



Linear Algebra

Matrices

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In This Video



Definition of Matrices



Importance of Matrices

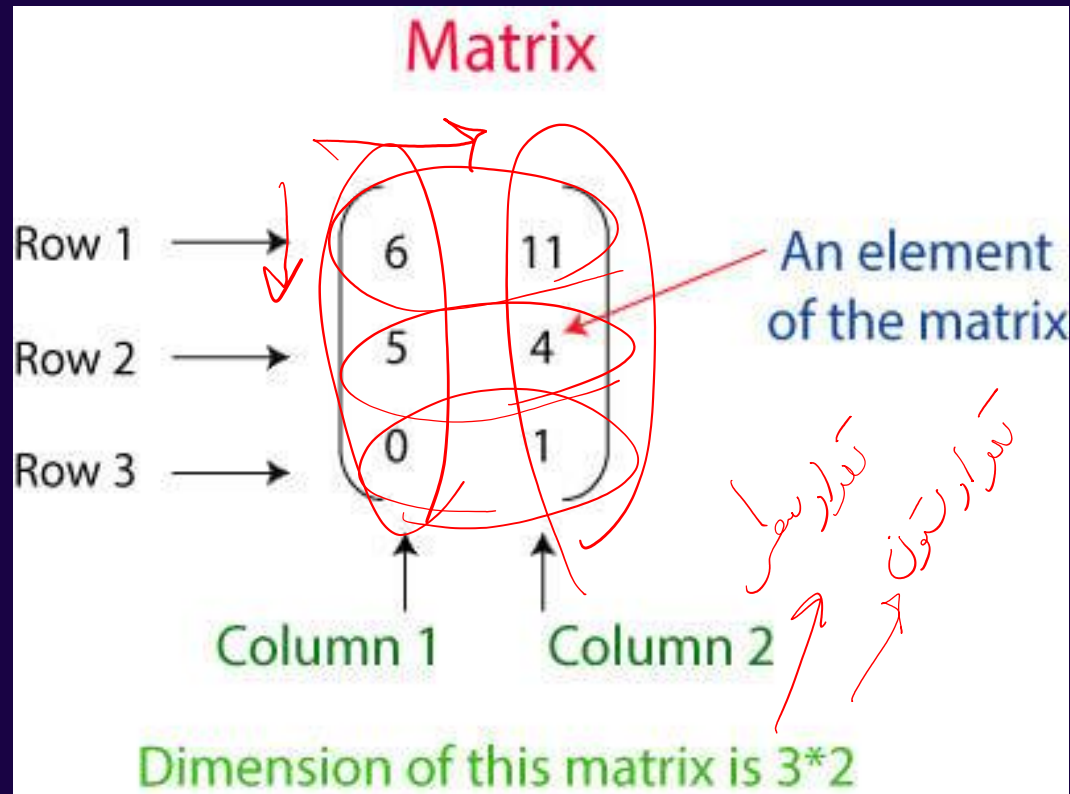


Example of Matrix Calculation

$$\begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 0 \end{bmatrix} \quad \begin{bmatrix} 1 & 6 & x \\ 2 & 7 & 1 \\ 0 & -1 & + \end{bmatrix}$$

What is Matrices



A matrix is a two-dimensional collection of numbers.

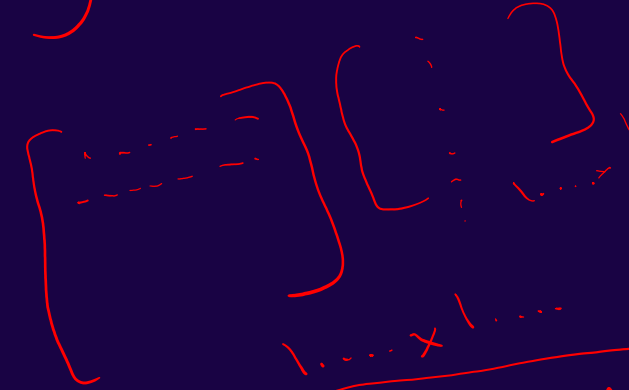


Importance of Matrices

- we can use a matrix to represent a dataset consisting of multiple vectors, simply by considering each vector as a row of the matrix
- as we'll see later, we can use an $n \times k$ matrix to represent a linear function that maps k -dimensional vectors to n -dimensional vectors
- matrices can be used to represent binary relationships



PCA



$$\begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix} \times \begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix} = \begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix}$$

$$\begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix} \times \begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix} = \begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix}$$

2000×2000

Example of Matrix Calculation

```
friend_matrix = [[0, 1, 1, 0, 0, 0, 0, 0, 0, 0], # user 0
                 [1, 0, 1, 1, 0, 0, 0, 0, 0, 0], # user 1
                 [1, 1, 0, 1, 0, 0, 0, 0, 0, 0], # user 2
                 [0, 1, 1, 0, 1, 0, 0, 0, 0, 0], # user 3
                 [0, 0, 0, 1, 0, 1, 0, 0, 0, 0], # user 4
                 [0, 0, 0, 0, 1, 0, 1, 1, 0, 0], # user 5
                 [0, 0, 0, 0, 0, 1, 0, 0, 1, 0], # user 6
                 [0, 0, 0, 0, 0, 0, 1, 0, 1, 0], # user 7
                 [0, 0, 0, 0, 0, 0, 1, 1, 0, 1], # user 8
                 [0, 0, 0, 0, 0, 0, 0, 0, 1, 0]] # user 9
```

$X = [0, 0, 1, 1, 0, 1]$

for i in X

for index i in $\text{enumerate}(X)$

0

$i = 0$
 $i = 0$
 $i = 1$
 $i = 1$
 $i = 0$
 $i = 1$

index $i = 0$
 $i = 1$
 $i = 2$

Exercise :

In the last example ,Find a user who have the most friends

```
friend_matrix = [[0, 1, 1, 0, 0, 0, 0, 0, 0, 0], # user 0
                 [1, 0, 1, 1, 0, 0, 0, 0, 0, 0], # user 1
                 [1, 1, 0, 1, 0, 0, 0, 0, 0, 0], # user 2
                 [0, 1, 1, 0, 1, 0, 0, 0, 0, 0], # user 3
                 [0, 0, 0, 1, 0, 1, 0, 0, 0, 0], # user 4
                 [0, 0, 0, 0, 1, 0, 1, 1, 0, 0], # user 5
                 [0, 0, 0, 0, 0, 1, 0, 0, 1, 0], # user 6
                 [0, 0, 0, 0, 0, 1, 0, 0, 1, 0], # user 7
                 [0, 0, 0, 0, 0, 0, 1, 1, 0, 1], # user 8
                 [0, 0, 0, 0, 0, 0, 0, 0, 1, 0]] # user 9
```