheating during an exam will be given a zero and referred to the Principal for further disciplinary measures. Cheating is a serious offense.

"Cheating" may include any of the following:

- Having course papers, notes, unapproved data sheets or other course-related materials in the exam room without the express permission of the subject class teacher in charge of the exam.
- Using or even having a cellphone or other electronic device in the exam room without the express permission of the subject class teacher in charge of the exam.
- Attempting to communicate, either verbally or non-verbally with other students during the exam.
- Having exam-related materials prior to the writing of the exam.

<b>Mark Breakdown:</b>	Student Name: _____  Score: _____
Part 1: Multiple Choice Questions $5pts \times 10$	
Part 2: Short Answer Questions $5pts \times 4$	
Part 3: Long Answer Questions $15pts \times 2$	
Total Score: 100	

### **Special Instructions/Materials Allowed:**

- Pen
- Calculator



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## Part I: Multiple Choice Questions ( $5pts \times 10$ )

1. If a root of  $f(x) = 0$  lies in  $[3, 4]$ , what is the midpoint after the first iteration of interval bisection?  
A) 3.25  
B) 3.5  
C) 3.75  
D) 3.0
2. The formula for the first approximation  $x_1$  using linear interpolation is:  
A)  $x_1 = a - \frac{f(a)(b-a)}{f(b)-f(a)}$   
B)  $x_1 = \frac{a+b}{2}$   
C)  $x_1 = a - \frac{f(a)}{f'(a)}$   
D)  $x_1 = \frac{f(b)-f(a)}{b-a}$
3. The directrix of the parabola  $y^2 = 24x$  is:  
A)  $x = -6$   
B)  $x = 6$   
C)  $y = -6$   
D)  $y = 6$
4. The modulus of  $z = 3 + 4i$  is:  
A) 5  
B) 7  
C) 12  
D) 25
5. The iteration formula is  $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$ . What condition is critical for convergence?  
A)  $f'(x_n) \neq 0$   
B)  $f(x_n) > 0$   
C)  $f(x_n) < 0$   
D)  $f'(x_n) = 0$
6. If  $z = 2 - 5i$ , then  $z + z^*$  equals:  
A) 4  
B)  $-10i$   
C)  $4 - 10i$   
D) 0
7. A root of a continuous function  $f(x)$  exists in  $[a, b]$  if:  
A)  $f(a)$  and  $f(b)$  are positive  
B)  $f(a) \cdot f(b) < 0$   
C)  $f(a) = f(b)$   
D)  $f(a) \cdot f(b) > 0$
8. The Cartesian equation for  $x = 2t$ ,  $y = 4t^2$  is:  
A)  $y = x^2$



- B)  $y = 2x^2$
- C)  $y = \frac{x^2}{4}$
- D)  $y = 4x^2$

9. The asymptotes of  $xy = 9$  are:

- A)  $x = 0$  and  $y = 0$
- B)  $x = 3$  and  $y = 3$
- C)  $x = 9$  and  $y = 9$
- D) None

10. If a quadratic equation has roots  $\alpha$  and  $\beta$ , then  $\alpha + \beta =$

- A)  $\frac{b}{a}$
- B)  $-\frac{b}{a}$
- C)  $\frac{c}{a}$
- D)  $-\frac{c}{a}$

## Part II: Short Answer Questions (5pts $\times$ 4)

1. After 3 iterations of interval bisection on  $[3, 4]$ , the interval length is \_\_\_\_\_.
2. For  $f(2) = -3$  and  $f(4) = 5$ , the next approximation using linear interpolation is \_\_\_\_\_.
3. The focus of the parabola  $y^2 = 28x$  is at \_\_\_\_\_.
4. The argument of  $z = -1 - i$  (in radians) is \_\_\_\_\_.

## Part III: Long Answer Questions (15pts $\times$ 2)

1. Let  $z^6 = 1$ .
  - (a) Find all the solutions to the equation.



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(b) Show each solution on an Argand diagram.

(c) Show that each solution lies on a circle with center  $(0, 0)$  and radius 1.

2. Given the quadratic equation  $x^2 - 5x + 6 = 0$  with roots  $\alpha$  and  $\beta$ :

(a) Use Vieta's formulas to find  $\alpha + \beta$  and  $\alpha\beta$ .

(b) Construct a new quadratic equation with roots  $2\alpha$  and  $2\beta$ .

(c) Use the Newton-Raphson method with  $x_0 = 3$  to approximate a root of the new equation. Perform 2 iterations and round your answers to 4 decimal places.