

# Statistics with Spa OWS

## Lecture 2

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# Outline

- Basic statistical concepts
  - Describing distributions
  - Describing sampling precision

# Basic statistical concepts

```
> head(d)
```

|   | BirdID | Cohort | CaptureDate | CaptureTime | Year | Tarsus | Bill | Wing | Mass | Sex | Sex.1  |
|---|--------|--------|-------------|-------------|------|--------|------|------|------|-----|--------|
| 1 | 4401   | 1991   | 21-Jun-00   | <NA>        | 2000 | 18.9   | NA   | 82   | 29.4 | 1   | male   |
| 2 | 4401   | 1991   | 02-Oct-00   | <NA>        | 2000 | 18.8   | NA   | 79   | 31.6 | 1   | male   |
| 3 | 4405   | 1994   | 20-Jun-00   | <NA>        | 2000 | 19.1   | NA   | 77   | 29.9 | 0   | female |
| 4 | 4405   | 1994   | 04-Oct-00   | <NA>        | 2000 | 19.0   | NA   | 78   | 31.6 | 0   | female |
| 5 | 4405   | 1994   | 07-Oct-00   | <NA>        | 2000 | 19.1   | NA   | 77   | 31.0 | 0   | female |
| 6 | 4409   | 1994   | 23-Mar-00   | <NA>        | 2000 | 18.0   | NA   | 76   | 28.1 | 1   | male   |

```
> |
```

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# Lundy Sparrows



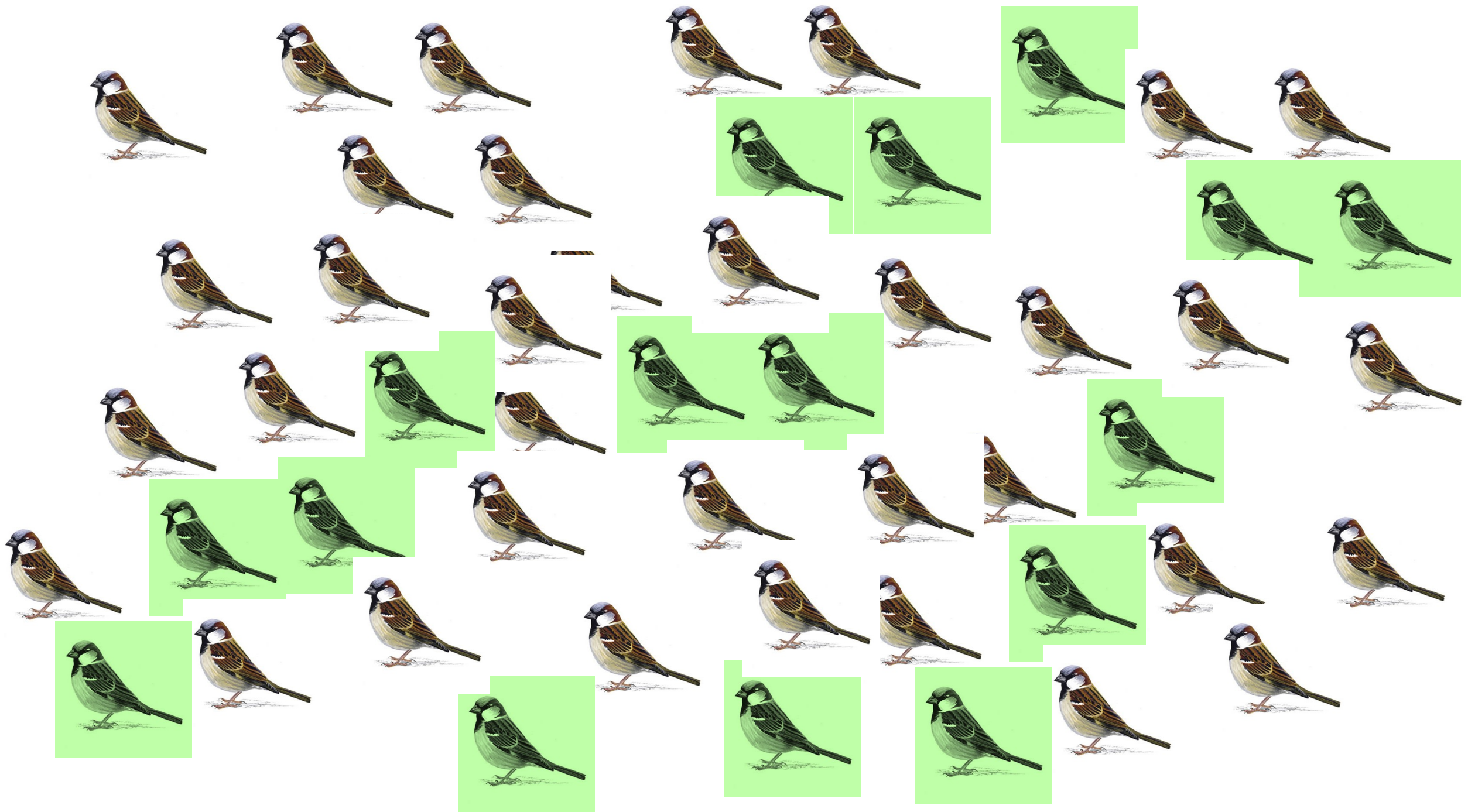
Griffith et al., 2000,  
Nakagawa et al., 2007,  
Cleasby et al., 2010,  
Schroeder et. al 2011, 2013,  
2015





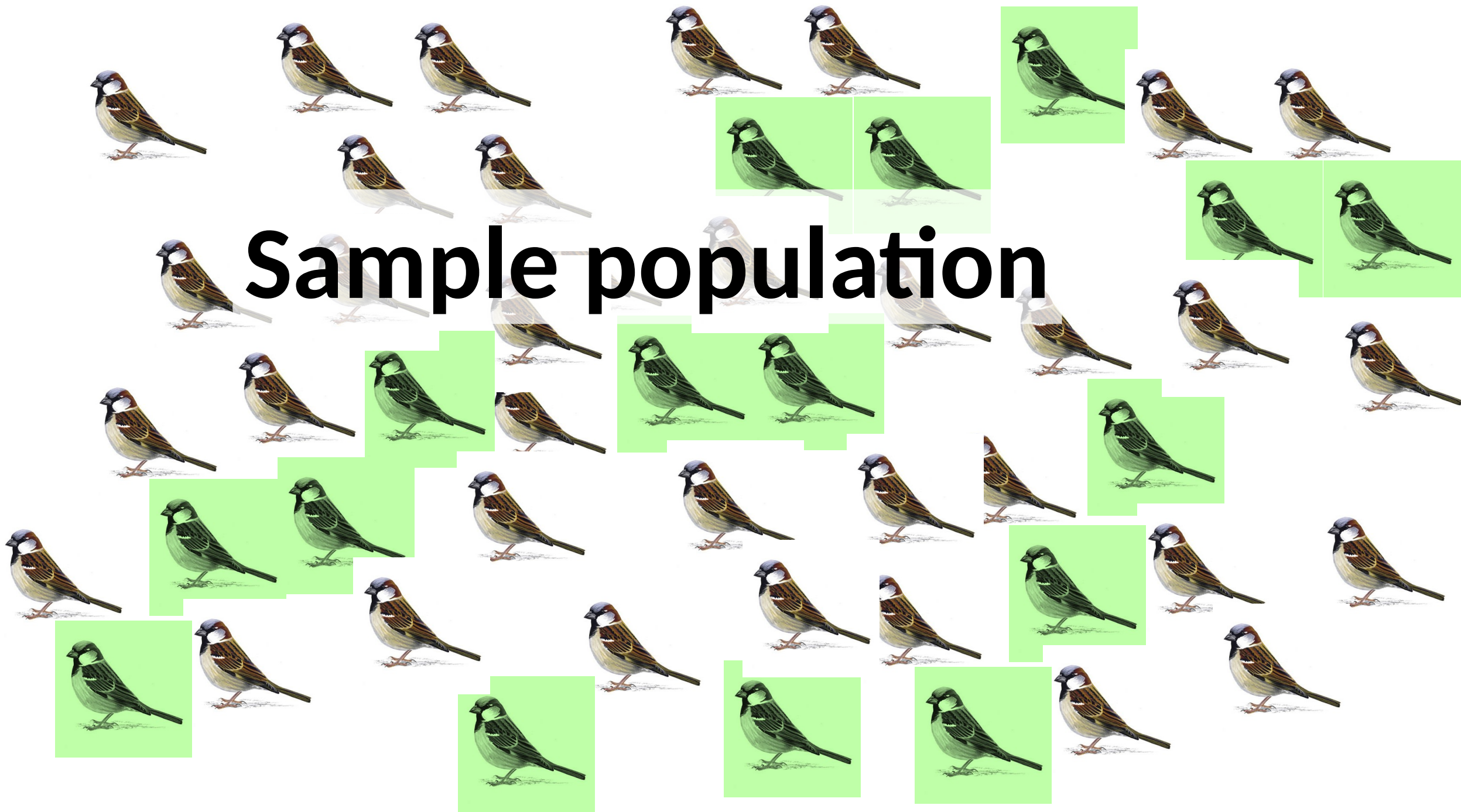


**Complete population**





# Sample population



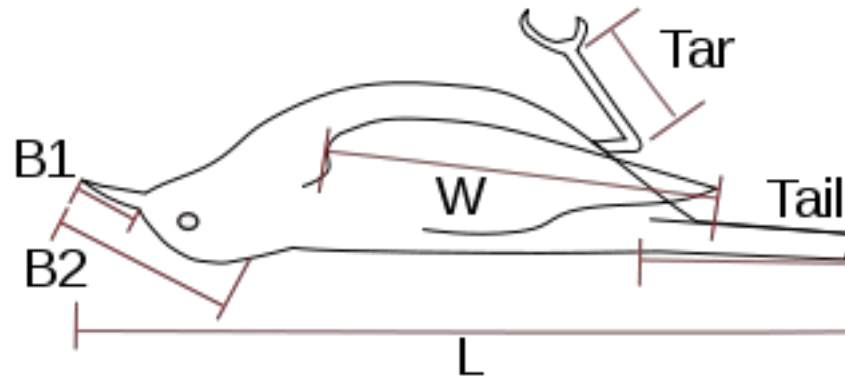


# Basic statistical concepts

```
> head(d)
```

|   | BirdID | Cohort | CaptureDate | CaptureTime | Tarsus | Bill | Wing | Mass | Sex | Sex.1  |
|---|--------|--------|-------------|-------------|--------|------|------|------|-----|--------|
| 1 | 4      | 2001   | 24-Jul-02   | <NA>        | 16.9   | NA   | 76   | 23.6 | 0   | female |
| 2 | 28     | 2001   | 22-Mar-02   | <NA>        | 19.0   | NA   | 77   | 26.2 | 0   | female |
| 3 | 29     | 2001   | 03-Jun-02   | <NA>        | 18.5   | NA   | 77   | 28.0 | 0   | female |
| 4 | 32     | 2001   | 11-Oct-01   | <NA>        | 17.9   | NA   | 75   | 28.1 | 0   | female |
| 5 | 32     | 2001   | 13-Aug-03   | 08:00       | 18.8   | 13.9 | 75   | 25.5 | 0   | female |
| 5 | 32     | 2001   | 09-May-04   | 12:00       | 18.9   | 13.9 | 76   | 25.6 | 0   | female |

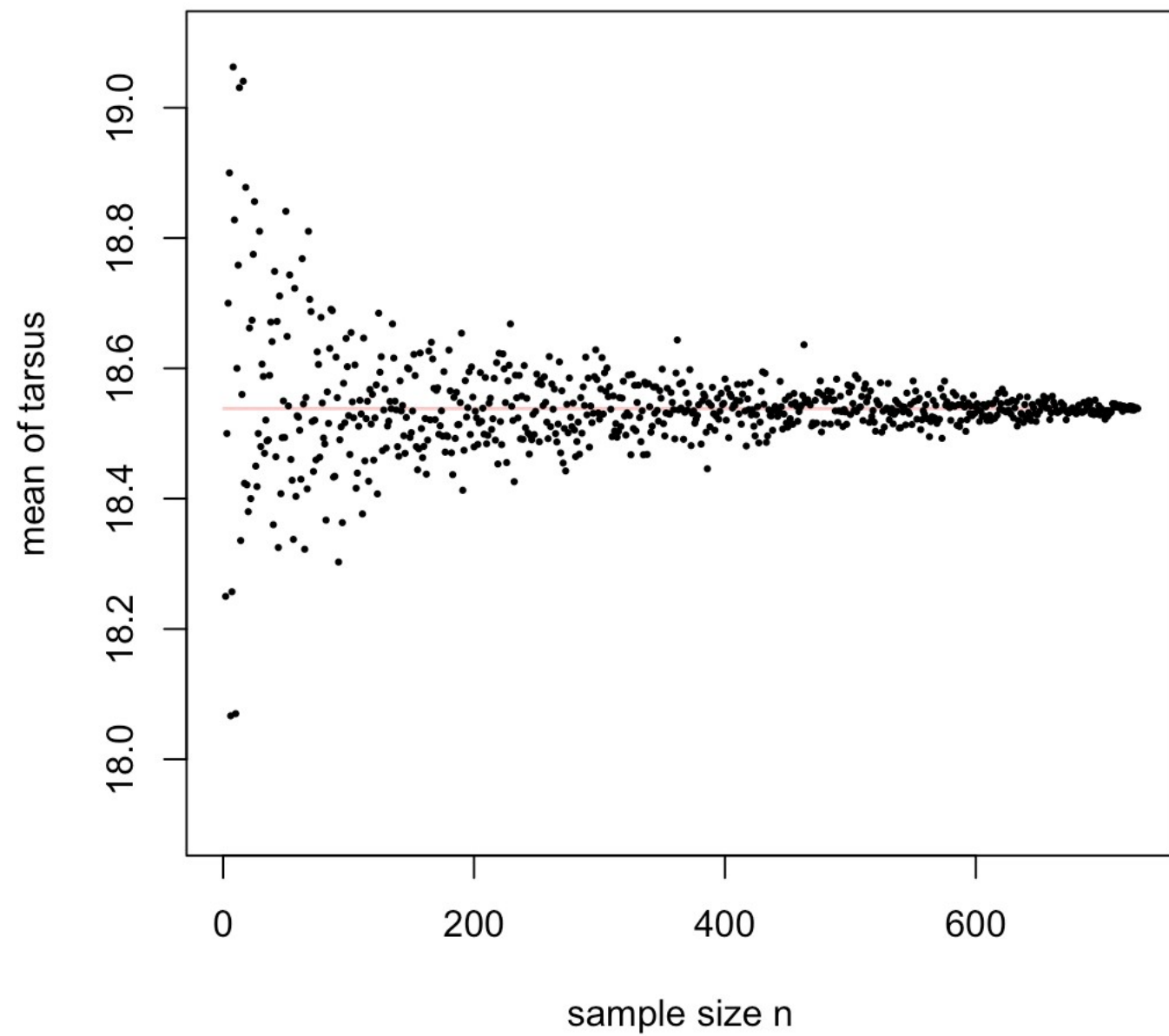
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>
```



# Estimate

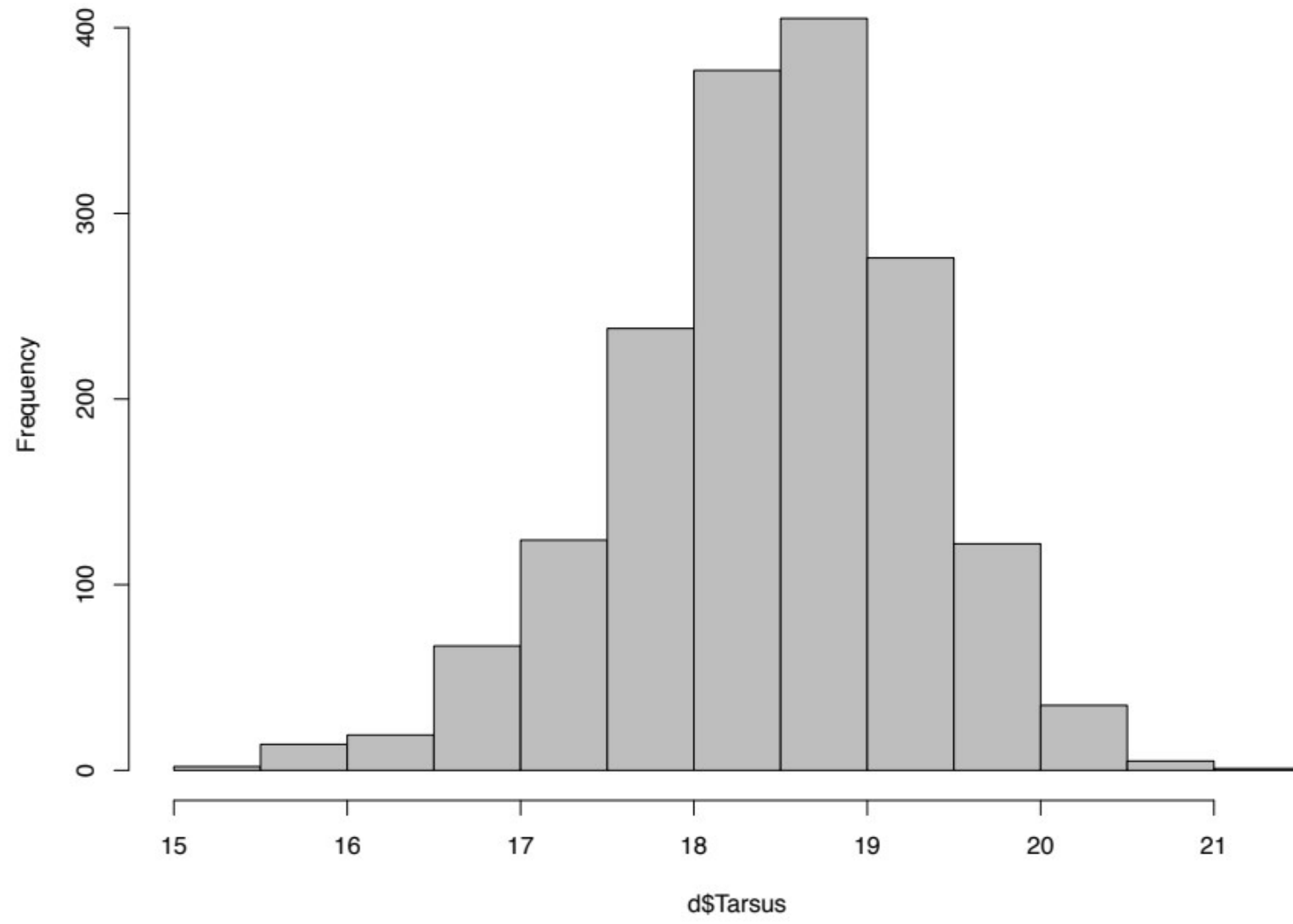
- Any parameter measured and computed from a sample is an estimate
- As such, it is not perfectly precise – there is unknown error
- We want to know how precise, and how reliable the parameter is



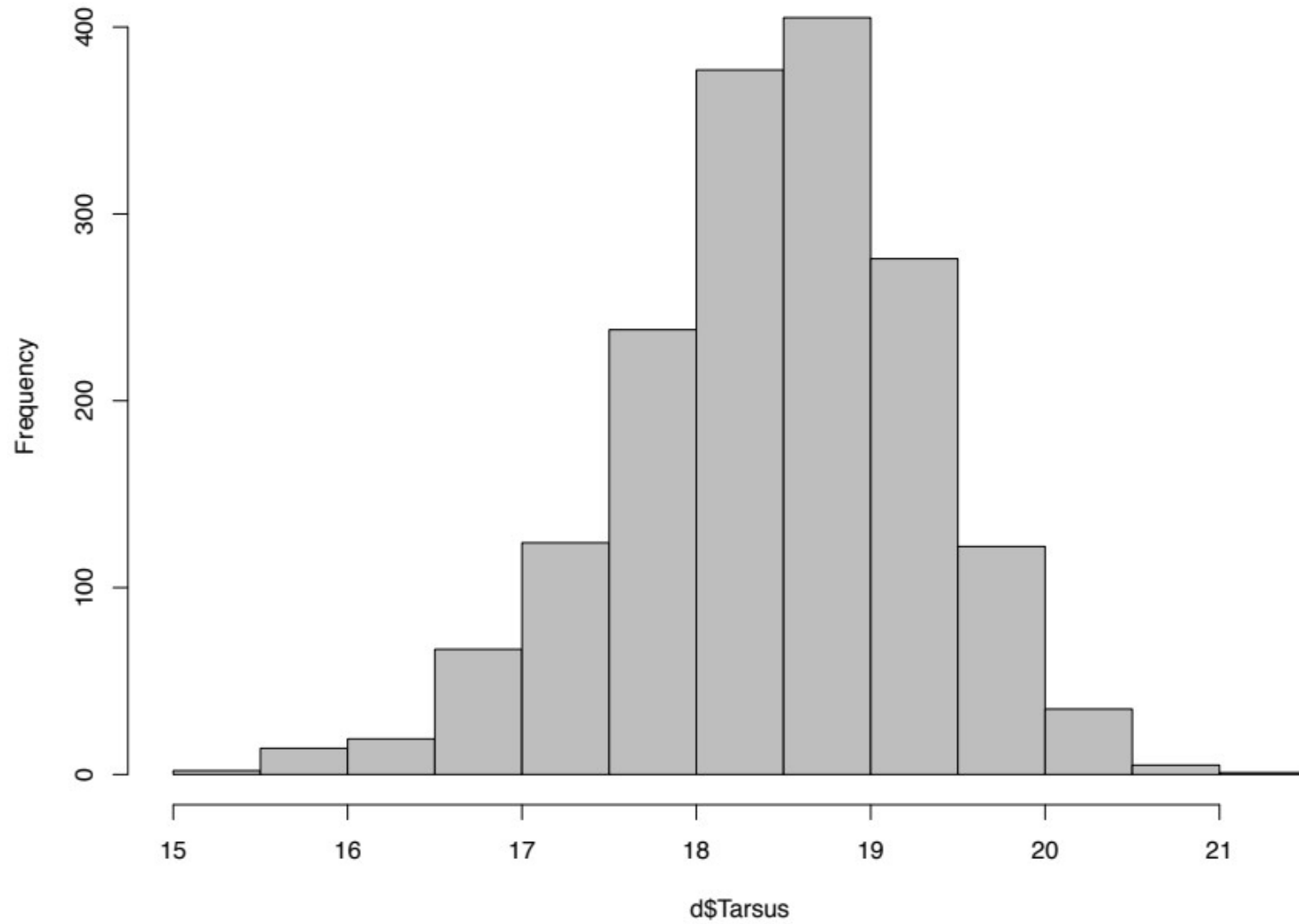




Histogram of d\$Tarsus



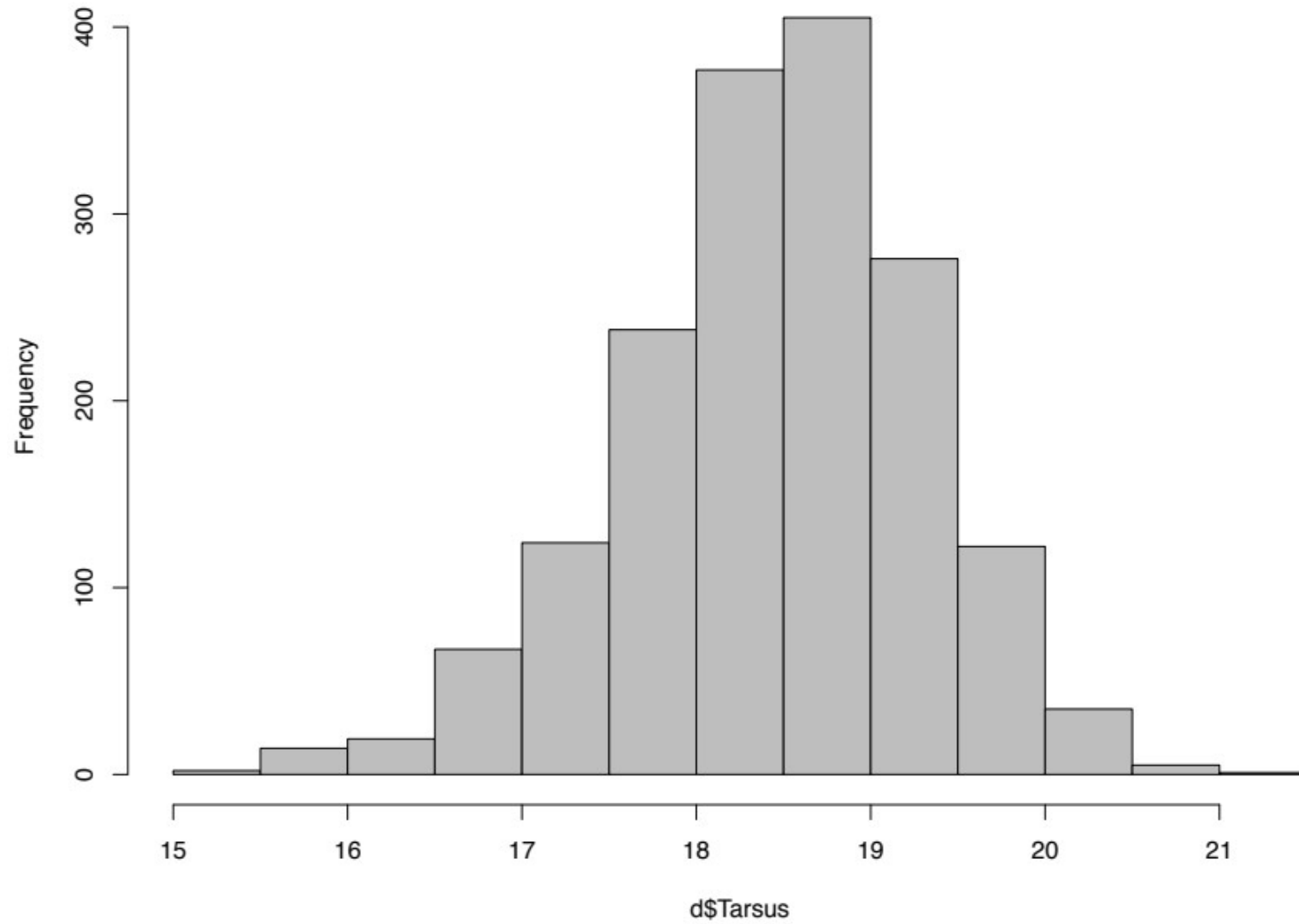
Histogram of d\$Tarsus



Describe data:

- Centrality
- Spread

Histogram of d\$Tarsus



Describe data:

- Centrality
- Spread

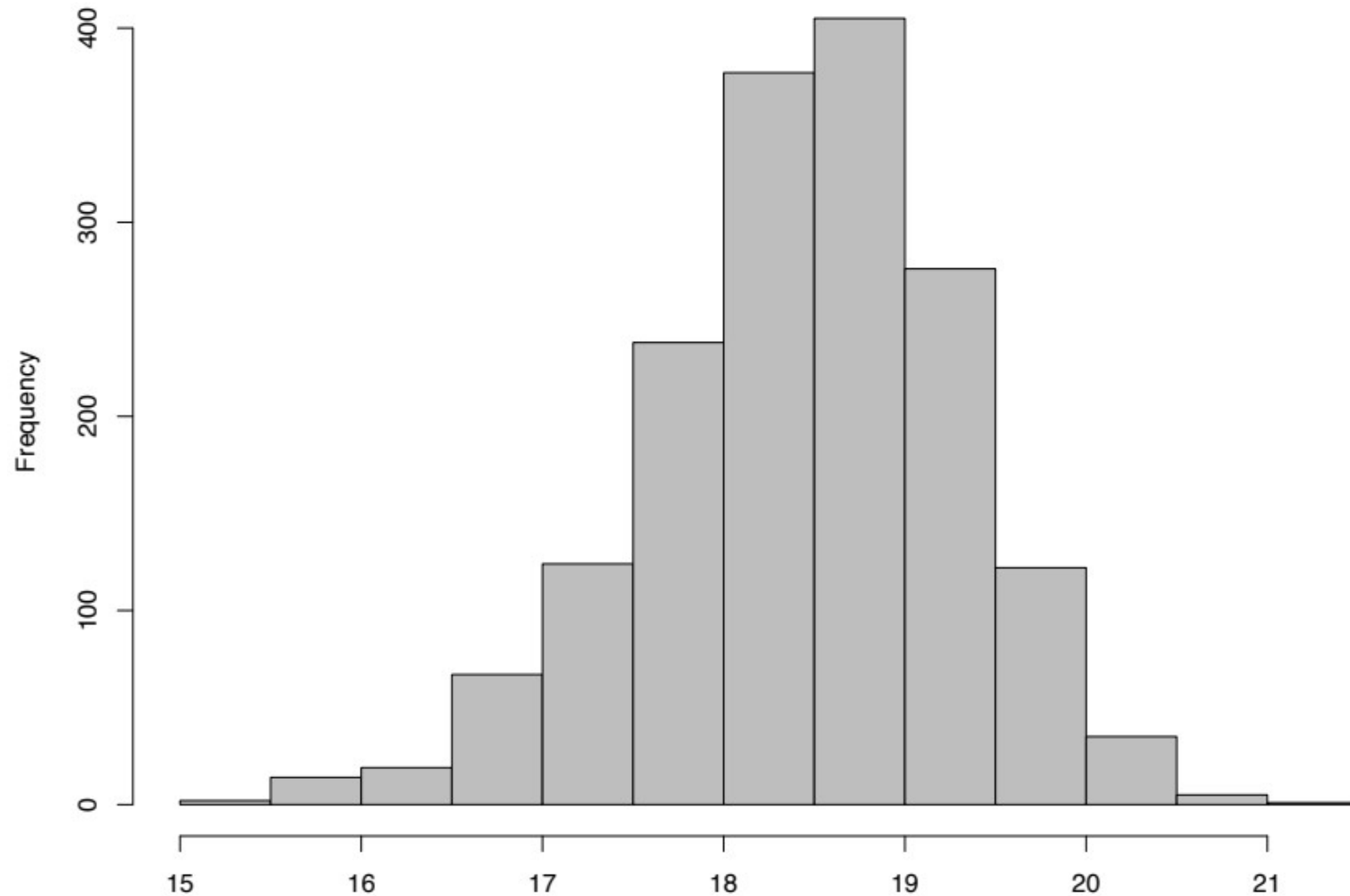
WHERE is the MIDDLE?

# Mean, median and mode

|        |   |
|--------|---|
| Mean   | <u>Sum of values</u><br>Number of values              |
| Median | Middle data value or midpoint<br>of two middle values |
| Mode   | Most frequent value(s)                                |



Histogram of d\$Tarsus



Describe data:

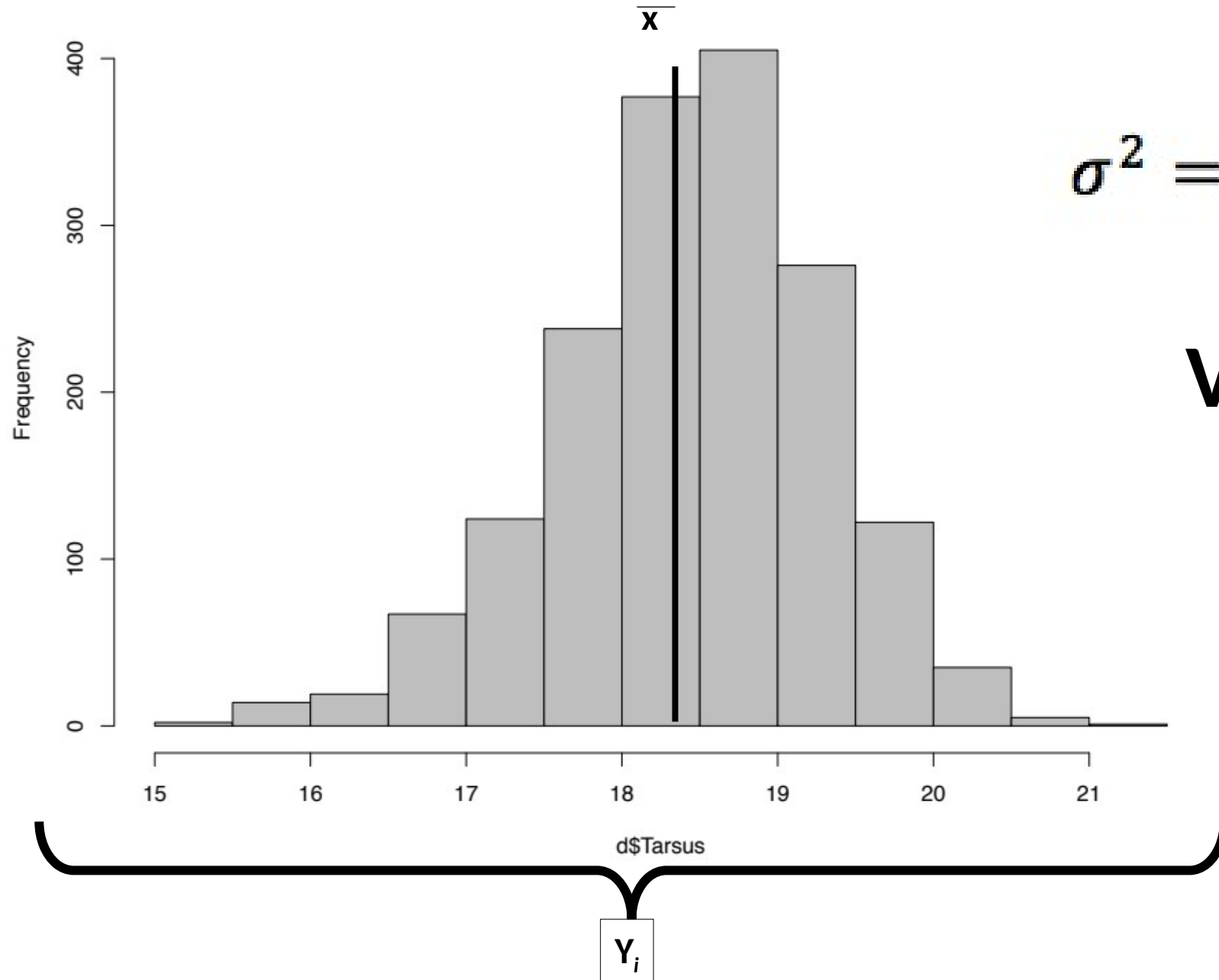
- Centrality
  - Mean
  - Median
  - Mode
- Spread
  - Range (min/max)
  - Variance

d\$Tarsus

$x_i$

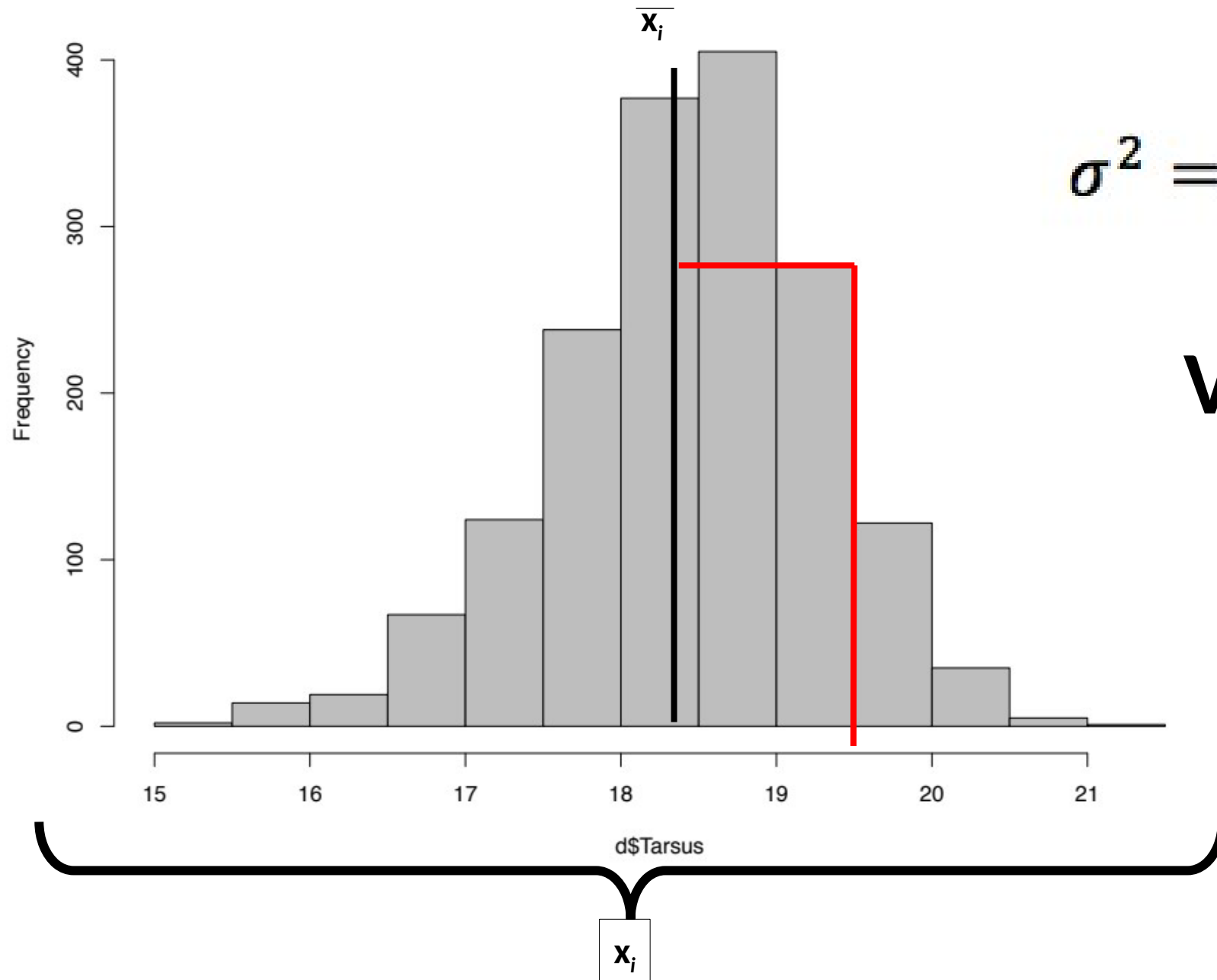
$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

**VARIANCE**



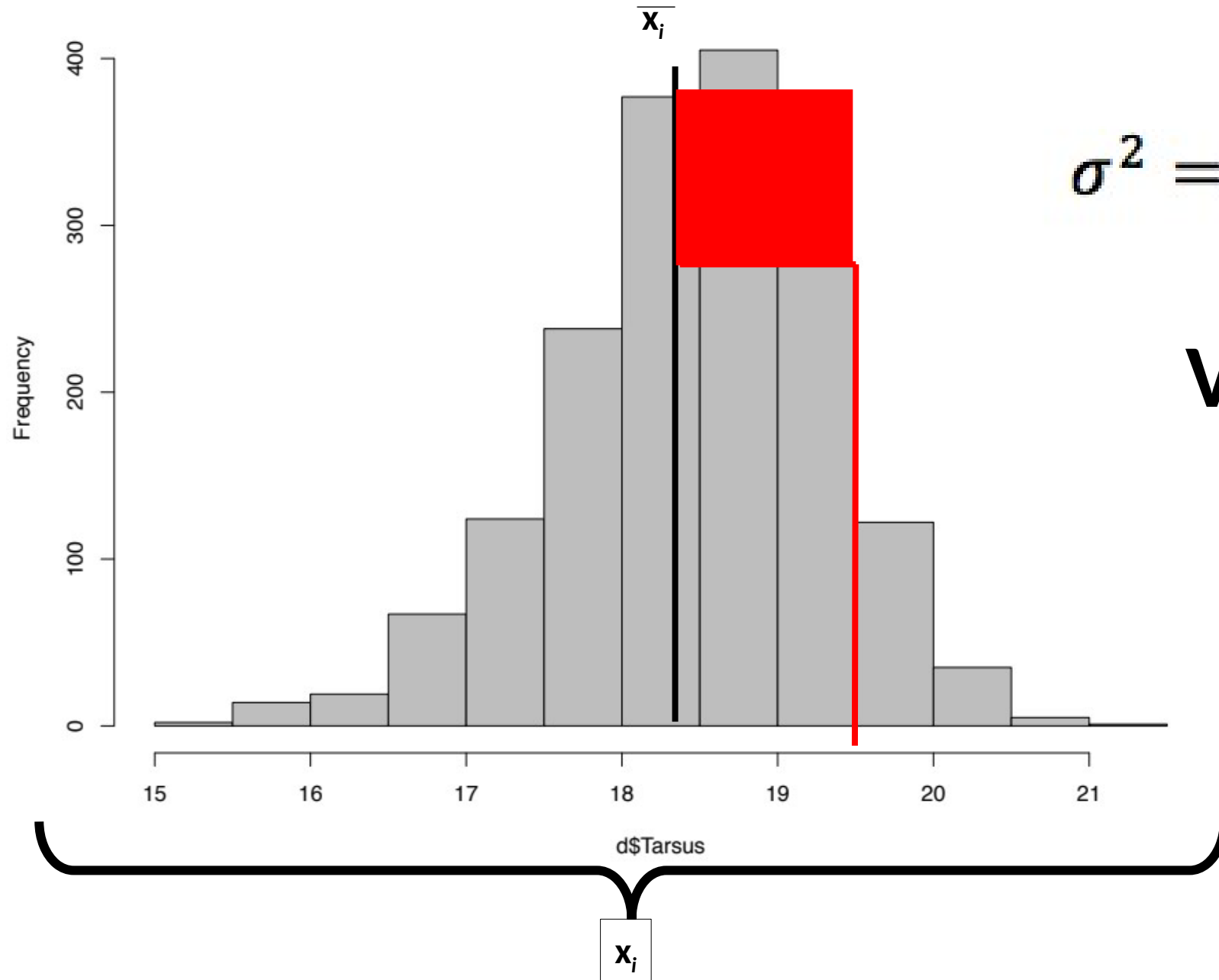
$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

**VARIANCE**



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**VARIANCE**







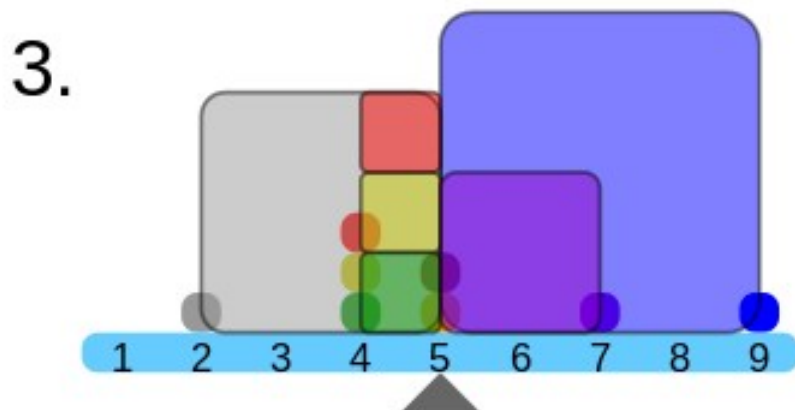
$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

**VARIANCE**



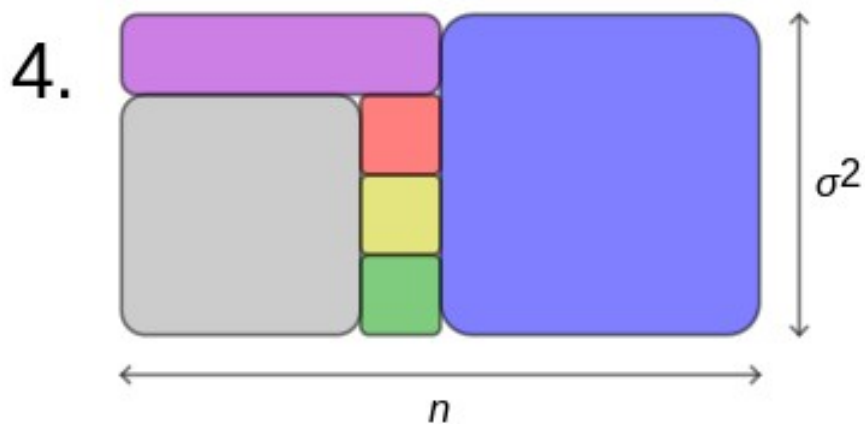
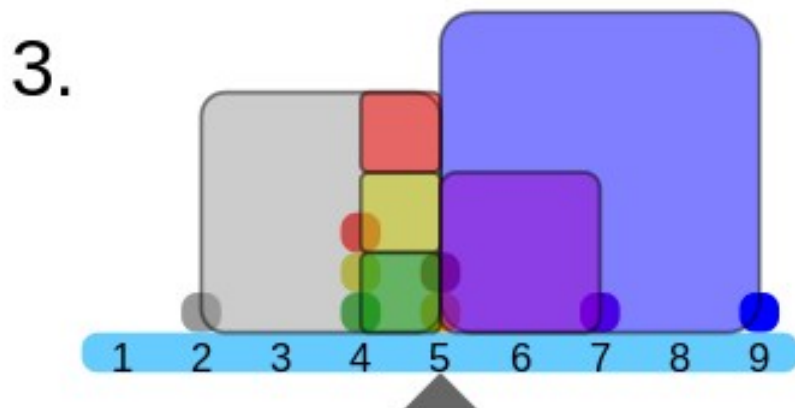
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**VARIANCE**



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**VARIANCE**



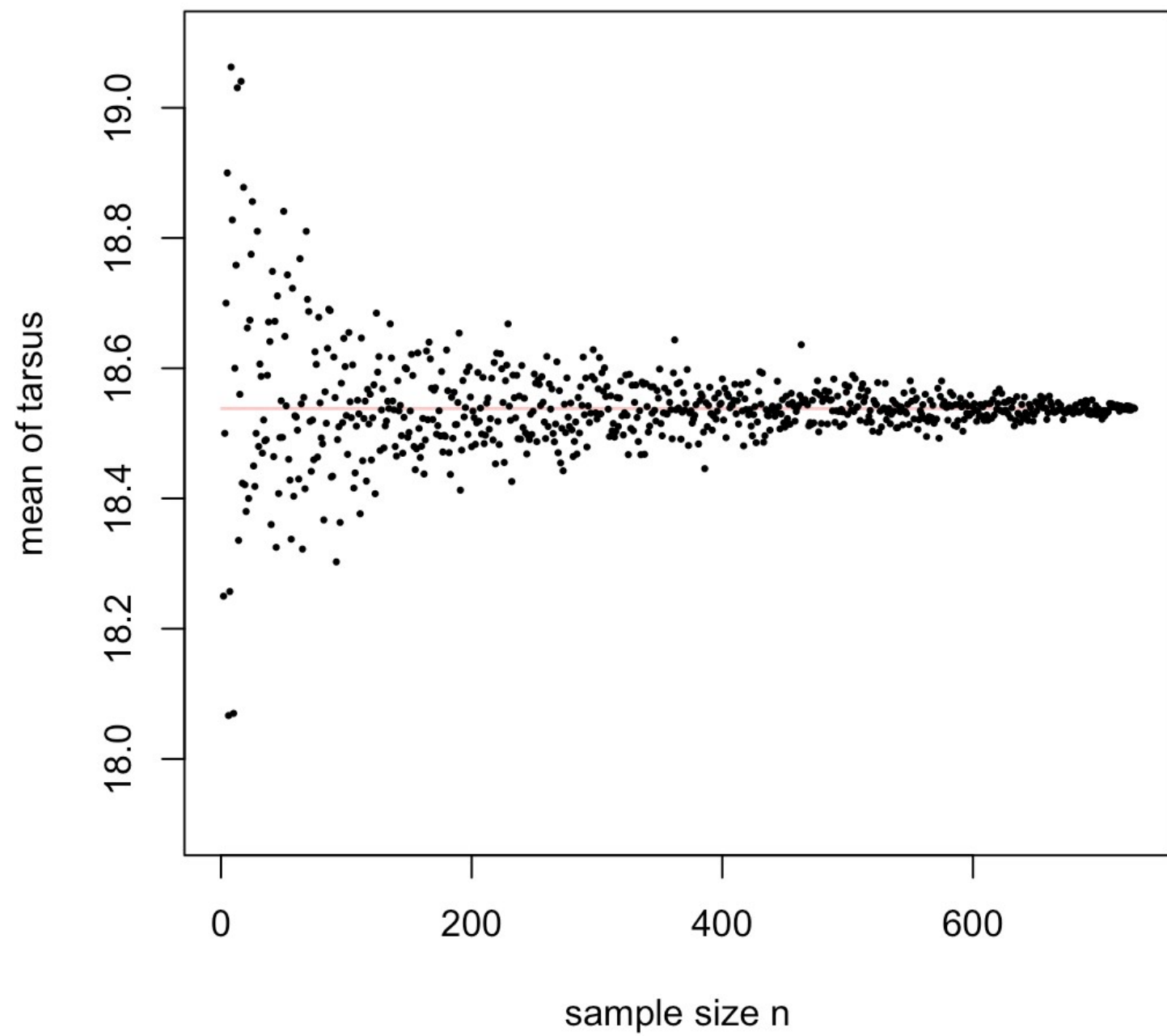
$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

**VARIANCE**



Standard deviation:

[stdev video](#)



# Learning aims

- Difference between population and sample
- Centrality: Mean, median, mode
- Spread: Range, quantiles, variance, standard deviation
- Sum of squares

# Exercise – DO IT NOW – HO 2

Calculate mean, variance and standard deviation of

- Bill length
  - Body mass
  - Wing length in R.
- 
- Plot all four histograms in a multi-panel figure
- 
- What does it mean when statisticians talk about the “sum of squares” (often abbreviated to SS)?

# Exercise – DO IT NOW

- What are NA?
- How can we deal with missing values? There are two ways!
- Why are there odd gaps in the histograms when we set breaks to larger numbers?
- What do these gaps tell us about how precise we should report results?
- Explain the warnings we got for `mlv(d2$Tarsus)`
- What is the variance of normally distributed data with a mean of 0 and a standard deviation of 1?
- What is the function in R to z-standardize data?
- Explain what quantiles are
- What are the boxes, whiskers and circles in a boxplot?
- Explain the terms: sums of squares, mean of sum of squares