

# Simulation of SIS model over networks

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## 1 Simulating an SIS infection

In this session you will have to simulate the spreading of a disease in the SIS model and check that the epidemic threshold for arbitrary networks is indeed  $\frac{1}{\lambda_1}$  as forecast by [Chakrabarti et al., 2008].

In particular, we consider the spreading of the disease following these rules at each time step:

- An infected node recovers with probability  $\gamma$
- An infected node attempts to infect each neighbor with probability  $\beta$

You should be careful when implementing your simulation; please make sure that the updates of the nodes' statuses are done in parallel, that is, to update the status for time  $t$  only statuses of time  $t - 1$  of the other nodes are considered.

Initially, only a random fraction  $p_0$  of nodes are infected.

## 2 Network models

You will run simulations on different types of networks, to see what their differences are in the spreading of the disease under the same initial conditions and with the same model parameters  $\beta, \gamma$ . We will consider networks of size  $n = 1000$ .

✓ In particular, you should consider the first three networks from the list below (ER, BA, WS) and at least two other:

- Erdős-Rényi random graphs
- Scale-free network of Barábasi-Albert

- Small-world network of Watts-Strogatz
- Fully connected network (complete graph)
- Trees
- Star network
- Regular lattices

## 3 Tasks

### 3.1 Task 1

For a fixed set of  $\beta, \gamma$  and  $p_0$  values, simulate what happens with the spread of the disease and plot the proportion of infected nodes over time (for each of the networks). Do you have among the networks you chose one that is more prone to epidemic? Check the leading eigenvalue of each network and see whether your result makes sense.

### 3.2 Task 2

For each of the network types you chose, check what its threshold is. Then, pick two sets of parameter values for  $\gamma, \beta$ , one slightly above and one slightly below the threshold and simulate the spread of the disease. Are your simulation results consistent with the theory?

## 4 Deliverables

You have to prepare a report detailing the results you obtain and any additional design decisions you may have taken while solving this lab session.

*To deliver:* You must deliver the report (explained above) and the source code in R (or other languages) that you have used (including some minimal comments that can help the reader).

*Procedure:* Submit your work through the raco platform as a single zipped file.

*Deadline:* Work must be delivered by the 29th of December (23:00 hrs). Late deliveries risk being penalized or not accepted at all. If you anticipate problems with the deadline, please tell us as soon as possible.

## References

- [Chakrabarti et al., 2008] Chakrabarti, D., Wang, Y., Wang, C., Leskovec, J., and Faloutsos, C. (2008). Epidemic thresholds in real networks. *ACM Transactions on Information and System Security (TISSEC)*, 10(4):1.