

#### Sino Bright School Chongqing

# Monthly Exam, 2024-2025 T2

Subject: Further Math
Date: May 2025
Time: 60 Minutes
Teacher Responsible: Shi Feng

#### IMPORTANT: Read together before beginning the exam.

Students must complete the assessments to the best of their ability. Any students found cheating during an exam will be given a zero and referred to the Principal for further disciplinary measures. Cheating is a serious offense.

"Cheating" may include any of the following:

- Having course papers, notes, unapproved data sheets or other course-related materials in the exam room without the express permission of the subject class teacher in charge of the exam.
- Using or even having a cellphone or other electronic device in the exam room without the express permission of the subject class teacher in charge of the exam.
- Attempting to communicate, either verbally or non-verbally with other students during the exam.
- Having exam-related materials prior to the writing of the exam.

Mark Breakdown:	
Part 1: Multiple Choice Questions $5pts \times 10$	Student Name:
Part 2: Short Answer Questions $5pts \times 4$	
Part 3: Long Answer Questions $15pts \times 2$	
Total Score: 100	Score:

#### Special Instructions/Materials Allowed:

- Pen
- Calculator



## Part I: Multiple Choice Questions ( $5pts \times 10$ )

- 1. If a root of f(x) = 0 lies in [3,4], what is the midpoint after the first iteration?
  - A) 3.25
  - B) 3.5
  - C) 3.75
  - D) 3.0
- 2. The formula for the next approximation  $x_1$  using linear interpolation is:
  - A)  $x_1 = a \frac{f(a)(b-a)}{f(b)-f(a)}$ B)  $x_1 = \frac{a+b}{2}$

  - C)  $x_1 = a \frac{f(a)}{f'(a)}$ D)  $x_1 = \frac{f(b) f(a)}{b a}$
- 3. The directrix of the parabola  $y^2 = 24x$  is:
  - A) x = -6
  - B) x = 6
  - C) y = -6
  - D) y = 6
- 4. The modulus of z = 3 + 4i is:
  - A) 5
  - B) 7
  - C) 12
  - D) 25
- 5. The iteration formula is  $x_{n+1} = x_n \frac{f(x_n)}{f'(x_n)}$ . What condition is critical for convergence?
  - A)  $f'(x_n) \neq 0$
  - B)  $f(x_n) > 0$
  - C)  $f(x_n) < 0$
  - D)  $f'(x_n) = 0$
- 6. If z = 2 5i, then  $z + z^*$  equals:
  - A) 4
  - B) -10i
  - C) 4 10i
  - D) 0
- 7. A root exists in [a, b] if:
  - A) f(a) and f(b) are positive
  - B)  $f(a) \times f(b) < 0$
  - C) f(a) = f(b)
  - D)  $f(a) \times f(b) > 0$
- 8. The Cartesian equation for x = 2t,  $y = 4t^2$  is:
  - A)  $y = x^2$



B) 
$$y = 2x^2$$

B) 
$$y = 2x^2$$
  
C)  $y = \frac{x^2}{4}$   
D)  $y = 4x^2$ 

$$D) y = 4x^2$$

- 9. The asymptotes of xy = 9 are:
  - A) x = 0 and y = 0
  - B) x = 3 and y = 3
  - C) x = 9 and y = 9
  - D) None
- 10. If a quadratic equation has roots  $\alpha$  and  $\beta$ , then  $\alpha + \beta =$ 

  - A)  $\frac{b}{a}$ B)  $-\frac{b}{a}$ C)  $\frac{c}{a}$ D)  $-\frac{c}{a}$

### Part II: Fill-in-the-Blank $(5pts \times 4)$

- 1. After 3 iterations of interval bisection on [3,4], the interval length is \_\_\_\_\_.
- 2. For f(2) = -3 and f(4) = 5, the next approximation using linear interpolation is \_
- 3. The focus of the parabola  $y^2 = 28x$  is at \_\_\_\_\_.
- 4. The argument of z = -1 i (in radians) is \_\_\_\_\_

## Section C: Long Answer Questions ( $15pts \times 2$ )

1. Use the Newton-Raphson method with  $x_0 = 2$  to approximate a root of  $f(x) = x^3 - 2x - 5$ . Perform 2 iterations.

2. Let 
$$z = 1 + \sqrt{3}i$$
.

(a) Find |z| and arg(z).

(b) Express z in modulus-argument form.

(c) Solve  $z^2 = 1 + \sqrt{3}i$ .