

lower bounds

