

# JAGS Model

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## Basic Model: Ambulance + Overdose

### Ambulance Call-outs Model

$n_A$ : sample size

$x_A$ : the total number who confirmed they did call an ambulance

$p_A$ : probability of a person call an ambulance

$$x_A \sim \text{Bin}(n_A, p_A)$$

We assume  $n_A = 1000, p_A = 0.8$ .

Suppose the prior of  $p_A$  is noninformative.

$$p(p_A) \sim \text{Beta}(1, 1)$$

### Overdose Model

Now we plug in this values into the overdose model and obtain possible  $O_t$  values **assuming we have  $U_t$  values.**

Also, we have priors.

$$z_t \sim N(\mu, \sigma^2)$$

$$\lambda_t^{OD} = \exp(z_t)$$

$$O_t \sim \text{Poi}(\lambda_t^{OD} N)$$

$$U_t \sim \text{Bin}(O_t, p_A)$$

For simplicity we set  $N = 10000$  for now. We need to generate reasonable  $U_t$  values first. Note that  $U_t$  comes from  $\mu, \sigma$  following all the way through the overdose model.

$\mu = \log 0.05, \sigma = 1, N = 10000$ .

We suppose survey data exists:  $(n_A, x_A)$  known.

We set for our prior parameters:

$$\mu \sim U(-10, 0)$$

$$\sigma \sim U(0, 5)$$

```
# install packages
if (!require(rjags)) install.packages("rjags", dependencies = TRUE)
if (!require(coda)) install.packages("coda", dependencies = TRUE)
if (!require(tidyverse)) install.packages("tidyverse", dependencies = TRUE)
if (!require(tinytex)) install.packages("tinytex", dependencies = TRUE)

library('rjags')
library('coda')
library('tidyverse')
library('tinytex')
```

The data is the same data from pymc3 with Python.

Todo: build a pipeline to connect the python (pymc3) and R (JAGS)

```
df <- read.csv('./basic_data.csv')
df$X <- NULL
head(df)
```

```
##      o_t  u_t x_a
## 1 2475 1969 799
## 2  262  217 798
## 3  318  253 795
## 4  149  119 816
## 5 1151  934 805
## 6   39   34 794
```

Now we set the model which defines the relations of overdose model and ambulance call model.

The model defined as follows.

```
cat("model{
## define the priors

p_a ~ dbeta(alpha, beta)
mu_z ~ dunif(mu_a, mu_b)
sigma_z ~ dunif(sigma_a, sigma_b)

## ambulance model
for (i in 1:n) {
  #Likelihood
  x_a[i] ~ dbin(p_a, n_a) # each survey result for month
}

# overdose
for (i in 1:n) {

  ## the latent variables
  z_t[i] ~ dnorm(mu_z, 1/(sigma_z^2))
  lmb_t[i] <- exp(z_t[i])

  ## overdose model
  o_t[i] ~ dpois(lmb_t[i]*N) # total overdoses per month
  # Note that from pymc3 gamma was used instead of Pois dist
  u_t[i] ~ dbin(p_a, o_t[i]) # ambulated overdoses per month
}

}", file='basic_model.txt')
```

Pre-set variables.

```
n_T <- length(df$o_t)
n_a <- 1000
N <- 10000
u_t <- df$u_t
x_a <- df$x_a
```

Define the list providing the values of the variables and the parameters for the priors of the model.

```

dat <- list(
  # priors for ambulance model
  'alpha' = 1,
  'beta' = 1,

  # priors for overdose model
  'mu_a'=(-10),
  'mu_b'=0,
  'sigma_a'=0,
  'sigma_b'=5,

  # likelihood
  'u_t'=u_t, # giving data
  'x_a'=x_a, # giving data
  'N'=N, # the population 10000
  'n'= n_T, # total months 12
  'n_a'=n_a # survey size 1000

)

```

Note: for the list object usually named ‘data’ or ‘dat’ in JAGS context, do not use arrow but use equal sign to define elements of the list.

```

chains=2
# inits = list()
simple.model <- jags.model(file='basic_model.txt',
                          data=dat,
                          n.chains = chains)

```

```

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 24
##   Unobserved stochastic nodes: 27
##   Total graph size: 88
##
## Initializing model

```

```
simple.model
```

```

## JAGS model:
##
## model{
## ## define the priors
##
## p_a ~ dbeta(alpha, beta)
## mu_z ~ dunif(mu_a, mu_b)
## sigma_z ~ dunif(sigma_a, sigma_b)
##
##
## ## ambulance model
## for (i in 1:n) {
##   #Likelihood
##   x_a[i] ~ dbin(p_a, n_a) # each survey result for month

```

```
##
## }
##
## # overdose
## for (i in 1:n) {
##
##   ## the latent variables
##   z_t[i]~ dnorm(mu_z, 1/(sigma_z^2))
##   lmb_t[i] <- exp(z_t[i])
##
##   ## overdose model
##   o_t[i] ~ dpois(lmb_t[i]*N) # total overdoses per month
##   # Note that from pymc3 gamma was used instead of Pois dist
##   u_t[i] ~ dbin(p_a, o_t[i]) # ambulated overdoses per month
## }
##
## }
## Fully observed variables:
## N alpha beta mu_a mu_b n n_a sigma_a sigma_b u_t x_a
```

O\_t

```
params= c('o_t','p_a')
samples <- coda.samples(simple.model, params, n.iter = 1000)
# guess it's getting posterior samples ?
```

```
iterations = 1000
burnin= floor(iterations/2)
summary(window(samples), start=burnin)
```

```
##
## Iterations = 1001:2000
## Thinning interval = 1
## Number of chains = 2
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
##    plus standard error of the mean:
##
##      Mean      SD Naive SE Time-series SE
## o_t[1] 2477.4060 27.802746 6.217e-01 0.9911877
## o_t[2] 273.1270 8.638934 1.932e-01 0.2534807
## o_t[3] 317.9915 9.023976 2.018e-01 0.2493259
## o_t[4] 150.2440 6.326648 1.415e-01 0.1906376
## o_t[5] 1175.5660 17.962683 4.017e-01 0.5026958
## o_t[6] 42.9835 3.292666 7.363e-02 0.0896641
## o_t[7] 3009.8790 31.378251 7.016e-01 1.2014412
## o_t[8] 246.4995 8.131486 1.818e-01 0.2350357
## o_t[9] 715.8720 13.974271 3.125e-01 0.4215083
## o_t[10] 387.8660 10.265073 2.295e-01 0.2874126
## o_t[11] 2082.5475 25.846562 5.779e-01 0.8717076
## o_t[12] 69.5490 4.254368 9.513e-02 0.1198737
## p_a 0.7945 0.003794 8.483e-05 0.0001644
##
```

```
## 2. Quantiles for each variable:
##
##           2.5%      25%      50%      75%      97.5%
## o_t[1]  2424.0000 2459.000 2478.0000 2495.000 2533.0000
## o_t[2]   257.0000  267.000  273.0000  279.000  290.0000
## o_t[3]   302.0000  312.000  318.0000  324.000  337.0000
## o_t[4]   138.9750  146.000  150.0000  154.000  163.0000
## o_t[5]  1141.0000 1163.000 1176.0000 1188.000 1211.0000
## o_t[6]    37.0000   41.000   43.0000   45.000   50.0000
## o_t[7]  2950.9750 2988.750 3010.0000 3030.000 3076.0250
## o_t[8]   232.0000  241.000  246.0000  252.000  263.0000
## o_t[9]   690.0000  706.000  716.0000  725.000  743.0000
## o_t[10]  368.9750  381.000  387.5000  395.000  409.0000
## o_t[11] 2030.0000 2065.000 2082.0000 2099.000 2134.0250
## o_t[12]   62.0000   67.000   69.0000   72.000   79.0000
## p_a      0.7867    0.792    0.7946    0.797    0.8019
```

q1: what is the equivalent plot that we can see we have enough iteration?

Boxplots of O\_t

q2: I see two elements from the samples list. Which one I should use it or should I use both?

```
pst_mtx = as.matrix(samples)
temp = pst_mtx[,1:12]
p_a <- pst_mtx[,13]
head(temp)
```

```
##      o_t[1] o_t[2] o_t[3] o_t[4] o_t[5] o_t[6] o_t[7] o_t[8] o_t[9]
## [1,]  2442   292   315   157  1194    42  3036   263   702
## [2,]  2525   300   317   151  1194    45  2999   240   720
## [3,]  2487   281   316   155  1168    42  3016   246   729
## [4,]  2561   272   298   168  1184    48  3024   250   718
## [5,]  2497   275   326   155  1155    46  2990   241   708
## [6,]  2517   272   323   163  1146    44  3032   239   722
##      o_t[10] o_t[11] o_t[12]
## [1,]    373   2095     70
## [2,]    371   2125     74
## [3,]    372   2078     79
## [4,]    382   2082     69
## [5,]    396   2140     67
## [6,]    383   2086     64
```

```
length(p_a)
```

```
## [1] 2000
```

```
colnames(temp) <- seq(1,12)
df_o_t <- as.data.frame(temp)
head(df_o_t)
```

```
##      1  2  3  4  5  6  7  8  9 10 11 12
```

```

## 1 2442 292 315 157 1194 42 3036 263 702 373 2095 70
## 2 2525 300 317 151 1194 45 2999 240 720 371 2125 74
## 3 2487 281 316 155 1168 42 3016 246 729 372 2078 79
## 4 2561 272 298 168 1184 48 3024 250 718 382 2082 69
## 5 2497 275 326 155 1155 46 2990 241 708 396 2140 67
## 6 2517 272 323 163 1146 44 3032 239 722 383 2086 64

trace_o_t <- gather(df_o_t, key = 'month',value = 'o_t')
trace_o_t$month <- factor(trace_o_t$month,levels = seq(1,12))
str(trace_o_t)

## 'data.frame':    24000 obs. of  2 variables:
## $ month: Factor w/ 12 levels "1","2","3","4",...: 1 1 1 1 1 1 1 1 1 1 ...
## $ o_t  : num  2442 2525 2487 2561 2497 ...

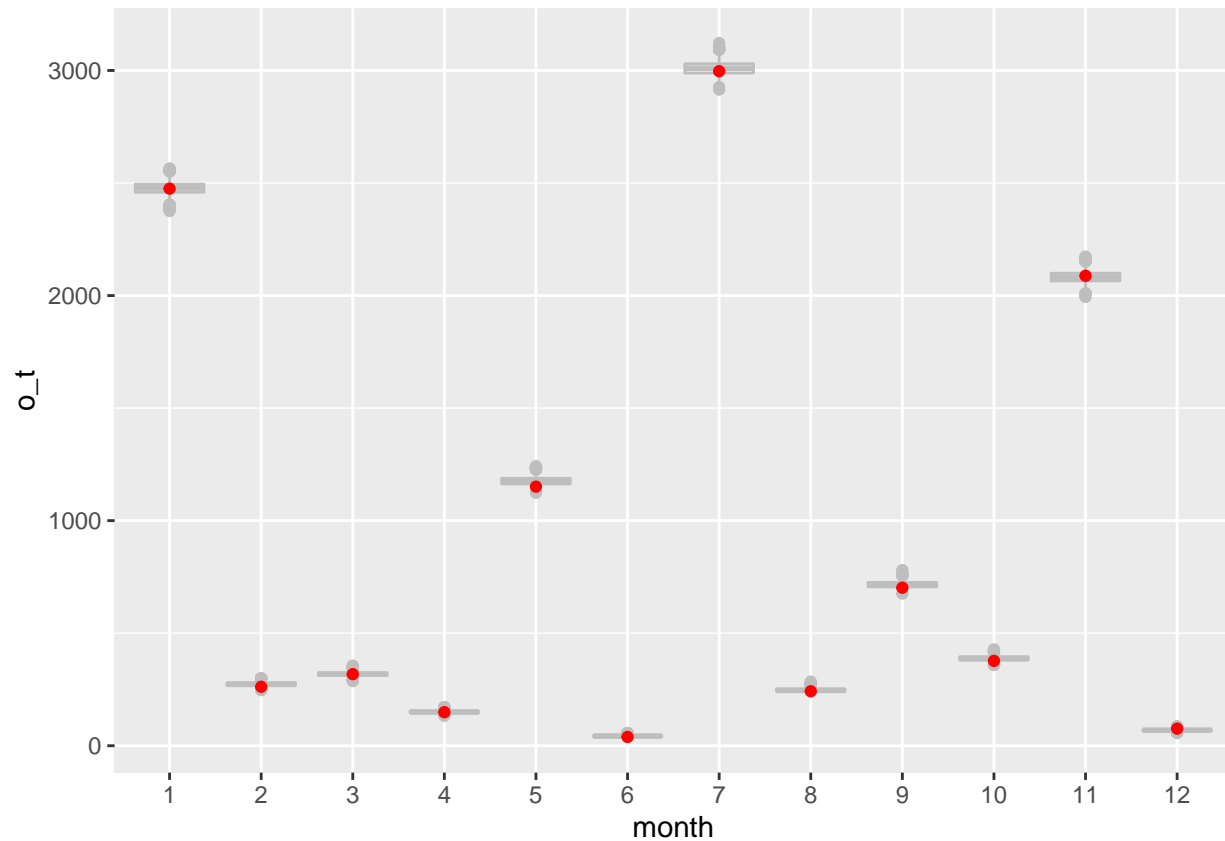
head(trace_o_t,n = 24)

##   month  o_t
## 1     1 2442
## 2     1 2525
## 3     1 2487
## 4     1 2561
## 5     1 2497
## 6     1 2517
## 7     1 2468
## 8     1 2471
## 9     1 2460
## 10    1 2497
## 11    1 2460
## 12    1 2509
## 13    1 2509
## 14    1 2544
## 15    1 2520
## 16    1 2481
## 17    1 2500
## 18    1 2474
## 19    1 2466
## 20    1 2522
## 21    1 2554
## 22    1 2486
## 23    1 2515
## 24    1 2497

# real values of the data set from pymc3 samples
o_t_values=data.frame('month'=seq(1,12),'o_t'=df$o_t)
# factorizing the months for box plot visualization
o_t_values$month <- factor(o_t_values$month,levels = seq(1,12))

ggplot()+
  # boxplot from the trace
  geom_boxplot(aes(x=month,y=o_t), color='grey',data = trace_o_t)+
  # real values as red dots
  geom_point(aes(x=o_t_values$month, y=o_t_values$o_t),color='red')

```



## Predictive Posterior Checks

```
df_u_t <- data.frame()
m=length(p_a)
for (i in 1:m) {
  obs <- rbinom(n=12,size = as.numeric(df_o_t[i,]),prob =p_a[i])
  df_u_t=rbind(df_u_t,obs)
}
colnames(df_u_t) <- factor(seq(1,12),levels = seq(1,12))
str(df_u_t)
```

```
## 'data.frame':    2000 obs. of  12 variables:
## $ 1 : int  1879 2018 1943 2017 1961 1998 1956 1965 1965 1978 ...
## $ 2 : int  223 239 218 224 218 220 208 213 216 202 ...
## $ 3 : int  253 254 261 233 256 254 251 258 254 239 ...
## $ 4 : int  129 120 121 136 122 125 118 119 117 126 ...
## $ 5 : int  940 937 924 967 924 918 919 947 947 920 ...
## $ 6 : int   36 33 31 39 35 36 36 35 31 35 ...
## $ 7 : int 2391 2382 2373 2389 2361 2359 2412 2326 2373 2332 ...
## $ 8 : int  221 192 190 204 194 181 195 195 198 193 ...
## $ 9 : int  568 565 603 557 568 569 572 584 574 543 ...
## $10: int  295 297 287 288 312 320 304 310 325 307 ...
## $11: int 1652 1687 1625 1642 1680 1697 1688 1674 1645 1647 ...
## $12: int   55 59 61 56 55 49 49 50 47 54 ...
```

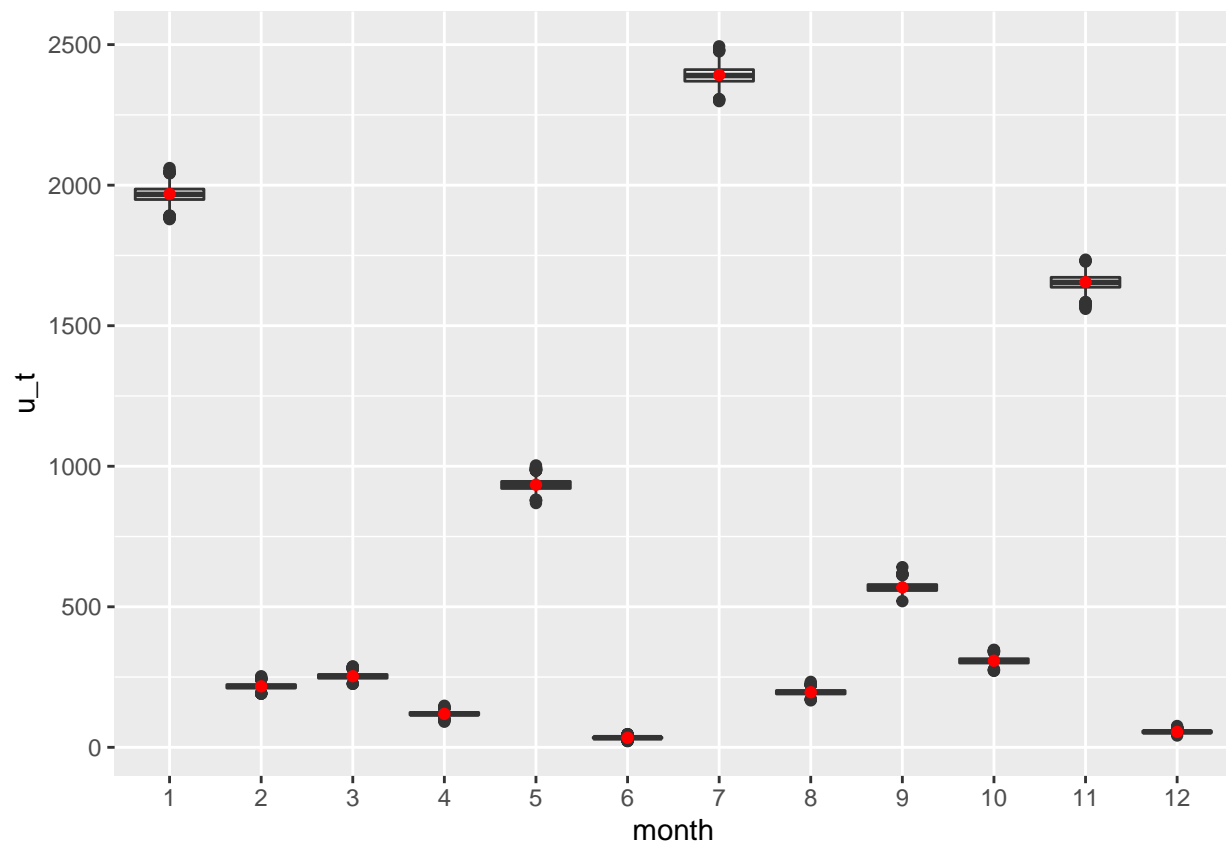
### $U_t$ : Predictive Posterior Checks

```
ppc_u_t <- gather(df_u_t, key = 'month', value = 'u_t')
summary(ppc_u_t)
```

```
##      month          u_t
## Length:24000      Min.   : 22.0
## Class :character  1st Qu.: 162.2
## Mode  :character  Median : 279.5
##                               Mean  : 724.8
##                               3rd Qu.:1142.2
##                               Max.   :2494.0
```

```
u_t_values=data.frame('month'=seq(1,12), 'u_t'=df$u_t)
# u_t_values$month <- factor(u_t_values$month, levels = seq(1,12))
ppc_u_t$month <- factor(ppc_u_t$month, levels = seq(1,12))
```

```
ggplot()+geom_boxplot(aes(x=month,y=u_t),data = ppc_u_t)+geom_point(aes(x=u_t_values$month, y=u_t_values$u_t))
```



todo: finish this part.

### $x_A$ : Predictive Posterior Checks

```
df_x_a <- vector()
for (i in 1:n_T) {
  obs <- rbinom(m,n_a,p_a)
  df_x_a <- cbind(df_x_a,obs)
```



```

}

head(df_x_a)

##      obs obs obs obs obs obs obs obs obs obs obs obs
## [1,] 791 763 797 807 784 783 768 783 779 775 785 773
## [2,] 789 804 789 800 804 799 820 794 793 794 807 789
## [3,] 794 781 779 776 809 803 794 795 817 791 789 789
## [4,] 776 794 769 783 799 778 772 796 792 814 786 777
## [5,] 803 818 789 808 792 796 804 805 793 759 815 785
## [6,] 802 800 809 799 800 808 796 801 826 798 781 801

colnames(df_x_a) <- seq(1:12)

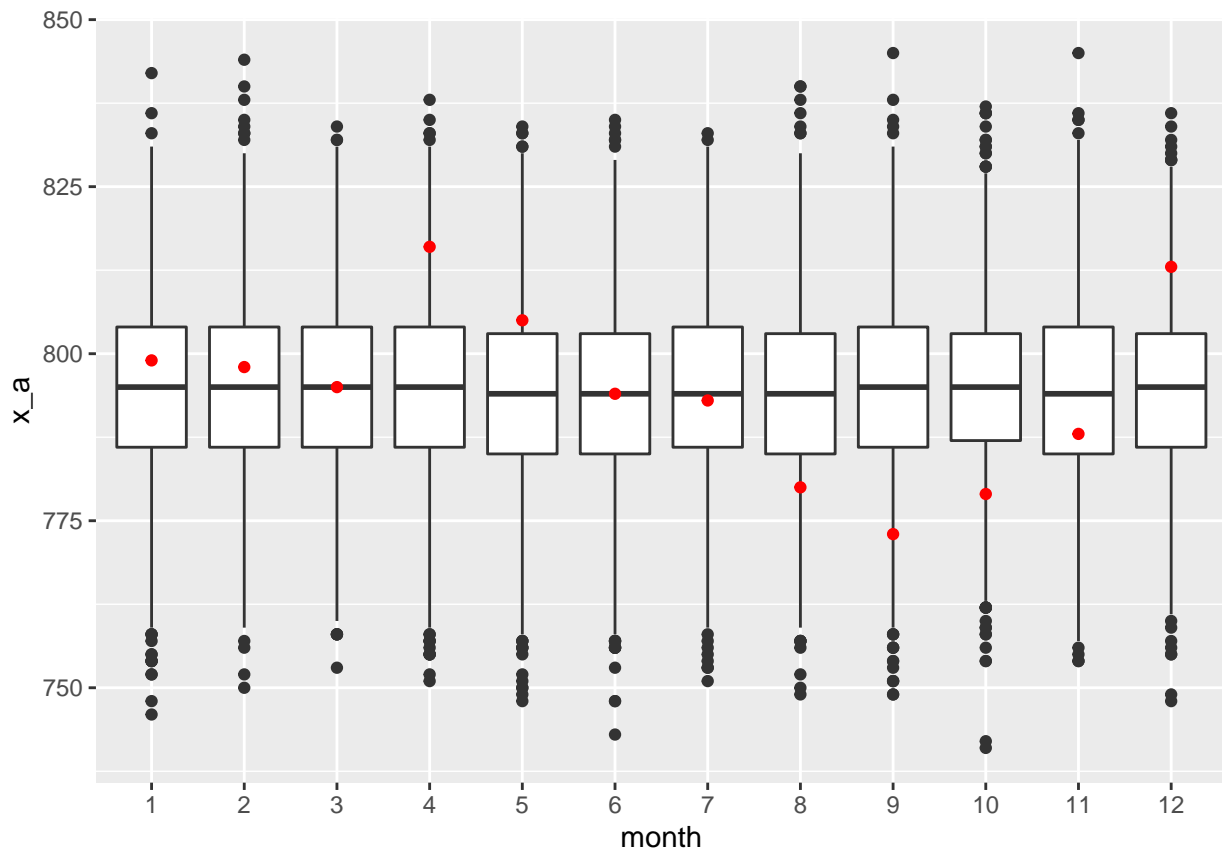
df_x_a <- as.data.frame(df_x_a)
ppc_x_a <- gather(df_x_a, key = 'month', value = 'x_a')

ppc_x_a$month <- factor(ppc_x_a$month, levels = seq(1,12))

x_a_values = data.frame('month' = seq(1,12), 'x_a' = df_x_a)
x_a_values$month <- factor(x_a_values$month, levels = seq(1,12))

ggplot()+geom_boxplot(aes(x=month, y=x_a), data = ppc_x_a) + geom_point(aes(x=x_a_values$month, y=x_a_values$

```



## Contamination of $p_A$

Now, suppose the survey data gives us a wrong (biased)  $p_A$  value.

$$\text{Bias} = \theta - \hat{\theta} = p_A - \hat{p}_A$$

$$\hat{p}_A = p_A + \text{bias}(p_A)$$

Three more data sets are given: unbiased, overestimated, underestimated  $p_A$ .

```
## write a function that led to compare o_t, u_t and x_a.
#first we need a fuction that gives us data, model, trace, and ppc.
test_robust <- function(file=file, random=1, N=10000, p_a=0.8, bias = -0.2, n_a=1000, n_T=12) {
  df <- read.csv(file = file)
  df$X <- NULL
  df$month <- seq(1:12)
  # obtain the (biased) data
  dat <- list(
    # priors for ambulance model
    'alpha' = 1,
    'beta' = 1,

    # priors for overdose model
    'mu_a'=(-10),
    'mu_b'=0,
    'sigma_a'=0,
    'sigma_b'=5,

    # likelihood
    'u_t'=df$u_t, # giving data
    'x_a'=df$x_a,  # giving data
    'N'=N, # the population 10000
    'n'= n_T, # total months 12
    'n_a'=n_a # survey size 1000
  )
  # run the model
  chains=2
  # target 1 to save
  simple.model <- jags.model(file='basic_model.txt',
                             data=dat,
                             n.chains = chains)

  # get the samples of O_t, p_a
  params= c('o_t','p_a')
  # target 2 to save
  samples <- coda.samples(simple.model, params, n.iter = 2000)
  pst_mtx = as.matrix(samples)
  # tidy p_a: target 3
  p_a <- pst_mtx[,13]

  ## tidy o_t
  temp = pst_mtx[,1:12]
  colnames(temp) <- seq(1,12)
  df_o_t <- as.data.frame(temp)
  trace_o_t <- gather(df_o_t, key = 'month', value = 'o_t')
```

```

trace_o_t$month <- factor(trace_o_t$month,levels = seq(1,12))

# tidy u_t pp samples
df_u_t <- data.frame()
m = length(p_a)
for (i in 1:m) {
  obs <- rbinom(n=12,size = as.numeric(df_o_t[i,]),prob =p_a[i])
  df_u_t=rbind(df_u_t,obs)
}
colnames(df_u_t) <- factor(seq(1,12),levels = seq(1,12))
ppc_u_t <- gather(df_u_t, key = 'month',value = 'u_t')
ppc_u_t$month <- factor(ppc_u_t$month,levels = seq(1,12))

## tidy x_a
df_x_a <- vector()
for (i in 1:n_T) {
  obs <- rbinom(m,n_a,p_a)
  df_x_a <- cbind(df_x_a,obs)
}
colnames(df_x_a) <- seq(1:12)
df_x_a <- as.data.frame(df_x_a)
ppc_x_a <- gather(df_x_a, key = 'month',value = 'x_a')
ppc_x_a$month <- factor(ppc_x_a$month,levels = seq(1,12))
ppc = list('u_t'=ppc_u_t, 'x_a'=ppc_x_a)
mylist=list('data'=df,'model'=simple.model,'trace'=trace_o_t,'ppc'=ppc)
return (mylist)
}

# then visualization function which gives us three different types of boxplots.

my_list_unbiased = test_robust(file = './basic_data.csv', bias =0)

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 24
##   Unobserved stochastic nodes: 27
##   Total graph size: 88
##
## Initializing model

my_list_under = test_robust(file = './under_p_a_data.csv',bias=-0.2)

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 24
##   Unobserved stochastic nodes: 27
##   Total graph size: 88
##
## Initializing model

```

```

my_list_over = test_robust(file='./over_p_a_data.csv',bias = +0.1)

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 24
##   Unobserved stochastic nodes: 27
##   Total graph size: 88
##
## Initializing model
print(my_list_unbiased$data$u_t)

## [1] 1969 217 253 119 934 34 2392 196 569 308 1655 55
print(my_list_under$data$u_t)

## [1] 1969 217 253 119 934 34 2392 196 569 308 1655 55
print(my_list_over$data$u_t)

## [1] 1969 217 253 119 934 34 2392 196 569 308 1655 55
print(my_list_unbiased$data$x_a)

## [1] 799 798 795 816 805 794 793 780 773 779 788 813
print(my_list_under$data$x_a)

## [1] 602 598 622 608 595 593 575 638 586 618 574 582
print(my_list_over$data$x_a)

## [1] 898 891 910 902 894 921 881 909 879 913 908 914
head(my_list_unbiased$ppc$u_t)

## month u_t
## 1 1 1955
## 2 1 1928
## 3 1 2016
## 4 1 1976
## 5 1 1988
## 6 1 1971

# finish this function
visualization <- function(mylist= None, post= F, u_t = F, x_a = F, string='string') {
  data= mylist$data
  if (post == T) {
    # boxplots of o_t
    trace_o_t = mylist$trace
    p <- ggplot()+
    # boxplot from the trace
    geom_boxplot(aes(x=month,y=o_t), color='grey',data = trace_o_t)+
    # real values as red dots
    geom_point(aes(x=o_t_values$month, y=o_t_values$o_t),color='red')
  }
}

```

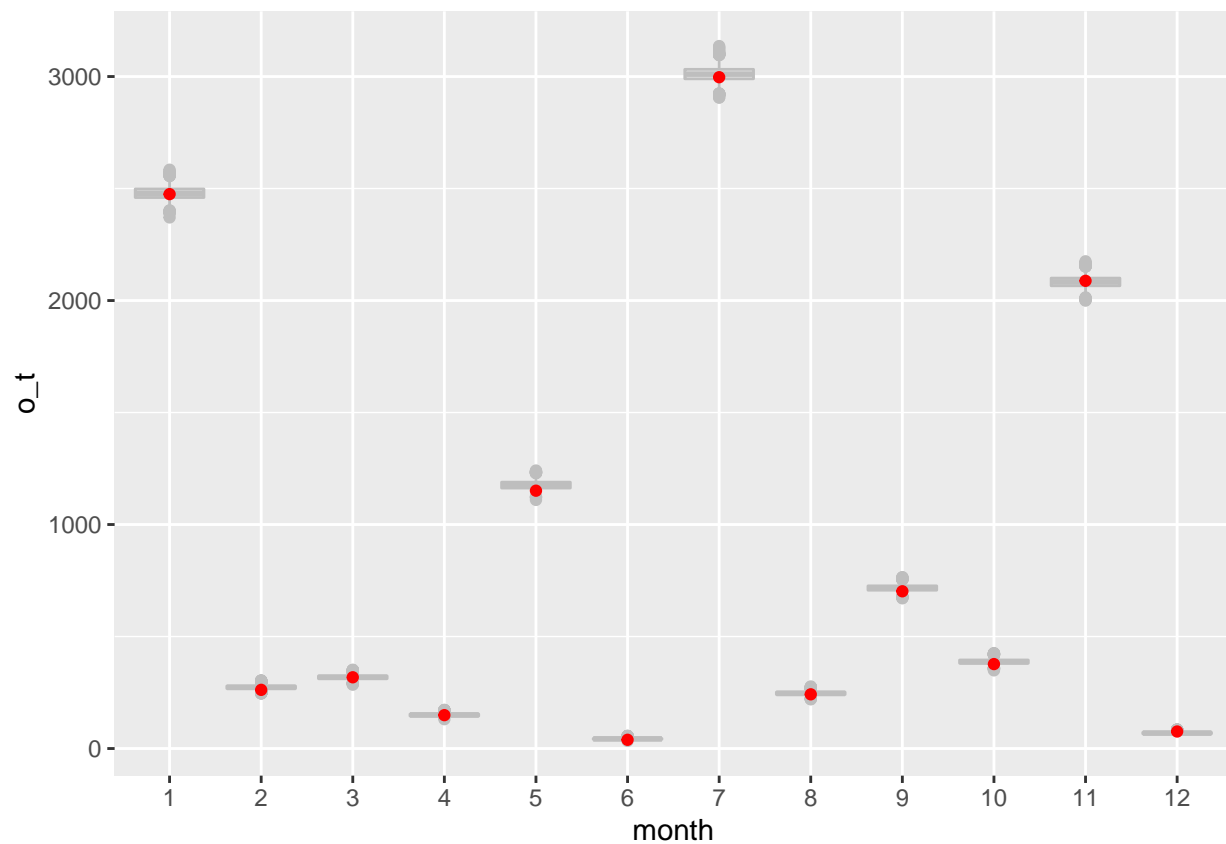
```

if (u_t == T) {
  ppc_u_t = mylist$ppc$u_t
  # boxplots of u_t
  p <- ggplot()+geom_boxplot(aes(x=month,y=u_t),data = ppc_u_t)+geom_point(aes(x=data$month, y=data$u_t,
  })

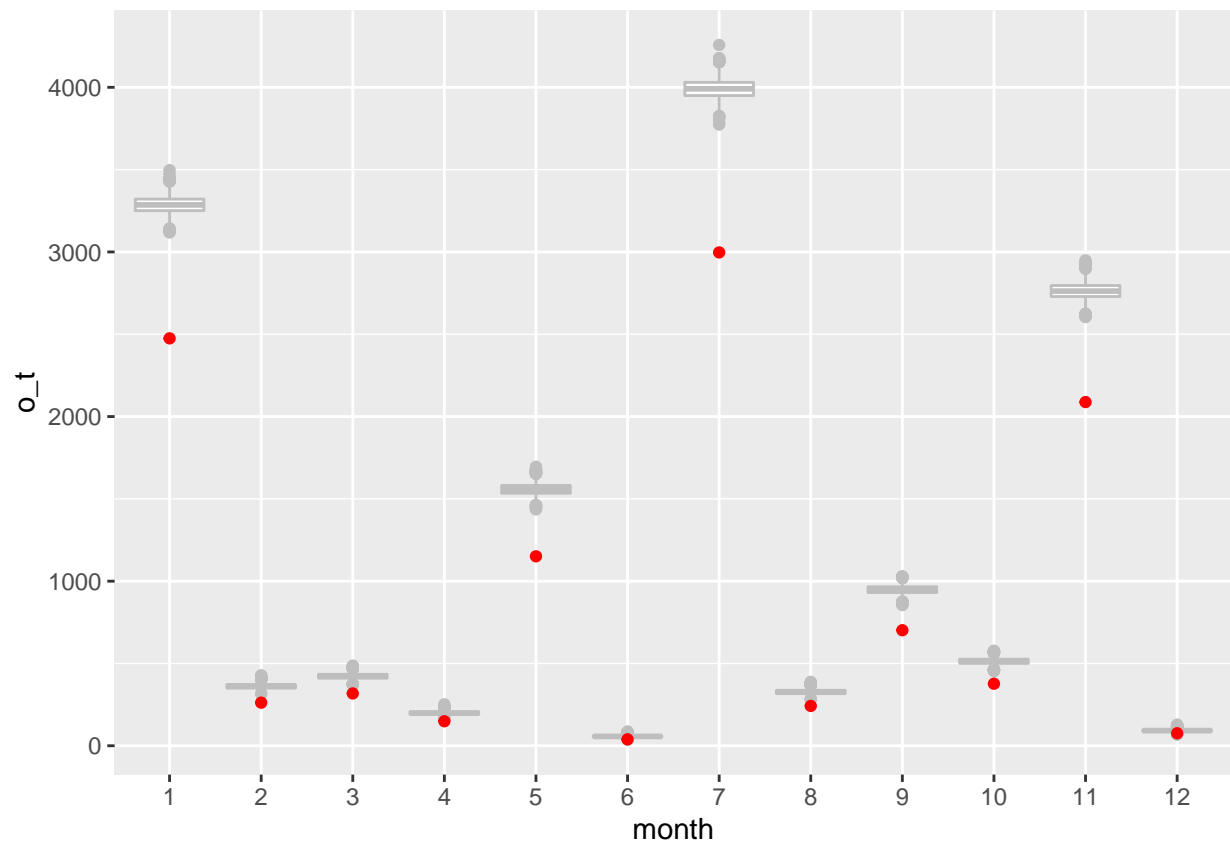
  if (x_a == T) {
    ppc_x_a = mylist$ppc$x_a
    p <- ggplot()+geom_boxplot(aes(x=month,y=x_a),data = ppc_x_a)+geom_point(aes(x=data$month, y=data$x_a,
    })
  }
  return(p)
}

```

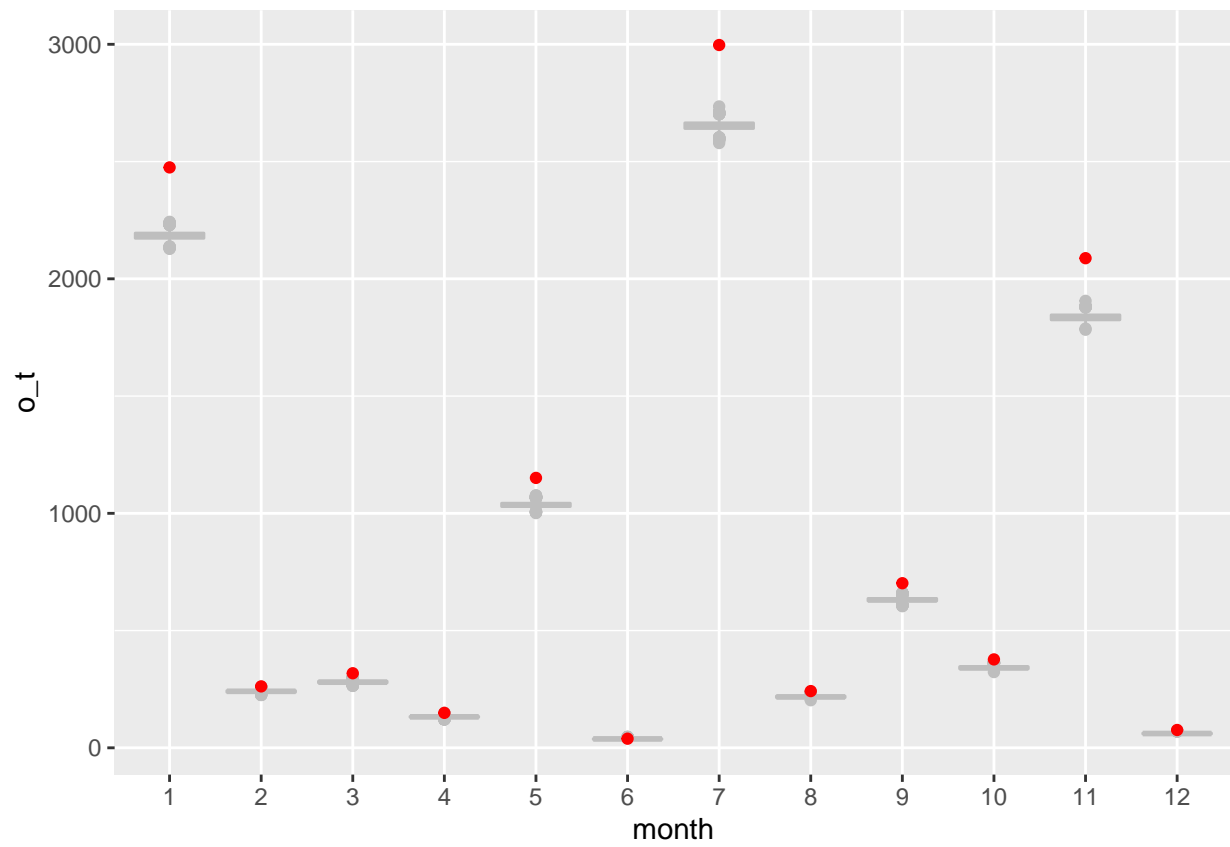
```
visualization(my_list_unbiased, post=T)
```



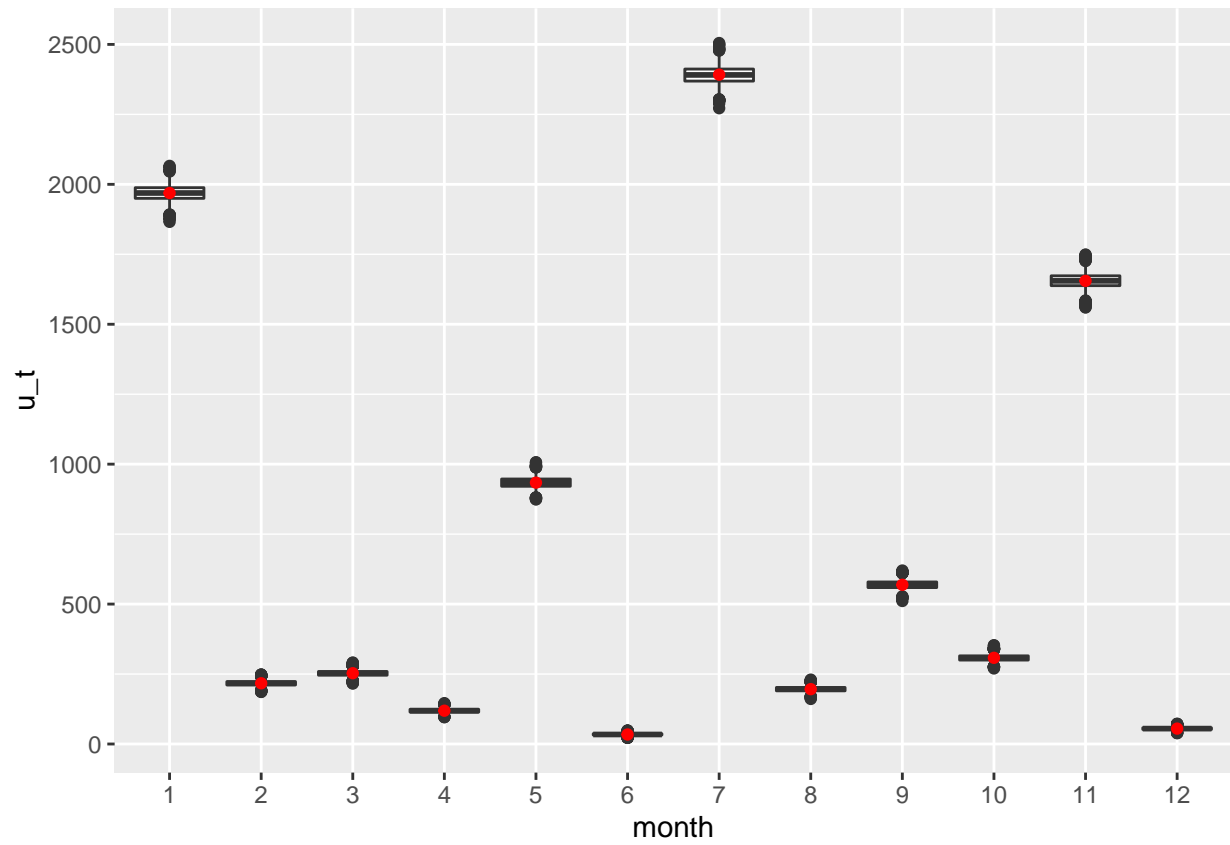
```
visualization(my_list_under,post= T)
```



```
visualization(my_list_over,post=T)
```

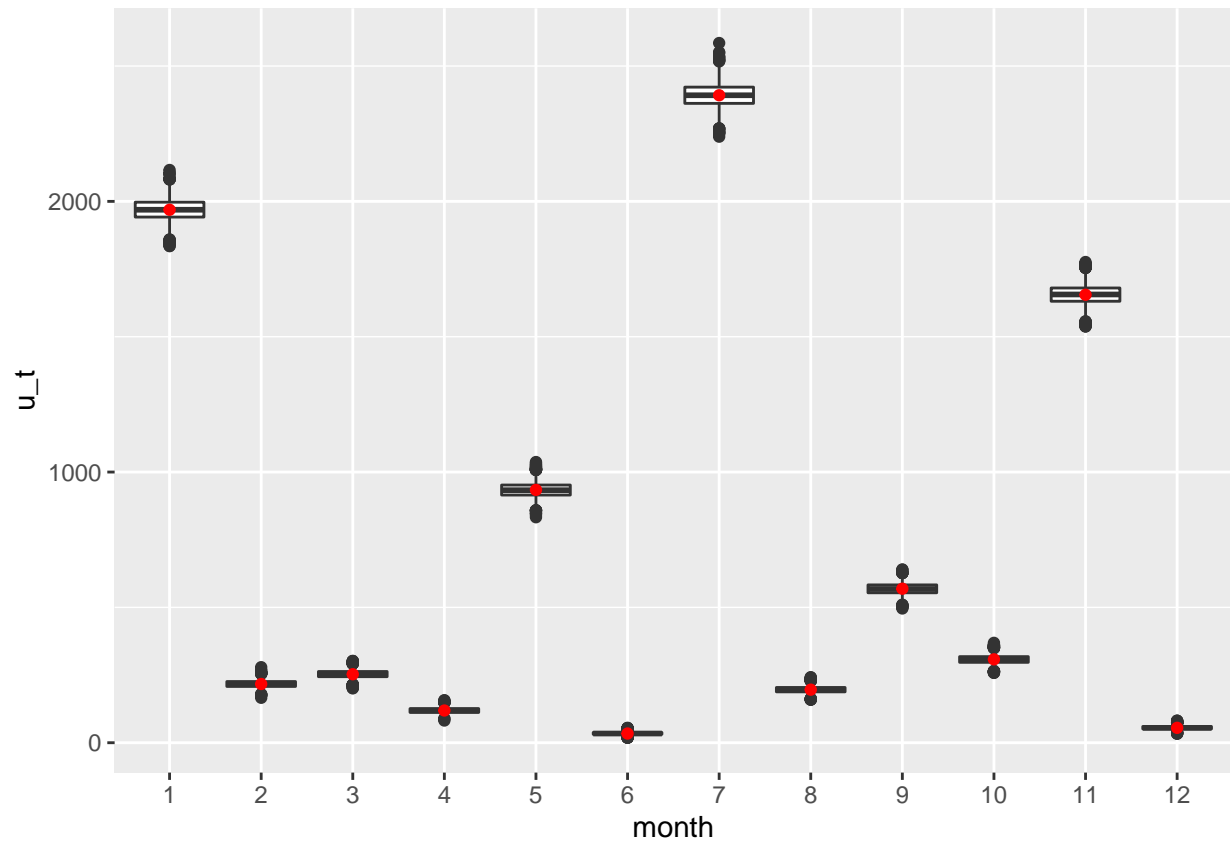


```
visualization(my_list_unbiased, u_t=T)
```

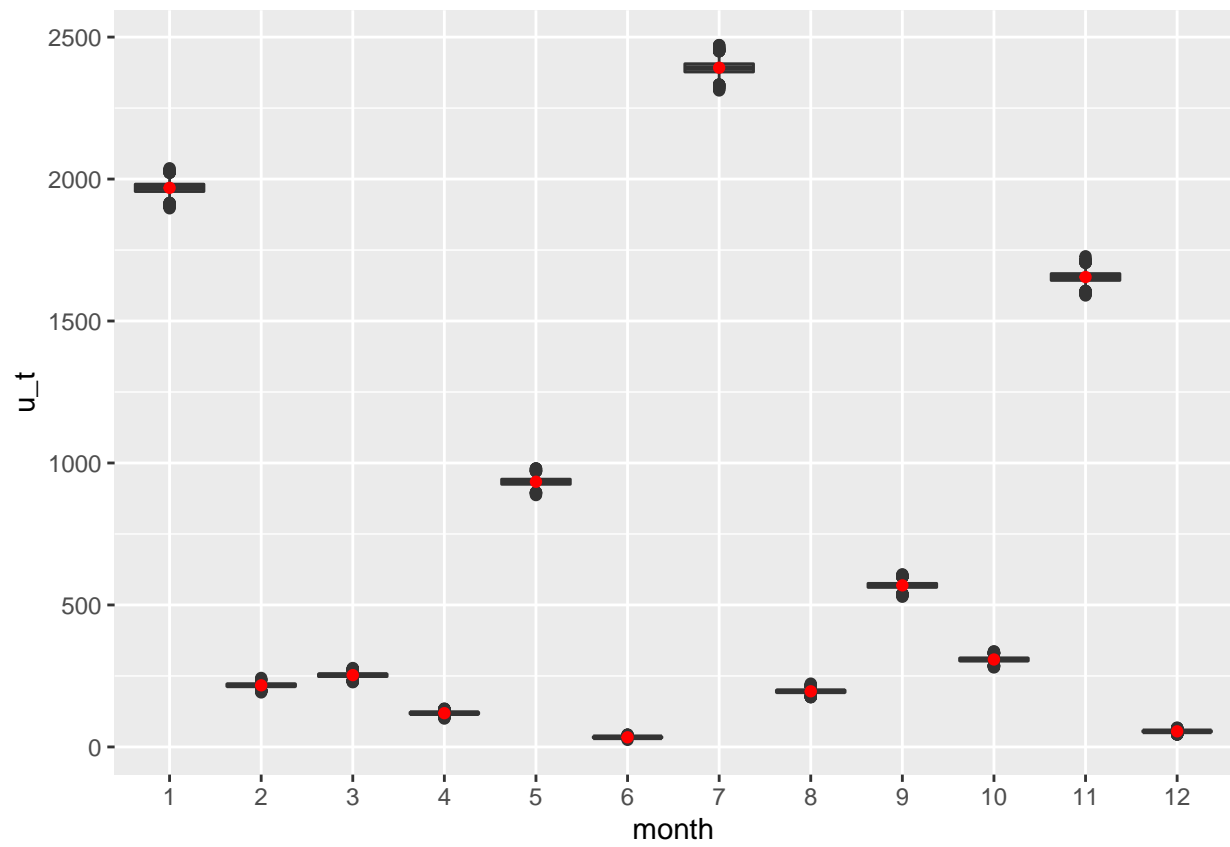


```
visualization(my_list_under,u_t= T)
```

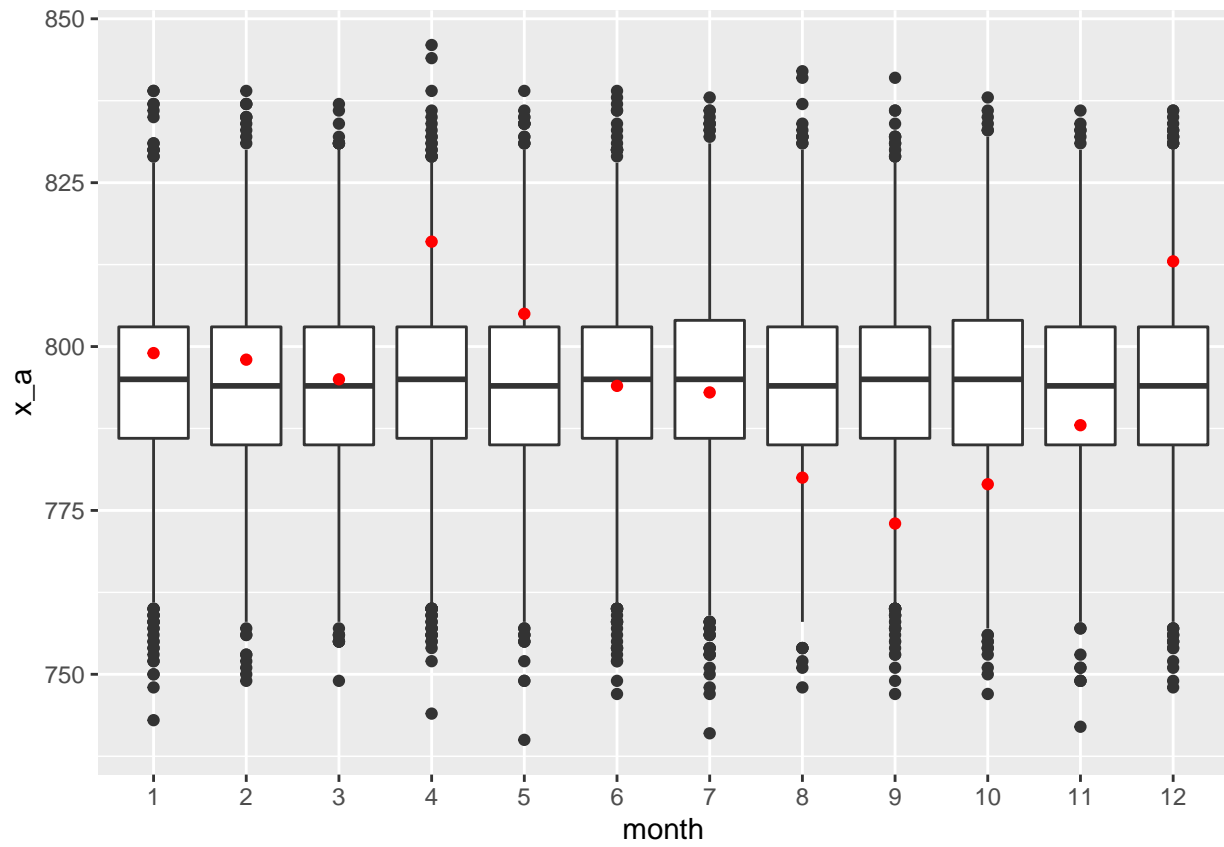




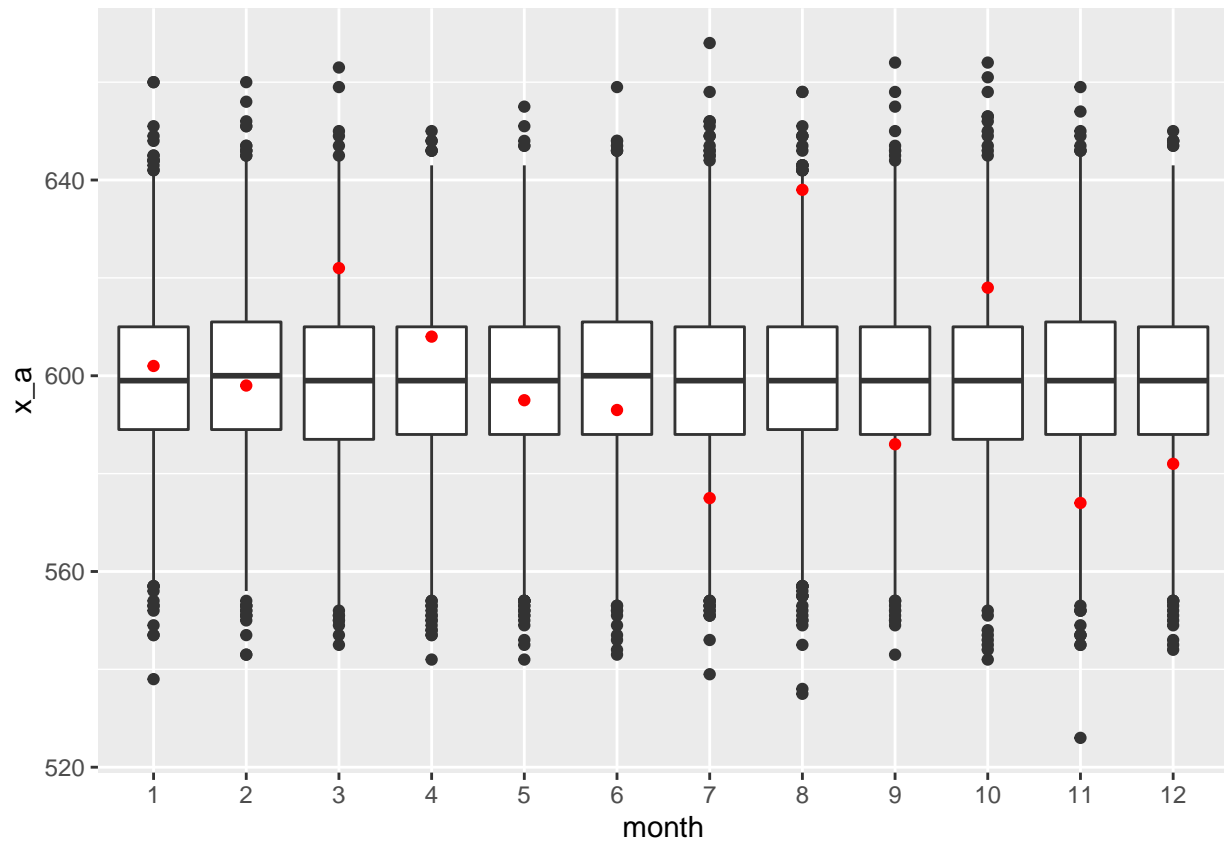
```
visualization(my_list_over,u_t=T)
```



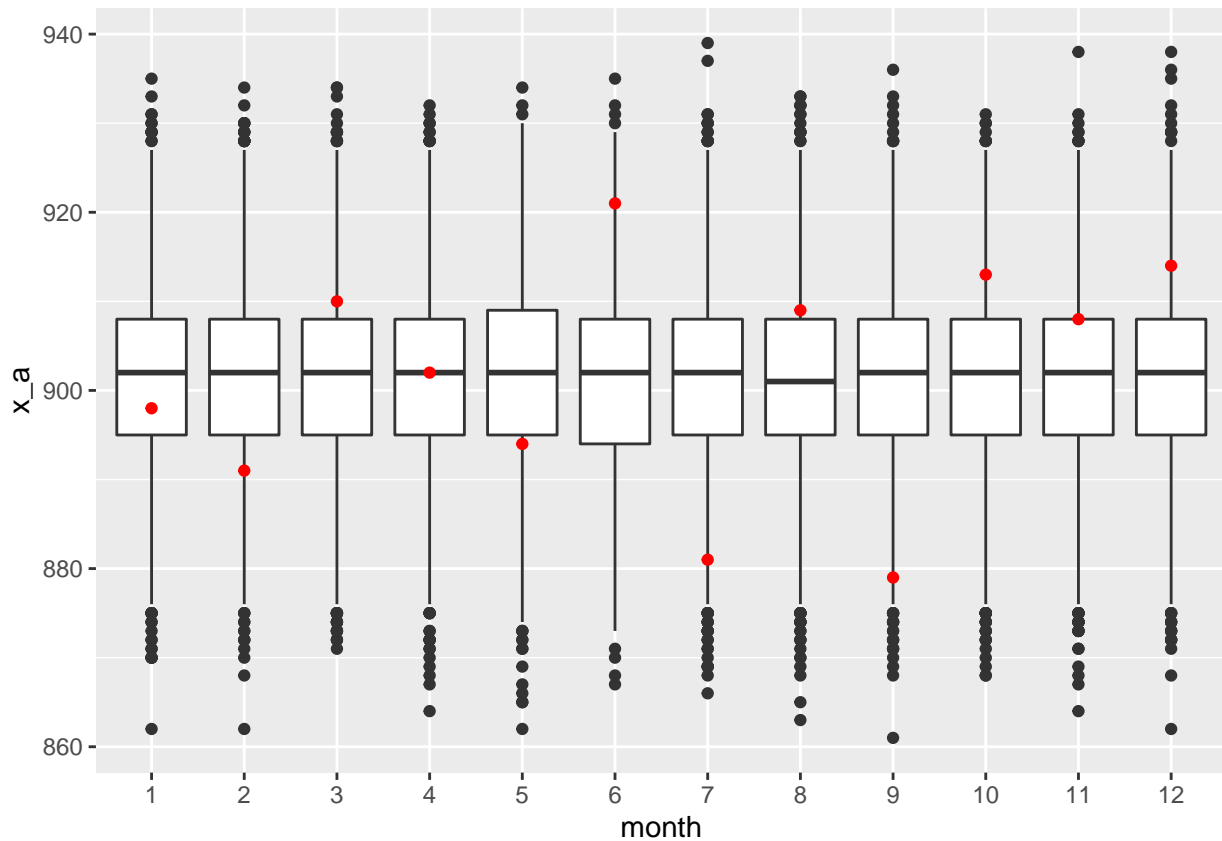
```
visualization(my_list_unbiased, x_a=T)
```



```
visualization(my_list_under, x_a= T)
```



```
visualization(my_list_over,x_a=T)
```



##### Below here is for the purpose of debugging

Trim here and make a function and give us the plots.

```
chains=2
under.model <- jags.model(file='basic_model.txt',
                          data=dat,
                          n.chains = chains)

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 24
##   Unobserved stochastic nodes: 27
##   Total graph size: 88
##
## Initializing model

# inits = list()

# get the samples of O_t, p_a
params= c('o_t','p_a')
samples <- coda.samples(under.model, params, n.iter = 1000)
pst_mtx = as.matrix(samples)
head(pst_mtx)
```

```
##      o_t[1] o_t[2] o_t[3] o_t[4] o_t[5] o_t[6] o_t[7] o_t[8] o_t[9]
## [1,]  2494   285   313   156  1161    38  3077   242   731
## [2,]  2444   277   317   153  1169    40  3060   248   709
## [3,]  2495   275   321   150  1170    43  3058   241   709
## [4,]  2454   277   325   151  1207    45  3018   231   719
## [5,]  2514   284   321   154  1183    44  3025   232   727
## [6,]  2473   274   322   151  1171    44  3045   238   713
##      o_t[10] o_t[11] o_t[12]      p_a
## [1,]    386   2027    71 0.7977980
## [2,]    393   2056    67 0.7934034
## [3,]    379   2041    68 0.7932773
## [4,]    379   2079    72 0.7912505
## [5,]    378   2083    65 0.7937473
## [6,]    382   2075    70 0.7892883
```

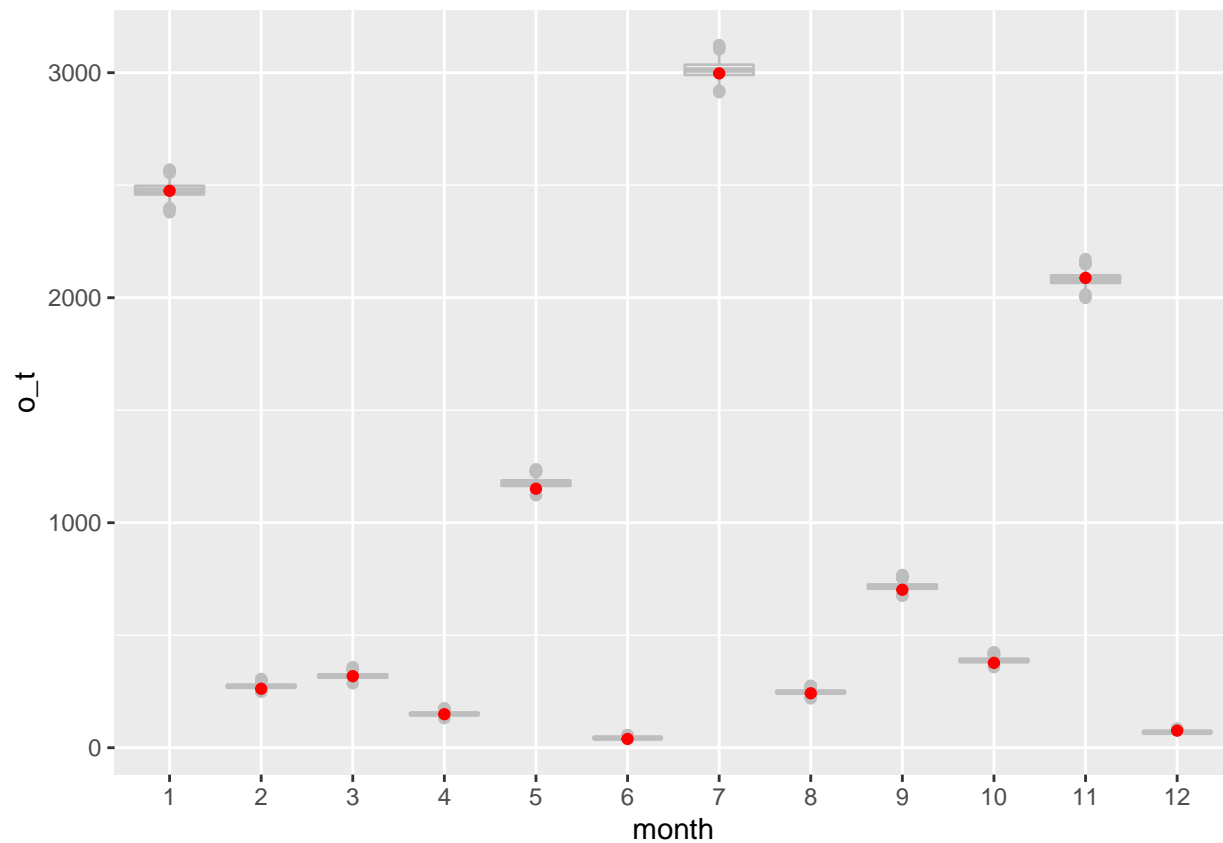
```
# tidy p_a
```

```
p_a <- pst_mtx[,13]
head(p_a)
```

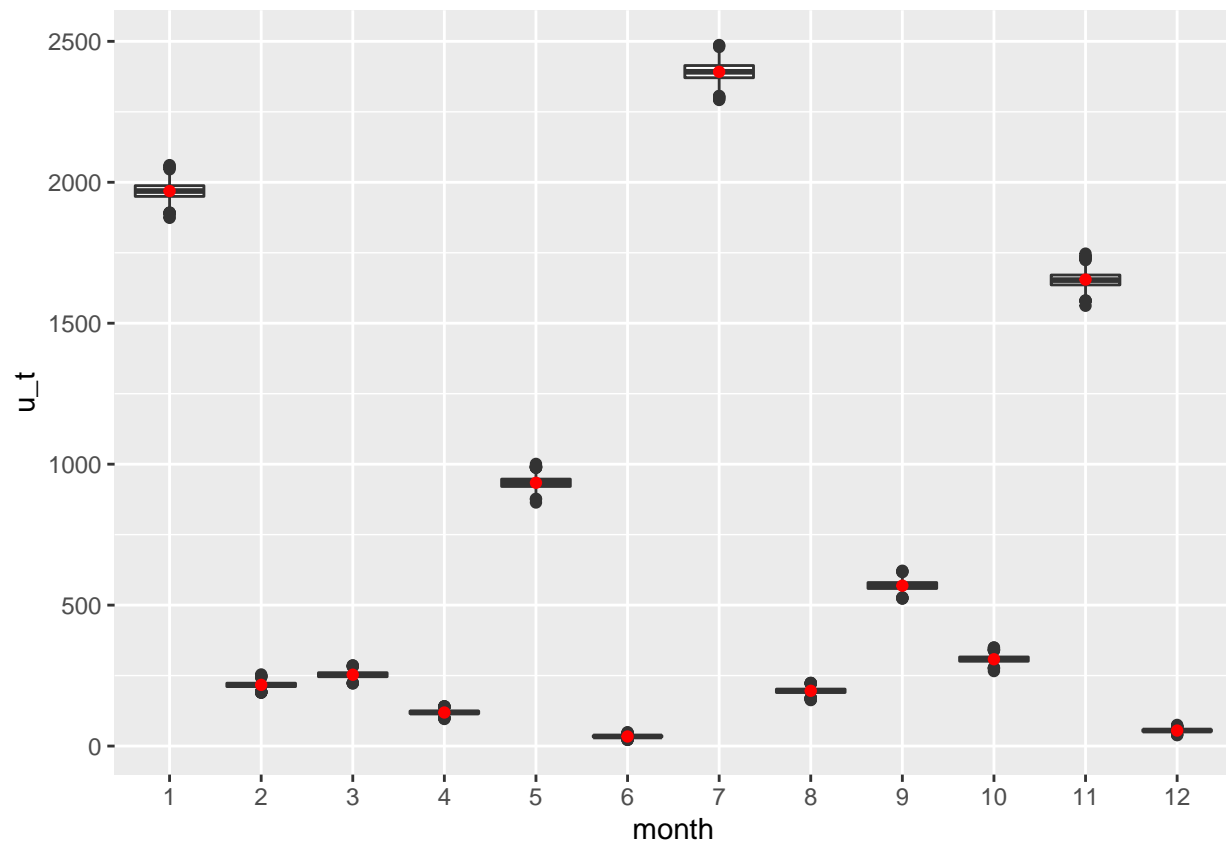
```
## [1] 0.7977980 0.7934034 0.7932773 0.7912505 0.7937473 0.7892883
```

```
## tidy o_t
```

```
pst_mtx = as.matrix(samples)
temp = pst_mtx[,1:12]
colnames(temp) <- seq(1,12)
df_o_t <- as.data.frame(temp)
trace_o_t <- gather(df_o_t, key = 'month', value = 'o_t')
trace_o_t$month <- factor(trace_o_t$month, levels = seq(1,12))
# real values of the data set from pymc3 samples
o_t_values = data.frame('month' = seq(1,12), 'o_t' = df_o_t)
# factorizing the months for box plot visualization
o_t_values$month <- factor(o_t_values$month, levels = seq(1,12))
# boxplots of o_t
ggplot()+
  # boxplot from the trace
  geom_boxplot(aes(x=month, y=o_t), color='grey', data = trace_o_t)+
  # real values as red dots
  geom_point(aes(x=o_t_values$month, y=o_t_values$o_t), color='red')
```



```
# tidy u_t pp samples
df_u_t <- data.frame()
for (i in 1:m) {
  obs <- rbinom(n=12,size = as.numeric(df_o_t[i,]),prob = p_a[i])
  df_u_t=rbind(df_u_t,obs)
}
colnames(df_u_t) <- factor(seq(1,12),levels = seq(1,12))
ppc_u_t <- gather(df_u_t, key = 'month',value = 'u_t')
ppc_u_t$month <- factor(ppc_u_t$month,levels = seq(1,12))
u_t_values=data.frame('month'=seq(1,12), 'u_t'=df$u_t)
# boxplots of u_t
ggplot()+geom_boxplot(aes(x=month,y=u_t),data = ppc_u_t)+geom_point(aes(x=u_t_values$month, y=u_t_values$u_t))
```

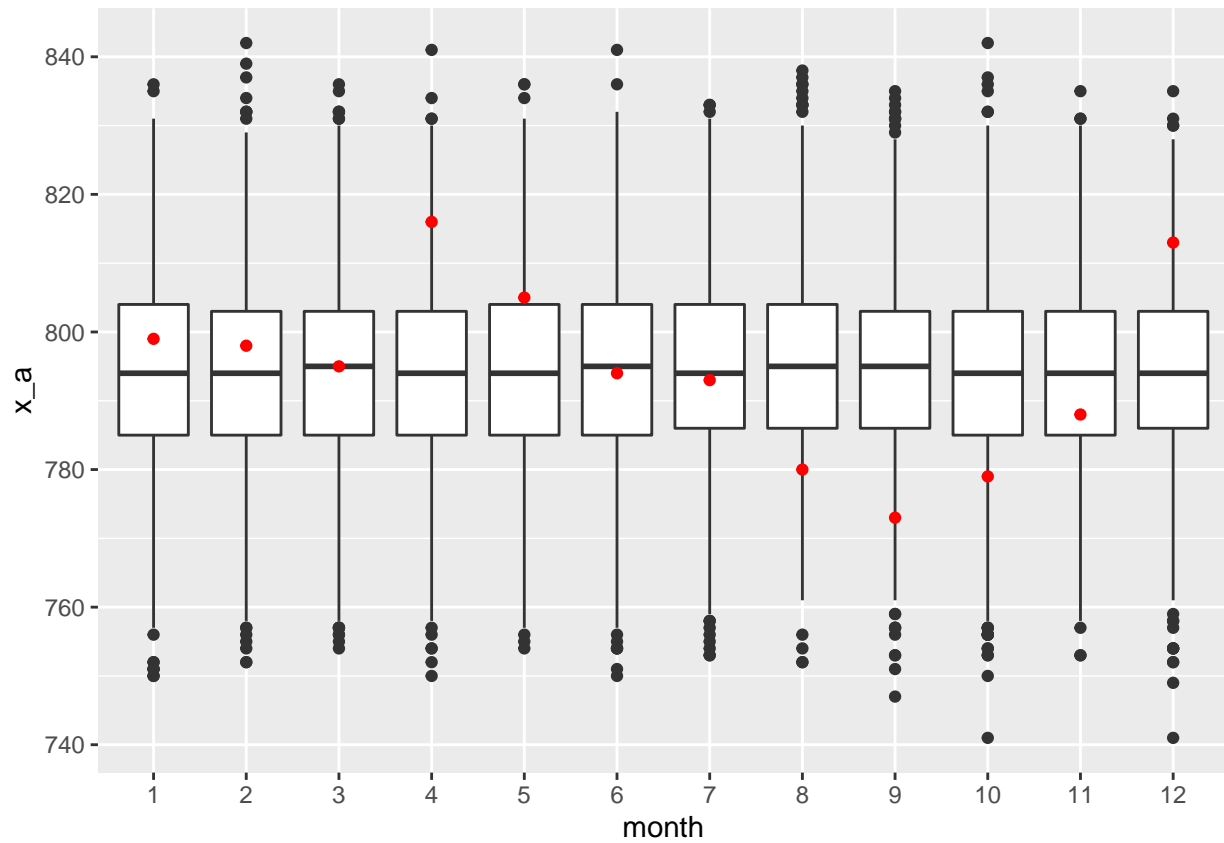


```
## tidy x_a
m=length(p_a)
df_x_a <- vector()
for (i in 1:n_T) {
  obs <- rbinom(m,n_a,p_a)
  df_x_a <- cbind(df_x_a,obs)
}

colnames(df_x_a) <- seq(1:12)
df_x_a <- as.data.frame(df_x_a)
ppc_x_a <- gather(df_x_a, key = 'month',value = 'x_a')
ppc_x_a$month <- factor(ppc_x_a$month,levels = seq(1,12))
x_a_values=data.frame('month'=seq(1,12), 'x_a'=df$x_a)
x_a_values$month <- factor(x_a_values$month,levels = seq(1,12))

ggplot()+geom_boxplot(aes(x=month,y=x_a),data = ppc_x_a)+geom_point(aes(x=x_a_values$month, y=x_a_values$
```





## Reference

first tutorial  
second tutorial  
JAGS manual  
error handling guide