

## 4.Relational Model :

### Basic Concepts

# Relational Model

- Most widely used database model : Relational Model
- Examples of Relational DBMS
  - MySQL, DB2, Oracle, Sybase, SQL server, . . .
- This model is based on the concept of a **relation**.
- A relation is a mathematical concept based on a **set**.
- Advantages of Relational Model
  - Simple (user friendly) data structure
  - Provide Data Abstraction
  - Provide Data Independence
  - Provide High-level programming

# Relation : Definition

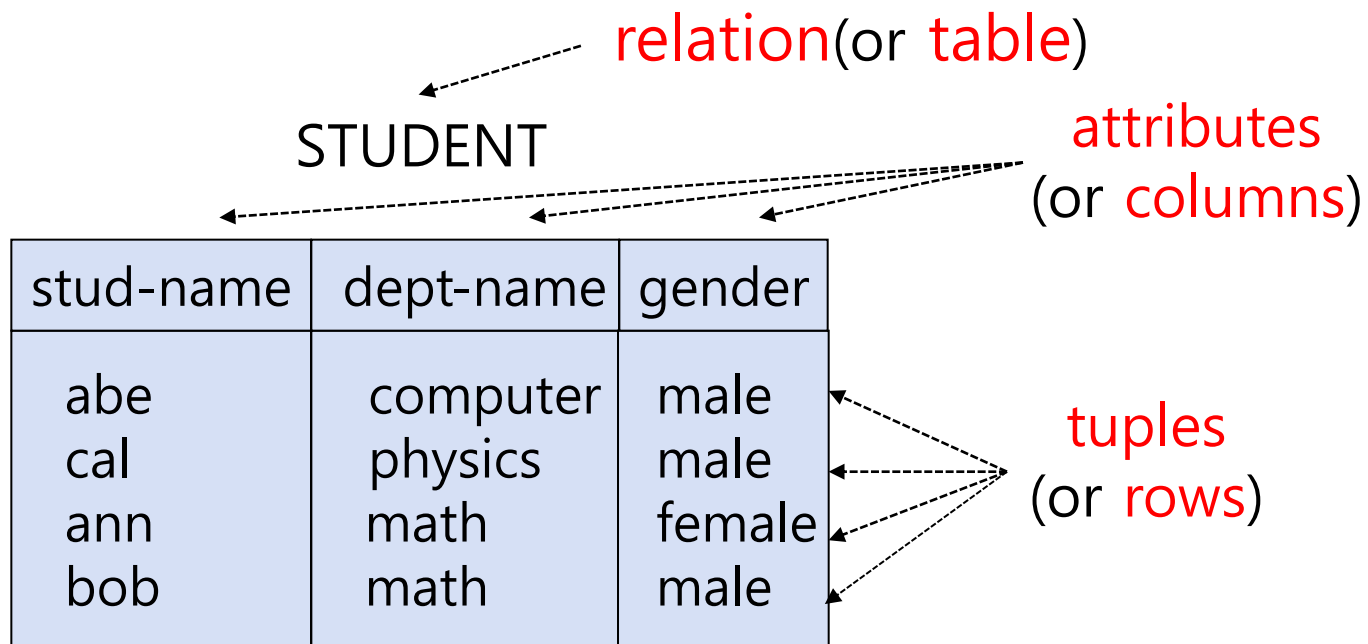
- Formally, a given  $n$  sets  $D_1, D_2, \dots, D_n$ , a **relation  $r$**  is a subset of  $D_1 \times D_2 \times \dots \times D_n$ . ( $\times$  : Cartesian Product)
- Here,  $\langle a_1, a_2, \dots, a_n \rangle$  where each  $a_i \in D_i$  is called a **tuple**.
- In other words, a relation is a **finite set of tuples**.
- Example : Let  $D_1 = \{0, 1\}$ ,  $D_2 = \{a, b, c\}$ ; Then,  
 $D_1 \times D_2 = \{\langle 0, a \rangle, \langle 0, b \rangle, \langle 0, c \rangle, \langle 1, a \rangle, \langle 1, b \rangle, \langle 1, c \rangle\}$ 
  - $r_1 = \{\langle 0, a \rangle, \langle 0, b \rangle, \langle 1, c \rangle\}$  is one possible relation.
  - $r_2 = \{\langle 1, a \rangle, \langle 1, b \rangle\}$  is another relation.

# Relation : Definition

- Another Example : Student  
stud\_name = {abe, cal, bob, ann}  
dept\_name = {physics, math, computer}  
gender = {male, female}
- $\mathbf{r} = \{(\text{abe}, \text{computer}, \text{male}), (\text{cal}, \text{physics}, \text{male}), (\text{ann}, \text{math}, \text{female}), (\text{bob}, \text{math}, \text{male})\}$   
is a relation over stud\_name x dept\_name x gender
- (abe, computer, male) is an example of tuple. Thus, this relation  $\mathbf{r}$  consists of 4 tuples;
- Show another examples of relations;

# Relation : Table 표현

- We can represent relation as "**table**"; A table consists of **rows** and **columns**.
- Each **row** corresponds to a **tuple**; It represents "entity" or "relationship".
- Each **column** corresponds to an **attribute**; It represents structure of table.



# Properties of Relation

- The number of tuples in a relation is **finite**.
- The order of tuples in a relation is **not** important.
- Any duplicated tuples in a relation are **not** allowed.
- Each attribute in a relation must have a **distinct** name.
- Values of Attributes:
  - (1) Values of each attribute must be **atomic**(indivisible).
    - Intersection of row and column has **single** value.
    - Multi-valued(or, composite) attributes are not allowed.
  - (2) Special value **"NULL"** is allowed.
    - NULL means "unknown", "unavailable", or "undefined".

# Relation : Another Example

STUDENT	Name	SSN	HomePhone	Address	OfficePhone	Age	GPA
	Dick Davidson	422-11-2320	null	3452 Elgin Road	749-1253	25	3.53
	Barbara Benson	533-69-1238	839-8461	7384 Fontana Lane	null	19	3.25
	Charles Cooper	489-22-1100	376-9821	265 Lark Lane	749-6492	28	3.93
	Katherine Ashly	381-62-1245	375-4409	125 Kirby Road	null	18	2.89
	Benjamin Bayer	305-61-2435	373-1616	2918 Bluebonnet Lane	null	19	3.21

- Order of tuples does not matter.
- All tuple are distinct; No duplicates are allowed.
- Each attribute has atomic(= only single) value.
- Some attributes have NULL values.

# Properties of Relation

- Values in a Tuple:

- Each attribute value in a tuple must be within its data type.
- For example, each attribute value in student tuple must be within;

Name: CHAR(20); SSN: CHAR(9); . . . Age: INT, . .

- Some Useful Notation:

- We refer to component values of a tuple  $t$  by
  - ✓  $t[A_i]$  or  $t.A_i$
  - ✓ This is the value  $V_i$  of attribute  $A_i$  for tuple  $t$
  - ✓ For example,  $t[\text{Name}]$ ,  $t[\text{Age}]$ , . . .
- Similarly,  $t[A_i, A_j, \dots, A_n]$  refers to the subtuple of  $t$  containing the values of attributes  $A_i, A_j, \dots, A_n$ , respectively in tuple  $t$



# Key

- **Super key**

- A set of attributes **K** of a relation **R** such that no two tuples in **R** must have the same value for **K**.
- Values of **K** can identify all tuples in **R** uniquely.

- **Key**

- A "minimal" superkey **K** that does not does not contain a subset of attributes that is itself a super key.
- Removal of any attribute from **K** results in a set of attributes that is no more a super key (thus, can not identify tuples)

- Every key is super key, but reverse is not true.

# Key

A	B	C	D
10	10	20	20
15	20	10	18
20	15	18	15
10	18	15	18

(1) 위 relation에서 super key 들을 모두 찾아라.

{B}, {C}, {A, D}, {A, B}, {A, C}, {B, C}, {B, D}, {C, D},  
{A, B, C}, {B, C, D}, {A, C, D}, {A, D, B}, {A, D, B, C}

(2) 위 relation에서 key 들을 모두 찾아라.

{B}, {C}, {A, D}

참조: Super key는 유일성(unique)만 만족하고, Key는 유일성과

최소성(minimal) 모두 만족함. 따라서, tuple들을 식별하기 위해

항상 key를 사용하고, 각 relation에는 key가 존재해야 함.

Key

STUDENT	Name	SSN	HomePhone	Address	OfficePhone	Age	GPA
	Dick Davidson	422-11-2320	null	3452 Elgin Road	749-1253	25	3.53
	Barbara Benson	533-69-1238	839-8461	7384 Fontana Lane	null	19	3.25
	Charles Cooper	489-22-1100	376-9821	265 Lark Lane	749-6492	28	3.93
	Katherine Ashly	381-62-1245	375-4409	125 Kirby Road	null	18	2.89
	Benjamin Bayer	305-61-2435	373-1616	2918 Bluebonnet Lane	null	19	3.21

- What is Key(s)? What is super key(s)?
  - Every student's SSN value must be distinct;
  - There may have the same student's names, but with distinct addresses.
  - There may have the same addresses, but with distinct student's names.
  - But there must not have same student's name with same addresses. (or same addresses with the same names)

# Key

- **Candidate Key**

- There may have more than one key in a relation; In this case, each of the keys is called a **candidate** key;

- Types of Keys

- Simple Key : Consists of single attribute;
- Composite Key : Consists of 2 or more attributes;

- **Primary Key**

- If a relation has several (candidate) keys, we must choose one for identification use in practice; The chosen key is called a **Primary Key** (PK). (PK는 밑줄 (underline)로 표시함)
- Every relation must have its own primary key.

# Key : Example

- Consider the following CAR Relation;  
CAR(License-number, Engine-serial-number, Make, Model, Year)
  - Key 1 = {License-number}
  - Key 2 = {Engine-serial-number}
- Both are also super keys of CAR. {Engine-serial-number, Make} is a super key, but not a key. {License-number, Model} is also a super key, but not a key.
- Any set of attributes that includes a key is a super key.  
A minimal super key is a key.
- There are two (candidate) keys. Primary key is used in practice to identify each tuple in a relation. Here, we select {License-number} as primary key in CAR relation, which is underlined.

# CAR Relation

**CAR**

<u>License_number</u>	Engine_serial_number	Make	Model	Year
Texas ABC-739	A69352	Ford	Mustang	02
Florida TVP-347	B43696	Oldsmobile	Cutlass	05
New York MPO-22	X83554	Oldsmobile	Delta	01
California 432-TFY	C43742	Mercedes	190-D	99
California RSK-629	Y82935	Toyota	Camry	04
Texas RSK-629	U028365	Jaguar	XJS	04

**Figure 5.4**

The CAR relation, with two candidate keys: License\_number and Engine\_serial\_number.

- keys = {License-number}, {Engine-serial-number}
- Super keys = Any set of attributes including {License-number} or {Engine-serial-number}
- Primary key = {License-number}

# Good Primary Keys

- **Stable** : Do not change over the life of the database
- **Definitive** : Values always exist
- **Numeric** : ID '12345' is better than name 'michael Jordan'
- **Minimal** : Fewest attributes as possible (3 or fewer)
- **Short** : Are not too long length (bytes)
- **Security** : No sensitive information hidden

# Key : Exercise

- Consider the following "Company" relations:

EMPLOYEE (eno, ename, age, addr, super\_eno, work\_dno)

DEPARTMENT (dno, dname, phone, mgr\_eno)

PROJECT (pno, pname, control\_dno)

WORK-ON (eno, pno, hours)

- Under your assumptions, answer following questions:

(1) Find (all) super keys.

(2) Find (all) keys.

(3) Specify primary keys.



# (Relational) Integrity Constraints

- Integrity Constraints are conditions that must be satisfied by all relations; There are three main types of constraints;
  - **Key** Integrity
  - **Entity** Integrity
  - **Referential** Integrity
- **Key Integrity**
  - Given any key **K**, for any two tuples  $t_1$  and  $t_2$  in a relation  $R$ ,  $t_1[K] \neq t_2[K]$ .
- **Entity Integrity**
  - **Primary key** in a relation  $R$  must not contain **null** values in any tuple in  $R$ ; That means;  $\mathbf{t[PK] \neq null}$  for any tuple  $\mathbf{t}$  in  $R$
  - If primary has several attributes, **null** is not allowed in any of these attributes

# Violating Key/Entity Integrity

STUDENT	Name	SSN	HomePhone	Address	OfficePhone	Age	GPA
	Dick Davidson	422-11-2320	null	3452 Elgin Road	749-1253	25	3.53
	Barbara Benson	533-69-1238	839-8461	7384 Fontana Lane	null	19	3.25
	Charles Cooper	489-22-1100	376-9821	265 Lark Lane	749-6492	28	3.93
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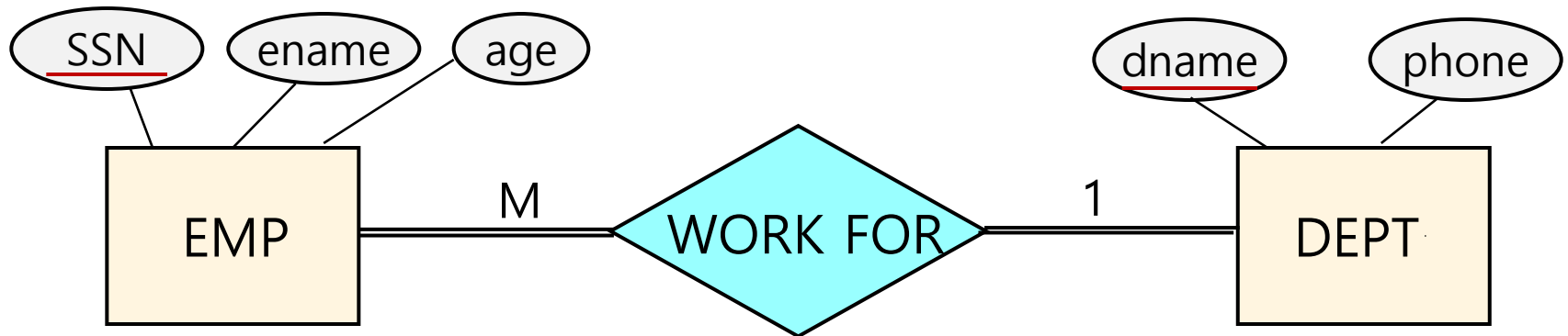
- 다음 각 연산에서 Key Integrity, Entity Integrity의 위반 유무를 판단하라.  
(단, Primary Key = {SSN})
  - Insert a student with <papa jones, 489-22-1100, 290-7118, . . >
  - Insert a student with only SSN value is unknown.
  - Insert a student with <mama jones, 123-45-6789, null, null, null, . . >
  - Update Charles Cooper's SSN by 533-69-1238.
  - Delete students with GPA = 3.25.

# Referential Integrity

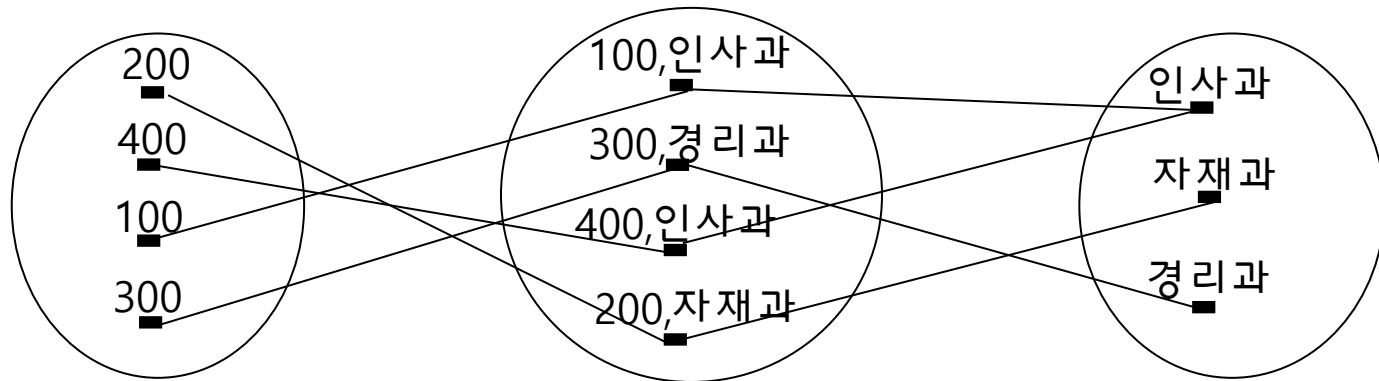
- This specifies a *relationship* among tuples in relations.
- When **referencing** relation **R1** wants to relate **referenced** relation **R2**, you must include a **common** attribute(s).
- The common attribute in **referenced** relation **R2** is **Primary Key (PK)**.
- The common attribute in **referencing** relation **R1** is called **Foreign Key (FK)**.
- Tuples in **referencing** relation **R1** have **FK** that reference the **PK** of **referenced** relation **R2**.

# Referential Integrity

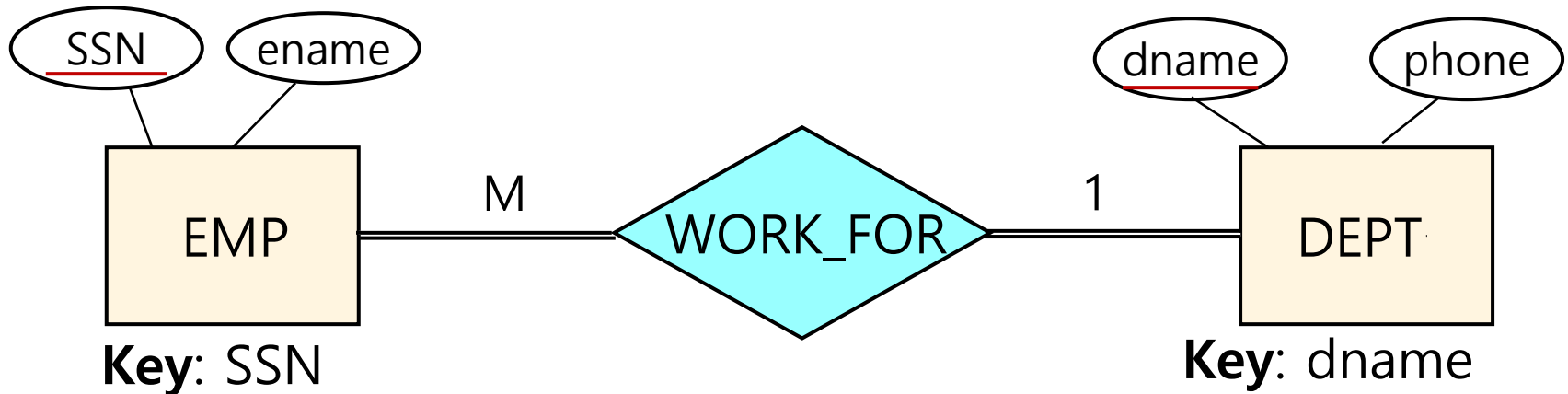
- 다음 ER Diagram을 relation 구조로 표현하라.



- Entity Type EMP와 DEPT은 (자연스럽게) relation 구조로 mapping 됨.  
그렇다면, Relation Type WORK FOR는?



# Referential Integrity



EMP (**Referencing**)

<u>SSN</u>	ename	age	dname
200	.	.	자재과
400	.	.	인사과
100	.	.	인사과
300	.	.	경리과

**PK:** SSN  
**FK:** dname

DEPT (**Referenced**)

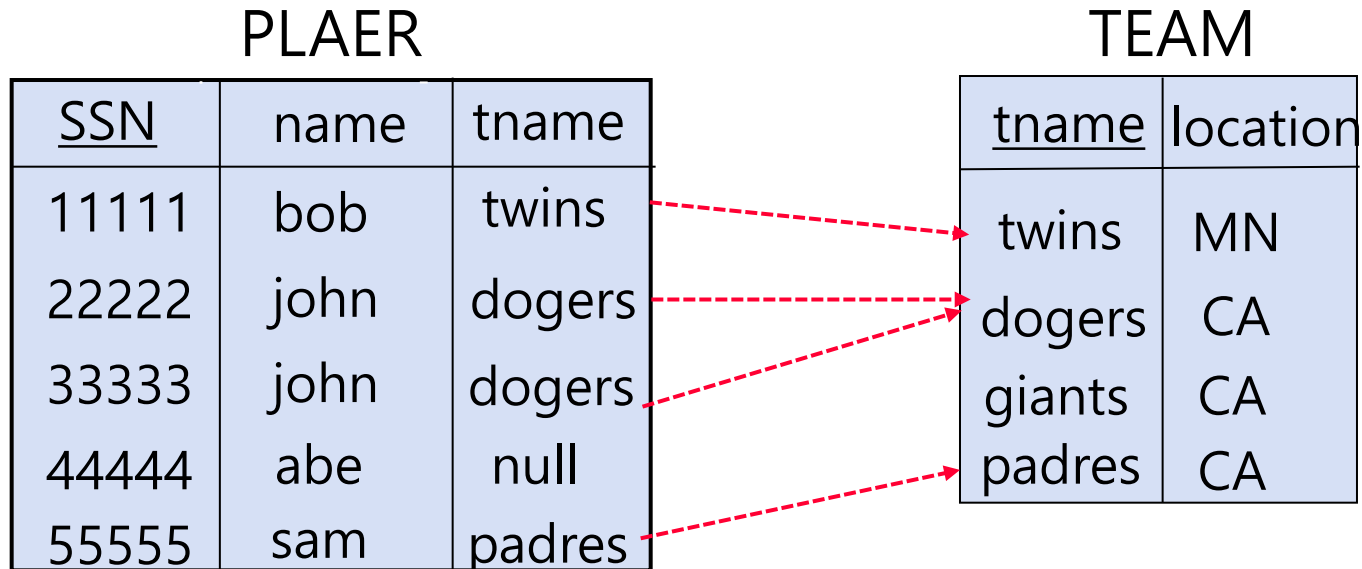
<u>dname</u>	phone
인사과	.....
자재과	.....
경리과	.....

**PK:** dname

# Referential Integrity

- The value in **FK** of **referencing** relation **R1** must be either
  - (1) an existing value of the corresponding primary key **PK** in the **referenced** relation **R2**,  
  
(In case (1), every **FK** values in referencing relation **R1** must **exist** in **PK** in the referenced relation **R2**)
  - or
  - (2) a **null** value  
  
(In case (2), the **FK** in **R1** should not be a part of its own primary key.)

# Referential Integrity



- Referencing relation

- **PK** : SSN
- **FK** : tname

- Referenced relation

- **PK** : tname

# Referential Integrity

EMPLOYEE

<u>SSN</u>	name	Super-SSN
11111	bob	22222
22222	john	33333
33333	john	44444
44444	abe	null
55555	sam	44444

- Referencing and referenced relation is the same.
- 한 relation의 FK가 자기 자신의 relation의 PK를 참조함.
  - What is **PK**?
  - What is **FK**?



# Referential Integrity

COURSE

<u>CID</u>	name
CS200	OS
CS250	DB
CS300	PL

ENROLL

CID	SID	credit
CS200	12345	3
CS200	23456	3
CS300	23456	4
CS250	23456	3
CS300	45678	3

STUDENT

<u>SID</u>	name	age
12345	Bob	22
23456	Ann	18
34567	Jim	30
45678	Eve	27

- Referenced:
    - **PK:** CID
  - Referencing:
    - two **FKs:** CID and SID
    - **PK:** {CID, SID}
  - Referenced:
    - **PK :** SID
- Note: Any NULL value is not allowed in either {CID} or {SID} in ENROLL relation. Why??

# Operations Causing Integrity Violation

- Key Integrity, Entity Integrity, and Referential Integrity can be violated by the following operations.
  - INSERT
  - DELETE
  - UPDATE
- If integrity is violated, several optional actions can be taken:
  - Perform the operation but ask to user to correct it.
  - Cancel the operation that causes the violation.  
(RESTRICT option)
  - Trigger additional updates so the violation is corrected.  
(CASCADE, SET NULL option)
  - Execute a user-specified error-correction routine.

# Possible Violations for INSERT operation

- **INSERT** may violate any of the constraints:
  - **Key Integrity:**
    - ✓ If the value of a **key** attribute in the new tuple already exists in another tuple in the relation
  - **Entity Integrity:**
    - ✓ If the primary **key** value is **null** in the new tuple
  - **Referential Integrity:**
    - ✓ If a **foreign key** value in the new tuple references a **primary key** value that does not exist in the referenced relation

# Possible violations for DELETE operation

- **DELETE** may violate only referential integrity:
  - If the **primary** key value of the tuple being deleted is referenced from other tuples in the relations.
  - Can be corrected by several actions:
    - RESTRICT option: Reject the delete operation
    - CASCADE option: Propagate the new primary key value into the foreign keys of the referencing tuples
    - SET NULL option: Set the foreign keys of the referencing tuples to NULL
  - One of the above options must be specified during database design for each foreign key constraint

# Possible violations for UPDATE Operation

- Any of the other constraints may also be violated, depending on the attribute being updated:
  - Updating the **primary key** (PK):
    - ✓ Similar to a DELETE followed by an INSERT
    - ✓ Need to specify similar options to DELETE
  - Updating a **foreign key** (FK):
    - ✓ May violate referential integrity
  - Updating an **ordinary attribute** (neither PK nor FK):
    - ✓ Can only violate domain constraints

# Violating Referential Integrity

- 다음 각 연산에서 referential integrity를 위반 유무를 판단하라.
  - Insert <77777, sam, eagles> into PLAYER; 위반했음; 사용자 실수
  - Delete <55555, sam, padres> from PLAYER; 위반 안 했음
  - Delete <twins, MN> from TEAM; 위반했음
  - Update tname "dogers" by "winners" from TEAM; 위반했음
  - Delete employee(s) with name 'abe' from EMPLOYEE; 위반했음
  - Delete <23456, Ann, 18> from STUDENT; 위반했음
  - Update CID CS200 by CS400 from COURSE; 위반했음
  - Delete <34567, Jim, 30> from STUDENT; 위반 안 했음

- 다음 relation들에서 foreign key를 명시하라.

**Figure 7.5** Schema diagram for the COMPANY relational database schema; the primary keys are underlined.

**Note :** FK와 이와 상응하는 PK는 반드시 이름이 같을 필요 없음;

**EMPLOYEE**

FNAME	MINIT	LNAME	<u>SSN</u>	BDATE	ADDRESS	SEX	SALARY	SUPERSSN	DNO
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**DEPARTMENT**

DNAME	<u>DNUMBER</u>	MGRSSN	MGRSTARTDATE
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**DEPT\_LOCATIONS**

<u>DNUMBER</u>	<u>DLOCATION</u>
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**PROJECT**

PNAME	<u>PNUMBER</u>	PLOCATION	DNUM
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**WORKS\_ON**

<u>ESSN</u>	<u>PNO</u>	HOURS
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**DEPENDENT**

<u>ESSN</u>	<u>DEPENDENT_NAME</u>	SEX	BDATE	RELATIONSHIP
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**EMPLOYEE**

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	B	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	M	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	M	38000	333445555	5
Joyce	A	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	M	25000	987654321	4
James	E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	M	55000	NULL	1

**DEPARTMENT**

Dname	Dnumber	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

**DEPT\_LOCATIONS**

Dnumber	Dlocation
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston

**WORKS\_ON**

Essn	Pno	Hours
123456789	1	32.5
123456789	2	7.5
666884444	3	40.0
453453453	1	20.0
453453453	2	20.0
333445555	2	10.0
333445555	3	10.0
333445555	10	10.0
333445555	20	10.0
999887777	30	30.0
999887777	10	10.0
987987987	10	35.0
987987987	30	5.0
987654321	30	20.0
987654321	20	15.0
888665555	20	NULL

**PROJECT**

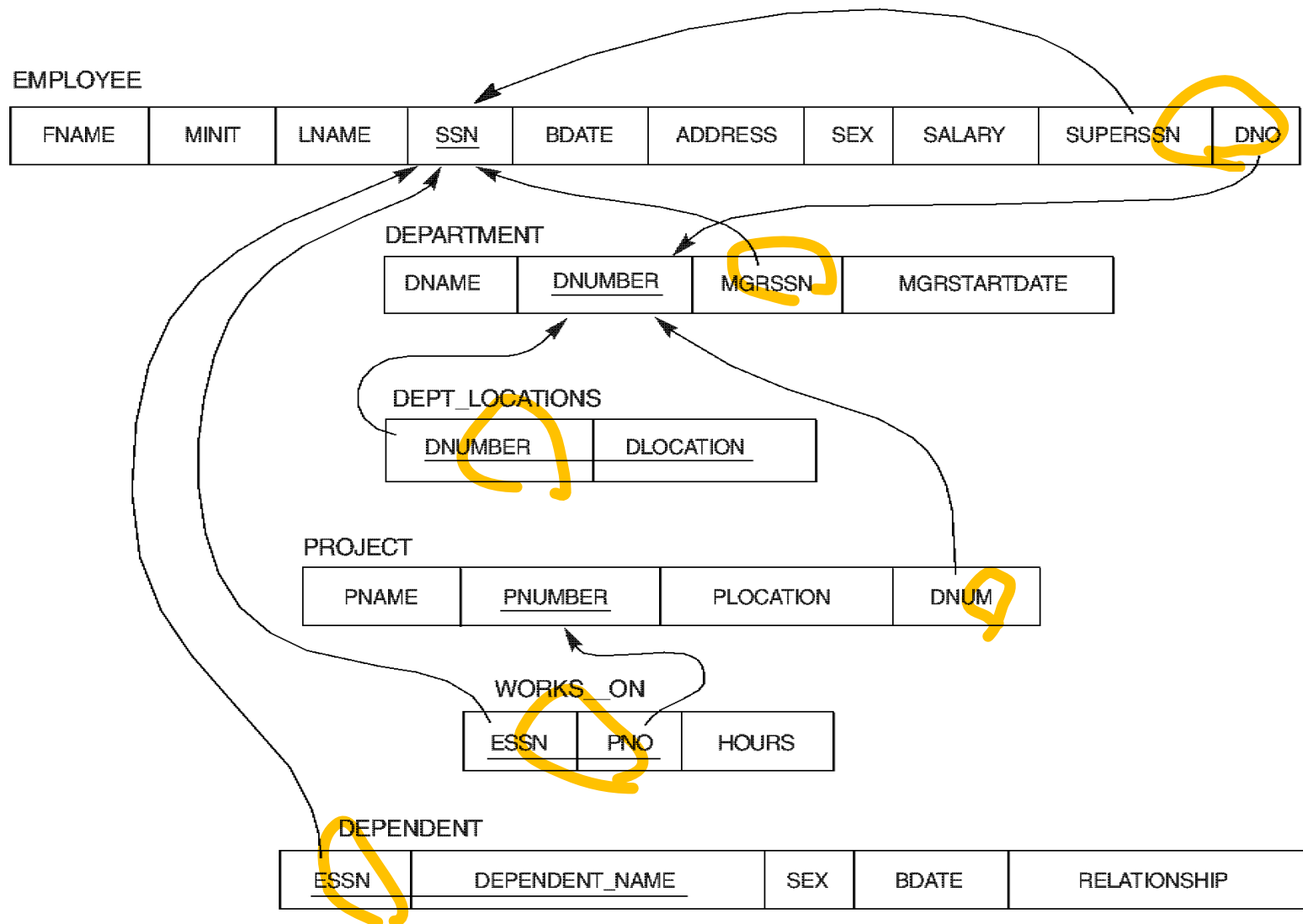
Pname	Pnumber	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

**DEPENDENT**

Essn	Dependent_name	Sex	Bdate	Relationship
333445555	Alice	F	1986-04-05	Daughter
333445555	Theodore	M	1983-10-25	Son
333445555	Joy	F	1958-05-03	Spouse
987654321	Abner	M	1942-02-28	Spouse
123456789	Michael	M	1988-01-04	Son
123456789	Alice	F	1988-12-30	Daughter
123456789	Elizabeth	F	1967-05-05	Spouse



**Figure 7.7** Referential integrity constraints displayed on the COMPANY relational database schema diagram.



# Referential Integrity : Exercise

- 다음 각 연산에서 referential integrity의 위반 유무를 판단하라.  
만약 위반시에 어느 relation들이 영향을 받는가?
  - Delete <123456789, Michael, . . . . > from DEPENDENT  
: 위반 안 했음. 영향 받는 relation들 없음.
  - Insert new employee <. . . . . . . . , 3> into EMPLOYEE  
: 위반 했음.
  - Delete <Franklin, . . . . , 33344555, . . > from EMPLOYEE  
: 위반 했음. EMP, DEPT, WORK-ON, DEPENDENT 모두 영향 받음.
  - Update Dnumber 5 by 7 from DEPARTMENT  
: 위반 했음. EMP, DEPT-LOCATION, PROJECT 모두 영향 받음.
  - Delete tuple(s) with Pno = 10 from WORKS-ON  
: 위반 안 했음. 영향 받는 relation들 없음.

# Referential Integrity: Exercise

- Draw a relational schema diagram by specifying the FKs.  
Note: Underlined attributes are primary keys.

BRANCH (branch-name, branch-city, assets)

LOAN (loan-number, branch-name, amount)

ACCOUNT (account-number, branch-name, balance)

DEPOSITOR (customer-name, account-number)

BORROWER (customer-name, loan-number)

CUSTOMER (customer-name, customer-street, customer-city)

# Referential Integrity: Exercise

branch (branch-name, branch-city, assets)

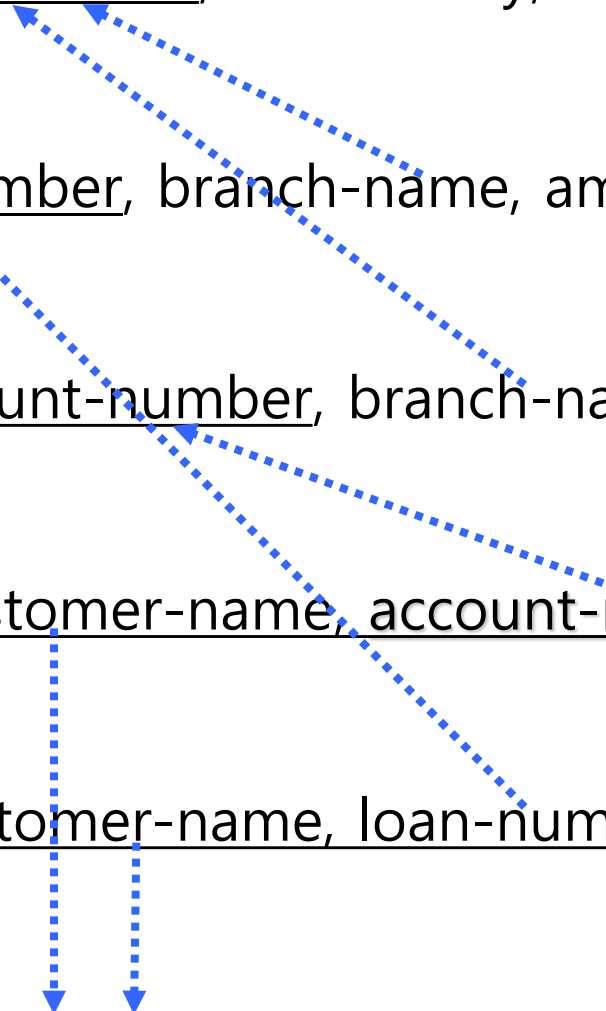
loan (loan-number, branch-name, amount)

account (account-number, branch-name, balance)

depositor (customer-name, account-number)

borrower (customer-name, loan-number)

customer (customer-name, customer-street, customer-city)



# Referential Integrity: Exercise

- Consider the following relations for a database that keeps track of student enrollment in courses and the books adopted for each course:

STUDENT (SSN, Name, Major, Bdate)

COURSE (Course#, Cname, Dept)

ENROLL (SSN, Course#, Quarter, Grade)

BOOK\_ADOPTION (Course#, Quarter, Book\_ISBN)

TEXT (Book\_ISBN, Book\_Title, Publisher, Author)

- Draw a relational schema diagram specifying the foreign keys for this schema.